Asymphotic notations are used to write fastest and slowest fastest and slowest also fastest summing time for an algorithm. These are of also respectively

Thouse types of szymptotic notation to represent the growth of

1) > Big Theta (0)

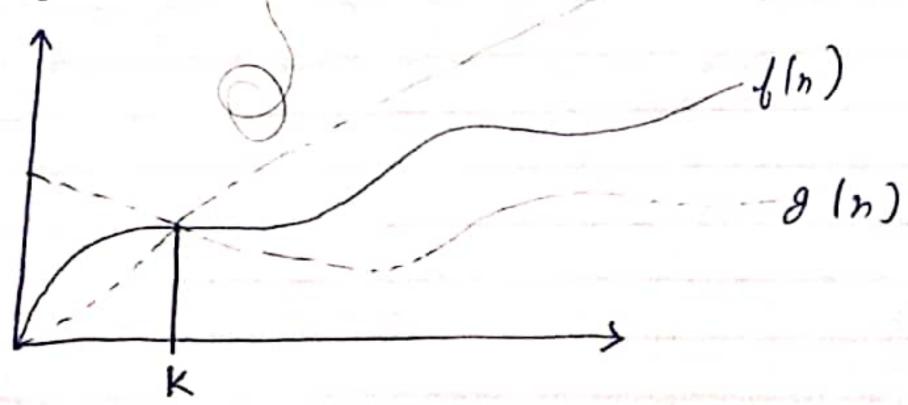
1) > Big -ch (O)

(II) s Big omega (IL)

1)- The time complexity superesented by the Big O notation is like the according walue as within which the actual time at execution at the algo will be

eg. 3 nt +5n we use the Big o notation to supercont this, then the time complexity would be O(n2) ignoring the constant cofficient and summering insignificant part, which is 5n.

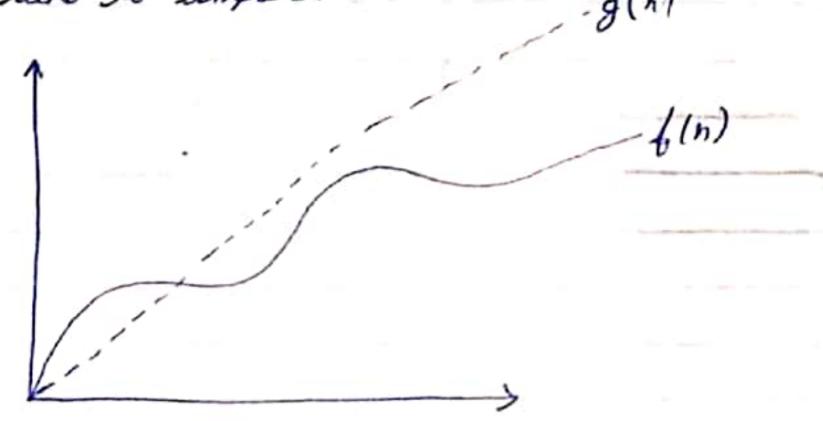
 $\theta$   $(f(n)) = (\theta(n))$  if and only if  $\theta(n) = O(f(n))$  and  $g(n) = \Omega(f(n))$  for all  $n > n_0$ 



Big Oh Notation (0)

The formal way to exposes upper bound of all algorithm running time. It measures the worset was time complexity on the largest amount of time all also can besseld take to complete.

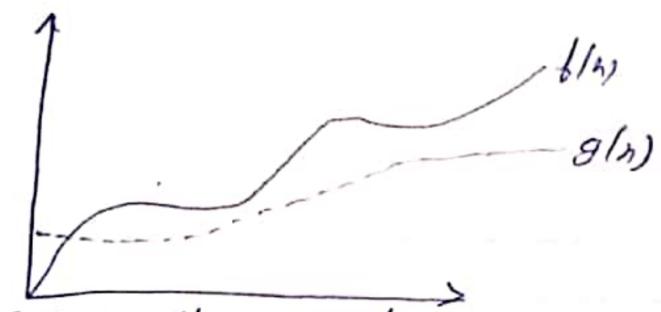
[1]



e.g > O(f(n)) = {g(n): there exist c>0 and no such that f(n) = (.g(n))
for all n>no}

(II) · Omego notation (S)

— it is the formal way to express the lower bound of an algo is sunning time. It measure the best use time on an algo use possibly take to complete.



Se (f(n)) ≥ Lg(x): thome exist c>0 and no and such that g(n) < (. f(n) for all n>no }

so using ap an = 0 or k-1  $a_n = n$ , a = 1, y = 2  $n = 3.2^{k-1}$   $n = 2 \times 2n = 2^k$ 

taking log bow 2 on both sid log, 2n = log, 2K log, 2 + log, n = 1 log, 2

 $1 + log_2 n = k$  $1 = Tl = b(log_2 n) = log n$  3.  $T(n) = \{3T(n-1) \cdot d, n > 0$   $T(n) = 3T(n-1) \cdot T(n) = 2$ using substitution  $T(n) = 3T(n-1) \rightarrow T(n-1) = 3T(n-2)$   $T(n) = 3[3T(n-2)) \rightarrow T(n-1) = 3T(n-3)$  T(n) = 3[3(3T(n-3))]  $T(n) = 3^{3}T(n-3)$ for k terms  $T(n) = 3^{k}T(n-k)$ 

$$n=k$$

$$Using \ n=k$$

$$T(n)=3^nT(n-n)$$

$$T(n)=3^n.1=3^n$$

let T(n-K) = T(0)

49

Sove T(n)=2T(n-1)-1 T(0)=7  $T(n)=2T(n-1)-1 \rightarrow T(n-1)=2T(n-2)-1$   $T(h)=2(2T(n-2)-1]-1 \rightarrow T(n-2)=2T(n-3)-1$  T(n)=2[2 ? 2T(n-3)-1 ? -1]-1 T(n)=2[4 1 [n-3)-2 ? -1=8T(n-3)-7for  $k^{th}$  town  $T(n)=2^{k}(T(n-k))-2^{k}-1$ Let T(n-k)=T(0) n=k using k=n  $T(n)=2^{n}(T(0))-(2^{n}-1)$   $T(n)=2^{n}-2^{n}+1$  T(n)=1

sol = 1 S=13 while (S=n) Charles of the first terms of the second of the 5 TO THE STATE OF 2 i++35=5+135 Here no of steps July 1 -- 1 -- 1 -- 2 so excess at goweth is not sonst. so general texm can be taken in K(k+1) let at n no of terms isk so  $n=k^2+k=2$   $2n=k^2+k$ ignoring lower order terms K=Jn TIN)=Jn 6+ fon(i=1) i \* i <= n; i++) country 201 is mound from 1 to Thwith linear growthse T(n)=0(Jn) 7-1 for (i=n/2) i == ngi++) for 1 = 13 j= n3 j= j \*2) for (1=1; k == n; k= ==2) (and) loop as moving from 1 to so with appearantial growth so T( for takes two look will be Ol logn) and I look young strough 1/2 to m so with constant aggreement 20 T(n)=0(n/2)=0(x) so award complexets of the of will be TIn)=O(n.logn.logn) 8 - T(n) = T(n-3)+n2 ナ(リニ) T(n)=T(n-3)+n2 -> T(n-0+(n-3)2 T(n)=T(n-6)+(n-3) + +n2 -> T(n-9)+(n-6)2 T(n)=T(n-9)+(n-6)2+(n-3)2+n2 -> T(n-12)+(n-9)2 T(n)=T(n-17)+(n-9)2+(n-6)2+(n-3)2+n2 so for 1045000 T(n)=T(n-K)+(n-(K-3))2+ (n-(K-6))2+(n-(K-9))2+(n-(K-9))2+(n-(X+2))2+ -+ (n-(k-K))2

```
Let T(n-k) = T(1)
     n=1+\gamma=1=n-1
 T(n) = T(n-(n-1)) + [n-(n-1-3)]^{2} + [n-(n-1-6)]^{2} + [n-(n-1-9)]^{2} + ... + m^{2}
T(n) = T(n-(n-1)) + [n-(n-1-3)]^{2} + [n-(n-1-6)]^{2} + [n-(n-1-9)]^{2} + ... + m^{2}
n=(3+x-2)2
      n=9k7+4-17K
      n=x2
       K =VB
    TIn)=0(Jn)
   for (j=ljjz=njj=j+i)

point(" +")

etops
 9- for li=1 ton)
      so total complexity is
       T(=n+n/2+n/3+n/9+n/5+
          => n[1+1/2+1/3+1/4+1/5+
           => n 5," 1/2 dar
           => n[logs],1 = n[logn-log[1)] = n logn
   10 + ib (>1, then the exponential c" bor outgrows any term so
        the ans is no is O((")
    11 - ent j-1, j=0;
        while (icx)
          & デニドリラ
        so i will so on till mand general formule for 1th touris
         n= (1/41)
           80 T(= O (5h)
```

(Ar T-(n)= F(129)+T(n)+(n2)

log (log n)

for (snit i=0; i < n; i=i+i)

formit ("+");

TIM)=T[NA)+T[N2)+In

TIMA) TIME T[M3) T[M8) T[M9)

T(n)=([n2+5n2/16+75n2/256+---] T(n)=0[n2)

15+ for ( inti=li je=n; 1+1) for [ int ]= 1; j < n; j+=1)

0(1);

j= n n/2 n/3 n/9

time complainty

t(n)=n+n/2+n/3+n/9+ ---- + N/2

 $T(n) = n \int \frac{1}{y_1} + y_3 + y_4 + - - - - + y_n J = n \int \frac{1}{3x} dx = n \int \frac{1}{3p_n} - \frac{1}{3p_n} = n \int \frac{1}{3p_n} dx$ 

16- for [ int [= ]; i = n; [= pow [ 1] (c))

for any of movering with exponential scate the The Lecome T(=0(leg(legn))

18 + a + 100 2 log log n 2 log n = nlogn 2 good (n). 2n 2n2 2n2 2n2 2n2 42

6-12 log(logs) < Jeg/10) < logn < log 2n < 2 logn < n logn < 2(21)

C+ 912 logs(n) 2 log, (n) 2n log, (n) 2 nlog, (n) 2 5n 28 n 227n3 82h 2 log(n!) <n!

Search (0, n, Kay)

low=0, high = n

while (low - high)

mid = Low+high

if o (mid) is key

section mid

elso ib o (mid) = key

low=mid+1

elso high=mid-1

Recoversion

I low - high

if low - high

med = Low+high

Joseph Lo, Low high, Kon)

if Josephigh

med = Low + high

if o (mid ] < Kon

Search Lo, mid + 1, high, kon)

Less if a (mid ] > kon

Search Lo, low, mid - 1, Kon)

\_ els ration mid

Linear search T(=O(n) S(= constant
Binary" T(=O(logn) S(=))

24 - TIn )=TIn)+[