



# Question (LeetCode 88: Merge Sorted Array)

Given two sorted integer arrays `nums1` and `nums2`, merge `nums2` into `nums1` as one sorted array. The number of elements initialized in `nums1` and `nums2` are `m` and `n` respectively. `nums1` has enough space (size equal to `m + n`) to hold additional elements from `nums2`.

**Example:**

- Input: `nums1 = [1,2,3,0,0,0]`, `m = 3`, `nums2 = [2,5,6]`, `n = 3`
- Output: `[1,2,2,3,5,6]`



## Merge Sorted Arrays



### 1. Definition and Purpose

- Merge two sorted arrays into one sorted array in-place.
- Commonly used in sorting algorithms, merging datasets, or maintaining ordered sequences.



### 2. Syntax and Structure (Python)

```
# nums1: first array with extra space at the end
# m: number of initialized elements in nums1
# nums2: second array
# n: number of elements in nums2
```



### 3. Two Approaches



#### Approach 1: Brute Force

- Concatenate `nums2` into `nums1` and sort.

```
def merge_bruteforce(nums1, m, nums2, n):
    nums1[m:] = nums2 # Step 1: Copy nums2 into nums1
    nums1.sort()      # Step 2: Sort the combined array
```

- **Time Complexity:**  $O((m+n) \log(m+n))$
- **Space Complexity:**  $O(1)$  (in-place)



#### Approach 2: Optimized (Two Pointers from End)

- Start from the end of both arrays to fill `nums1` from back to front.
- Avoid overwriting elements in `nums1`.

## 4. Optimized Pseudocode

```
i = m - 1      # pointer for last element in nums1 initialized portion
j = n - 1      # pointer for last element in nums2
k = m + n - 1  # pointer for last position in nums1 array
while j >= 0:
    if i >= 0 and nums1[i] > nums2[j]:
        nums1[k] = nums1[i]
        i -= 1
    else:
        nums1[k] = nums2[j]
        j -= 1
    k -= 1
```

## 5. Python Implementation with Detailed Comments

```
from typing import List

def merge(nums1: List[int], m: int, nums2: List[int], n: int) -> None:
    """
    Merge nums2 into nums1 in-place.
    """
    # Initialize pointers for nums1, nums2, and the last index
    i = m - 1      # Last initialized element in nums1
    j = n - 1      # Last element in nums2
    k = m + n - 1  # Last position in nums1 to fill

    # Traverse from the end to the beginning
    while j >= 0:
        if i >= 0 and nums1[i] > nums2[j]:
            nums1[k] = nums1[i] # Place larger element at end
            i -= 1
        else:
            nums1[k] = nums2[j] # Place element from nums2
            j -= 1
        k -= 1 # Move backwards in nums1

    # Example Usage
    nums1 = [1,2,3,0,0,0]
    m = 3
    nums2 = [2,5,6]
    n = 3
    merge(nums1, m, nums2, n)
    print(nums1) # Output: [1,2,2,3,5,6]
```

## 6. Internal Working

- Filling from end ensures no overwriting.
- Two-pointer comparison chooses the largest element each iteration.
- Only modifies nums1 array in-place.

## 7. Best Practices

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- Always check bounds ( $i \geq 0$ ,  $j \geq 0$ ) to avoid index errors.
- Use the two-pointer optimized approach for large arrays.

## 8. Related Concepts

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- Two-pointer technique
- In-place array manipulation
- Merge step in Merge Sort

## 9. Complexity Analysis

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- **Optimized Approach:**
  - Time:  $O(m+n)$
  - Space:  $O(1)$
- **Brute Force:**
  - Time:  $O((m+n) \log(m+n))$
  - Space:  $O(1)$  in-place

## 10. Practice and Application

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- LeetCode: 88 Merge Sorted Array, 21 Merge Two Sorted Lists
- Used in merging sorted datasets in data pipelines.
- Efficient in-place operations in memory-sensitive applications.