



DESIGN & ANALYSIS OF ALGORITHM

PCC-CS402



DESIGN & ANALYSIS OF ALGORITHM

SCHEDULE ----TOPIC WISE

	Topic	Sub Topic
1	INTRODUCTION	DESIGN OF ALGORITHM ,ANALYSIS OF ALGORITHM, ALGORITHM PROPERTIES
2	FRAMEWORK FOR ALGORITHM ANALYSIS	HOW TO COUNT EXECUTION TIME OF ALGORITHM,INPUT INSTANCES
3	ASYMPTOTIC NOTATION	BEST CASE,AVERAGE CASE, WORST CASE
4	SOLVING RECURRENCE RELATION	SUBSTITUTION METHOD, MASTER THEOREM
5	ALGORITHM DESIGN TECHNIQUES	DIVIDE & CONQUER, GREEDY,DYNAMIC PROGRAMMING, BACKTRACKING,
6	DISJOINT SET MANIPULATION	UNION FIND
7	NETWORK FLOW PROBLEM	FORD FULKERSON ALGORITHM
8	NP COMPLETENESS	NP,NP HARD.....ALGORITHM
9	APPROXIMATION ALGORITHM	COMPLEXITY ANALYSIS OF NP COMPETE PROBLEM



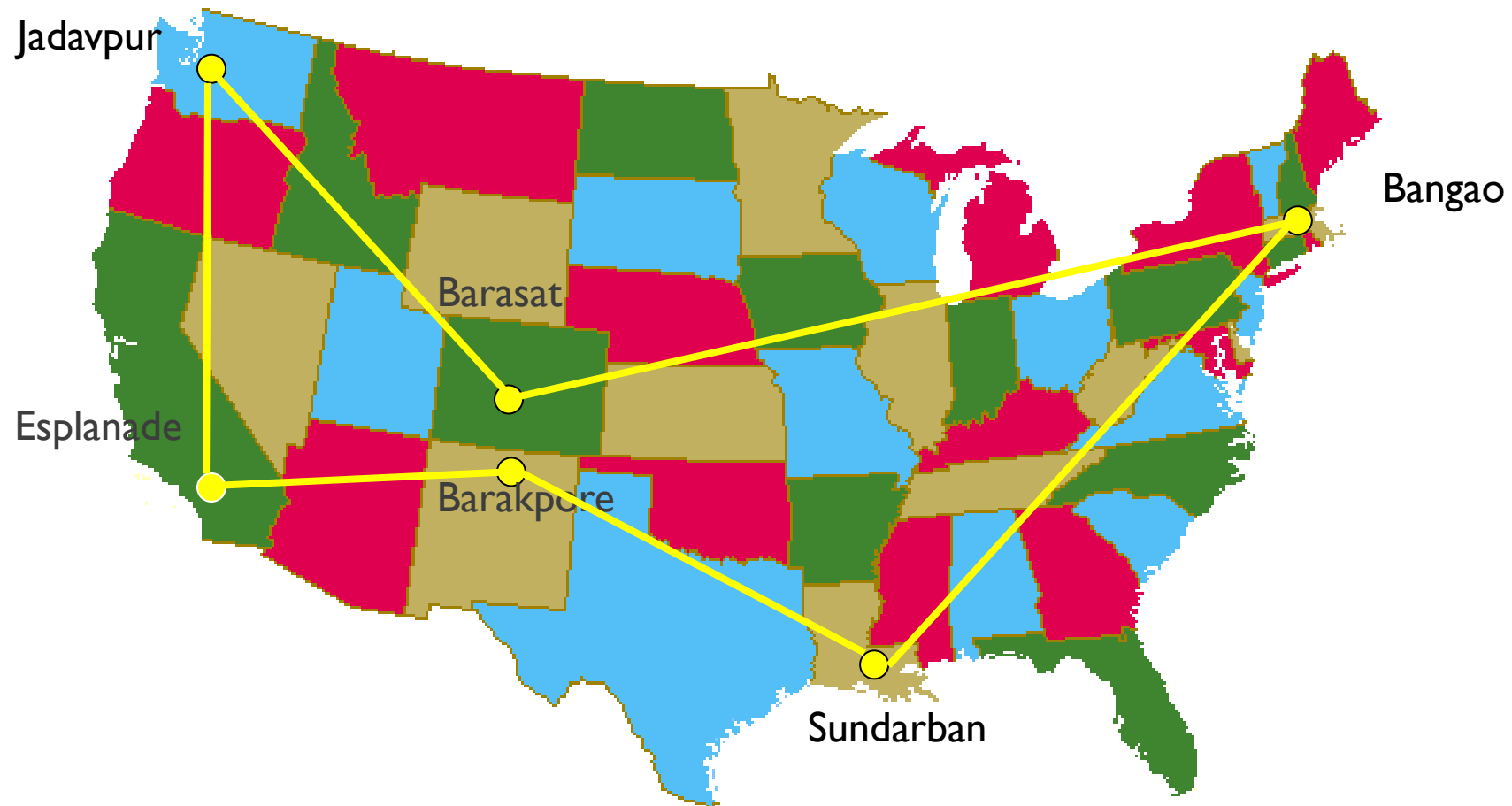
■ TRAVELLING SALESMAN PROBLEM

TRAVELING SALESMAN PROBLEM

- Given a list of cities and the distances between each pair of cities, what is the shortest possible route that visits each city exactly once and returns to the origin city?
- **OUTCOME-**
Identify the smallest weight cycle.

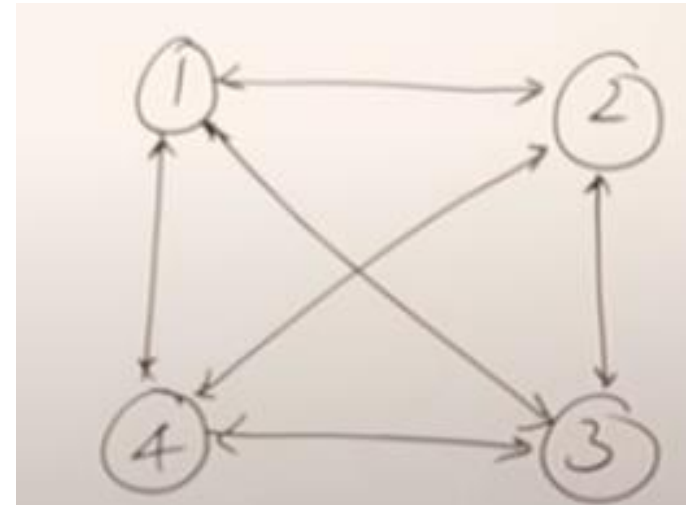
TRAVELING SALESMAN PROBLEM

6 CITIES ----- SHORTEST POSSIBLE ROUTE-----EXACTLY ONCE



TRAVELING SALESMAN PROBLEM VS HAMILTONIAN CYCLE

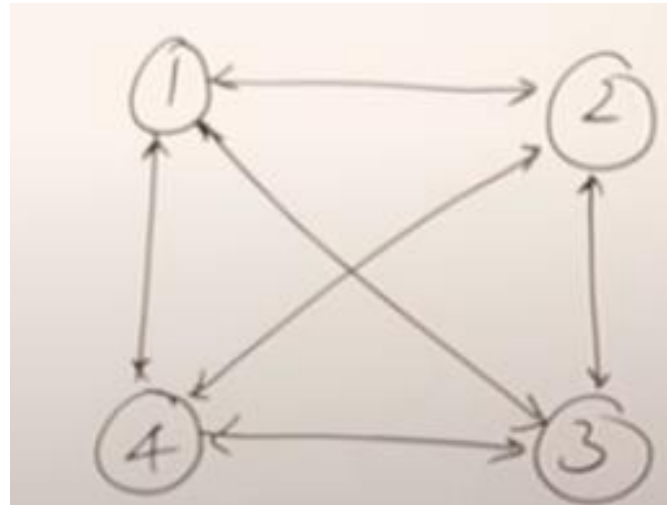
- Find a minimum weight Hamiltonian Cycle



The TSP has many practical applications

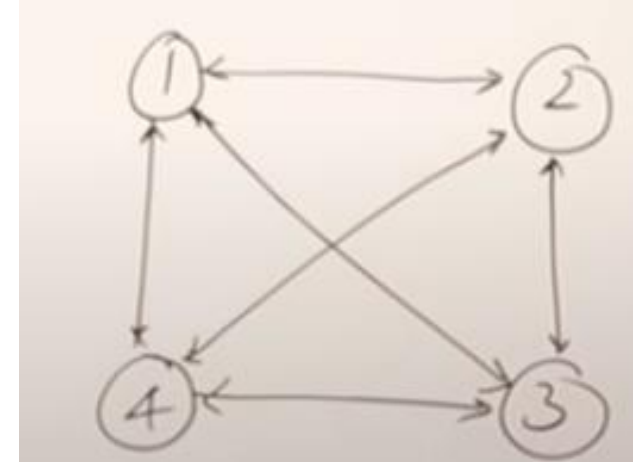
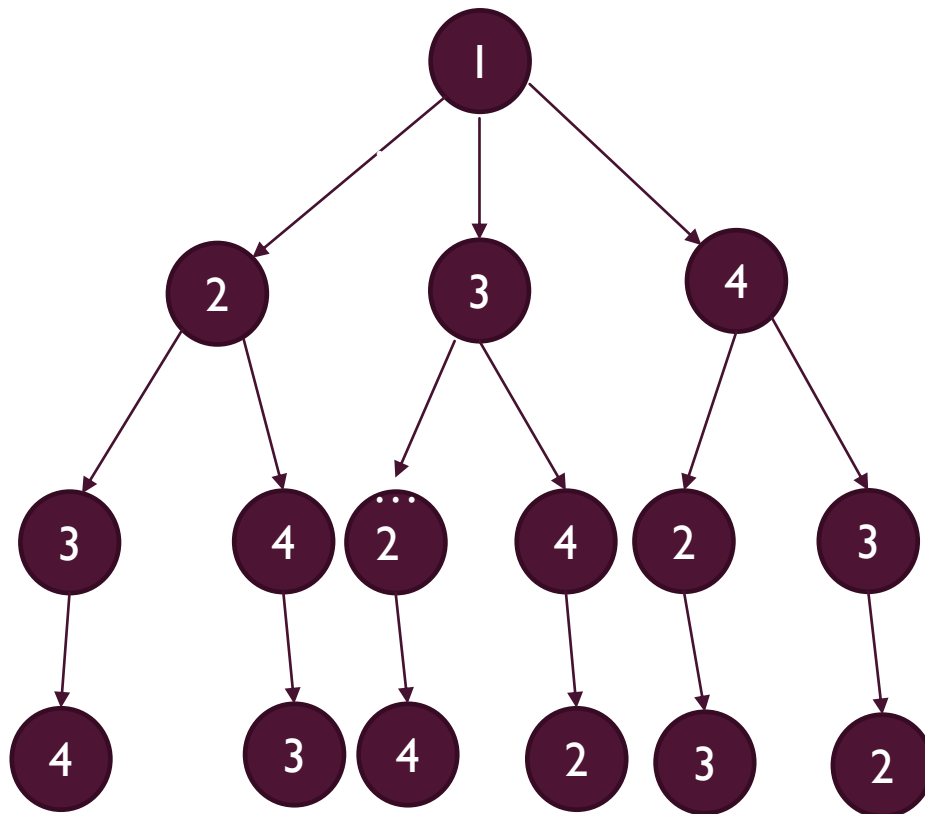
- manufacturing
- plane routing
- telephone routing
- networks
- traveling salespeople
- structure of crystals

TRAVELING SALESMAN PROBLEM

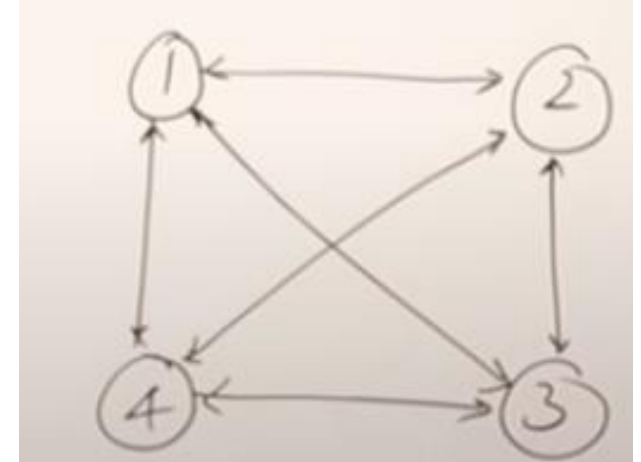
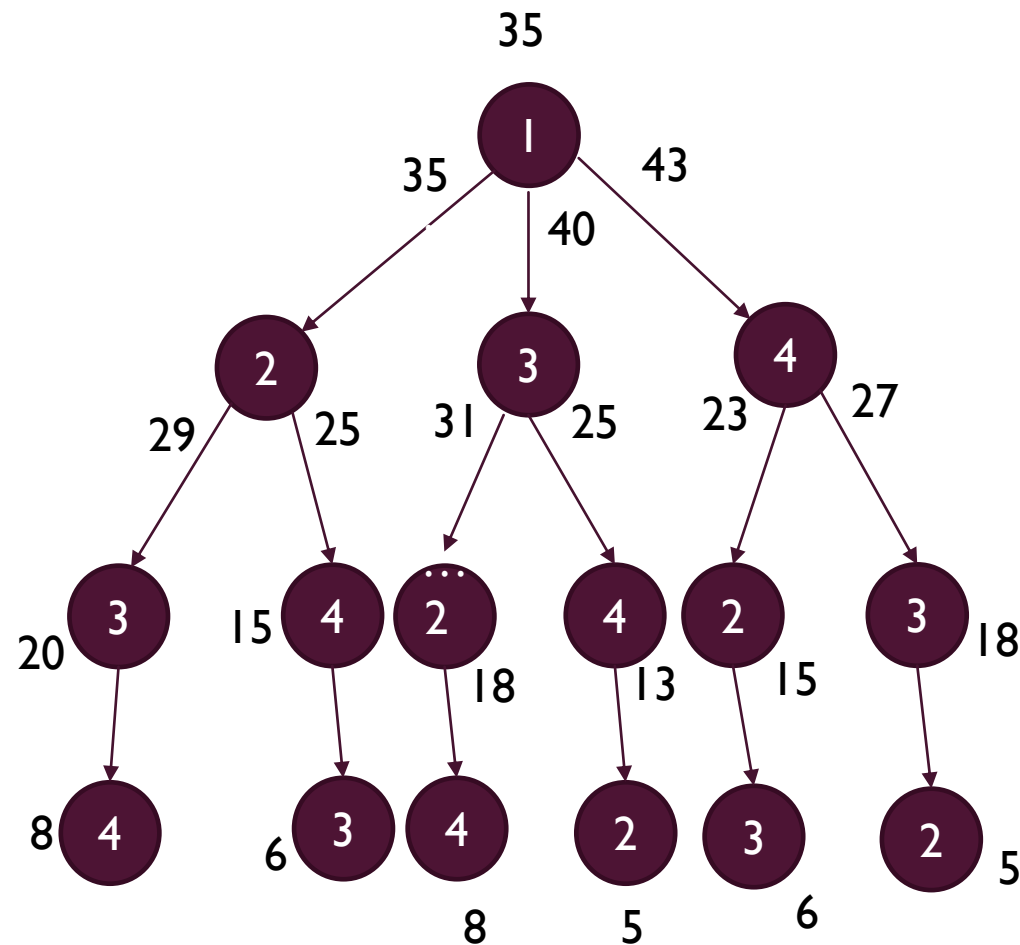

$$A = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 10 & 15 & 20 \\ 5 & 0 & 9 & 10 \\ 6 & 13 & 0 & 12 \\ 8 & 8 & 9 & 0 \end{bmatrix} \end{matrix}$$

TRAVELING SALESMAN PROBLEM

STATE SPACE TREE

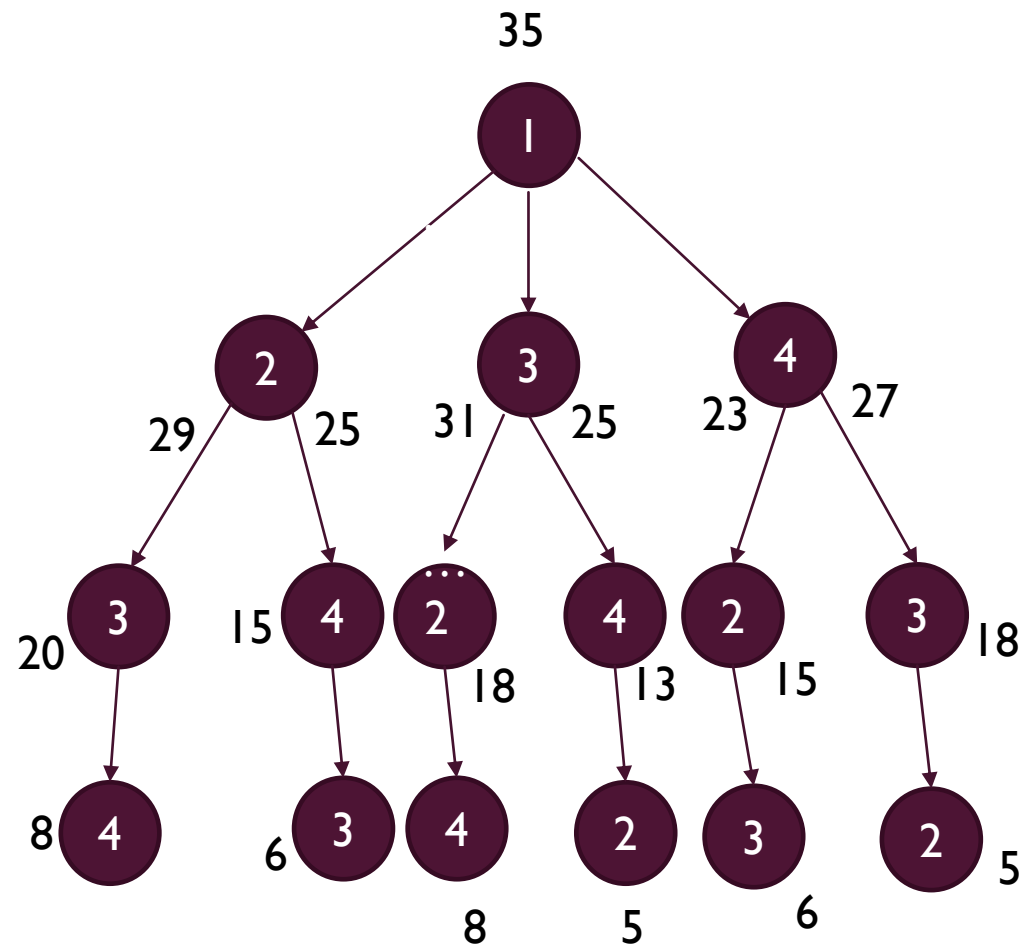

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TRAVELING SALESMAN PROBLEM BRUTE FORCE APPROACH


$$A = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 10 & 15 & 20 \\ 5 & 0 & 9 & 10 \\ 6 & 13 & 0 & 12 \\ 8 & 8 & 9 & 0 \end{bmatrix} \end{matrix}$$

TRAVELING SALESMAN PROBLEM

DYNAMIC PROGRAMMING APPROACH



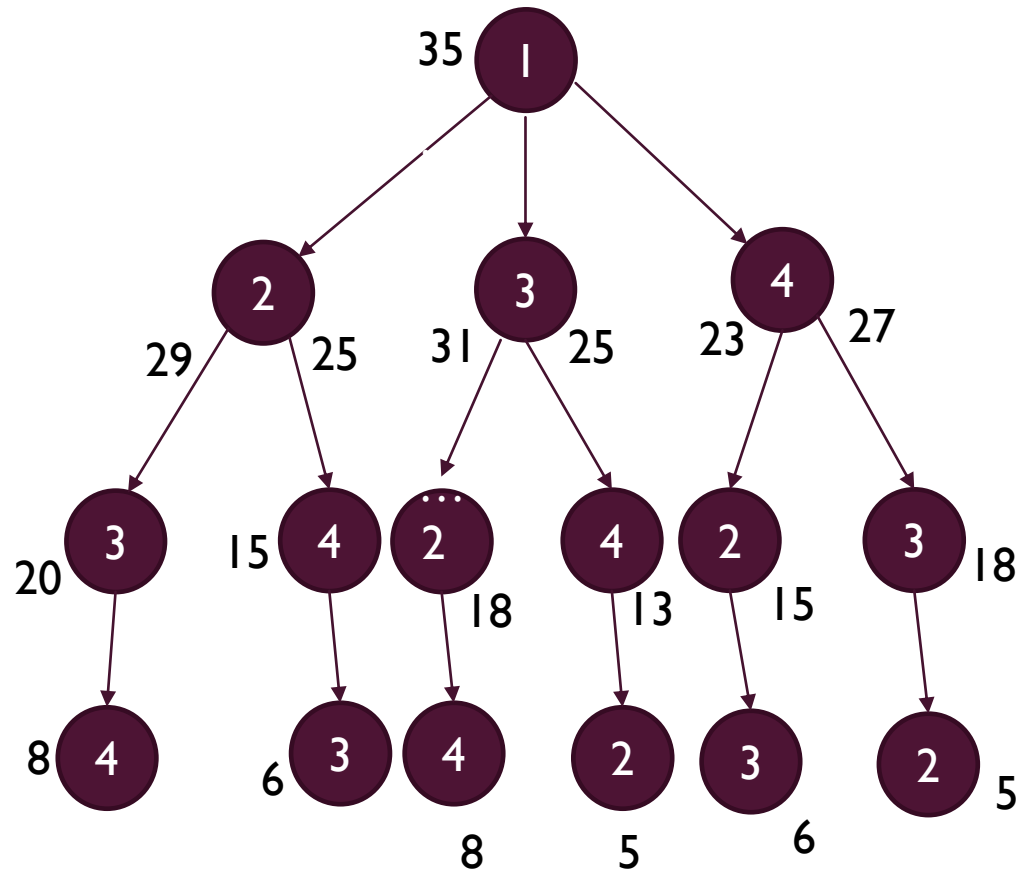
$$g(i,S)=\min\{C_{i,k} + g(k, S-\{k\})\}_{k \in S}$$

$$g(1,\{2,3,4\})=\min\{C_{1,k} + g(k,\{2,3,4\}-\{k\})\}$$

TRAVELING SALESMAN PROBLEM

$g(i,S)=\min\{C_{i,k} + g(k, S-\{k\})\}$ DYNAMIC PROGRAMMING APPROACH

$$g(1,\{2,3,4\})=\min\{C_{1,k} + g(k,\{2,3,4\}-\{k\})\}$$



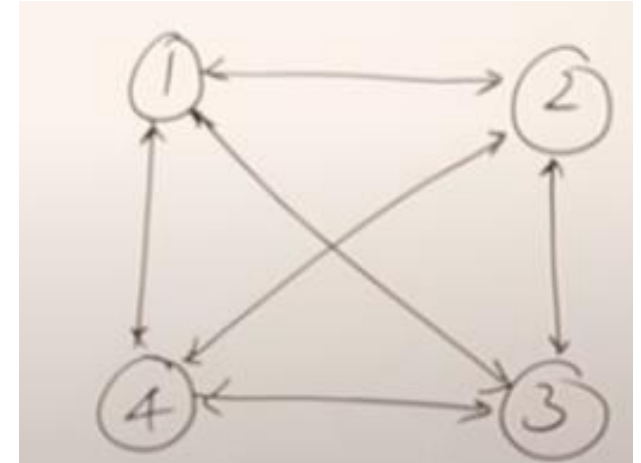
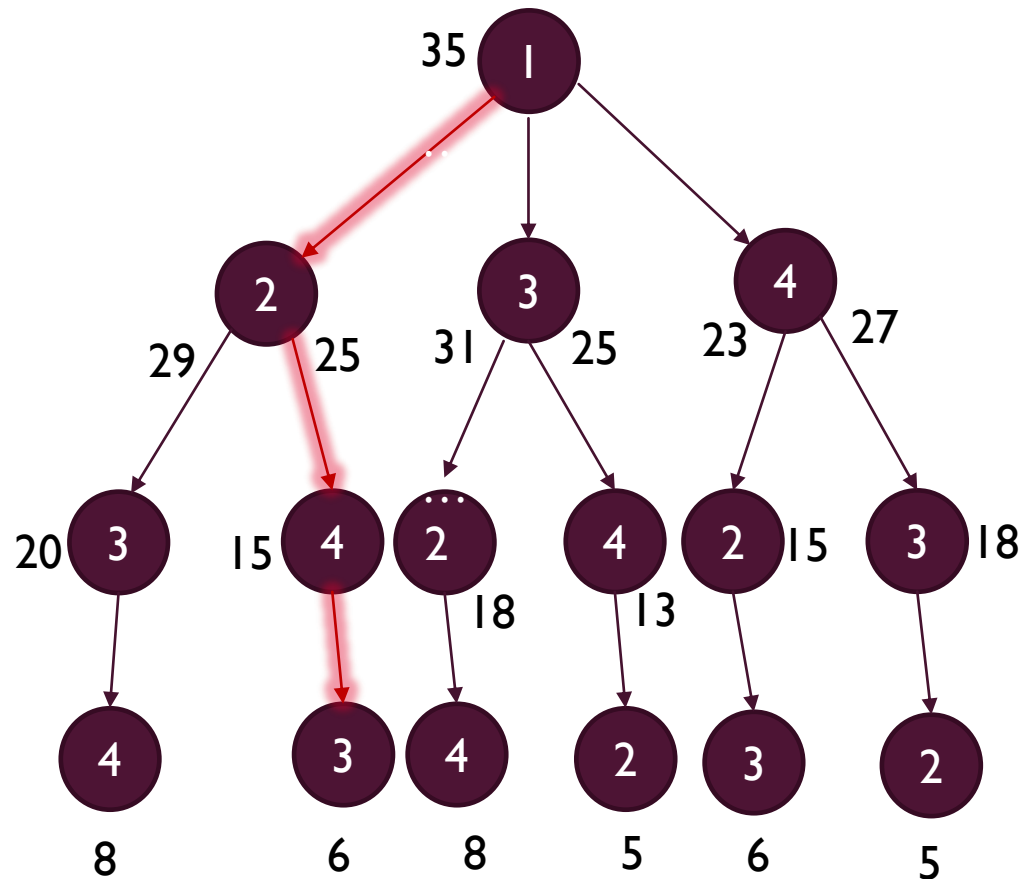
$g(2,\emptyset)$	5
$g(3,\emptyset)$	6
$g(4,\emptyset)$	8
$g(2,\{3\})$	15
$g(2,\{4\})$	18
$g(3,\{2\})$	18
$g(3,\{4\})$	20
$g(4,\{2\})$	13
$g(4,\{3\})$	15
$g(2,\{3,4\})$	25
$g(3,\{2,4\})$	25
$g(4,\{2,3\})$	23

TRAVELING SALESMAN PROBLEM

OUTCOME

DYNAMIC PROGRAMMING APPROACH

PATH $\rightarrow 1 \rightarrow 2 \rightarrow 4 \rightarrow 3$



$A =$

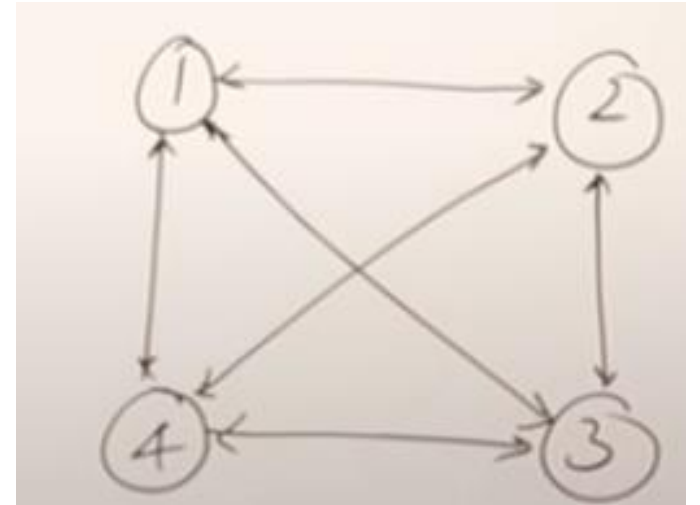
	1	2	3	4
1	0	10	15	20
2	5	0	9	10
3	6	13	0	12
4	8	8	9	0

TRAVELING SALESMAN PROBLEM ANALYSIS

DYNAMIC PROGRAMMING APPROACH

$$g(i,S)=\min\{C_{i,k} + g(k, S-\{k\})\}$$

- $|S|=n$ (no of nodes)
- There are at most $O(n*2^n)$ sub-problems.
- Each sub-problem takes linear time to solve.
- The total running time is therefore $O(n^2*2^n)$.



TRAVELING SALESMAN PROBLEM

- **Combinatorial optimization problems.**
- **Exponential** in terms of time complexity.
- Requires **exploring all possible permutations** in worst case.
- The **Branch and Bound** Algorithm technique solves these problems relatively quickly.

NEXT CLASS

- Travelling Salesman Problem using Branch & Bound.