

EXPERIMENT 3

Aim:

Given a grammar find the first and follow set of non-terminals.

Theory:

FIRST SET

FIRST(X) for a grammar symbol X is the set of terminals that begin the strings derivable from X.

Rules to compute FIRST set:

1. If x is a terminal, then $\text{FIRST}(x) = \{ 'x' \}$
2. If $x \rightarrow \epsilon$, is a production rule, then add ϵ to $\text{FIRST}(x)$.
3. If $X \rightarrow Y_1 Y_2 Y_3 \dots Y_n$ is a production,
 1. $\text{FIRST}(X) = \text{FIRST}(Y_1)$
 2. If $\text{FIRST}(Y_1)$ contains ϵ then $\text{FIRST}(X) = \{ \text{FIRST}(Y_1) - \epsilon \} \cup \{ \text{FIRST}(Y_2) \}$
 3. If $\text{FIRST}(Y_i)$ contains ϵ for all $i = 1$ to n , then add ϵ to $\text{FIRST}(X)$.

Example:

Production Rules of Grammar

$S \rightarrow ACB \mid Cbb \mid Ba$

$A \rightarrow da \mid BC$

$B \rightarrow g \mid \epsilon$

$C \rightarrow h \mid \epsilon$

FIRST sets

$\text{FIRST}(S) = \text{FIRST}(ACB) \cup \text{FIRST}(Cbb) \cup \text{FIRST}(Ba)$

$= \{ d, g, h, b, a, \epsilon \}$

$\text{FIRST}(A) = \{ d \} \cup \text{FIRST}(BC)$

$= \{ d, g, h, \epsilon \}$

$\text{FIRST}(B) = \{ g, \epsilon \}$

$\text{FIRST}(C) = \{ h, \epsilon \}$

1. The grammar used above is Context-Free Grammar (CFG). Syntax of most of the programming language can be specified using CFG.
2. CFG is of the form $A \rightarrow B$, where A is a single Non-Terminal, and B can be a set of grammar symbols (i.e. Terminals as well as Non-Terminals)

FOLLOW SET

Follow(X) to be the set of terminals that can appear immediately to the right of Non-Terminal X in some sentential form.

Rules to compute FOLLOW set:

1. $\text{FOLLOW}(S) = \{ \$ \}$ // where S is the starting Non-Terminal
2. If $A \rightarrow pBq$ is a production, where p, B and q are any grammar symbols, then everything in $\text{FIRST}(q)$ except ϵ is in $\text{FOLLOW}(B)$.
3. If $A \rightarrow pB$ is a production, then everything in $\text{FOLLOW}(A)$ is in $\text{FOLLOW}(B)$.
4. If $A \rightarrow pBq$ is a production and $\text{FIRST}(q)$ contains ϵ , then $\text{FOLLOW}(B)$ contains $\{ \text{FIRST}(q) - \epsilon \} \cup \text{FOLLOW}(A)$

Example:

Production Rules:

$E \rightarrow TE'$
 $E' \rightarrow +TE' \mid \epsilon$
 $T \rightarrow FT'$
 $T' \rightarrow *FT' \mid \epsilon$
 $F \rightarrow (E) \mid \text{id}$

FIRST set

$\text{FIRST}(E) = \text{FIRST}(T) = \{ (, \text{id} \}$
 $\text{FIRST}(E') = \{ +, \epsilon \}$
 $\text{FIRST}(T) = \text{FIRST}(F) = \{ (, \text{id} \}$
 $\text{FIRST}(T') = \{ *, \epsilon \}$
 $\text{FIRST}(F) = \{ (, \text{id} \}$

FOLLOW Set

$\text{FOLLOW}(E) = \{ \$,) \}$ // Note ')' is there because of 5th rule
 $\text{FOLLOW}(E') = \text{FOLLOW}(E) = \{ \$,) \}$ // See 1st production rule
 $\text{FOLLOW}(T) = \{ \text{FIRST}(E') - \epsilon \} \cup \text{FOLLOW}(E') \cup \text{FOLLOW}(E) = \{ +, \$,) \}$
 $\text{FOLLOW}(T') = \text{FOLLOW}(T) = \{ +, \$,) \}$
 $\text{FOLLOW}(F) = \{ \text{FIRST}(T') - \epsilon \} \cup \text{FOLLOW}(T') \cup \text{FOLLOW}(T) = \{ *, +, \$,) \}$

1. ϵ as a FOLLOW doesn't mean anything (ϵ is an empty string).
2. \$ is called end-marker, which represents the end of the input string, hence used while parsing to indicate that the input string has been completely processed.
3. The grammar used above is Context-Free Grammar (CFG). The syntax of a programming language can be specified using CFG.
4. CFG is of the form $A \rightarrow B$, where A is a single Non-Terminal, and B can be a set of grammar symbols (i.e. Terminals as well as Non-Terminals)

Implementation

Code:

```
def first_set(var):
    global productions, variables, terminals
    first = set()
    prods = []
    if var in terminals:
        return {var}

    for production in productions:
        if production[0] == var:
            prods.append(production[1])
    for prod in prods:
        if len(prod)==0:
            first.add('')
        elif prod[0] in terminals:
            first.add(prod[0])
        else:
            c = 0
            flag = True
            while flag:
                first_var = first_set(prod[c])
                if '' in first_var:
                    first_var.remove('')
                else:
                    flag=False

                first = first|first_var
                c+=1
                if c== len(prod) and flag:
                    first.add('')
                    flag = False

    return first

def follow_set(var):
    global productions, variables, terminals, starting
    prods = []
    for production in productions:
        if var in production[1]:
            prods.append(production)
    follow = set()

    if var == starting:
```

```

        follow.add('$')

    for prod in prods:
        pos = []
        for i in range(len(prod[1])):
            if prod[1][i] == var:
                try:
                    if pos[-1]==i-1:
                        pos[-1]+=1
                    else:
                        pos.append(i)
                except:
                    pos.append(i)
        for p in pos:
            if p == len(prod[1])-1:
                if prod[0]!=var:
                    follow = follow|follow_set(prod[0])
            else:
                first_next= first_set(prod[1][p+1])
                if '' in first_next:
                    if prod[0] != var:
                        follow = follow|follow_set(prod[0])
                    first_next.remove('')
                follow = follow|first_next
    return follow

terminals = set()
variables = set()
productions = []
starting = ''

while True:
    lhs = input(" + Enter the LHS of the production: ")
    rhs = input(" + Enter the RHS of the production: ")

    variables.add(lhs)
    for i in rhs:
        if i.lower() == i:
            terminals.add(i)
        else:
            variables.add(i)

    if len(rhs)==0:

```

```

        productions.append((lhs, ''))
        terminals.add('')
    else:
        productions.append((lhs, [i for i in rhs]))

    end = input(" - Any more productions? (y/n) :- ")
    if end == 'n':
        break

starting = input(" + Enter the starting non terminal: ")

first = dict()
follow = dict()

for i in variables:
    first[i] = first_set(i)
    follow[i] = follow_set(i)

print("-----FIRST-----")
for i in sorted(list(variables)):
    print(' ', i, first[i])

print("-----FOLLOW-----")
for i in sorted(list(variables)):
    print(' ', i, follow[i])

```

Result:

Explanation:

S->aBbDh	First(S)={a}
B->cC	First(B)={c}
C->bc/ ϵ	First(C)={b/ ϵ }
D->EF	First(D)={First(E)- ϵ U First (F)}={g,f, ϵ }
E->g/ ϵ	First(E) = {g, ϵ }
F->f/ ϵ	First(F) = {f, ϵ }
	Follow(S)={}
	Follow(B)={b}
	Follow(C)={b}
	Follow(D)={h}
	Follow(E)={f,h}
	Follow(F)={h}

Output: (considering ' ' as ϵ)

```
PS D:\SPIT\SEM 6\CC Lab> py exe3.py
+ Enter the LHS of the production: S
+ Enter the RHS of the production: aBbDh
- Any more productions? (y/n) :- y
+ Enter the LHS of the production: B
+ Enter the RHS of the production: cC
- Any more productions? (y/n) :- y
+ Enter the LHS of the production: C
+ Enter the RHS of the production: bc
- Any more productions? (y/n) :- y
+ Enter the LHS of the production: C
+ Enter the RHS of the production:
- Any more productions? (y/n) :- y
+ Enter the LHS of the production: D
+ Enter the RHS of the production: EF
- Any more productions? (y/n) :- y
+ Enter the LHS of the production: E
+ Enter the RHS of the production: g
- Any more productions? (y/n) :- y
+ Enter the LHS of the production: E
+ Enter the RHS of the production:
- Any more productions? (y/n) :- y
+ Enter the LHS of the production: F
+ Enter the RHS of the production: f
- Any more productions? (y/n) :- y
+ Enter the LHS of the production: F
+ Enter the RHS of the production:
- Any more productions? (y/n) :- n
+ Enter the starting non terminal: S

-----FIRST-----
B {'c'}
C {'', 'b'}
D {'', 'g', 'f'}
E {'', 'g'}
F {'', 'f'}
S {'a'}

-----FOLLOW-----
B {'b'}
C {'b'}
D {'h'}
E {'f', 'h'}
F {'h'}
S {'$'}
```

```

PS D:\SPIT\SEM 6\CC Lab> py exe3.py
+ Enter the LHS of the production: S
+ Enter the RHS of the production: AaAb
- Any more productions? (y/n) :- y
+ Enter the LHS of the production: S
+ Enter the RHS of the production: BbBa
- Any more productions? (y/n) :- y
+ Enter the LHS of the production: A
+ Enter the RHS of the production:
- Any more productions? (y/n) :- y
+ Enter the LHS of the production: B
+ Enter the RHS of the production:
- Any more productions? (y/n) :- n
+ Enter the starting non terminal: S

```

-----FIRST-----

```

A {''}
B {''}
S {'a', 'b'}

```

-----FOLLOW-----

```

A {'a', 'b'}
B {'a', 'b'}
S {'$'}

```

S->AaAb/BbBa

A->ε

B->ε

First(A)={ε}

First(B)={ε}

First(S)={First(A)- ε U First(a)} U {First(B)- ε U First(b)={a,b}}

Follow(S)={\$}

Follow(A)={a,b}

Follow(B)={b,a}

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Conclusion:

From the above experiment, I was able to implement code and programmatically execute and verify the working of FIRST and FOLLOW SET by finding it for a given grammar.

Ref.:

- <https://www.geeksforgeeks.org/first-set-in-syntax-analysis/>
- <https://www.geeksforgeeks.org/follow-set-in-syntax-analysis/>