



DESIGN & ANALYSIS OF ALGORITHM

PCC-CS501



DESIGN & ANALYSIS OF ALGORITHM

SCHEDULE ----TOPIC WISE

	Topic	Sub Topic
1	INTRODUCTION	DESIGN OF ALGORITHM ,ANALYSIS OF ALGORITHM, ALGORITHM PROPERTIES
2	FRAMEWORK FOR ALGORITHM ANALYSIS	HOW TO COUNT EXECUTION TIME OF ALGORITHM,INPUT INSTANCES
3	ASYMPTOTIC NOTATION	BEST CASE,AVERAGE CASE, WORST CASE
4	SOLVING RECURRENCE RELATION	SUBSTITUTION METHOD, MASTER THEOREM
5	ALGORITHM DESIGN TECHNIQUES	DIVIDE & CONQUER, GREEDY,DYNAMIC PROGRAMMING, BACKTRACKING,
6	DISJOINT SET MANIPULATION	UNION FIND
7	NETWORK FLOW PROBLEM	FORD FULKERSON ALGORITHM
8	NP COMPLETENESS	NP,NP HARD.....ALGORITHM
9	APPROXIMATION ALGORITHM	COMPLEXITY ANALYSIS OF NP COMPETE PROBLEM

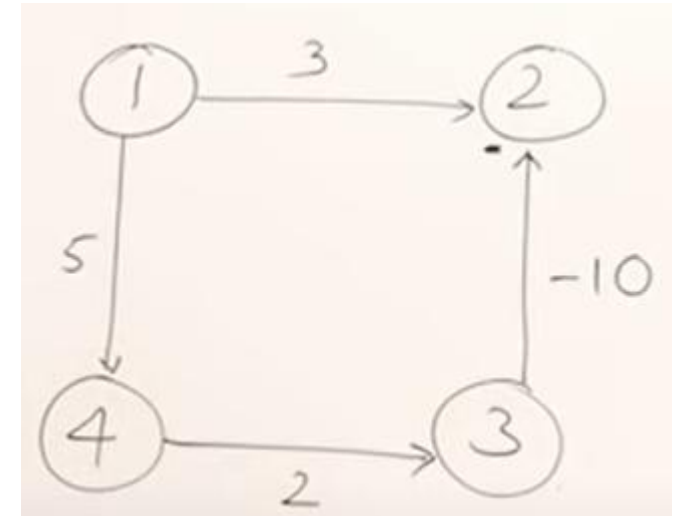
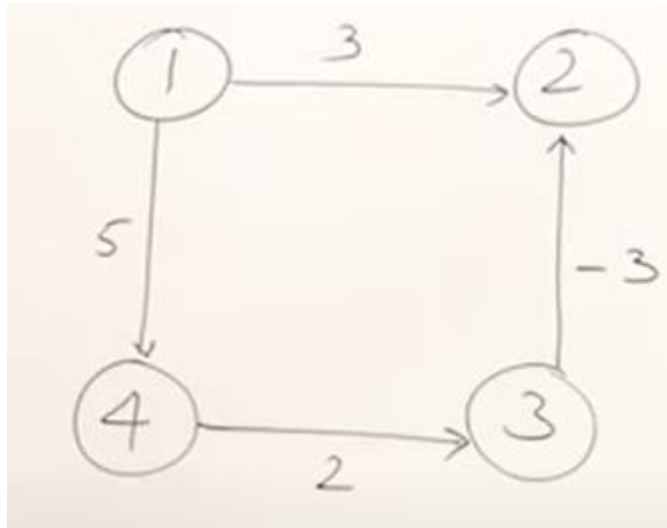
BELLMAN FORD ALGORITHM

- SINGLE SOURCE SHORTEST PATH ALGORITHM

DRAWBACK

DIJKSTRA ALGORITHM

- May or May not Support Negative weight edge.

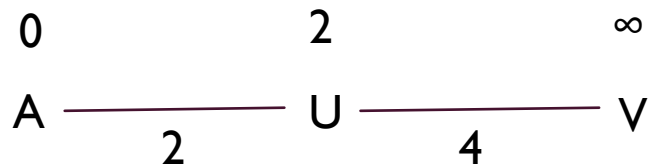


BELLMAN FORD ALGORITHM

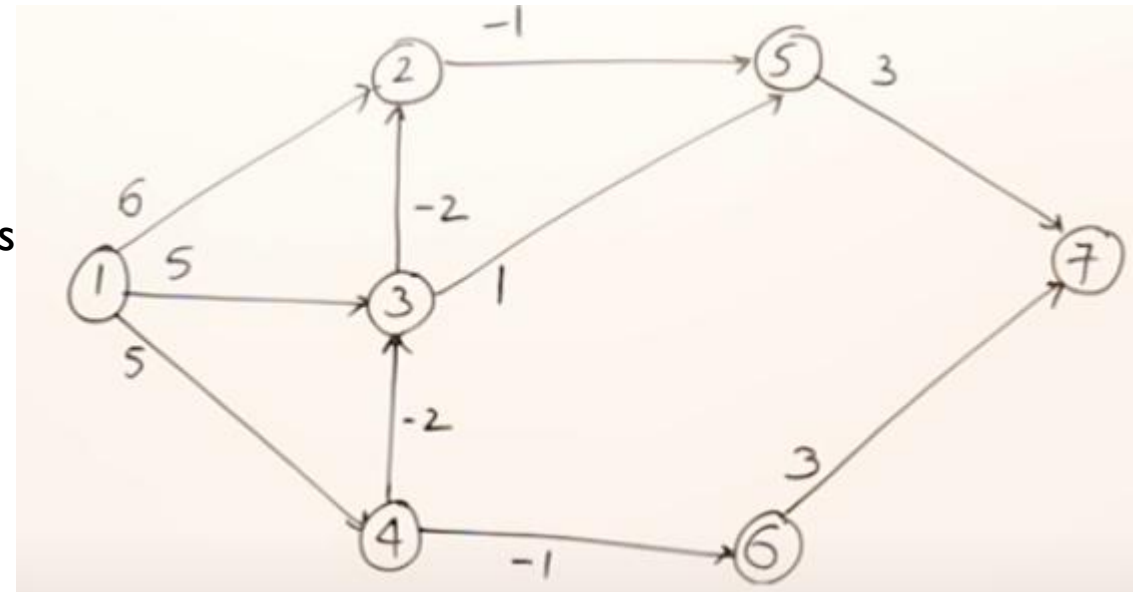
DYNAMIC PROGRAMMING

- Applicable on directed / undirected graph
- Optimization Problem
- Rule of Relaxation

It is similar to Dijkstra's algorithm but it can work with graphs in which edges can have negative weights.

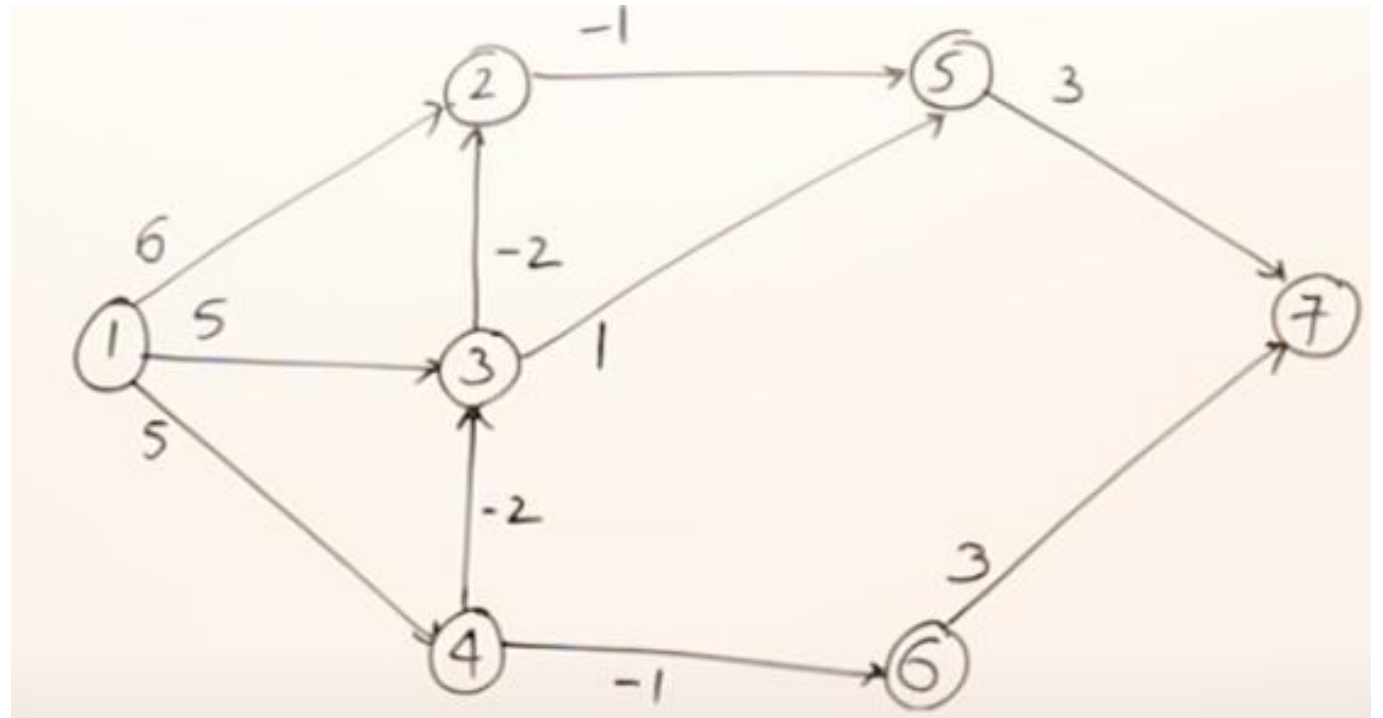


IF $(d[U] + C[U, V]) < d[V]$ THEN
SET $d[V] \leftarrow d[U] + C[U, V]$



BELLMAN FORD ALGORITHM

- Start vertex : 1
- Visit $|V|-1$ time all the edges.

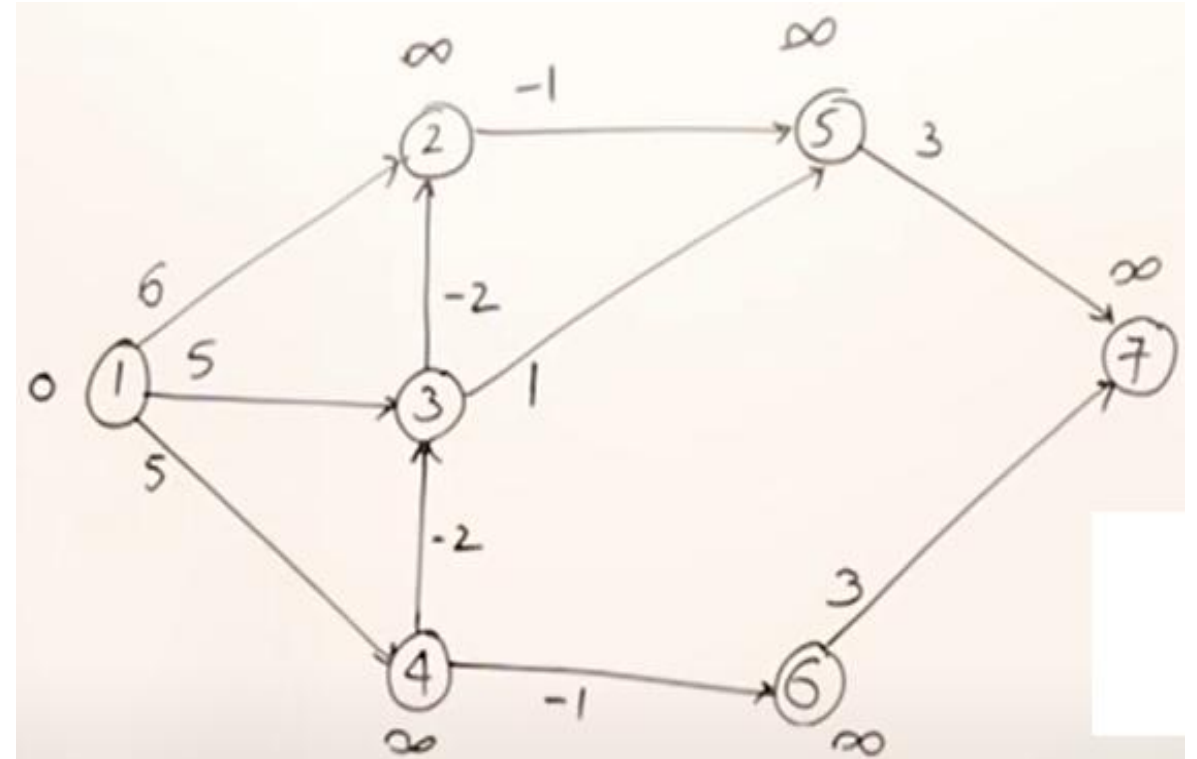


BELLMAN FORD ALGORITHM

RELAX THE EDGES (1,2)(1,3)(1,4)(2,5)(3,2)(3,5)(4,3)(4,6)(5,6)(6,7)

- Start vertex : 1

1	2	3	4	5	6	7
0	∞	∞	∞	∞	∞	∞

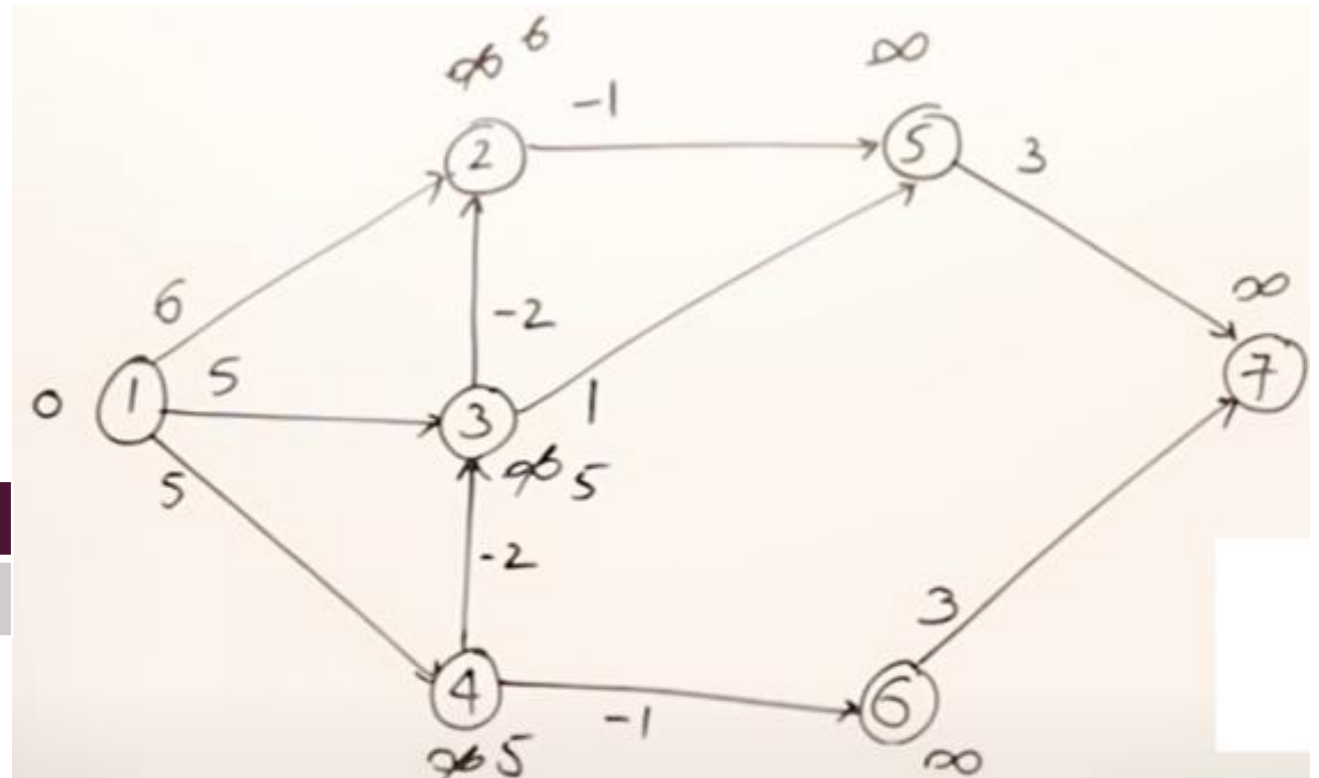


BELLMAN FORD ALGORITHM

RELAX THE EDGES ~~(1,2)~~~~(1,3)~~~~(1,4)~~(2,5)(3,2)(3,5)(4,3)(4,6)(5,7)(6,7)

■ Start vertex : 1

1	2	3	4	5	6	7
0	6	5	5	∞	∞	∞

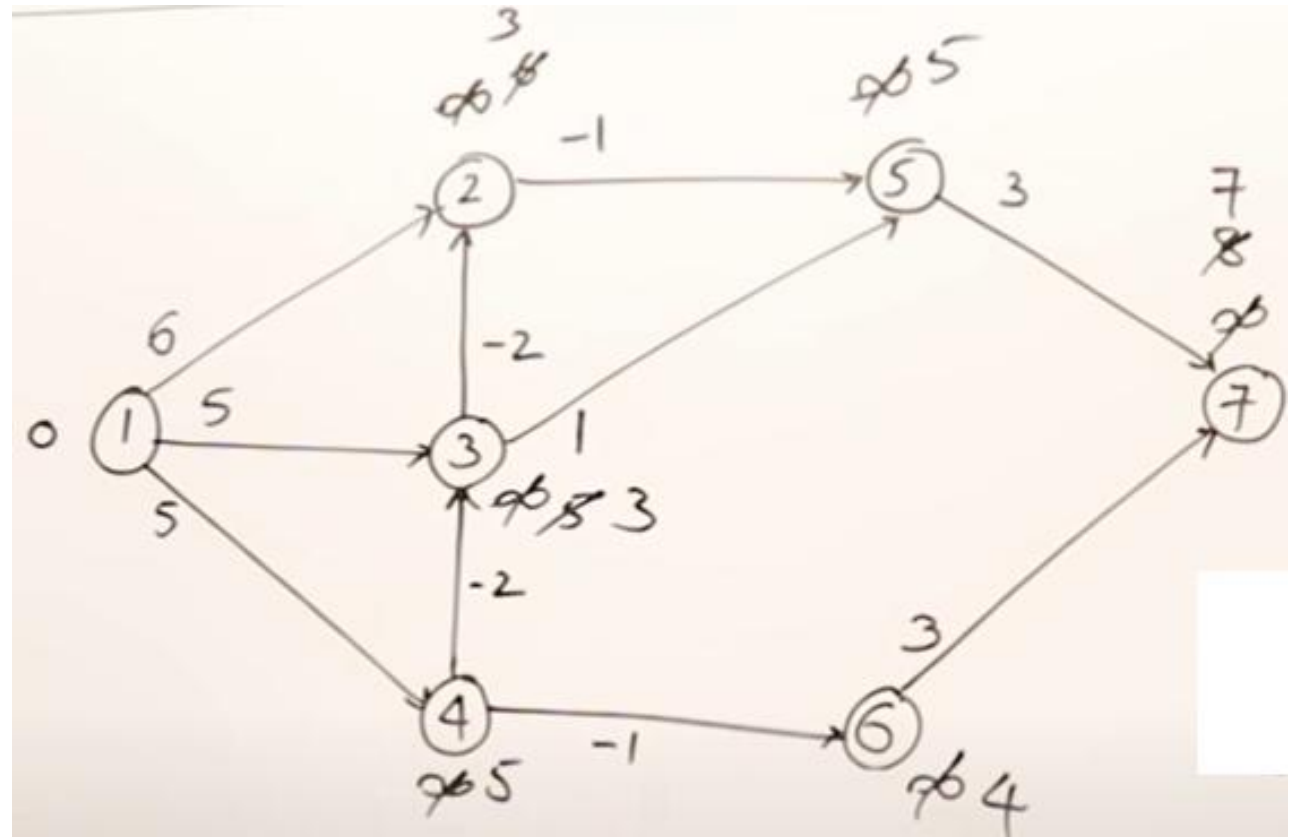


BELLMAN FORD ALGORITHM

RELAX THE EDGES ~~(1,2)~~~~(1,3)~~~~(1,4)~~~~(2,5)~~~~(3,2)~~~~(3,5)~~~~(4,3)~~~~(4,6)~~~~(5,7)~~~~(6,7)~~

■ Start vertex : 1

1	2	3	4	5	6	7
0	3	3	5	5	4	7

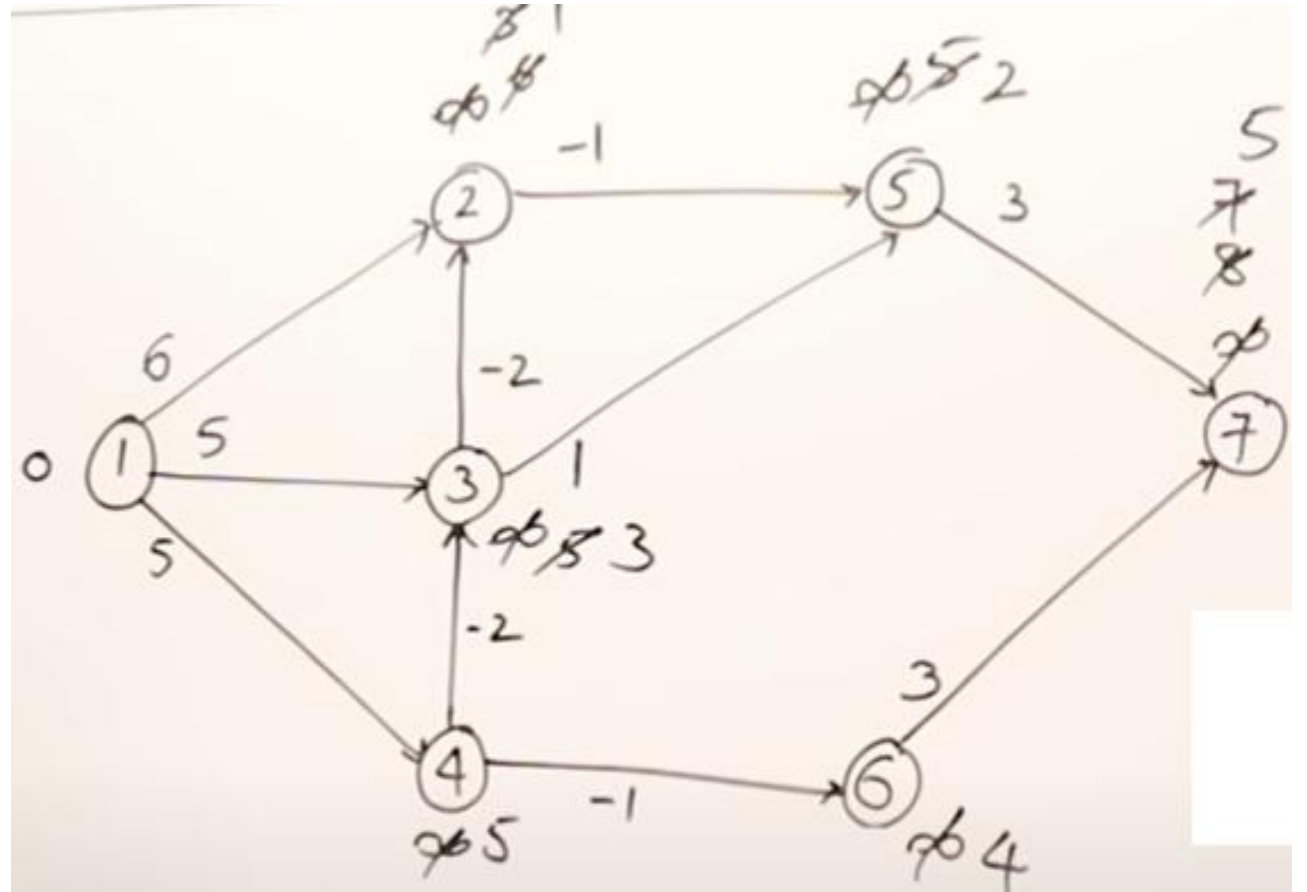


BELLMAN FORD ALGORITHM

RELAX THE EDGES (1,2)(1,3)(1,4)(2,5)(3,2)(3,5)(4,3)(4,6)(5,7)(6,7)

■ After 2nd visit.

1	2	3	4	5	6	7
0	1	3	5	2	4	5

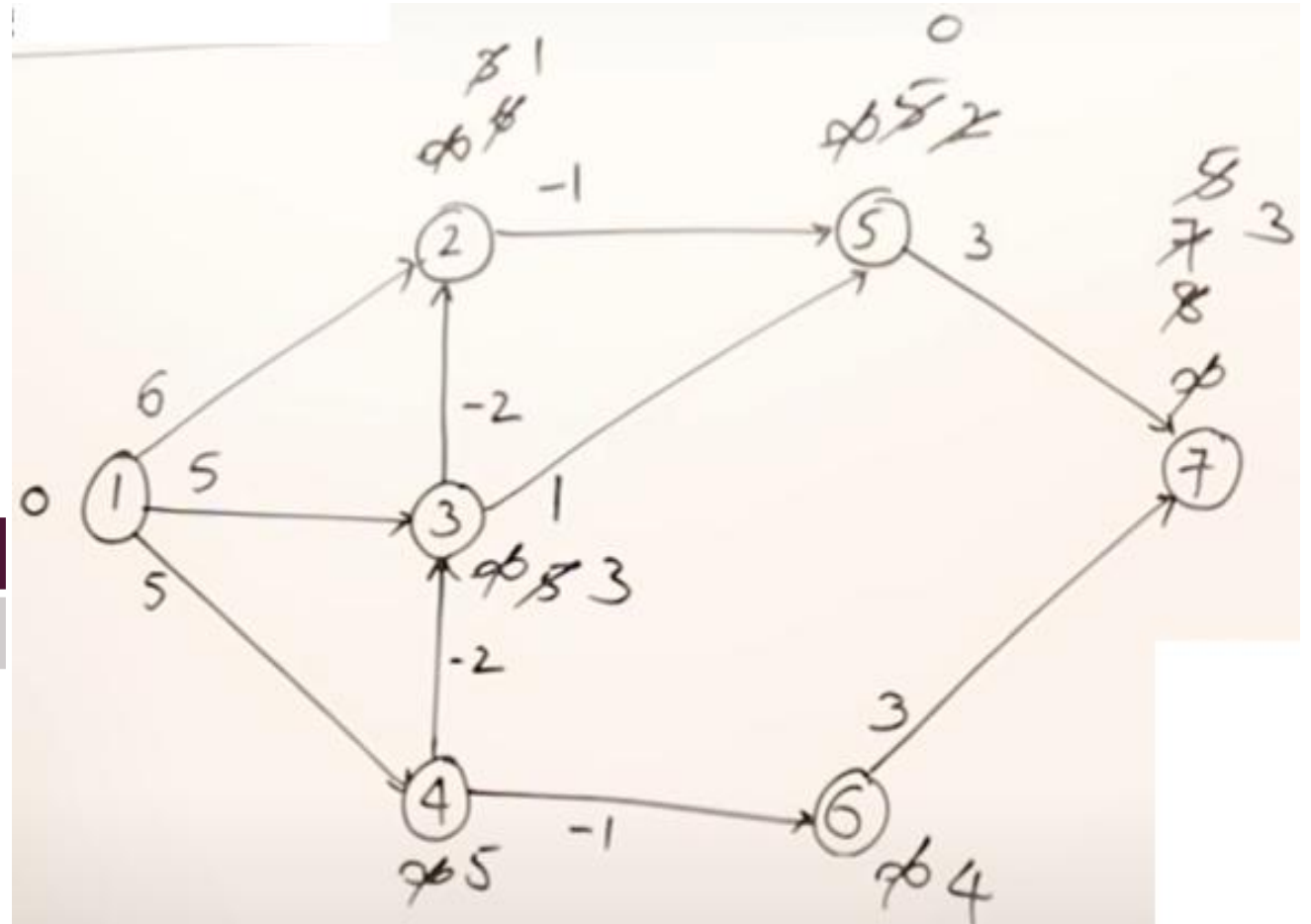


BELLMAN FORD ALGORITHM

RELAX THE EDGES (1,2)(1,3)(1,4)(2,5)(3,2)(3,5)(4,3)(4,6)(5,6)(6,7)

■ After 3rd visit.

1	2	3	4	5	6	7
0	1	3	5	0	4	3

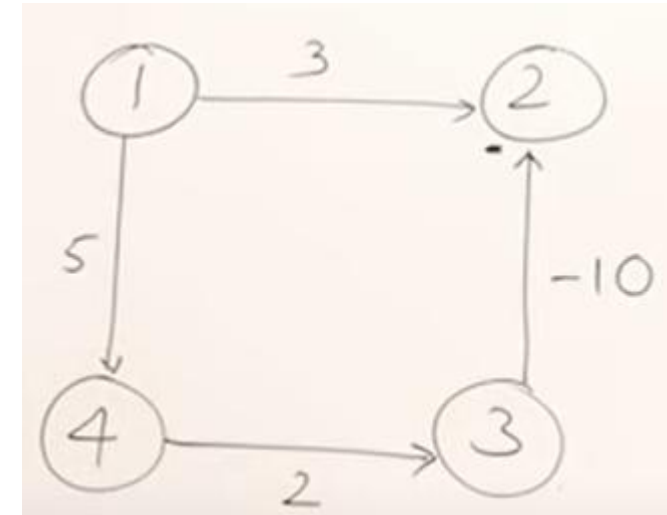
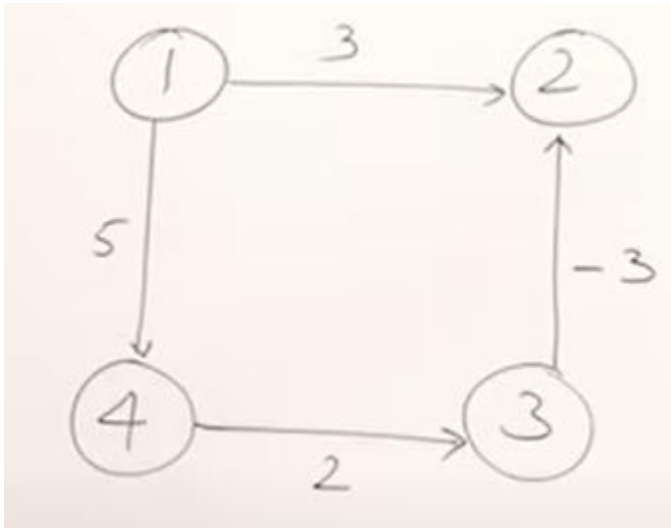


BELLMAN FORD ALGORITHM

ANALYSIS

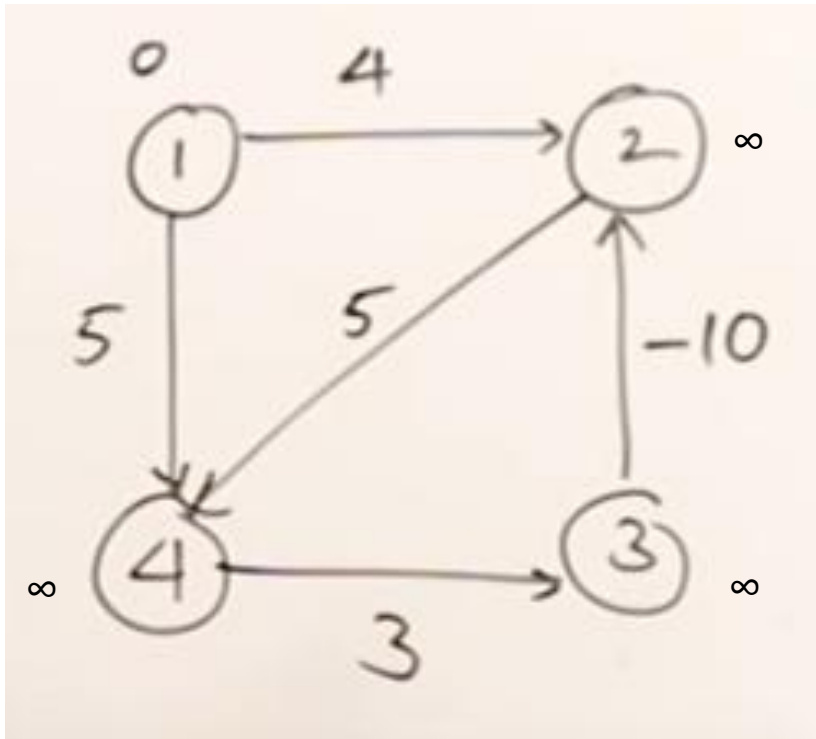
- $(|V|-1) E \rightarrow O(|V||E|) \rightarrow O(n^2)$
- For complete Graph $E = n(n-1)/2 \dots\dots\dots O(|V||E|) \rightarrow O(n^3)$

BELLMAN FORD ALGORITHM



BELLMAN FORD ALGORITHM

(1,2)(1,4)(2,4)(3,2)(4,3)



$|V|-1$

After 3rd time visit

1	2	3	4
0	-2	6	3

NEGATIVE WEIGHT CYCLE

NEXT CLASS

- Travelling Salesman Problem.