## Anti-Lock Brake system

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#### Anti-lock brake system

# Mathematical modelling of ABS and simulation in MATLAB Simulink

#### 1.1 Introduction

Anti-lock braking systems (ABS) are meant to control the wheel slip in order to maintain the friction coefficient close to the optimal value. Wheel slip is defined as the relative motion between a wheel (tire) and the surface of the road, during vehicle movement. Wheel slip occurs when the angular speed of the wheel (tire) is greater or less compared to its free-rolling speed. In order to simulate the braking dynamics of a vehicle, we are going to implement simplified mathematical models (quarter-car model) for both vehicle and wheel. Also, a simplified ABS controller is going to be implemented in order to emulate the braking torque in slip conditions.

#### 1.2 Vehicle Model

If we consider the vehicle is moving in forward direction under braking condition. The equation of the system will be as follows.

$$F_t = F_i \tag{1}$$

 $F_t \rightarrow friction force between wheel and ground$ 

 $F_i \rightarrow inertia\ force\ of\ the\ vehicle$ 

$$N = W \tag{2}$$

 $N \rightarrow Normal force of the vehicle$ 

 $W \rightarrow weight of the vehicle$ 

$$F_t = \mu . N \tag{3}$$

 $\mu \to \textit{friction coffecient}$ 

$$W = m_{1} \cdot g \tag{4}$$

 $m_v \rightarrow mass\ of\ the\ vehicle$ 

 $g \rightarrow accelaration due to gravity$ 

From equation 3 and 4

$$F_t = \mu . m_v . g \tag{5}$$

Inertia force

$$F_i = m_v \cdot a_v = m_v \cdot \frac{dv_v}{dt}$$

$$\frac{dv_v}{dt} = \frac{1}{m_v} (\mu \cdot m_v \cdot g) \tag{6}$$

Vehicle velocity is obtain by integration the equation 6. Limit equation.

#### 1.3 Wheel model

Wheel equation is shown as below.

$$T_b - F_f \cdot r_w - \frac{J_w d\omega}{dt} = 0 \tag{7}$$

Integrating above equation with limit give us angular velocity (rpm) of the wheel.

#### 1.4 Wheel slip

ABS has to control the wheel slip. Below equation gives is the wheel slip.

Wheel slip = 
$$1 - \frac{\omega_w}{\omega_n}$$
 (8)

 $\omega_w \rightarrow Angular \ velocity \ of \ the \ wheel$ 

 $\omega_v \rightarrow$  Equivalent anguar velocity of the vehicle

$$\omega_v = \frac{V_v}{r_v} \tag{9}$$

 $V_v \rightarrow linear\ velocity\ of\ the\ vehicle$ 

 $r_v \rightarrow radius \ of \ the \ wheel$ 

#### 1.5 Coefficient of friction

- Coefficient of friction depends upon many factors like.
- Wheel slip

- Vehicle speed
- Type of road surface
- Environment conditions

For our simulation purpose and for simplification we will use lookup table, entries are as follows.

Coefficient	slip
of friction	_
0.00	0.000
0.05	0.400
0.10	0.800
0.15	0.970
0.20	1.000
0.25	0.980
0.30	0.960
0.35	0.940
0.40	0.920
0.45	0.900
0.50	0.880
0.55	0.855
0.60	0.830
0.65	0.810
0.70	0.790
0.75	0.770
0.80	0.750
0.85	0.730
0.90	0.720
0.95	0.710
1.00	0.700

Table 1.0

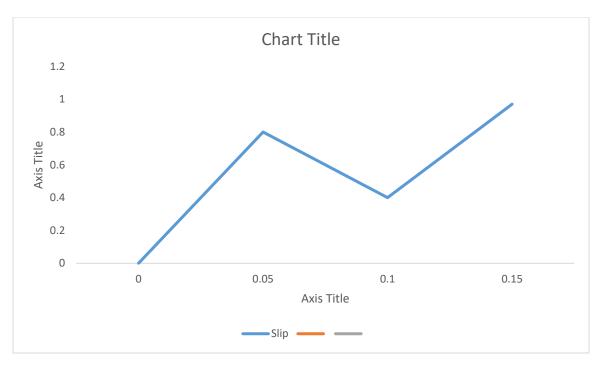


Fig - 1.1 Slip v/s Coefficient of friction

#### 1.6 Model parameters

Symbol	unit	value	description
$m_{12}$	Kg	1200	Mass of the
			vehicle
$J_{w}$	$Kg.m^2$	6	Moment of
			inertia of the
			wheel
$r_{w}$	m	1.25	Radius of the
			wheel
$V_0$	m	44	Initial velocity
	S		of vehicle
			before braking
g	$m/s^2$	9.81	Acceleration due
	,		to gravity

Table - 1.2

#### 1.7 Simulation in MATLAB-Simulink

Final Model obtain after modelling above equation and model parameters.  $% \left( 1\right) =\left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right)$ 

#### Problem 3 (300 points)

Design a complex automotive system of your choice. Create a small report of this project and demonstrate following skills in your model. Highlight these skills in your report.

- 1. Callbacks
- 2. Data Inspector
- 3. Solver selection strategy
- 4. MATLAB function block
- 5. Look-up table
- Signal Builder to generate test signals. Demonstrate how your system is performing under various test conditions

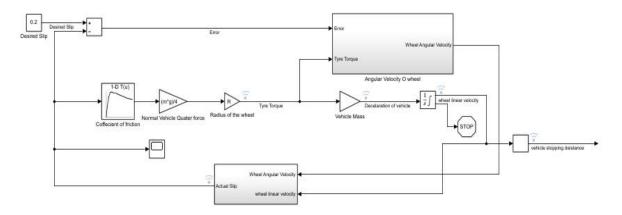


Fig 1.2 Block Model

#### Angular velocity of the wheel Block

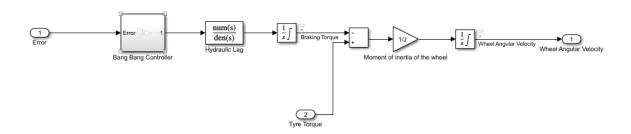


Fig - 1.3 Angular velocity of wheel

- 1. Bang-Bang controller
  If the input is greater than zero it gives output +1
  If the input is less than zero it gives output -1.
- 2. Hydraulic lag

This is the lag generated between pressing the brake paddle and actually brake being applied. This is simulated through arbitrary transfer function.

- 3. Integrator
  - Integrating the output of the transfer function we get braking torque.
- 4. Difference between tyre torque and braking torque is the resultant torque moving the tyre.
- 5. Integrating the output with constant 1/Jw moment of inertia gives us wheel's angular velocity.

#### Tyre torque

Coefficient of friction from the lookup table.

 $rac{dv_v}{dt} = rac{1}{m_v} (\mu \,.\, m_v \,.\, g)$  This equation is simulated in this section which produce tyre torque.

From tyre torque vehicle linear velocity if determined. Integrating the tyre torque with constant 1/m (mass of the vehicle) give us velocity of the vehicle and then multiplying it by 1/R gives us equivalent angular velocity of the vehicle.

#### Slip Calculation

 $\label{eq:Wheelslip} Wheelslip = 1 - \frac{\omega_w}{\omega_v} \qquad \text{This equation is simulated to calculate the slip. Which is subtracted from desired slip to calculate the error which feed to the bang-bang controller.}$ 

#### OUTPUT

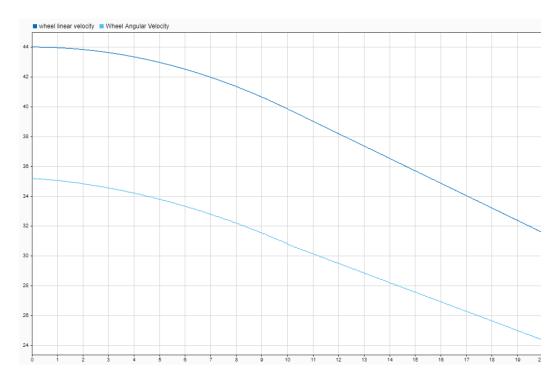
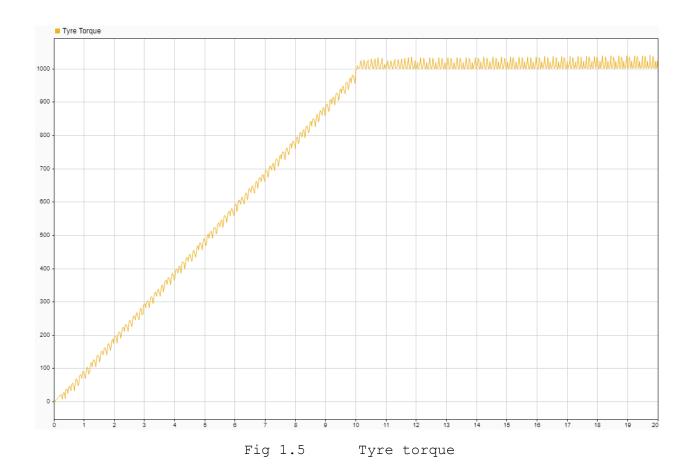


Fig 1.4 Wheel angular velocity and wheel linear velocity



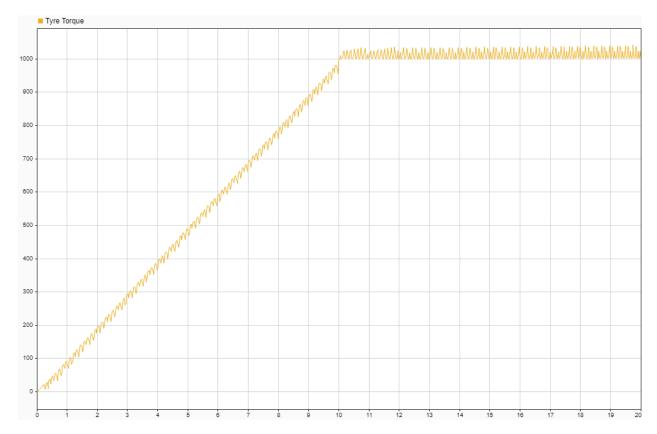


Fig 1.6 Braking torque

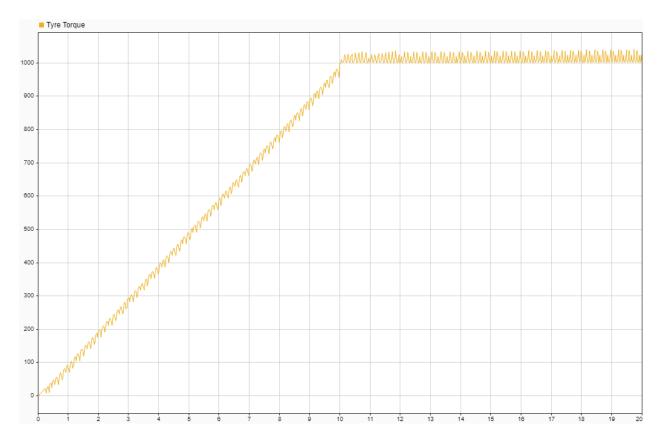


Fig 1.7 Deceleration of the vehicle

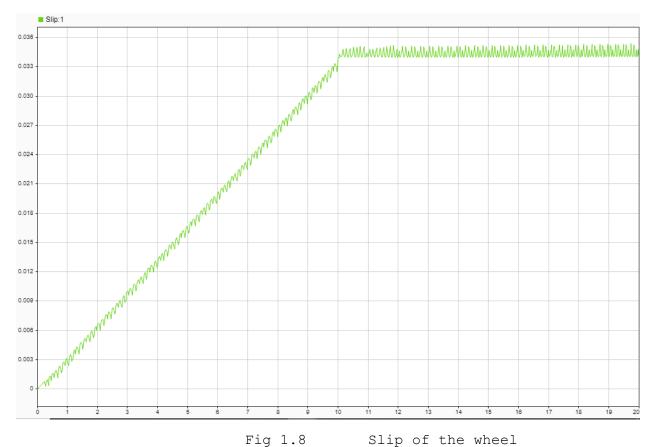


Fig 1.8

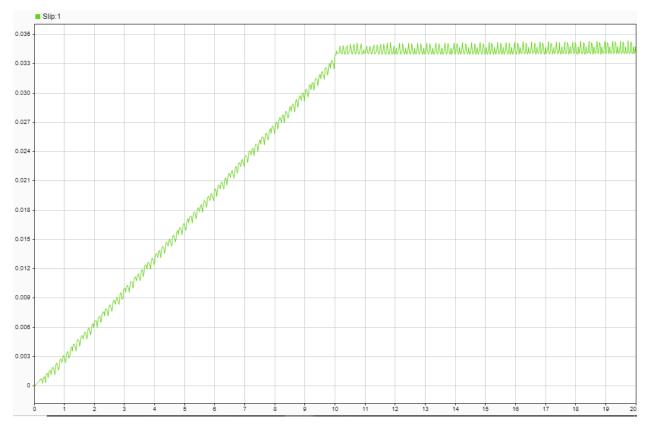


Fig 1.9 Stopping distance