



Good

Evening

Everyone ::

## Stock Portfolio Performance Tracking

Tracking the performance of stocks over time is crucial for making informed decisions. You want to develop a feature for a banking app that allows users to quickly assess their stock portfolio's profit or loss over specified periods. To efficiently calculate the total profit or loss over any given range of time, you decide to implement this feature using the prefix sum technique.

### Example

Stock\_Prices [] = [ -5    10    20    40    50    -10    80    -90    -20    -10 ]

### Queries

Start Day	End Day	Net Stock Price
0	9	62
1	4	120
0	0	-5
7	9	-120
2	7	90

Given  $N$  elements and  $Q$  queries. For each query, calculate sum of all elements from  $L$  to  $R$  [0 based index]

$$A[] = \begin{bmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ -3 & 6 & 2 & 4 & 5 & 2 & 8 & -9 & 3 & 1 \end{bmatrix}$$

Queries

$L$	$R$	Solution
4	8	9
3	7	10
1	3	12
0	4	14
7	7	-9

Queries

0	4	8
1	3	7
2	1	3
3	0	4

Brute Force:

size of array =  $n$   
queries size =  $\mathcal{Q}$ .

function querySum (Queries [] [], Array [],  
querySize, size) {

for ( $i \rightarrow 0 \rightarrow \text{Queries.length} - 1$ ) {

$L = \text{Queries}[i][0]$ ;

$R = \text{Queries}[i][1]$ ;

$\text{sum} = 0$

for ( $j \rightarrow L \rightarrow R$ ) {

$\text{sum} = \text{sum} + \text{Array}[j]$

}

print (sum)

}

}

TC:  $O(NQ)$

SC:  $O(1)$

Quiz 1.

10 overs Scores :

[7<sup>th</sup> over]

1	2	3	4	5	6	7	8	9	10
2	8	14	29	31	49	65	79	88	97

Score before  $\Rightarrow$  49

Score after 7  $\Rightarrow$  65

Score in the 7<sup>th</sup> over  $\Rightarrow$   $65 - 49$   
 $= \underline{16}$ .

Quiz 2 10 overs Score ( $6^{\text{th}}$  to  $10^{\text{th}}$  over)

1	2	3	4	5	6	7	8	9	10
2	8	14	29	31	49	65	79	88	97

before 6<sup>th</sup> score [5]

after 10<sup>th</sup> score [10]

Score [10] - Score [5]

97 - 31  $\Rightarrow$  66

Quiz 3.

10 overs Score

[10<sup>th</sup> over]

[ 2 8 14 29 31 49 65 79 88 97 ]

before  $\Rightarrow$  score [9]  
after  $\Rightarrow$  score [10]

$$97 - 88 = \underline{9}.$$

Quiz 4.

10 overs Score

[End to 6<sup>th</sup> over]

[ 1 2 3 4 5 6 7 8 9 10  
2 8 14 29 31 49 65 79 88 97 ]

Score [6] - Score [2]

$$49 - 8 \Rightarrow 41$$

## Quiz 2:

10 overs Score

[4<sup>th</sup> to 9<sup>th</sup> Over])

1	2	3	4	5	6	7	8	9	10
2	8	<u>14</u>	29	31	49	65	79	88	97

lower

Upper

$$\underline{88 - 14} \Rightarrow \underline{74}.$$

$$\text{Score}[R] - \text{Score}[l-1]$$

## Observations

- ↳ Answer queries in  $O(1)$  time when I have cumulative sum.
- ↳ We need to create a cumulative / Prefix Sum Array to answer the question within a range.

## How to create Prefix Sum Array

	0	1	2	3	4
arr =	2	5	-1	7	1

Prefix =	2	7	6	13	14
----------	---	---	---	----	----

arr	2	-5	4	3	-2
-----	---	----	---	---	----

P(arr) =	2	-3	1	4	2
----------	---	----	---	---	---

Quiz:

Calculate prefix sum array:

arr [ 0 1 2 3 4 5 ]  
[ 10 " 32 " 6 " 12 " 20 " ]

pf[0] [ 10 42 48 60 80 81 ]

Code:

pf[N]

for ( $i \rightarrow 0$  to  $N-1$ )

Sum = 0

$O(n^2)$

for ( $j \rightarrow 0$  to  $i$ )

Sum = Sum + A[j]

{

pf[i] = Sum

}

pf[0]  $\Rightarrow$  A[0]

pf[1] = A[0] + A[1]

pf[2] = A[0] + A[1] + A[2]

$$\begin{aligned}
 Pf[0] &\Rightarrow A[0] \\
 Pf[1] &\Rightarrow Pf[0] + A[1] \\
 Pf[2] &\Rightarrow Pf[1] + A[2]
 \end{aligned}$$

$$Pf[i] = Pf[i-1] + A[i]$$

Optimised code:

$$\begin{aligned}
 Pf[N] \\
 Pf[0] = A[0]
 \end{aligned}$$

TC: O(N)

for ( $i \rightarrow 1$  to  $N-1$ )

$$Pf[i] = Pf[i-1] + A[i]$$

{}

## How to answer the Queries

$$A[] = [ \begin{matrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ -3 & 6 & 2 & 4 & 5 & 8 & 8 & -9 & 3 & 1 \end{matrix} ]$$

$$pf[] = [ \begin{matrix} -3 & 3 & 5 & 9 & 14 & 16 & 24 & 15 & 18 & 19 \end{matrix} ]$$

L

R

4

8

$$pf[8] - pf[3] \Rightarrow 15 - 5 = 10$$

3

7

$$pf[7] - pf[2] \Rightarrow 24 - 3 = 21$$

1

3

$$pf[2] - pf[0] \Rightarrow 5.$$

7

7

$$pf[7] - pf[6] \Rightarrow 8$$

Generalised

$$\text{Sum}[L R] = pf[R] - pf[L-1].$$

$$\text{gf } L == 1 \Rightarrow \text{sum}[LR] = pf[R]$$

1 based  
indexing

$$\text{gf } L == 0 \Rightarrow \text{sum}[LR] = pf[R]$$

0 based  
indexing

0	1	2	3	4
ar	1	2	-4	3

pf <sup>r</sup> ]	1	3	-1	2	9
-------------------	---	---	----	---	---

L

R

1

3

$$pf[2] - pf[0] \Rightarrow$$

$$2 - 1 = \underline{1}$$

0

2

$$pf[R] \Rightarrow$$

$$pf[2] \Rightarrow -1$$

Code:

function querySum (Queries [][], Array [], querySize, size) {

    pf [N]

    pf [0] = A [0]

    for (i → 1 to N-1) {

        TC : O(N+Q)

        SC : O(N)

            pf [i] = pf [i-1] + A [i]

}

// answer queries

    for (i → 0 to Queries.length - 1) {

        L = Queries[i][0]

        R = Queries[i][1]

        if (L == 0) {

            sum = pf[R]

        }

        else {

            sum = pf[R] - pf[L-1]

        }

        print (sum)

}

}

## Sum of Even indexed Elements

Given an array of size N and Q queries with start(s) and (e) index  
For every query, return the sum of all even index elements from  
s to e (0 based index).

A[] = { 2 3 1 6 4 5 }

Query

1	3	1
2	5	5
0	4	7
3	3	0

Brute force  $O(NQ)$ .

A[]  $\Rightarrow$  [ 2 3 1 6 4 5 ]

pf[]  $\Rightarrow$  [ 2 2 3 3 7 7 ]

if i is even

pf[i]  $\Rightarrow$  pf[i-1] + A[i]

else

pf[i]  $\Rightarrow$  pf[i-1].

Quiz 1.

0	1	2	3	4
2	4	3	1	5

pf[] [2 2 5 5 10]

Ques<sup>6</sup>

0 [2 4]

0 [2 4 3 1 5]

1 [0 2]

pf[] [2 2 5 5 10]

Code:

Function sumOfEvenIndexed (Array [], Queries, N, Q) {

PSe [N]

TC : O(N+Q)

PSe [0] = Array [0]

SC : O(N)

for (i → 1 to N) {

if (i%2 == 0) {

PSe [i] = PSe [i-1] + Array [i]

}

else

PSe [i] = PSe [i-1]

}

}

for (i → 0 to Queries.length - 1)

s = Queries [i] [0] // 2 // 0

e = Queries [i] [1] // 0 // 2

if (s == 0)

print (PSe [e])

}

else

}

point  $(pse[e] - pse[s-1])$

}

}

## PROBLEM :- COUNT OF PAIRS ag

Given a string s lowercase characters, return the count of pairs  $(i, j)$ , such that  $i < j$  and

$s[i]$  is 'a'

$s[j]$  is 'g'

String  $s = "abegag"$

$\begin{matrix} & \downarrow & \downarrow \\ a & b & e & g & a & g \\ \downarrow & & & & & \\ 2 & & 1 & & & \end{matrix} = \underline{3}$

Quiz 8.  $s = "acgdgag"$

$[0, 2] [5, 6]$

$[0, 4]$

$[0, 6] \Rightarrow \underline{4}$ .

Ques.

$s = "bc\overset{0}{a}aggaaag"$

$\begin{matrix} [2 \ 3] \\ [2 \ 4] \\ [2 \ 7] \end{matrix}$      $\begin{matrix} [5 \ 7] \\ [6 \ 7] \end{matrix}$

$\Rightarrow$  5 pairs.

Brute Force

function count\_ag ( str )

TC :  $O(N^2)$   
SC :  $O(1)$ .

result = 0

for ( $i \rightarrow 0$  to  $n-1$ ) -

    if ( $str[i] == 'a'$ ) {

        for ( $j \rightarrow i+1$  to  $N-1$ )

            if ( $str[j] == 'g'$ ) {

                result = result + 1

}

}

}

$\text{ans} \Rightarrow 2$   
 $+ 3$   
 $\Rightarrow 5$   
 $+ 3$   
 $\Rightarrow 8$

String . a c b a g k a g g

count\_a = 2

$$\text{ans} = 2 + 3 = 5 + 3 = 8$$

function count\_ag (str) {

result = 0

TC : O(N)

SC : O(1)

count\_a = 0

for (i → 0 to n-1) {

if (str[i] == 'a') {

count\_a ++

}

else if (str[i] == 'g') {

result = result + count\_a

}

return result

}

## Introduction to Subarrays

A Subarray is a contiguous part of an array. It is formed by selecting a range of elements from the array. A subarray can have one or more elements and must be contiguous part of original array.

{ 4 1 2 3 -1 6 9 8 12 }

✓ { 2 3 -1 6 } → is a subarray of length 4

✓ { 9 }

✓ { 4 1 2 3 -1 6 9 8 12 }

X { 4 12 }

X { 1 2 6 } not continuous .

X { 3 2 1 4 }

order has to same  
and it has to continuous.

Quiz:

$$A[] = \{ 2 \ 4 \ 1 \ 6 \ -3 \ 7 \ 8 \ 4 \}$$

✓ 1 6 8 X not continuous

✓ 1 4 X order

✓ 6 1 4 2 X order and places

✓ 7 8 4 ✓ Subarray.

## Representation of a Subarray

① By specifying start index → end index

② By specifying start and length of subarray.

0	1	2	3	4	5	6	7	8	9
4	1	2	3	-1	6	9	4	2	8

{ 2 3 -1 6 }

s = 2      e = 5      length = 4.

Quiz 11:

How many subarrays start from index 0

[ 4 2 10 3 12 -2 15 ]  
 0 1 2 3 4 5 6

[4]

$\Rightarrow \textcircled{7}$ .

[ 4 2 ]

[ 4 2 10 ]

[ 4 2 10 3 ], [ 4 2 10 3 15 ]

[ 4 2 10 3 12 -2 ]

[ 4 2 10 3 12 -2 15 ]

Quiz 12:

How many subarrays start from index 1

[ 4 2 10 3 12 -2 15 ]  
 0 1 2 3 4 5 6

[2]

$\Rightarrow 1 \rightarrow 1$

[ 2 10 ]

$\Rightarrow 1 \rightarrow 2$

[ 2 10 3 ]

$\Rightarrow 1 \rightarrow 3$

[ 2 10 3 12 ]

$1 \rightarrow 4$

[ 2 10 3 12 -2 ]

$1 \rightarrow 5$

[ 2 10 3 12 -2 15 ]

$1 \rightarrow 6$

## PRINT ALL POSSIBLE SUBARRAYS OF ARRAY

Given an array of integers, print all possible subarrays

Input:  $\begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & \underline{3} \end{bmatrix}$

$[1]$   
 $[1 2]$   
 $[1 2 3]$   
 $[2]$   
 $[2 3]$   
 $[3]$

$s \ e$   
 $(0, 0)$   
 $0, 1)$   
 $(0, 2)$   
 $\rightarrow (1, 1)$   
 $(1, 2)$   
 $(2, 2)$

$\begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \end{bmatrix}$

$i = 0$        $\rightarrow$        $\begin{array}{l} \{ \rightarrow 0 \\ \} \rightarrow 1 \\ \} \rightarrow 2 \end{array}$        $\begin{array}{ll} 0 \text{ to } 2 & \text{start end} \\ \rightarrow 0 & 0 \quad 0 \\ \rightarrow 1 & 0 \quad 1 \\ \rightarrow 2 & 0 \quad 2 \end{array}$        $\left| \begin{array}{l} [1] \\ [1 2] \\ [1 2 3] \end{array} \right.$

$i = 1$        $\rightarrow$        $\begin{array}{l} \{ \rightarrow 1 \\ \} \rightarrow 2 \end{array}$        $\begin{array}{ll} 1 \text{ to } 2 & \text{start end} \\ \rightarrow 1 & 1 \quad 1 \\ \rightarrow 2 & 1 \quad 2 \end{array}$        $\left| \begin{array}{l} [2] \\ [2 3] \end{array} \right.$

$i = 2$        $\rightarrow$        $\{ \rightarrow 2 \text{ to } 2$        $\rightarrow 2 \quad 2 \quad 2$        $\left[ \begin{array}{l} 2 \end{array} \right]$

Code:

```
function printSubarrays (arr[], n) {
```

```
    for (i → 0 to n-1) {
```

```
        for (j → i to n-1) {
```

} start = i

} end = j

```
        for (k → start to end)
```

```
            print arr[k]
```

}

}

}

TC :  $O(n^3)$

SC :  $O(1)$