

Probability

$\frac{6}{6} \rightarrow$ chances of event occurring.

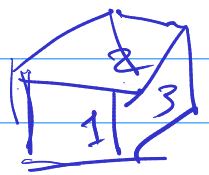
$$\text{Probability (P)} = \frac{\text{no. of favorable outcome}}{\text{Total outcome.}}$$

one ① Tossing a coin = $\{H, T\} = 2$ Total

$$P(H) = \frac{1}{2}$$

$$P(T) = \frac{1}{2}$$

one ② Throwing a Dice = $\{1, 2, 3, 4, 5, 6\}$
= 6



$$P(1) = \frac{1}{6} \quad P(2) = \frac{1}{6} \quad P(3) = \frac{1}{6} \quad P(4) = \frac{1}{6}$$

$$P(5) = \frac{1}{6} \quad P(6) = \frac{1}{6}$$

no. of events occurring
two dice

Total outcome = $\{36\} = \text{outcome}$

= $\{1, 1\} \{1, 2\} \{1, 3\} (1, 4) (1, 5) (1, 6)$
 $(2, 1) (2, 2) (2, 3) - - - -$

$- - - -$
 $(6, 1) (6, 2) (6, 3) (6, 4) (6, 5) (6, 6)$

$P(2) = (1,1) = \frac{1}{36} \rightarrow$ Total chance.

$P(3) = (1,2)(2,1) = \frac{2}{36}$

$P(4) = (1,3)(3,1)(2,2) = \frac{3}{36}$

$P(11) = (1,5)(5,1) = \frac{2}{36}$

$P(12) = (6,6) = \frac{1}{36}$

Probability Distribution

It is a list of all possible outcome of Random Variable along with their corresponding probability.

Throwing a dice.

1	2	3	4	5	6
$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$

one event

Two dice
3 dice?

Probability Distribution Function

It is a mathematical expression that describe the probability of different possible outcome for an experiment.

$$Y = f(x) = Y = \begin{cases} \frac{1}{6} & \text{if } x \in (1, 2, 3, 4, 5, 6) \\ 0 & \text{otherwise.} \end{cases}$$

Two Type of Probability Distribution.

① Discrete Distribution

ex = no. of student in class.

② Continuous Distribution.

ex: height, Distance, Weight, BP, Time.

Discrete Distribution

① Probability Mass Function. (PMF)

② Cumulative Mass function. (CMF)

Continuous Distribution.

① probability Density function. (PDF)

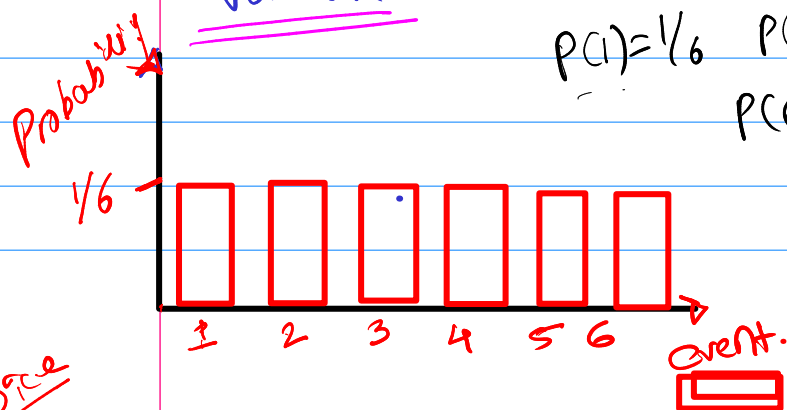
② Cumulative Distribution function. (CDF)

A. Probability Mass Function. (PMF).

⇒ It is a statistical term that describes the probability Distribution of a discrete random variable.

$$P(1) = 1/6 \quad P(2) = 1/6 \quad P(3) = 1/6 \quad P(4) = 1/6 \quad P(5) = 1/6 \\ P(6) = 1/6.$$

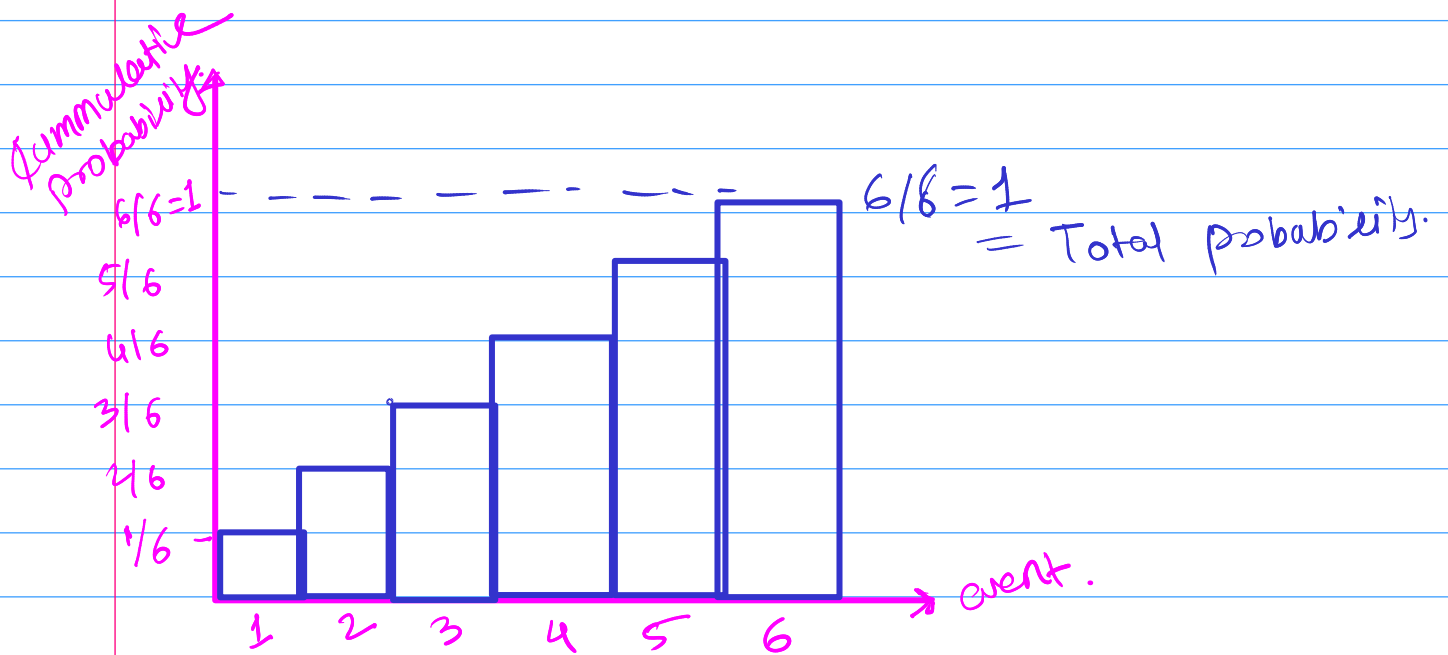
$$P(x \leq 4) = P(1) + P(2) + P(3) + P(4) \\ = 1/6 + 1/6 + 1/6 + 1/6 = \frac{4}{6} = \frac{2}{3}$$



B. Cumulative Mass Function (CMF)

It is another method to describe cumulative probability of Discrete random variable.

ex $1, 1, 2, 3, 5, 8, 13,$



C. Probability Density Function (PDF)

It is a statistical term that describe the probability distribution of continuous random variable.

ex = Age. in 10th class.

data = [16, 17, 18, 19, 20, 21, ...] 100 student

$$16 = 1$$

$$20 = 16$$

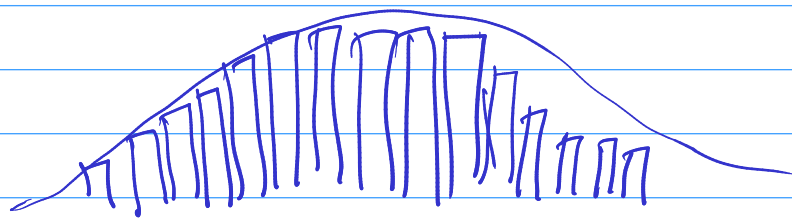
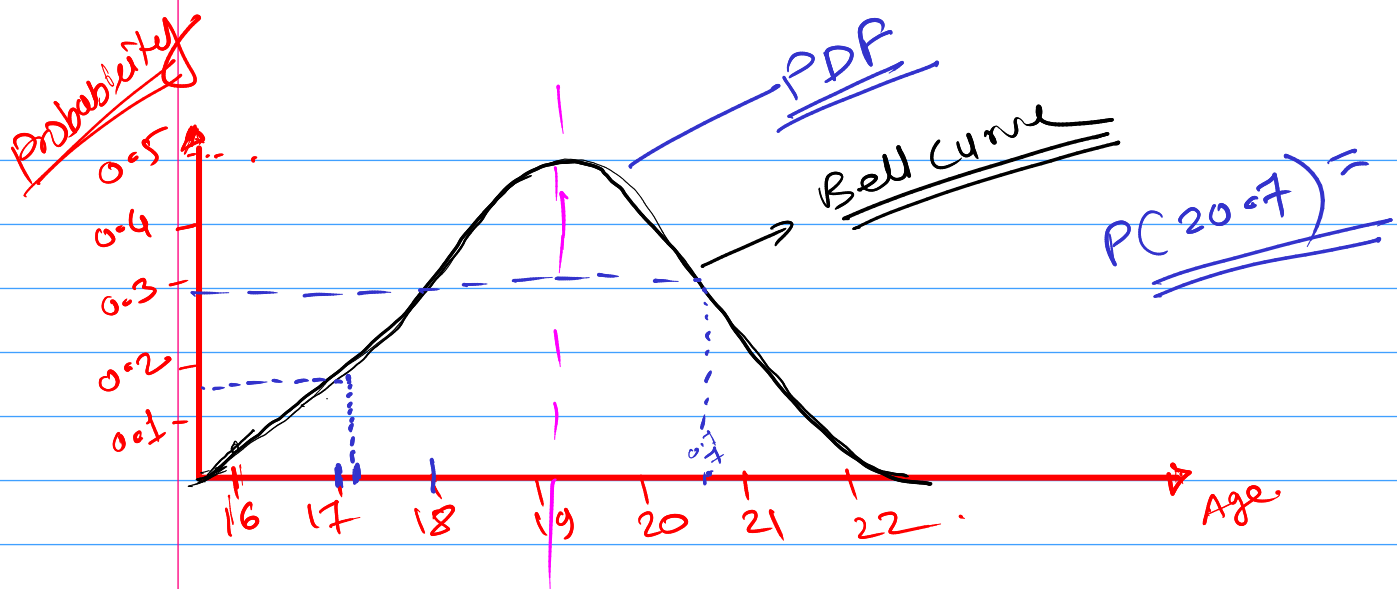
$$17 = 2$$

$$21 = 1$$

$$18 = 20$$

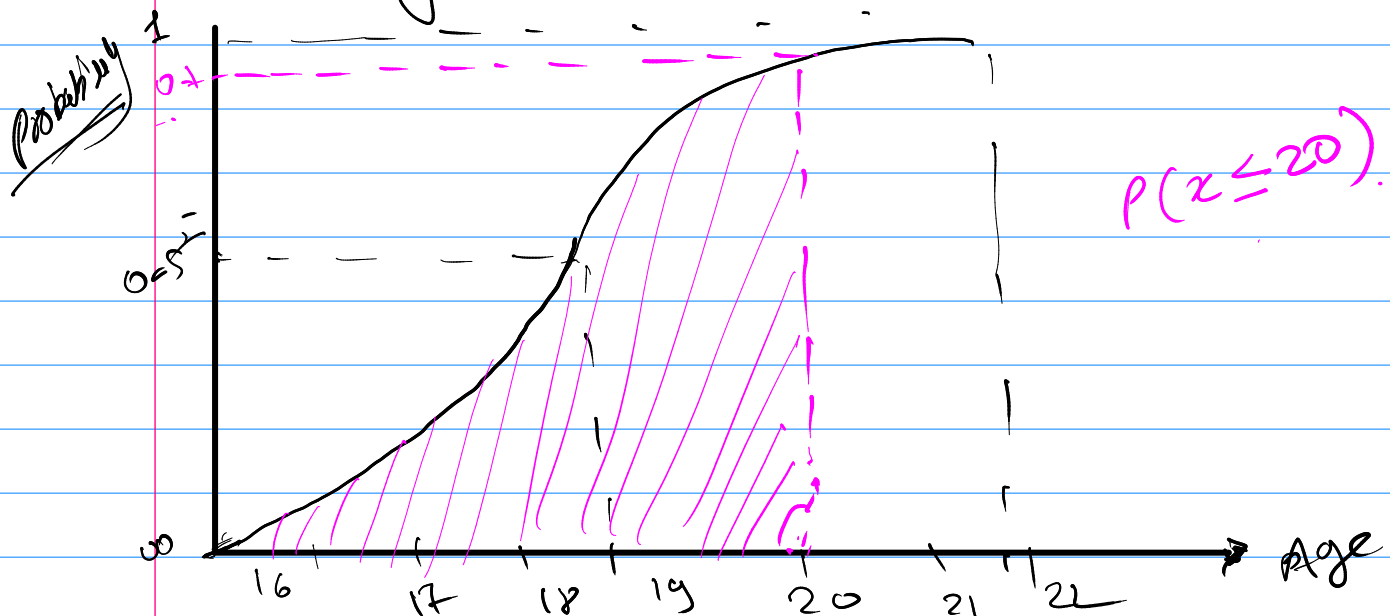
$$19 = 40$$

→ Normal distribution.



D. Cumulative Distribution Function (CDF)

It is another method to describe the total distribution of Continuous Random Variable.



Standard distribution

- ① Normal.
- ② Bernoulli
- ③ Binomial.
- ④ Standard normal.
- ⑤ Uniform.
- ⑥ Poisson.
- ⑦ Log-normal.