

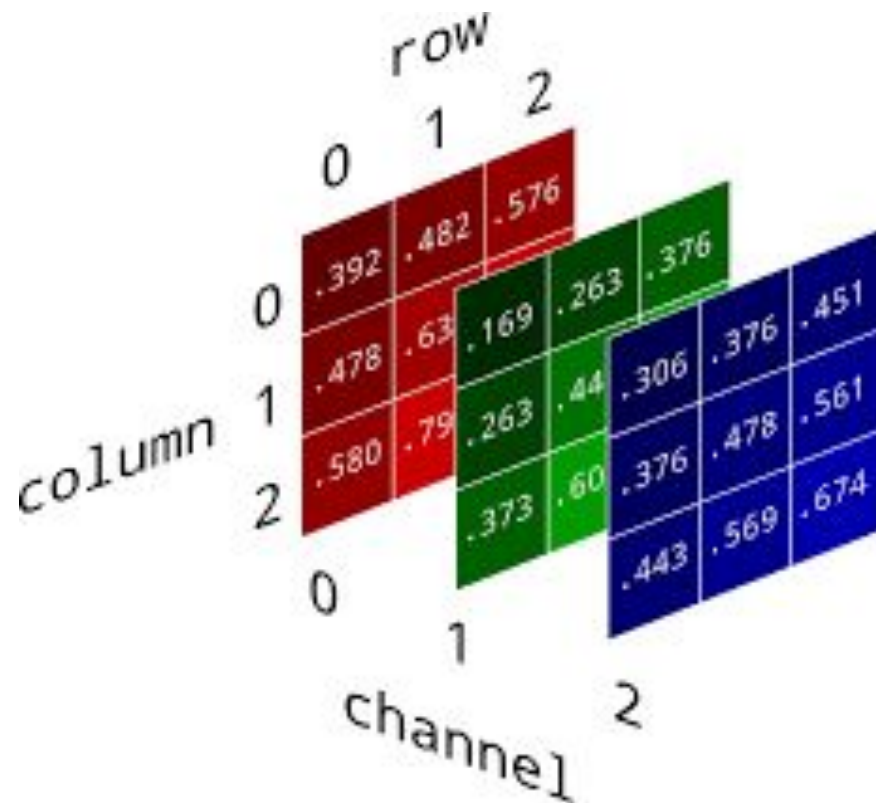
# How do we represent an Image?



157	153	174	168	150	152	129	151	172	161	155	156
155	182	163	74	75	62	33	17	110	210	180	154
180	180	50	14	34	6	10	33	48	106	199	181
206	109	5	124	131	111	120	204	166	15	56	180
194	68	137	251	237	239	239	228	227	87	71	201
172	105	207	233	233	214	220	239	228	98	74	206
188	88	179	209	185	215	211	158	139	75	20	169
189	97	165	84	10	168	134	11	31	62	22	148
199	168	191	193	158	227	178	143	182	106	36	190
205	174	155	252	236	231	149	178	228	43	95	234
190	216	116	149	236	187	85	150	79	38	218	241
190	224	147	108	227	210	127	102	36	101	255	224
190	214	173	66	103	143	96	50	2	109	249	215
187	196	235	75	1	81	47	0	6	217	255	211
183	202	237	145	0	0	12	108	200	138	243	236
195	206	123	207	177	121	123	200	175	13	96	218

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205	174	155	252	236	231	149	178	228	43	95	234
190	216	116	149	236	187	85	150	79	38	218	241
190	224	147	108	227	210	127	102	36	101	255	224
190	214	173	66	103	143	96	50	2	109	249	215
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183	202	237	145	0	0	12	108	200	138	243	236
195	206	123	207	177	121	123	200	175	13	96	218

# RGB Image Representation



# Convolution

1 <sub>x1</sub>	1 <sub>x0</sub>	1 <sub>x1</sub>	0	0
0 <sub>x0</sub>	1 <sub>x1</sub>	1 <sub>x0</sub>	1	0
0 <sub>x1</sub>	0 <sub>x0</sub>	1 <sub>x1</sub>	1	1
0	0	1	1	0
0	1	1	0	0

Image

4		

Convolved  
Feature

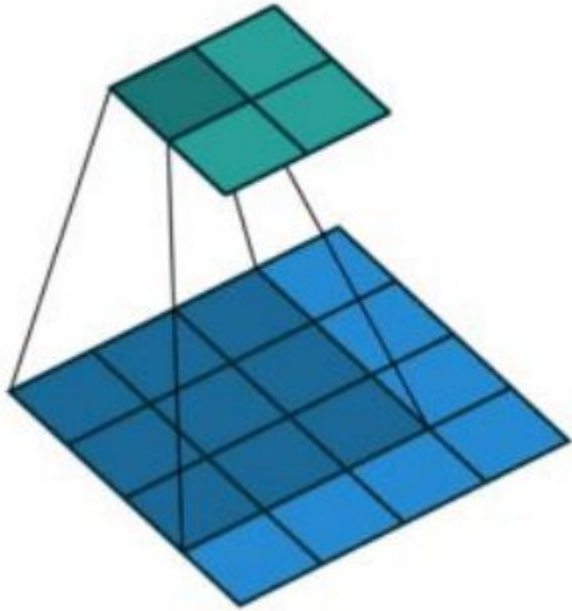
# Convolutional Filter

The building blocks of a CNN are the convolutional filters or kernels

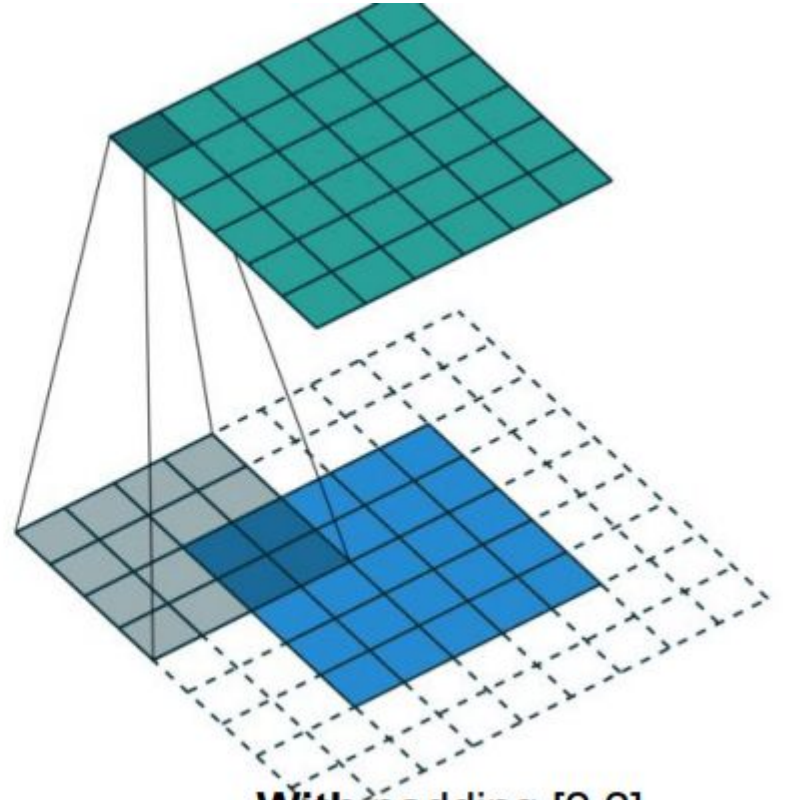
A convolutional filter is defined by the following hyperparameters:

- Kernel size: spatial dimensions of the filter
- Stride: number of steps by which the filter slides over the input
- Padding width: number of extra rows and columns added along the boundary of the input

# Padding



**Without** padding (i.e.,  $[0,0]$ )



**With** padding  $[2,2]$

# Padding

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	5	3	8	1	6	0	0
0	0	4	7	2	9	0	0	0
0	0	3	5	7	8	1	0	0
0	0	2	6	0	4	3	0	0
0	0	9	1	5	2	7	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Zero/Constant Padding

5	5	5	3	8	1	6	6	6
5	5	5	3	8	1	6	6	6
5	5	5	3	8	1	6	6	6
4	4	4	7	2	9	0	0	0
3	3	3	5	7	8	1	1	1
2	2	2	6	0	4	3	3	3
9	9	9	1	5	2	7	7	7
9	9	9	1	5	2	7	7	7
9	9	9	1	5	2	7	7	7

Replicate/Edge Padding

7	4	4	7	2	9	0	0	9
3	5	5	3	8	1	6	6	1
3	5	5	3	8	1	6	6	1
7	4	4	7	2	9	0	0	9
5	3	3	5	7	8	1	1	8
6	2	2	6	0	4	3	3	4
1	9	9	1	5	2	7	7	2
1	9	9	1	5	2	7	7	2
6	2	2	6	0	4	3	3	4

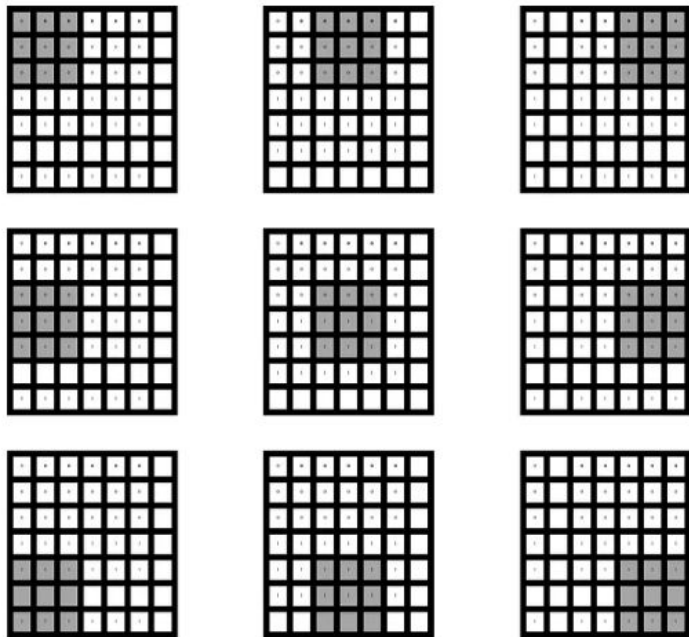
Reflective Padding

4	3	2	6	0	4	3	2	6
2	7	9	1	5	2	7	9	1
1	6	5	3	8	1	6	5	3
9	0	4	7	2	9	0	4	7
8	1	3	5	7	8	1	3	5
4	3	2	6	0	4	3	2	6
2	7	9	1	5	2	7	9	1
1	6	5	3	8	1	6	5	3
9	0	4	7	2	9	0	4	7

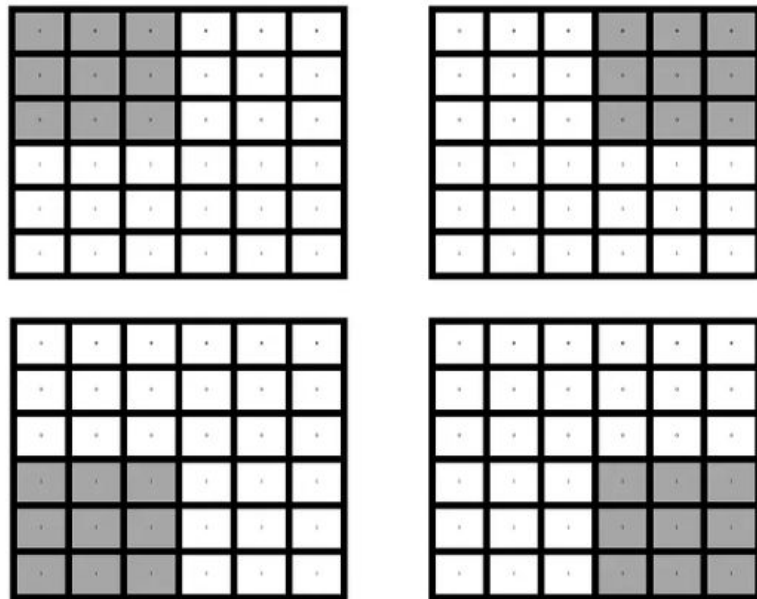
Circular Padding

# Stride

Stride=2

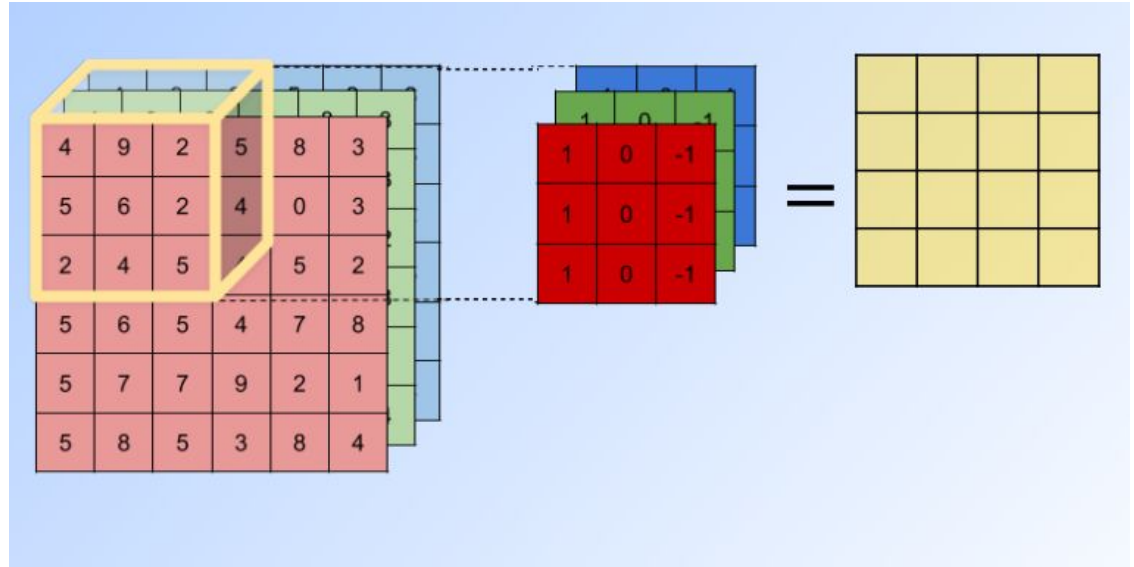


Stride=3



# Convolutional Filters

- The number of channels of the input must match the number of channels of the convolutional filter.
- The filters are applied channel-wise and the result of the convolution operation for each channel are summed to constitute the final output.





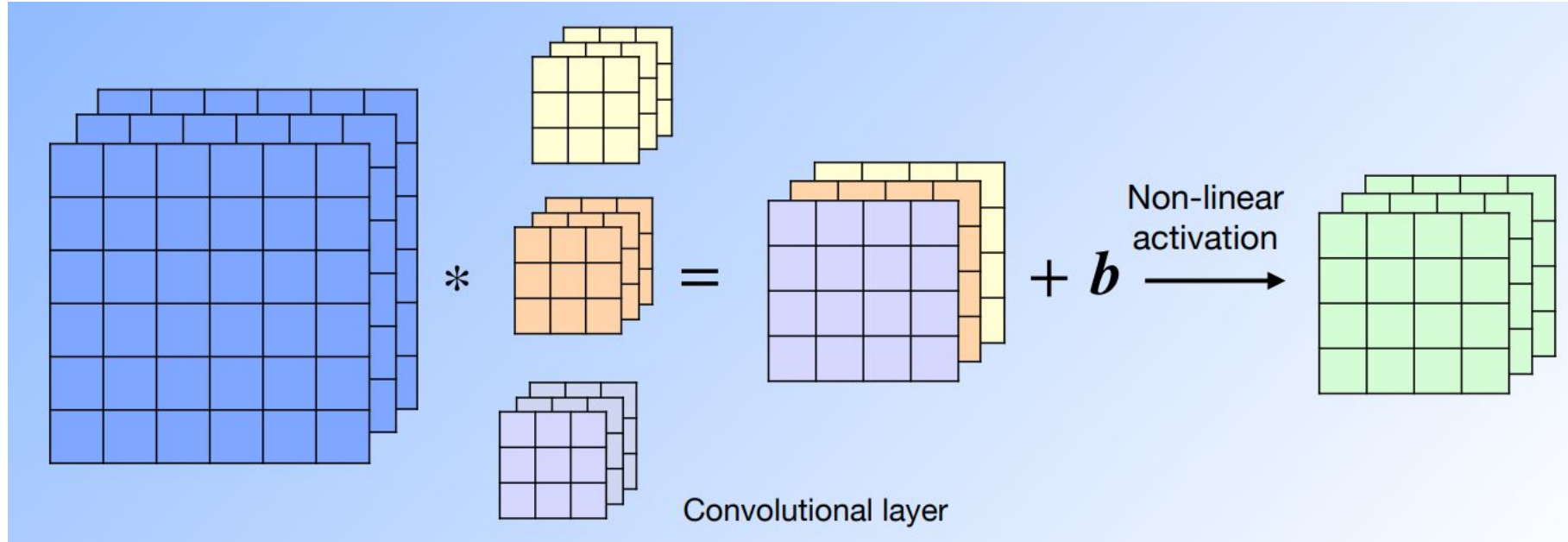
# Convolutional Filters

The diagram illustrates a 2D convolution operation. On the left is an 11x11 input feature map (orange cells) with a 3x3 kernel (red box) highlighted. The kernel values are 1, 0, -1 for the first row and 1, 0, -1 for the second and third rows. To the right of the input is a 3x3 green kernel matrix with values 1, 0, -1. An asterisk (\*) indicates the convolution operation. To the right of the asterisk is an equals sign (=) followed by a 3x3 yellow output feature map. The top-left 3x3 portion of the output is shown with values -15 and 6.

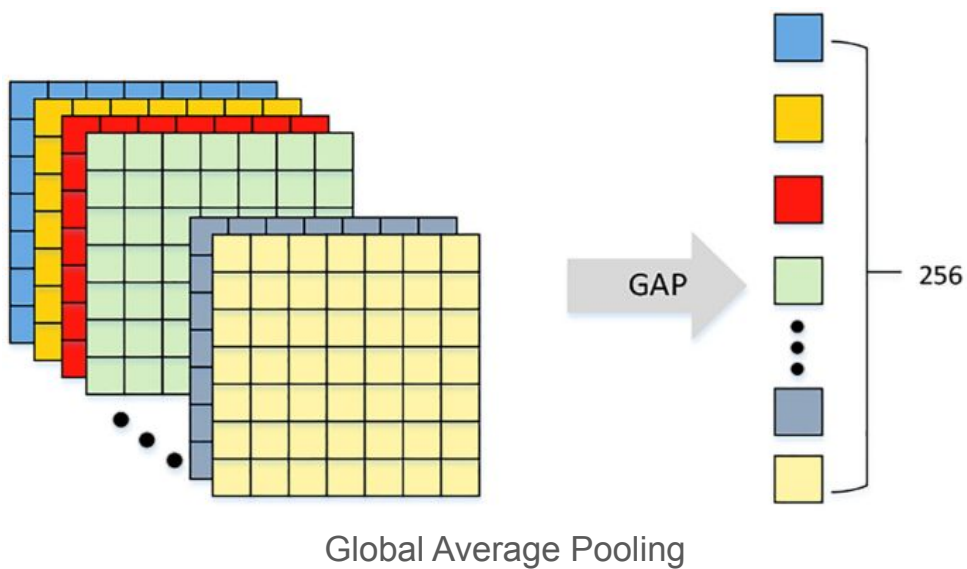
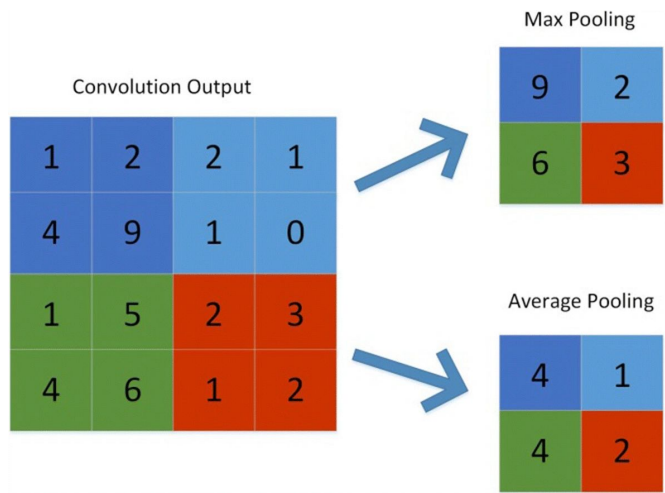
$$\lfloor W_o = \frac{W_i + 2P - K}{S} + 1 \rfloor$$

$W_o$  : size of output feature map,  $W_i$  : size of input image/feature map  
 $P$ : padding size,  $K$  : filter/kernel size,  $S$  : stride

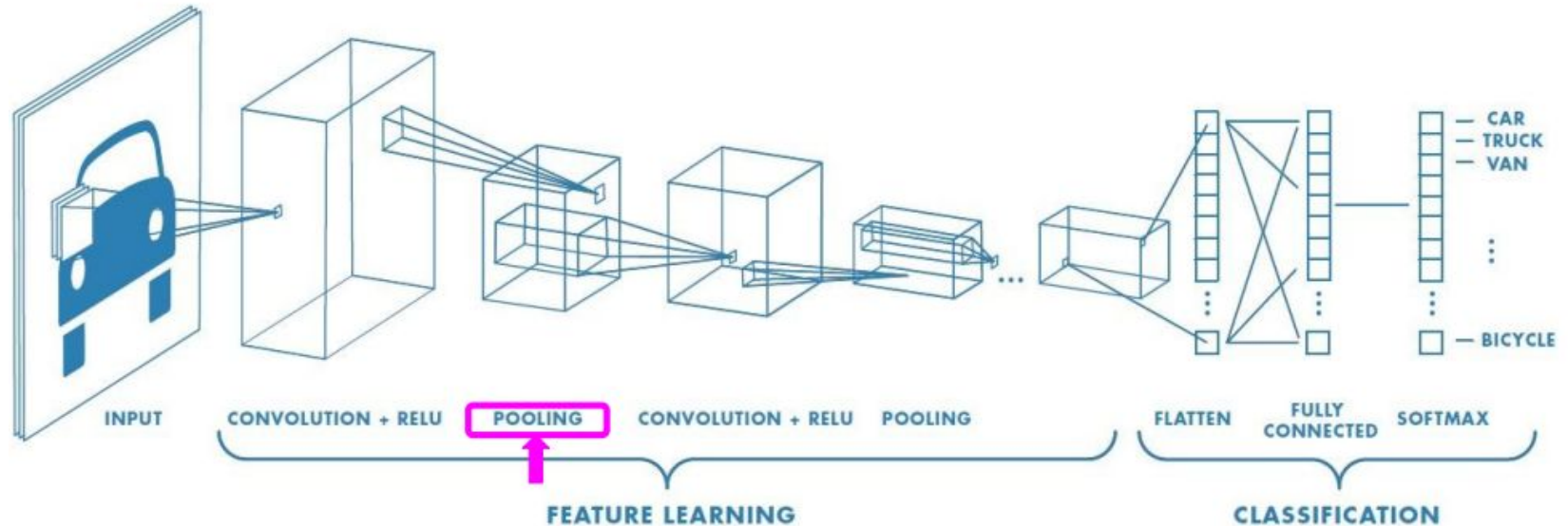
# Convolutional Layer



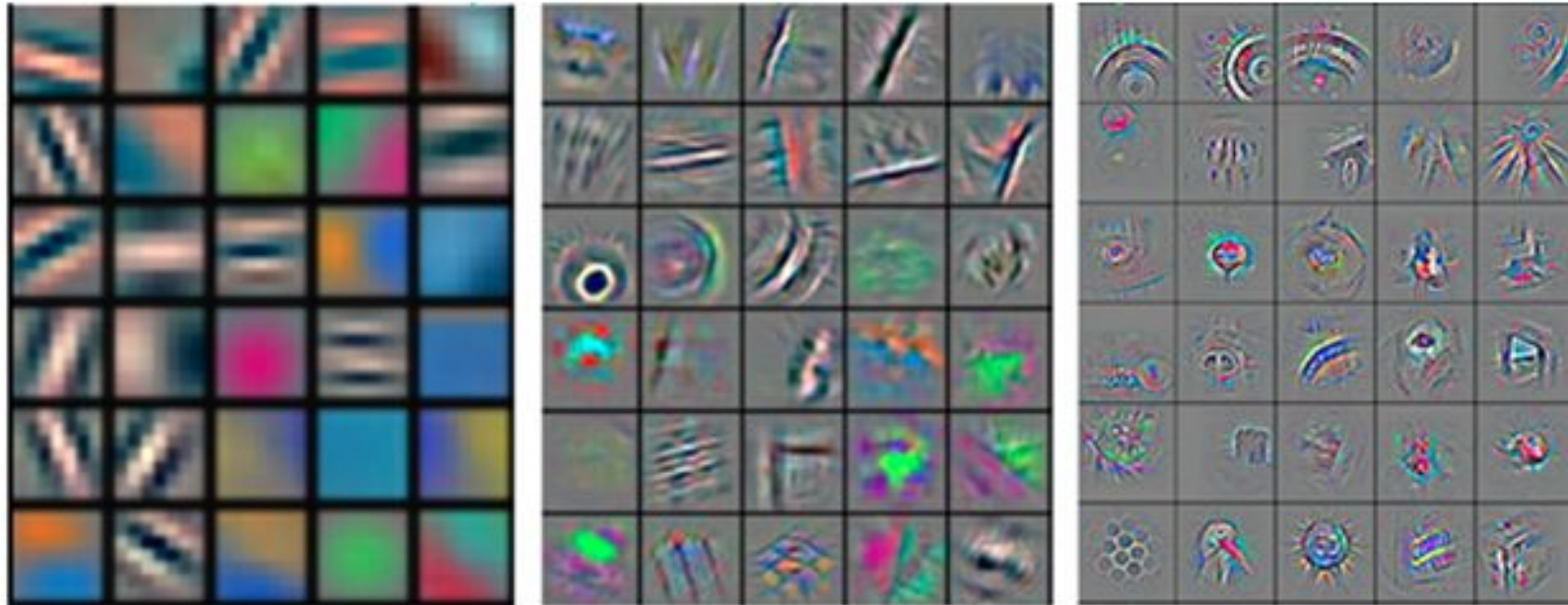
# Pooling Layer



# Different layers of a CNN



# Features learned at different depths



# 1x1 convolution

