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SUBJECT	Design and Analysis of Algorithms
EXPERIMENT NO:	06
AIM:	To implement Single source shortest path
Algorithm:	<p>Bellman Ford Algorithm</p> <pre> function bellmanFordAlgorithm(G, s) //G is the graph and s is the source vertex for each vertex V in G dist[V] <- infinite // dist is distance prev[V] <- NULL // prev is previous dist[s] <- 0 for each vertex V in G for each edge (u,v) in G temporaryDist <- dist[u] + edgeweight(u, v) if temporaryDist < dist[v] dist[v] <- temporaryDist prev[v] <- u for each edge (U,V) in G If dist[U] + edgeweight(U, V) < dist[V] Error: Negative Cycle Exists </pre>

	<pre>return dist[], previ[]</pre> <p>Dijkstra Algorithm</p> <ol style="list-style-type: none"> 1. function Dijkstra(Graph, source): 2. for each vertex v in Graph.Vertices: 3. dist[v] ← INFINITY 4. prev[v] ← UNDEFINED 5. add v to Q 6. dist[source] ← 0 7. while Q is not empty: 8. u ← vertex in Q with min dist[u] 9. remove u from Q 10. for each neighbor v of u still in Q: 11. alt ← dist[u] + Graph.Edges(u, v) 12. if alt < dist[v]: 13. dist[v] ← alt 14. prev[v] ← u 15. return dist[], prev[]
Code Part 1:	<p>A weighted, directed graph in which edge weights may be negative $G=(V; E)$ with source s (Bellman-Ford)</p> <p>Source Code</p> <pre>#include<bits/stdc++.h> using namespace std; int V; void printSolution(int dist[]) { cout << "Vertex \t Distance from Source" << endl; for (int i = 0; i < V; i++) cout << i << " \t\t\t" << dist[i] << endl; }</pre>

```

void BellmanFord(int ** graph,int src, vector<pair<int,int>> edges){

    int dist[V];

    for(int i=0;i<V;i++){
        dist[V]=INT_MAX;
    }
    dist[src]=0;

    for(int it=1;it<=V-1;it++){

        for(int i=0;i<edges.size();i++){
            int u=edges[i].first;
            int v=edges[i].second;

            if(dist[u]!=INT_MAX && dist[u]+graph[u][v]<dist[v]){
                dist[v]=dist[u]+graph[u][v];
            }

        }
    }

    for (int i = 0; i < edges.size(); i++) {
        int u=edges[i].first;
        int v=edges[i].second;
        int weight = graph[u][v];
        if (dist[u] != INT_MAX && dist[u] + weight < dist[v]) {
            printf("Graph contains negative weight cycle");
            return;
        }
    }

    printSolution(dist);

}

int main(){

```

```

cout<<"Enter the number of vertices :";
cin>>V;

int **graph=new int*[V];
    for(int i=0;i<V;i++)
    {
        graph[i]=new int[V];
    }

for(int i=0;i<V;i++){
    for(int j=0;j<V;j++){
        graph[i][j]=INT_MAX;
    }
}

cout<<"Enter the number of edges :";
int e; cin >> e;

vector<pair<int,int>> edges;

for(int i=0;i<e;i++){

    cout<<"\nEnter the Vertices of the edge "<<i<<" :";
    int a,b,w;
    cin>>a>>b;
    a--;b--;
    edges.push_back(make_pair(a,b));

    cout<<"Enter the Weight of the edge "<<i<<" :";
    cin>>w;

    graph[a][b]=w;

}

BellmanFord(graph,0,edges);

return 0;

```

	<pre> }</pre>
Output:	<pre> Enter the number of vertices :5 Enter the number of edges :6 Enter the Vertices of the edge 0 :1 2 Enter the Weight of the edge 0 :5 Enter the Vertices of the edge 1 :1 5 Enter the Weight of the edge 1 :1 Enter the Vertices of the edge 2 :1 4 Enter the Weight of the edge 2 :4 Enter the Vertices of the edge 3 :2 3 Enter the Weight of the edge 3 :-2 Enter the Vertices of the edge 4 :3 4 Enter the Weight of the edge 4 :3 Enter the Vertices of the edge 5 :4 5 Enter the Weight of the edge 5 :5 Vertex Distance from Source 1 0 2 5 3 3 Enter the Vertices of the edge 2 :1 4 Enter the Weight of the edge 2 :4 Enter the Vertices of the edge 3 :2 3 Enter the Weight of the edge 3 :-2 Enter the Vertices of the edge 4 :3 4 Enter the Weight of the edge 4 :3 Enter the Vertices of the edge 5 :4 5 Enter the Weight of the edge 5 :5 Vertex Distance from Source 1 0 2 5 3 3 4 4 5 1 PS C:\Users\Harshith\Desktop\DAA\Exp 6></pre>

Code Part 2:

A weighted, directed graph $G=(V; E)$ for the case in which all edge weights are nonnegative with source s (Dijkstra)

Source Code

```
#include<bits/stdc++.h>
using namespace std;

int V;

int minDistance(int distance[],bool sptSet[]){

    int minDist=INT_MAX;
    int minVertex=0;

    for(int i=0;i<V;i++){
        if(sptSet[i]==false && distance[i]<=minDist){
            minDist=distance[i];
            minVertex=i;
        }
    }
    return minVertex;
}

void printSolution(int dist[])
{
    cout << "\nVertex \t Distance from Source" << endl;
    for (int i = 0; i < V; i++)
        cout << i << " \t\t\t" << dist[i] << endl;
}

void dijkstra(int **graph, int src)
{
    int dist[V];

    bool sptSet[V];
```

```

for (int i = 0; i < V; i++){

    dist[i] = INT_MAX;
    sptSet[i] = false; // All s=distance initialised to INF

}

dist[src] = 0;

for (int count = 0; count < V - 1; count++) {

    int u = minDistance(dist, sptSet); //u is vertex with min distance

    sptSet[u]=true; // u included

    // Update dist value of the adjacent vertices of the picked vertex.
    for (int v = 0; v < V; v++)

        // Update dist[v] only if is not in sptSet, there is an edge from
        u to v,
        // and total weight of path from src to v through u is smaller
        than current value of dist[v]
        if (!sptSet[v] && graph[u][v] && dist[u] != INT_MAX &&
dist[u] + graph[u][v] < dist[v])
            dist[v] = dist[u] + graph[u][v];
    }

    // print the constructed distance array
    printSolution(dist);
}

int main(){

    cout<<"Enter the number of vertices :";
    cin>>V;

    int **graph=new int*[V];
    for(int i=0;i<V;i++)

```

```
{
    graph[i]=new int[V];
}

for(int i=0;i<V;i++){

    for(int j=0;j<V;j++){

        graph[i][j]=0;

    }
}

cout<<"Enter the number of edges :";
int e; cin >> e;

for(int i=0;i<e;i++){

    cout<<"\nEnter the Vertices of the edge "<<i<<" :";
    int a,b,w;

    cin>>a>>b;
    cout<<"Enter the Weight of the edge "<<i<<" :";

    cin>>w;

    graph[a][b]=w;

    graph[b][a]=w;

}

dijkstra(graph,0);

return 0;

}
```


Output 2:

```
shubham@shubham-virtual-machine:~/semester4/daa/experiments/experiment 6$ g++ dijkstra.cpp
shubham@shubham-virtual-machine:~/semester4/daa/experiments/experiment 6$ ./a.out
Enter the number of vertices :5
Enter the number of edges :6

Enter the Vertices of the edge 0 :0 1
Enter the Weight of the edge 0 :4

Enter the Vertices of the edge 1 :0 2
Enter the Weight of the edge 1 :5

Enter the Vertices of the edge 2 :1 4
Enter the Weight of the edge 2 :7

Enter the Vertices of the edge 3 :2 4
Enter the Weight of the edge 3 :10

Enter the Vertices of the edge 4 :1 3
Enter the Weight of the edge 4 :9

Enter the Vertices of the edge 5 :4 3
Enter the Weight of the edge 5 :5

Vertex    Distance from Source
0          0
1          4
2          5
3         13
4         11
shubham@shubham-virtual-machine:~/semester4/daa/experiments/experiment 6$
```

Conclusion:

Thus we have implemented Bellman Ford and Dijkstra Algorithm to find the shortest path between two nodes in a graph