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IT/Computer Engineering Department

Subject: Foundation of Signal Processing Class: TE Computer / IT SEM-VI

Assignment-3 Topic: Fast Fourier Transform Date: 10-3-2023

NOTE: [1] All questions are Compulsory.

- [2] Do not write answers for FAQs in your assignment. But you should be in a position to answer FAQs at the time of correction.
- [3] Deadline for submission of corrected assignment is 20th March 2023.
- [4] After deadline you will have to attempt all questions.

Module: 03

References:

- [1] Proakis and Manolakis, "Digital Signal Processing", 4th Edition, Pearson Education.
- [2] Ashok Ambardar, 'Digital Signal Processing', Cengage Learning, 2007, ISBN: 978-81-315-0179-5.
- [3]. Emmanuel C. Ifeachor, Barrie W. Jervis, "Digital Signal Processing: A Practical Approach", Pearson Education ISBN 0-201-59619-9
- [4] S. Salivahanan, A. Vallavaraj, C. Gnanapriya, 'Digital Signal Processing 'TataMcgraw Hill Publication First edition (2010). ISBN 978-0-07-066924-6.

>FFT Algorithms [Attempt any Two]

- Q(1) Given $x[n] = \{ 1, 1, 1, 1, 0, 0, 0, 0, 0 \}$ Find X[k] using DIT-FFT and DIF-FFT.
- Q(2) Let $x[n] = \{a, b, c, d\}$ and the corresponding DFT $X[k] = \{A, B, C, D\}$. Let $p[n] = \{a, 0, 0, b, 0, 0, c, 0, 0, d, 0, 0\}$ Find P[k] using X[k].

ANS: $P[k] = \{ A, B, C, D, A, B, C, D, A, B, C, D \}$

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- Q(3) Let $p[n] = \{1, 2, 3, 4\}$ and $q[n] = \{5, 6, 7, 8\}$. Find DFT of each of the sequence using FFT only once.
- **Q(4)** Given that $x[n] = \{ (1+2j), (1+j), (2+j), (2+2j) \}$
 - (a) Find X [k] using DIT-FFT algorithm.
 - (b) Using the results in and not otherwise find the DFT of p[n] and q[n] where $p[n] = \{1, 1, 2, 2\}$ and $q[n] = \{2, 1, 1, 2\}$.

➤ Linear Convolution and Circular Convolution using FFT [Attempt Any one]

- Q(5) Given $x[n] = \{x[0], x[1], x[2], x[3]\}$ and $h[n] = \{h[0], h[1], h[2]\}$. Give step by step procedure to obtain Circular Convolution using FFT-IFFT.
- Q(6) Given $x[n] = \{x[0], x[1], x[2], x[3]\}$ and $h[n] = \{h[0], h[1], h[2]\}$. Both are non-periodic finite length sequences. Give step by step procedure to obtain linear convolution using FFT-IFFT.
- Q(7) Impulse response of 3^{rd} order Linear Phase Low-Pass FIR filter is given by $h[n]=\{1, 2, 2, 1\}$. Give step by step procedure to find output of the filter to the input $x[n]=\{1, 2, 3, 4\}$ using FFT-IFFT.

ANS: Output of Digital filter is linear convolution of x[n] with h[n].

➤ Linear FIR Filtering [Attempt Any one]

- Q(8) Given $h[n] = \{ 1, 0, 2 \}$ Find the response of a Digital FIR filter to the input $x[n] = \{ 1, 2, 3, 4, 0, 0, 1, 2, 3, 4 \}$ using Overlap **Add** Method.
- Q(9) Given $h[n] = \{ 1, 0, 2 \}$ Find the response of a Digital FIR filter to the input $x[n] = \{ 1, 2, 3, 4, 0, 0, 1, 2, 3, 4 \}$ using Overlap **Save** Method.