Prediction of Remaining Useful Life (RUL) of Batteries using ODE-RNNs

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1 Objective

To predict the Remaining Useful Life (RUL) of a battery by giving 20 observations which consists of the various features of the batteries using a neural ODE without using the capacity (mAH) feature which is used in traditional methods. The model was to be trained on the given dataset.

1.1 Dataset

The dataset to be used is the Battery Remaining Useful Life Prediction dataset on Kaggle. The Hawaii Natural Energy Institute examined 14 NMC-LCO 18650 batteries with a nominal capacity of 2.8 Ah, which were cycled over 1000 times at 25°C with a CC-CV charge rate of C/2 rate and discharge rate of 1.5C. This data released by Hawaii Natural Energy Institute was used to make this dataset. It contains the following features:

Cycle Index The Cycle number of current cycle

Discharge Time (s) time that takes the voltage to reach its minimum value in one discharge cycle.

Decrement 3.6-3.4V (s) It represents the time taken for voltage to drop from 3.6V to 3.4V during a discharge cycle.

Max. Voltage Dischar. (V) The initial and maximum voltage in the discharging phase.

Min. Voltage Charg. (V) The initial value of voltage when charging.

Time at 4.15V (s) The time to reach 4.15V in charging phase.

Time constant current (s) The time in which the current stays constant at its max. value.

Charging time (s) The total time for charging.

RUL The Remaining Useful Life of battery after every cycle.

2 Mathematical Formulation and Explaination

In this section, we'll look at and recap the mathematical formulation of the various techniques and components used in the model

2.1 Neural ODE

Numerous Models build complicated transformations by composing a sequence of transformations to the input or a maintained hidden state. These transformations are mathematically expressed as:

$$\mathbf{z}_{t+1} = \mathbf{z}_t + f(\mathbf{z}_t, \theta_t)$$

where $t \in \{0, \ldots, T\}$ and $h_t \in \mathbb{R}$. These iterative updates can be seen as an Euler discretization of a continuous transformation. Neural ODE aims to parameterize the continuous dynamics of z_t given by the equation:

$$\frac{d\mathbf{z}(t)}{dt} = f(\mathbf{z}(t), t, \theta)$$

The output of Neural ODE is generated with a black box differential equation solver. Therefore, the $\mathbf{z}(T)$ can be obtained by:

$$\mathbf{z}(T) = \mathbf{z}(t_0) + \int_{t_0}^{T} \mathbf{f}(\mathbf{z}(t), t; \theta) \, dt = \text{ODESolve}(\mathbf{z}(t_0), f, t_0, T, \theta)$$

In order to avoid backpropogating through the black box differential solver, Neural ODE uses adjoint sensitivity method to calculate required gradients. At every point, it maintains an adjoint state $\mathbf{a}(t)$ whose dynamics are given by another ODE:

$$\frac{d\mathbf{a}(t)}{dt} = -\mathbf{a}(t)^T \frac{\partial \mathbf{f}(\mathbf{z}(t), t; \theta)}{\partial \mathbf{z}(t)}$$