```
import numpy as np
import matplotlib.pyplot as plt
import sympy as sp
# Define the variable and function
x = sp.symbols('x')
function = (x + 3) ** 2 # Define the function y = (x + 3)^2
# Compute the derivative (gradient) of the function
derivative = sp.diff(function, x)
# Convert the derivative to a Python function
gf = sp.lambdify(x, derivative, 'numpy')
# Initialize parameters
x current = 2 # Start
lr = 0.01 # Learning Rate
precision = 0.000001
previous step size = 1
\max iter = 10000
iters = 0
# List to store the values of x for plotting
ad = []
# Gradient Descent Loop
while precision < previous step size and iters < max iter:
    prev = x current
    x current = x current - lr * gf(prev)
    previous step size = abs(x current - prev)
    iters += 1
    print('Iteration: ', iters, 'Value: ',x current)
    gd.append(x current)
Iteration: 1 Value: 1.9
Iteration: 2 Value: 1.801999999999998
Iteration: 3 Value: 1.70596
Iteration: 4 Value: 1.6118408
Iteration: 5 Value: 1.519603984
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Iteration: 7 Value: 1.3406276662336
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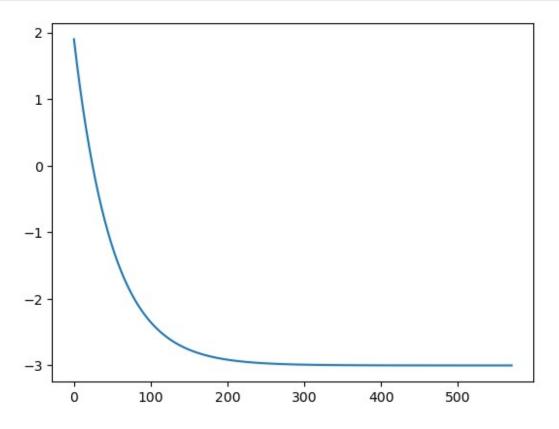
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Iteration:
print('Local Minima : ', x current)
Local Minima: -2.999951128099859
# Plotting the convergence of x values
plt.plot(range(iters), gd)
[<matplotlib.lines.Line2D at 0x204c87891f0>]
```



```
# import numpy as np
# import matplotlib.pyplot as plt
# # Initialize parameters
\# x = 2 \# Starting point
\# lr = 0.01 \# Learning Rate
\# precision = 0.000001
# previous_step_size = 1
\# \max iter = 10000
# iters = 0
# # Gradient function: derivative of (x + 3)^2
# gf = lambda x: 2 * (x + 3)
# # List to store the values of x for plotting
# gd = []
# # Gradient Descent Loop
# while previous_step_size > precision and iters < max_iter:</pre>
#
     prev = x
     x = x - lr * gf(prev) # Update x using the gradient
      previous step size = abs(x - prev) # Calculate the step size
     iters += 1
#
      print('Iteration: ', iters, 'Value: ', x)
      qd.append(x)
# print('Local Minima: ', x)
# # Plotting the convergence of x values
# plt.plot(range(iters), gd)
# pip install sympy
```