

1. (4 points) Give an example of a programming language for each category in this  $2 \times 2$  matrix:

	Imperative	Functional
Static		
Dynamic		

AST

2. (7 points) Draw a ~~program~~ for the expression  $2 + 3^2 * 4$ , assuming the usual operator precedence (here  $\wedge$  is exponentiation).

3. (5 points) What would the following program print?

```
def f(x):
    return [ i**x for i in range(2, 6) ]

result = f(3)
print(result[2])
```

4. (8 points) Write Python code that has the same effect as this list comprehension, without using a list comprehension or map:

```
result = [ f(x) for x in range(n) ]
```

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5. (8 points) Show the parse tree resulting from the input "if  $x > y$  then  $x = 4$ " using the following grammar:

$\langle \text{stmt} \rangle ::= \langle \text{ifstmt} \rangle \mid \langle \text{assignstmt} \rangle$   
 $\langle \text{ifstmt} \rangle ::= \text{if } \langle \text{expr} \rangle \text{ then } \langle \text{stmt} \rangle$   
 $\langle \text{assignstmt} \rangle ::= \langle \text{var} \rangle = \langle \text{expr} \rangle$   
 $\langle \text{expr} \rangle ::= \langle \text{expr} \rangle = \langle \text{expr} \rangle \mid \langle \text{expr} \rangle > \langle \text{expr} \rangle \mid \langle \text{var} \rangle \mid \langle \text{num} \rangle$   
 $\langle \text{var} \rangle ::= a \mid b \mid c \mid \dots \mid y \mid z$   
 $\langle \text{num} \rangle ::= 0 \mid 1 \mid 2 \mid \dots \mid 9$

6. (8 points) Recall the Church booleans in lambda calculus:

- $\lambda x. \lambda y. x \equiv \text{true}$
- $\lambda x. \lambda y. y \equiv \text{false}$

Write the Boolean "nand" function (which is true as long as at least one of its two inputs is false) in lambda calculus and show its operation on inputs "true false".

7. (3 points) Draw the following bit patterns of memory cells (a, b, c, d, e)

a. 8 bytes using the following binary code

Address 0	0000 0000
Address 1	0000 0001
Address 2	0000 0010
Address 3	0000 0011
Address 4	0000 0100
Address 5	0000 0101
Address 6	0000 0110
Address 7	0000 0111

b. What is the memory address of containing the following expression? If the result is a function, just write "function". If there is no result, write "void".

`int a`

`int b = 0`

`int c = a`

`if (a`

`> b) {`

`c = a;`

8. (3 points) Write an expression that gives the last element of a list but uses only one and/or

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10. (8 points) Write a Racket function to count the number of 0's in a (non-nested) list using reduce (without using filter).
11. (8 points) Write a Racket function "append" that takes two lists and returns a single list with all elements of the first list (in order) followed by all elements of the second list (in order). That is,  
`(append '(1 2 (3)) '((4) (5 6))) = '(1 2 (3) (4) (5 6)).`
12. (10 points) Write a Racket function "curry" that converts a two argument function to a series of one argument functions, so that instead of calling it as `(f x y)`, we can call `((curry f) x) y`.

13. (10 points) Given the following Haskell code:

```
x :: Int
x = 42
```

```
y :: Int
y = 10
```

```
f :: Int -> Int -> Int -> Int
f x y z
| x > y      = if x > z then x else z
| x == y     = z
| otherwise   = f (x+2) z y
```

```
g :: Int -> Int
g 0 = 1
g 1 = 3
g n = n * g(n - 2)
```

What is the result of evaluating the following expressions? If the result is a function, just write "function". If there's an error or it doesn't produce a value, write "error".

$x > y$  \_\_\_\_\_

$x / y$  \_\_\_\_\_

$\text{if } x \text{ then } 1 \text{ else } 2$  \_\_\_\_\_

$\text{mod } x \text{ } y$  \_\_\_\_\_

$f 3$  \_\_\_\_\_

$f 5 \text{ } 4 \text{ } 3$  \_\_\_\_\_

$\text{map } (f \text{ } 5 \text{ } 4) [3..6]$  \_\_\_\_\_

$f 3 \text{ } 4 \text{ } 5$  \_\_\_\_\_

$g 3$  \_\_\_\_\_

$g (-3)$  \_\_\_\_\_

14. (5 points) Write a Haskell expression to count the number of 0's in a (non-empty) list using filter.

count0s xs =