

# Chapter 30 Cryptography

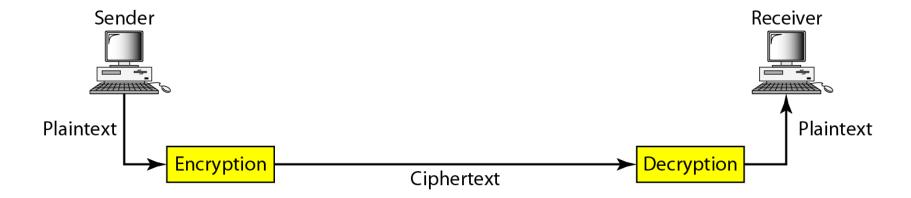
#### **30-1 INTRODUCTION**

Let us introduce the issues involved in cryptography. First, we need to define some terms; then we give some taxonomies.

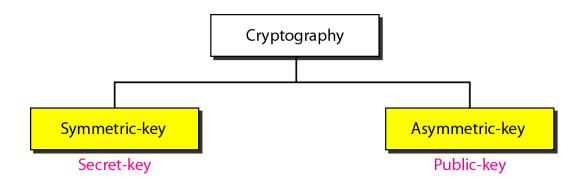
Topics discussed in this section:

**Definitions Two Categories** 

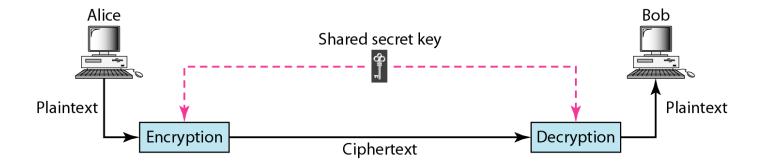
#### Figure 30.1 Cryptography components



#### Figure 30.2 Categories of cryptography



#### Figure 30.3 Symmetric-key cryptography

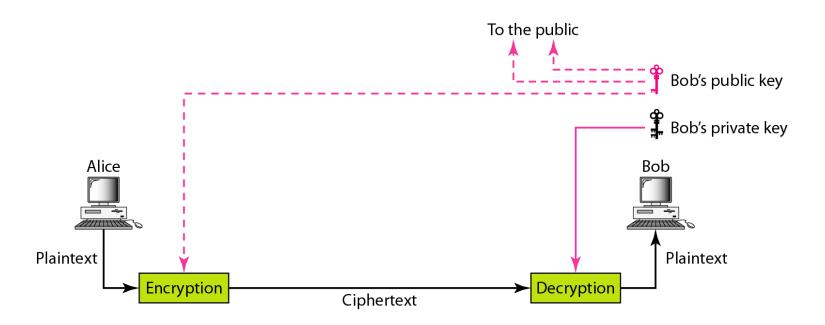


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#### Note

In symmetric-key cryptography, the same key is used by the sender (for encryption) and the receiver (for decryption). The key is shared.

#### Figure 30.4 Asymmetric-key cryptography



#### Figure 30.5 Keys used in cryptography

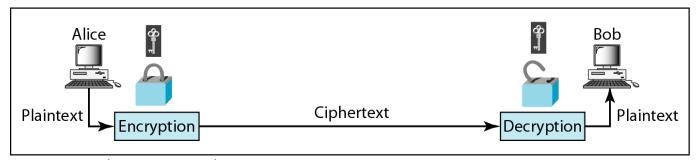


Symmetric-key cryptography

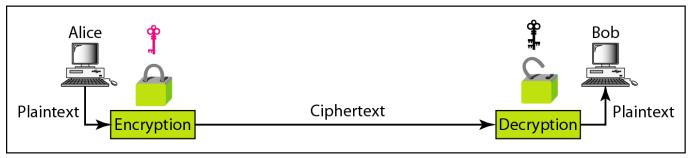


Asymmetric-key cryptography

#### Figure 30.6 Comparison between two categories of cryptography



a. Symmetric-key cryptography



b. Asymmetric-key cryptography

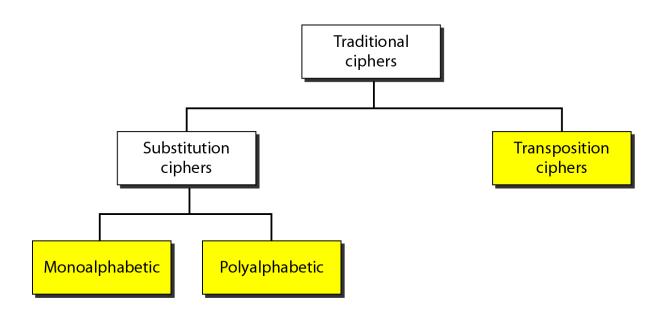
#### **30-2 SYMMETRIC-KEY CRYPTOGRAPHY**

Symmetric-key cryptography started thousands of years ago when people needed to exchange secrets (for example, in a war). We still mainly use symmetric-key cryptography in our network security.

#### Topics discussed in this section:

Traditional Ciphers
Simple Modern Ciphers
Modern Round Ciphers
Mode of Operation

#### Figure 30.7 Traditional ciphers





#### Note

## A substitution cipher replaces one symbol with another.

## Example 30.1

The following shows a plaintext and its corresponding ciphertext. Is the cipher monoalphabetic?

**Plaintext: HELLO** 

Ciphertext: KHOOR

#### Solution

The cipher is probably monoalphabetic because both occurrences of L's are encrypted as O's.

### Example 30.2

The following shows a plaintext and its corresponding ciphertext. Is the cipher monoalphabetic?

**Plaintext: HELLO** 

**Ciphertext:** ABNZF

#### Solution

The cipher is not monoalphabetic because each occurrence of L is encrypted by a different character. The first L is encrypted as N; the second as Z.

Note

## The shift cipher is sometimes referred to as the Caesar cipher.

### Example 30.3

Use the shift cipher with key = 15 to encrypt the message "HELLO."

#### Solution

We encrypt one character at a time. Each character is shifted 15 characters down. Letter H is encrypted to W. Letter E is encrypted to T. The first L is encrypted to A. The second L is also encrypted to A. And O is encrypted to D. The cipher text is WTAAD.

## Example 30.4

Use the shift cipher with key = 15 to decrypt the message "WTAAD."

#### Solution

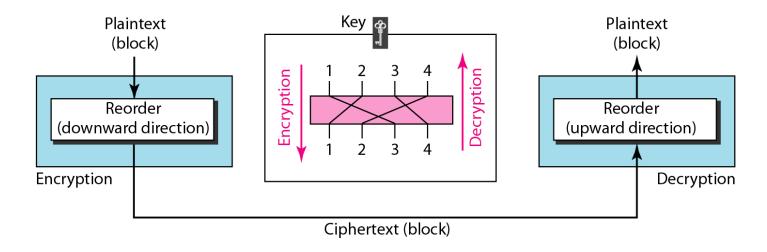
We decrypt one character at a time. Each character is shifted 15 characters up. Letter W is decrypted to H. Letter T is decrypted to E. The first A is decrypted to L. The second A is decrypted to L. And, finally, D is decrypted to O. The plaintext is HELLO.

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#### Note

# A transposition cipher reorders (permutes) symbols in a block of symbols.

#### Figure 30.8 Transposition cipher



## Example 30.5

Encrypt the message "HELLO MY DEAR," using the key shown in Figure 30.8.

#### Solution

We first remove the spaces in the message. We then divide the text into blocks of four characters. We add a bogus character Z at the end of the third block. The result is HELL OMYD EARZ. We create a three-block ciphertext ELHLMDOYAZER.

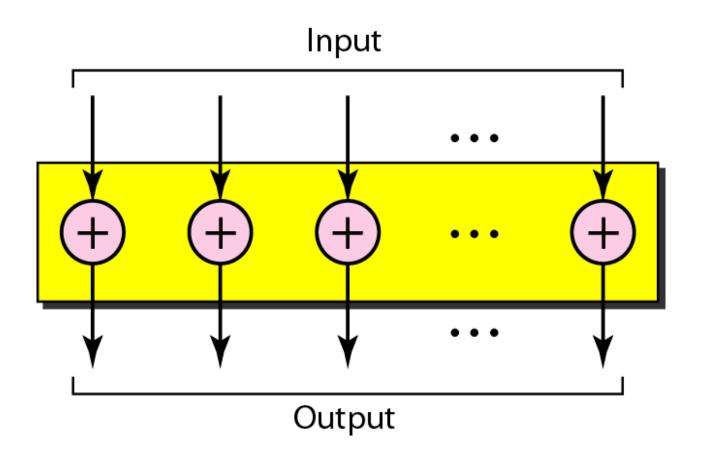
## Example 30.6

Using Example 30.5, decrypt the message "ELHLMDOYAZER".

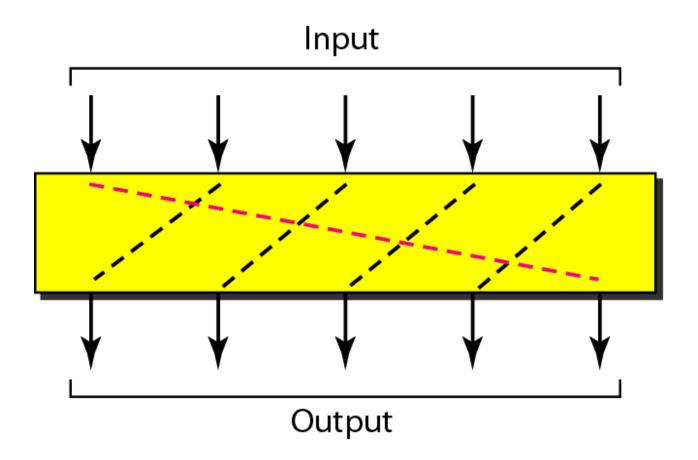
#### Solution

The result is HELL OMYD EARZ. After removing the bogus character and combining the characters, we get the original message "HELLO MY DEAR."

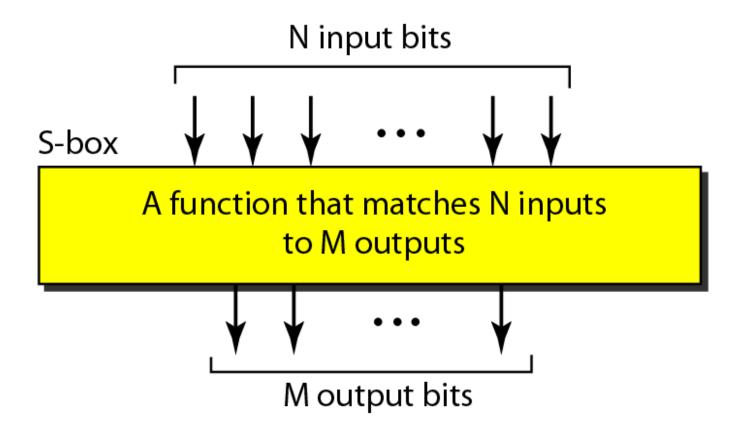
#### Figure 30.9 XOR cipher



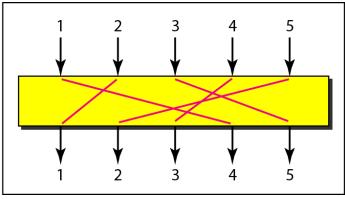
#### Figure 30.10 Rotation cipher



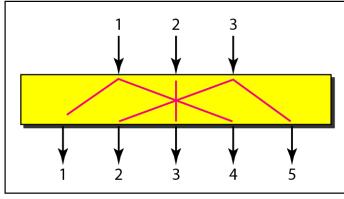
#### **Figure 30.11** *S-box*



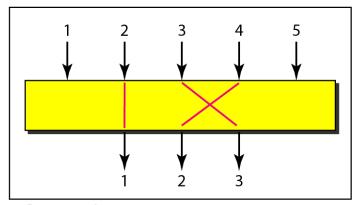
#### Figure 30.12 P-boxes: straight, expansion, and compression



a. Straight

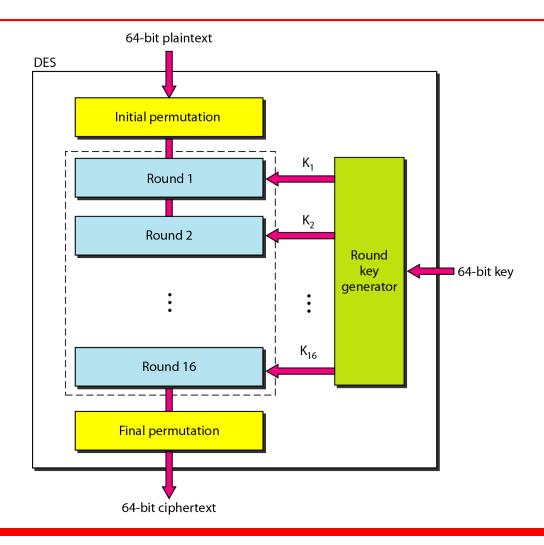


b. Expansion

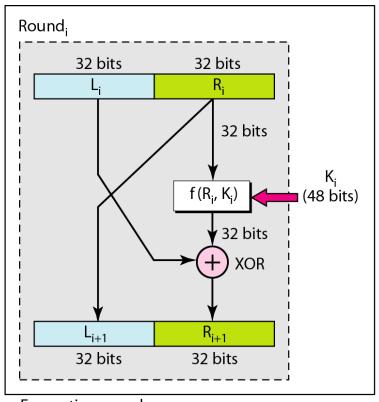


c. Compression

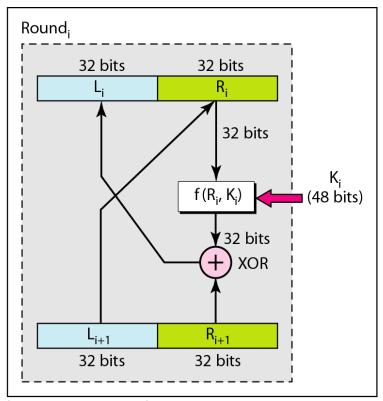
#### **Figure 30.13** *DES*



#### Figure 30.14 One round in DES ciphers

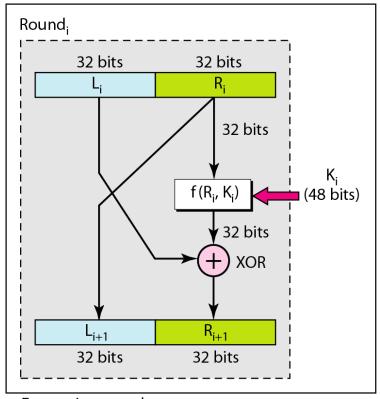


a. Encryption round

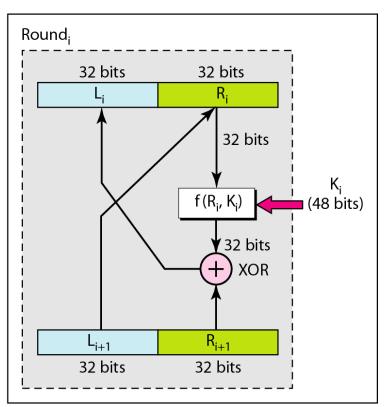


b. Decryption round

#### Figure 30.15 DES function

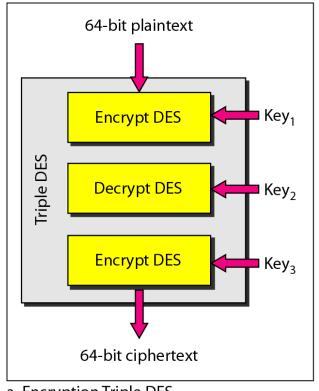


a. Encryption round

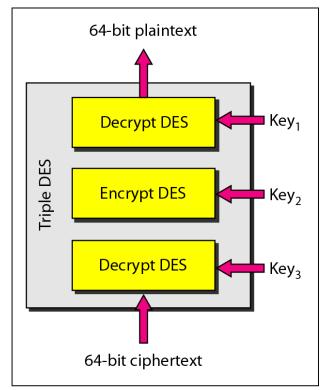


b. Decryption round

#### Figure 30.16 Triple DES



a. Encryption Triple DES



b. Decryption Triple DES

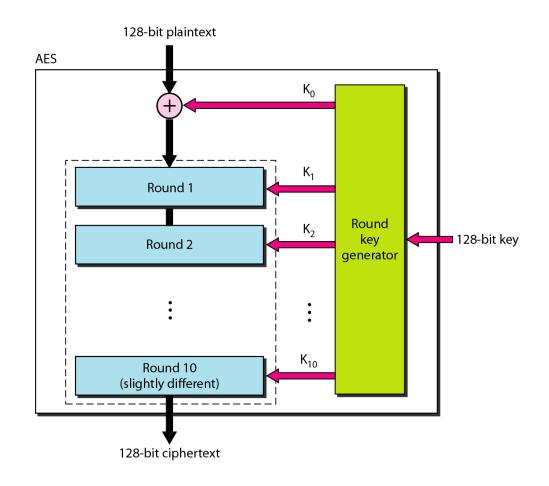
#### Table 30.1 AES configuration

Size of Data Block	Number of Rounds	Key Size
128 bits	10	128 bits
	12	192 bits
	14	256 bits

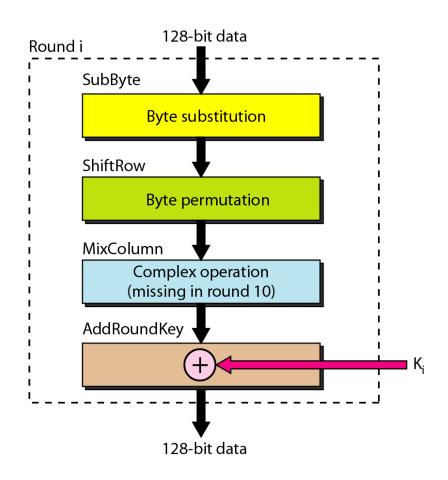
Note

# AES has three different configurations with respect to the number of rounds and key size.

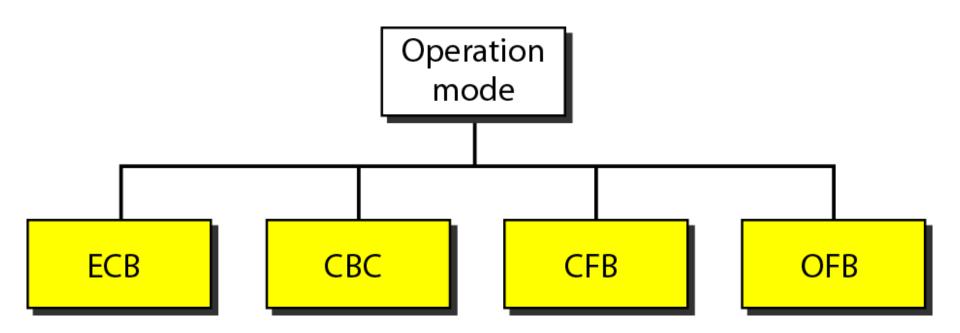
#### **Figure 30.17** *AES*



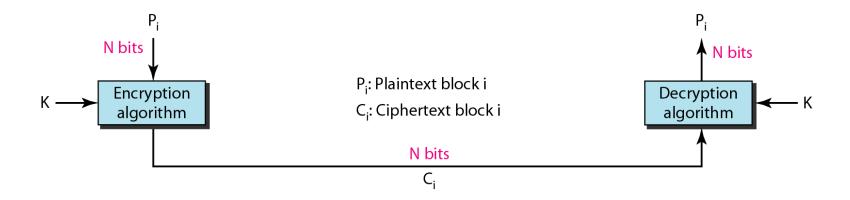
#### Figure 30.18 Structure of each round



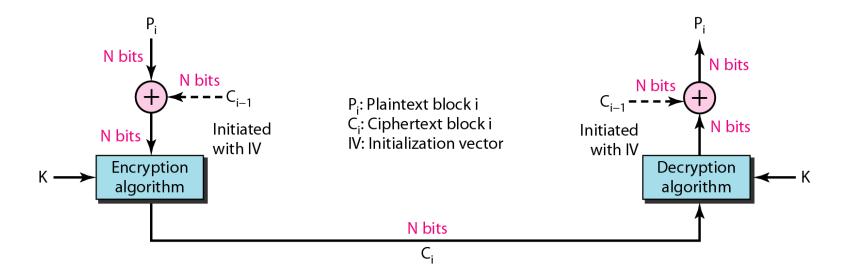
#### Figure 30.19 Modes of operation for block ciphers



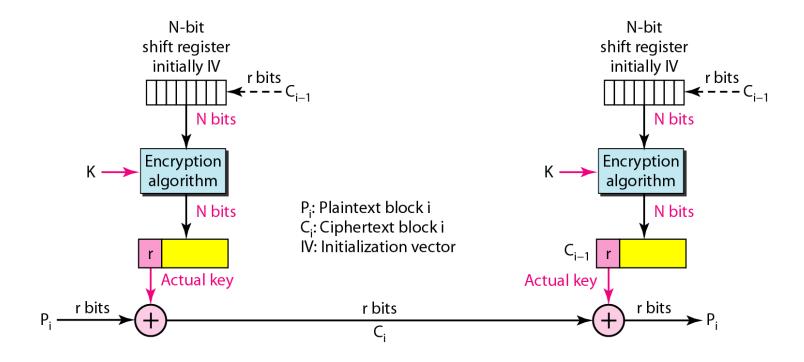
#### Figure 30.20 ECB mode



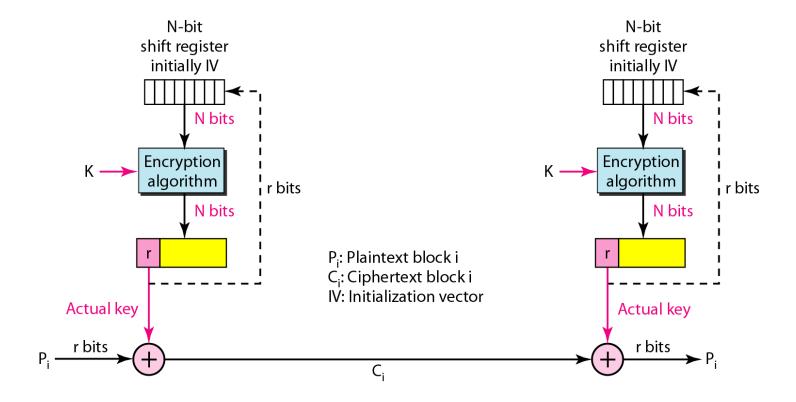
#### Figure 30.21 CBC mode



#### Figure 30.22 CFB mode



#### Figure 30.23 OFB mode



#### **30-3 ASYMMETRIC-KEY CRYPTOGRAPHY**

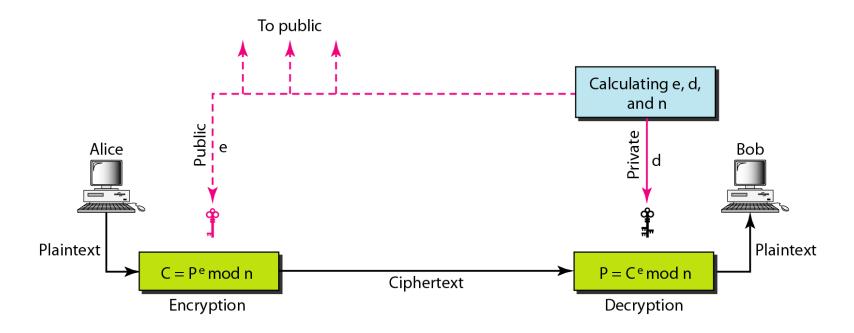
An asymmetric-key (or public-key) cipher uses two keys: one private and one public. We discuss two algorithms: RSA and Diffie-Hellman.

Topics discussed in this section:

RSA

**Diffie-Hellman** 

#### Figure 30.24 RSA



Note

In RSA, e and n are announced to the public; d and  $\Phi$  are kept secret.

Bob chooses 7 and 11 as p and q and calculates  $n = 7 \cdot 11 = 77$ . The value of  $\Phi = (7 - 1)(11 - 1)$  or 60. Now he chooses two keys, e and d. If he chooses e to be 13, then d is 37. Now imagine Alice sends the plaintext 5 to Bob. She uses the public key 13 to encrypt 5.

Plaintext: 5

 $C = 5^{13} = 26 \mod 77$ 

Ciphertext: 26

# E

#### Example 30.7 (continued)

Bob receives the ciphertext 26 and uses the private key 37 to decipher the ciphertext:

Ciphertext: 26

 $P = 26^{37} = 5 \mod 77$ 

Plaintext: 5

The plaintext 5 sent by Alice is received as plaintext 5 by Bob.

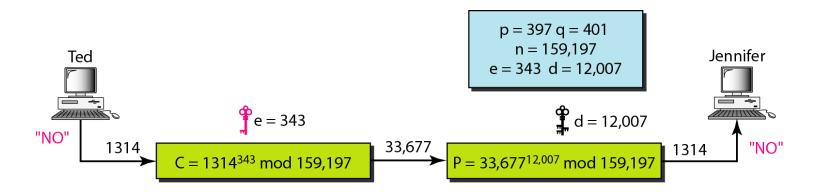
Jennifer creates a pair of keys for herself. She chooses p = 397 and q = 401. She calculates n = 159,197 and  $\Phi = 396 \cdot 400 = 158,400$ . She then chooses e = 343 and d = 12,007. Show how Ted can send a message to Jennifer if he knows e and e.

### Example 30.8 (continuted)

#### Solution

Suppose Ted wants to send the message "NO" to Jennifer. He changes each character to a number (from 00 to 25) with each character coded as two digits. He then concatenates the two coded characters and gets a fourdigit number. The plaintext is 1314. Ted then uses e and n to encrypt the message. The ciphertext is  $1314^{343} = 33,677$ mod 159,197. Jennifer receives the message 33,677 and uses the decryption key d to decipher it as  $33.677^{12,007}$  = 1314 mod 159,197. Jennifer then decodes 1314 as the message "NO". Figure 30.25 shows the process.

#### **Figure 30.25** *Example 30.8*



Let us give a realistic example. We randomly chose an integer of 512 bits. The integer p is a 159-digit number.

```
p = 96130345313583504574191581280615427909309845594996215822583150879647940 45505647063849125716018034750312098666606492420191808780667421096063354 219926661209
```

#### The integer q is a 160-digit number.

 $\mathbf{q} = 12060191957231446918276794204450896001555925054637033936061798321731482\\ 14848376465921538945320917522527322683010712069560460251388714552496900\\ 0359660045617$ 

### Example 30.9 (continued)

#### We calculate n. It has 309 digits:

**n** = 11593504173967614968892509864615887523771457375454144775485526137614788 54083263508172768788159683251684688493006254857641112501624145523391829 27162507656772727460097082714127730434960500556347274566628060099924037 10299142447229221577279853172703383938133469268413732762200096667667183 1831088373420823444370953

#### We calculate $\Phi$ . It has 309 digits:



#### Example 30.9 (continued)

We choose e = 35,535. We then find d.

```
e = 35535
```

**d** = 58008302860037763936093661289677917594669062089650962180422866111380593852 82235873170628691003002171085904433840217072986908760061153062025249598844 48047568240966247081485817130463240644077704833134010850947385295645071936 77406119732655742423721761767462077637164207600337085333288532144708859551 36670294831

Alice wants to send the message "THIS IS A TEST" which can be changed to a numeric value by using the 00–26 encoding scheme (26 is the space character).

 $\mathbf{P} = 1907081826081826002619041819$ 

### Example 30.9 (continued)

The ciphertext calculated by Alice is  $C = P^e$ , which is.

C = 4753091236462268272063655506105451809423717960704917165232392430544529 6061319932856661784341835911415119741125200568297979457173603610127821 8847892741566090480023507190715277185914975188465888632101148354103361 6578984679683867637337657774656250792805211481418440481418443081277305 9004692874248559166462108656

## Bob can recover the plaintext from the ciphertext by using $P = C^d$ , which is

 $\mathbf{P} = 1907081826081826002619041819$ 

The recovered plaintext is THIS IS A TEST after decoding.

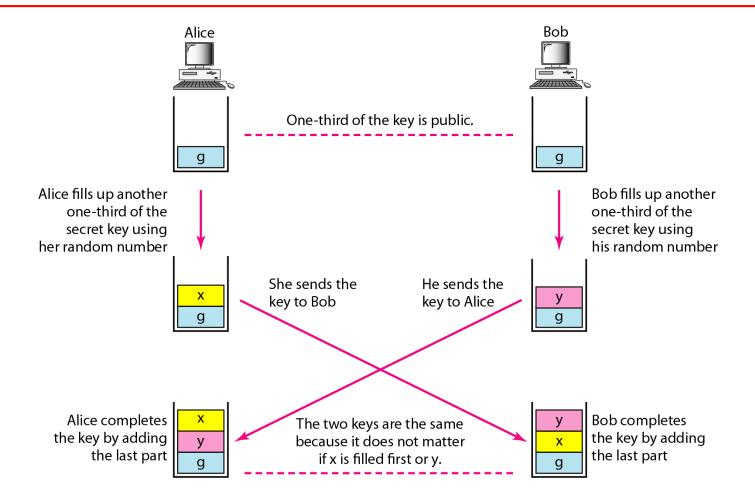
Note

### The symmetric (shared) key in the Diffie-Hellman protocol is K = g<sup>xy</sup> mod p.

Let us give a trivial example to make the procedure clear. Our example uses small numbers, but note that in a real situation, the numbers are very large. Assume g = 7 and p = 23. The steps are as follows:

- 1. Alice chooses x = 3 and calculates  $R_1 = 7^3 \mod 23 = 21$ .
- 2. Bob chooses y = 6 and calculates  $R_2 = 7^6 \mod 23 = 4$ .
- 3. Alice sends the number 21 to Bob.
- 4. Bob sends the number 4 to Alice.
- 5. Alice calculates the symmetric key  $K = 4^3 \mod 23 = 18$ .
- 6. Bob calculates the symmetric key  $K = 21^6 \mod 23 = 18$ . The value of K is the same for both Alice and Bob;  $g^{xy} \mod p = 7^{18} \mod 23 = 18$ .

#### Figure 30.27 Diffie-Hellman idea



#### Figure 30.28 Man-in-the-middle attack

