

Tutorial-9
PHYSICS-2

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Batch: F2

1. (i) $a \neq b \neq c$
 $\alpha \neq \beta \neq \gamma$
 \Rightarrow Triclinic

(ii) $a = b \neq c$
 $\alpha = \beta = 90^\circ, \gamma = 120^\circ$
 \Rightarrow Hexagonal

(iii) $a = b = c$
 $\alpha = \beta = \gamma = 90^\circ$
 \Rightarrow Cubic

2. NaCl is FCC structure where contribution of all corners Na^+ ions in unit cell will be -

$$N_c = 8 \times \frac{1}{8} = 1$$

And face centred Na^+ ions

$$N_f = 6 \times \frac{1}{2} = 3$$

Contribution of Cl^- ions in unit cell $= \left(\frac{1}{4} \times 12\right) + 1 (\text{bcc Cl}^-)$

So total no. of Na^+ ions = 4 and Cl^- ions = 4

Therefore total no. of NaCl molecules per unit cell will be

$$[4] \text{Na}^+ + [4] \text{Cl}^- = 4 \text{ molecules}$$

3. $\rho = 8.89 \text{ gm/cm}^3 = 8890 \text{ kg/m}^3$
 $n = 4$

$$M_A = 63.5 \text{ gm/mol} = 63.5 \text{ kg}$$

$$N_A = 6.02 \times 10^{26} (\text{kmol})^{-1}$$

$$\text{We know } \rightarrow a = \left[\frac{n M_A}{N_A \rho} \right]^{1/3}$$

$$= \left(\frac{4 \times 63.5}{8890 \times 6.02 \times 10^{26}} \right)^{1/3}$$

$$= 3.61 \text{ \AA}$$

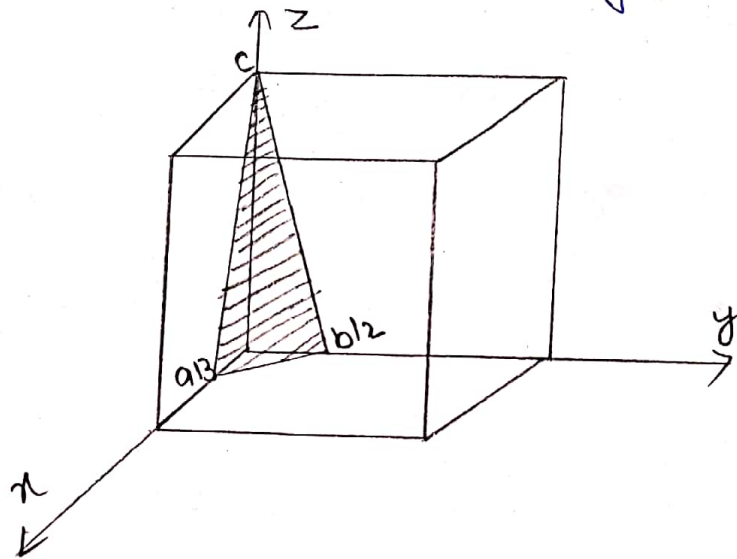
But a is for $\sigma \rightarrow$
 $2a^2 = (4\sigma)^2 \Rightarrow \sigma = a/2\sqrt{2}$

$$\sigma = \frac{3.61}{2\sqrt{2}} = \boxed{1.28 \text{ \AA}}$$

4 Here the unit translations are \rightarrow
 $a=3, b=2$ and $c=1$

(i) Intercepts	1	2	0.5
(ii) Division by unit translation	$1/3$	$2/2$	$\frac{0.5}{1}$
(iii) Reciprocals	3	1	2
(iv) After clearing fraction	Not Applicable		

The required Miller Indices of plane are $(3 \ 1 \ 2)$



5 Interplanar spacing for a simple cubic lattice is given by - $d_{hkl} = \frac{a}{\sqrt{h^2 + k^2 + l^2}}$
 for (100) planes

$$d_{100} = \frac{a}{\sqrt{1^2 + 0^2 + 0^2}} = a$$

For (110) planes \rightarrow

$$d_{110} = \frac{a}{\sqrt{1^2+1^2+0}} = \frac{a}{\sqrt{2}}$$

for (111) planes \rightarrow

$$d_{111} = \frac{a}{\sqrt{1^2+1^2+1^2}} = \frac{a}{\sqrt{3}}$$

$$\text{Now } \frac{1}{d_{100}} : \frac{1}{d_{110}} : \frac{1}{d_{111}} = 1 : \sqrt{2} : \sqrt{3}$$

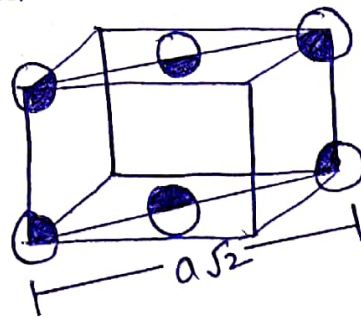
6. for fcc unit cell

d_{111} = same as d_{111} of simple cubic = $a/\sqrt{3}$

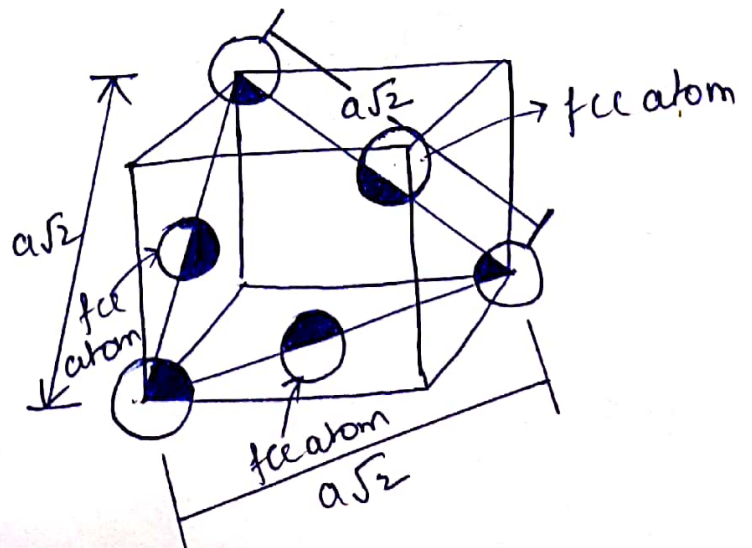
$$d_{110} = \frac{1}{2} (d_{110})_{sc} = \frac{1}{2} \cdot \frac{a}{\sqrt{2}}$$

Planar density = $\frac{\text{No. of atoms in given plane}}{\text{area of that plane}}$

$$\rho_{110} = \frac{4 \times \frac{1}{4} + 2 \times \frac{1}{2}}{\sqrt{2} a^2} = \frac{\sqrt{2}}{a^2}$$



$$\begin{aligned} \rho_{111} &= \frac{3 \times \frac{1}{6} + 3 \times \frac{1}{2}}{\frac{\sqrt{3}}{4} (a\sqrt{2})^2} \\ &= \frac{4}{\sqrt{3} a^2} \end{aligned}$$



7. $a = 5 \text{ \AA}$, $n = 1$, $\theta = 45^\circ$

(110) plane \rightarrow

$$d_{110} = \frac{a}{\sqrt{h^2 + k^2 + l^2}} = \frac{5}{\sqrt{2}} \text{ \AA}$$

using $2d_{hkl} \sin \theta = n\lambda$

$$\lambda = \frac{2 \times 5}{\sqrt{2}} \times \sin 45^\circ = \frac{2 \times 5}{\sqrt{2}} \times \frac{1}{\sqrt{2}} = 5 \text{ \AA}$$

8. $i = nAeV_d$ here $n = \frac{\text{no. of atoms}}{\text{m}^3}$

$$V_d = \frac{i}{nAe}$$

$$= \frac{1}{8.48 \times 10^{23} \times 10^{-6} \times 1.6 \times 10^{-19}}$$

$$= \boxed{7.37 \times 10^{-5} \text{ m/s}}$$

$$= \frac{\text{Mass/m}^3}{\text{mass/atom}}$$

$$= \frac{8.48 \times 10^3 \text{ kg/m}^3}{63.5 \times 1.66 \times 10^{-27} \text{ kg}}$$

$$= \boxed{8.48 \times 10^{28} \text{ e}^-/\text{m}^3}$$

9. $\sigma = 6.17 \times 10^7 \text{ mho/m}$, $\mu = 0.0056 \text{ m}^2/\text{V.s}$

(a) $V_d = 1 \text{ mm/s}$

So $\mu = \frac{V_d}{E}$ or $E = \frac{V_d}{\mu} = 0.1786 \text{ V/m}$

(b) $J = 10^7 \text{ A/m}^2$

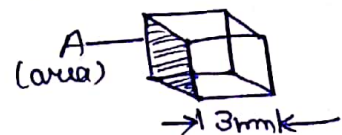
using $J = \sigma E \Rightarrow E = \frac{J}{\sigma} = 0.1621 \text{ V/m}$

(c) $I = 80 \text{ Amp}$, $J = \frac{I}{A} = \sigma E$

$$E = J/\sigma = 0.1441 \text{ V/m}$$

(d) $V = 50 \text{ mV}$

$$E = \frac{V}{d} \Rightarrow E = 1 \text{ V/m}$$



$$\underline{10.} \quad v_{rms} = \sqrt{\frac{8k_B T}{m}} = \sqrt{\frac{3 \times 1.38 \times 10^{-23} \times 293}{9.1 \times 10^{-31}}} \\ = 1.15 \times 10^5 \text{ m/s}$$

$$\text{Relaxation time } \tau = \frac{m}{\hbar n e^2} = 2.5 \times 10^{-14} \text{ sec}$$

$$\text{Mean free path } \lambda = v_{rms} \times \tau \\ = 2.8 \text{ nm}$$

$$\text{Mobility } \mu = \frac{1}{n e \tau}$$

$$\text{or } = \frac{e \tau}{m} \\ = 4.84 \times 10^{-3} \text{ m}^2/(\text{V}\cdot\text{s})$$

$$\sigma = \frac{1}{\rho} = \frac{n e^2 \tau}{m} = 5.92 \times 10^7 \text{ mho/m}$$

$$\text{drift velocity } \cdot v_d = \mu E = \boxed{4.84 \text{ mm/s}}$$

$$\text{here } \boxed{v_d \ll v_{rms}}$$