



# DESIGN & ANALYSIS OF ALGORITHM

PCC-CS501

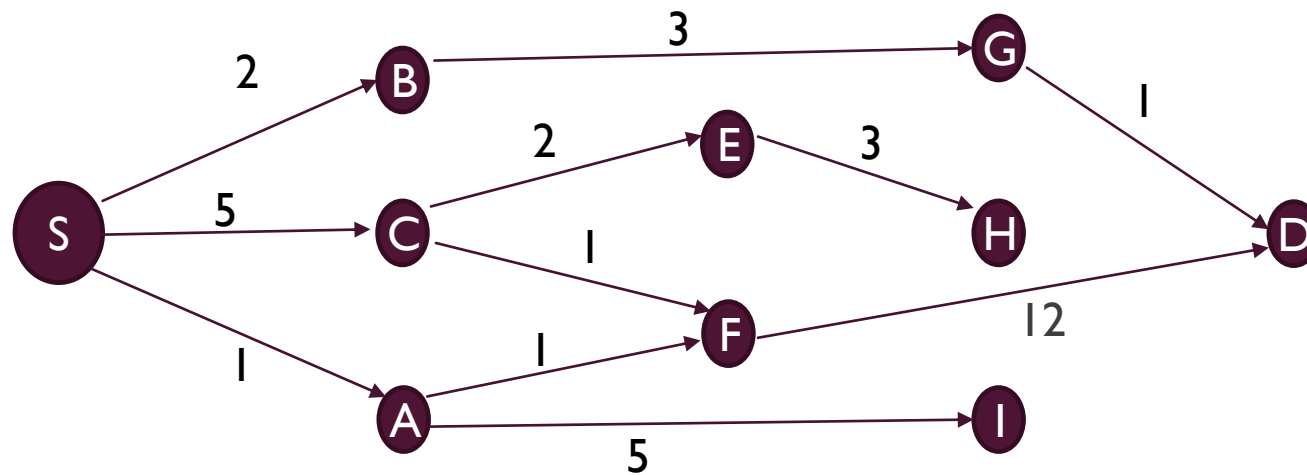


# DESIGN & ANALYSIS OF ALGORITHM

## SCHEDULE ----TOPIC WISE

	Topic	Sub Topic
1	INTRODUCTION	DESIGN OF ALGORITHM ,ANALYSIS OF ALGORITHM, ALGORITHM PROPERTIES
2	FRAMEWORK FOR ALGORITHM ANALYSIS	HOW TO COUNT EXECUTION TIME OF ALGORITHM,INPUT INSTANCES
3	ASYMPTOTIC NOTATION	BEST CASE,AVERAGE CASE, WORST CASE
4	SOLVING RECURRENCE RELATION	SUBSTITUTION METHOD, MASTER THEOREM
5	ALGORITHM DESIGN TECHNIQUES	DIVIDE & CONQUER, GREEDY,DYNAMIC PROGRAMMING, BACKTRACKING,
6	DISJOINT SET MANIPULATION	UNION FIND
7	NETWORK FLOW PROBLEM	FORD FULKERSON ALGORITHM
8	NP COMPLETENESS	NP,NP HARD.....ALGORITHM
9	APPROXIMATION ALGORITHM	COMPLEXITY ANALYSIS OF NP COMPETE PROBLEM

# QUESTION DOES GREEDY ENSURE OPTIMALITY?



## GREEDY APPROACH

## DISADVANTAGE

- GREEDY DOES NOT ENSURE OPTIMAL SOLUTION.

# DYNAMIC PROGRAMMING

- Considers All possible solution, then consider the optimal solution.
- Time consuming Method.
- Follows Principle of Optimality: Problem must be solved in sequence of decision.
- Overlapping Sub-problem.
- Memorization
- Tabulation

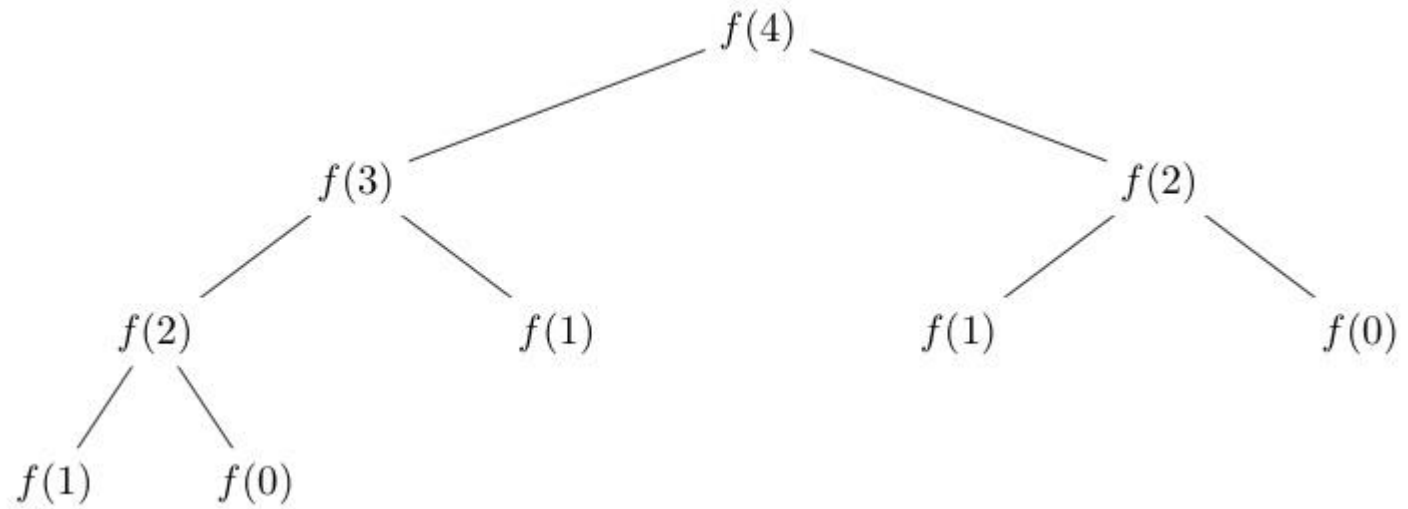
# FIBONACCI SERIES

For  $n \geq 2$ ,  $f_n = f_{n-1} + f_{n-2}$

For  $n=0$ ,  $f_n=0$

For  $n=1$ ,  $f_n=1$

```
■ Int fibo(int n)
{
    if(n <= 1)
        return n
    return fibo(n-1)+fibo(n-2)
}
```



$$T(n) = 2T(n-1) + 1$$

$$O(2^n)$$

# MEMORIZATION

# TOP-DOWN

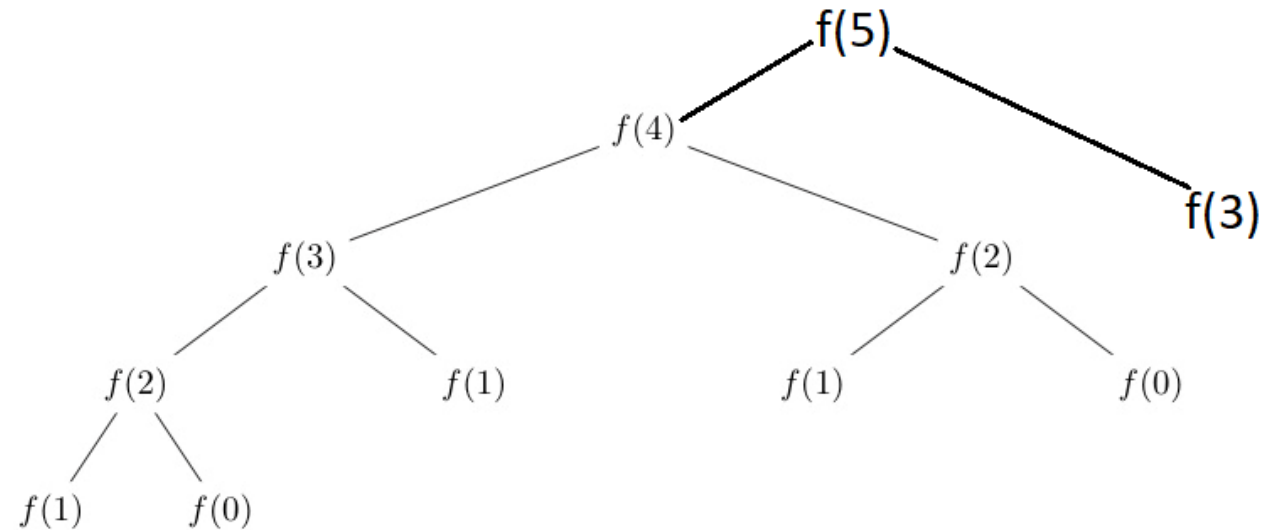
# FIBONACCI SERIES



0 1 2 3 4 5

```
■ Int fibo(int n)
{
    if(n<=1)
        return n
    return fibo(n-1)+fibo(n-2)
}
```

$\text{fibo}(n)=n+1$



$$T(n) = 2T(n-1) + 1$$

$$O(2^n)$$

# MEMORIZATION

# FIBONACCI SERIES

The memoized version of the recursive Fibonacci algorithm looks like this:

- If  $n$  is 0 or 1, return  $n$
- Otherwise, if  $n$  is in the memo, return the memo's value for  $n$
- Otherwise,
  - Calculate  $\text{fibonacci}(n - 1) + \text{fibonacci}(n - 2)$
  - Store result in memo
  - Return result

$n$	Original	Memoized
5	15	9
6	25	11
7	41	13
8	67	15
9	109	17
10	177	19



# TABULATION METHOD

# BOTTOM-UP

# FIBONACCI SERIES

■ Int fibo(n)

{

if(n<=1)

return n

F[0]=0 F[1]=1

for(i=2;i<n;i++)

F[i]=F[i-1]+F[i-2]

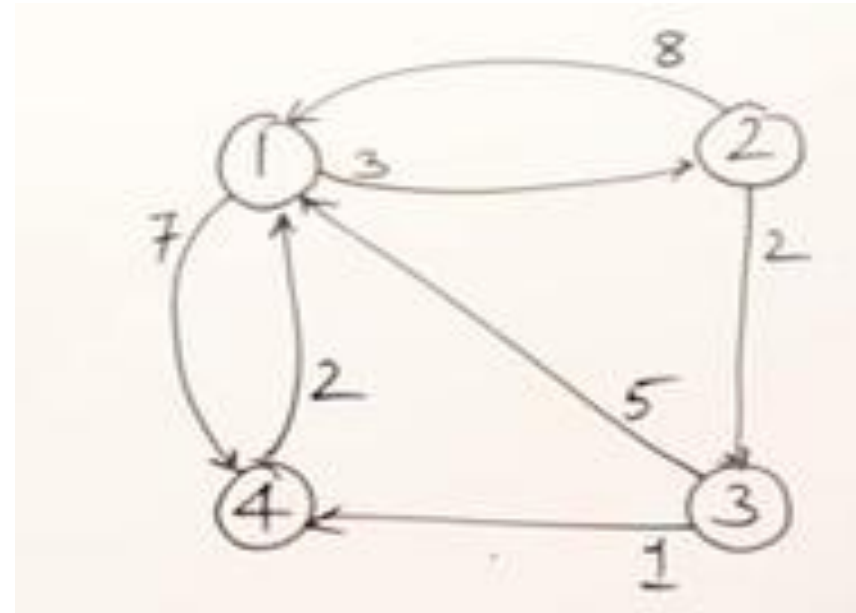
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# DYNAMIC PROGRAMMING

## FLOYD WARSHALL'S ALGORITHM

- All Pair Shortest Path Problem.

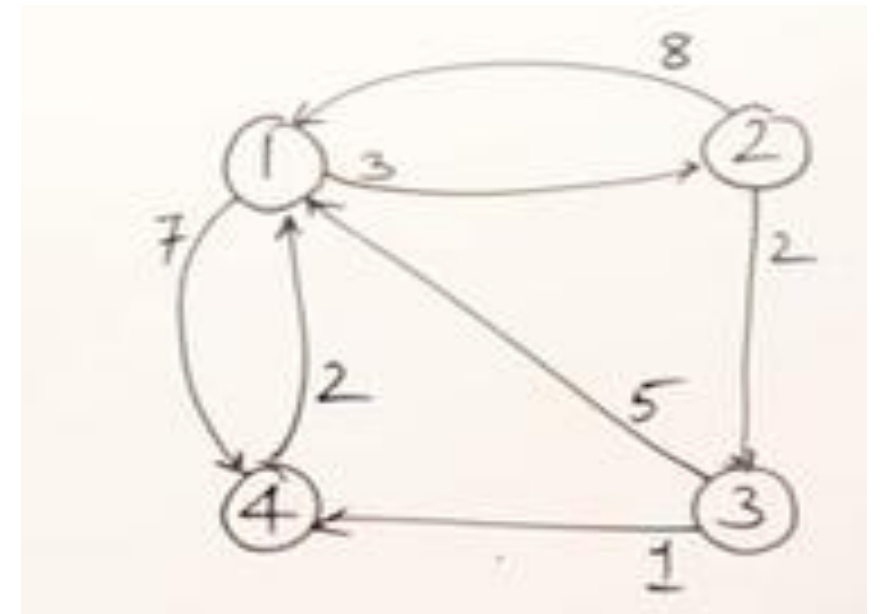


# DYNAMIC PROGRAMMING

## FLOYD WARSHALL'S ALGORITHM

$$A^0 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 3 & \infty & 7 \\ 8 & 0 & 2 & \infty \\ 5 & \infty & 0 & 1 \\ 2 & \infty & \infty & 0 \end{bmatrix} \end{matrix}$$

- $\min(\text{dist}[i][k] + \text{dist}[k][j], \text{dist}[i][j])$ .



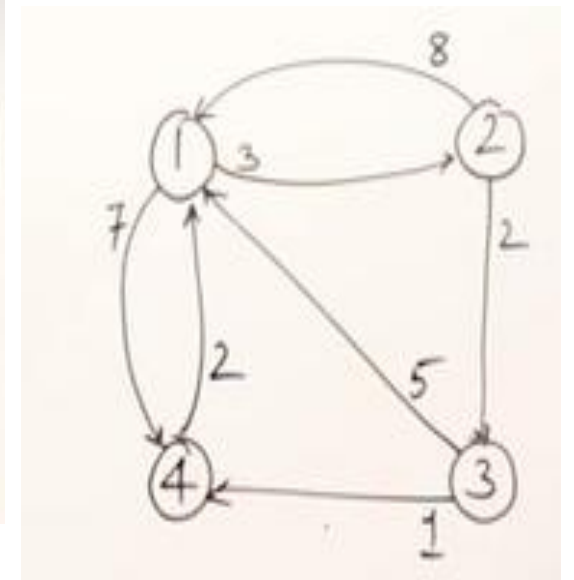
# DYNAMIC PROGRAMMING

# FLOYD WARSHALL'S ALGORITHM

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$$A^1 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 3 & \infty & 7 \\ 8 & 0 & & \\ 5 & & 0 & \\ 2 & & & 0 \end{bmatrix} \end{matrix}$$

$$A^2 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 3 & \infty & 7 \\ 8 & 0 & 2 & 15 \\ 5 & 8 & 0 & 1 \\ 2 & 5 & \infty & 0 \end{bmatrix} \end{matrix}$$

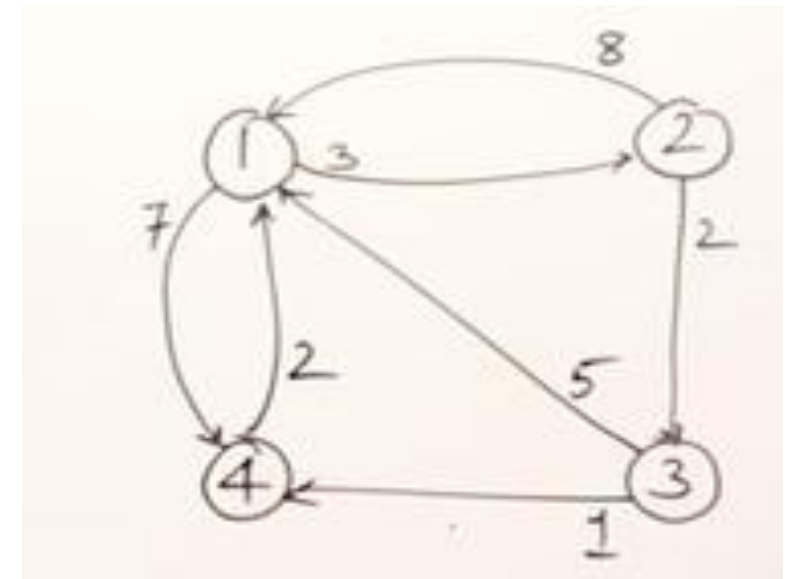


$$\min(\text{dist}[i][k] + \text{dist}[k][j], \text{dist}[i][j])$$

# DYNAMIC PROGRAMMING

# FLOYD WARSHALL'S ALGORITHM

$$A^1 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 3 & \infty & 7 \\ 8 & 0 & 2 & 15 \\ 5 & 8 & 0 & 1 \\ 2 & 5 & \infty & 0 \end{bmatrix} \end{matrix}$$
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$$A^3 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 3 & 5 & 6 \\ 7 & 0 & 2 & 3 \\ 5 & 8 & 0 & 1 \\ 2 & 5 & 7 & 0 \end{bmatrix} \end{matrix}$$
$$A^4 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 3 & 5 & 6 \\ 5 & 0 & 2 & 3 \\ 3 & 6 & 0 & 1 \\ 2 & 5 & 7 & 0 \end{bmatrix} \end{matrix}$$



```
■ for (k = 0; k < V; k++)  
■ {  
■   for (i = 0; i < V; i++)  
■     {  
■       for (j = 0; j < V; j++)  
■         {  
■           if (dist[i][k] + dist[k][j] < dist[i][j])  
■             dist[i][j] = dist[i][k] + dist[k][j];  
■         }  
■     }  
■ }
```

# NEXT CLASS

- KNAPSACK USING DYNAMIC PROGRAMMING