



DESIGN & ANALYSIS OF ALGORITHM

PCC-CS501



DESIGN & ANALYSIS OF ALGORITHM

SCHEDULE ----TOPIC WISE

	Topic	Sub Topic
1	INTRODUCTION	DESIGN OF ALGORITHM ,ANALYSIS OF ALGORITHM, ALGORITHM PROPERTIES
2	FRAMEWORK FOR ALGORITHM ANALYSIS	HOW TO COUNT EXECUTION TIME OF ALGORITHM,INPUT INSTANCES
3	ASYMPTOTIC NOTATION	BEST CASE,AVERAGE CASE, WORST CASE
4	SOLVING RECURRENCE RELATION	SUBSTITUTION METHOD, MASTER THEOREM
5	ALGORITHM DESIGN TECHNIQUES	DIVIDE & CONQUER, GREEDY,DYNAMIC PROGRAMMING, BACKTRACKING,
6	DISJOINT SET MANIPULATION	UNION FIND
7	NETWORK FLOW PROBLEM	FORD FULKERSON ALGORITHM
8	NP COMPLETENESS	NP,NP HARD.....ALGORITHM
9	APPROXIMATION ALGORITHM	COMPLEXITY ANALYSIS OF NP COMPETE PROBLEM

NEXT CLASS

DISJOINT SET MANIPULATION

■ Kruskal's Algorithm

- INITIALIZE AN EMPTY EDGE SET T.
- SORT ALL GRAPH EDGES BY THE ASCENDING ORDER OF THEIR WEIGHT VALUES.
- FOR EACH EDGE IN THE SORTED EDGE LIST **CHECK WHETHER IT WILL CREATE A CYCLE** WITH THE EDGES INSIDE T.
- IF THE EDGE DOESN'T INTRODUCE ANY **CYCLES**, ADD IT INTO T.
- IF T HAS $(V-1)$ EDGES, EXIT THE LOOP.
- RETURN T

DISJOINT SET

- DISJOINT SET & OPERATIONS
- DETECTING A CYCLE
- GRAPHICAL REPRESENTATION
- ARRAY REPRESENTATION
- WEIGHTED UNION & COLLAPSING FIND

DISJOINT SET & OPERATIONS

- SET with **Distinct elements**.

Example- A :{2,4,8,16} B:{3,9,18}

- **FIND** – Find a vertex & returns the disjoint set.
- **UNION** – If Find operation generates two different set for an edge then union combines them to a single disjoint set.
- **Application**- kruskal's Algorithm

DISJOINT SET & OPERATIONS

- $A : \{2, 4, 8, 16\}$ $B : \{3, 9, 18\}$
- Find(2) output A
- Find(3) output B
- Union(2,3) $\rightarrow C : \{2, 4, 8, 16, 3, 9, 18\}$

DISJOINT SET & OPERATIONS

- Find(Edge)-----Edge(x,y)-----Find(x) & Find(y)
- If Find(x) & Find(y) outputs are different then using Union(x ,y) can merge the two set into a single set otherwise cycle is confirmed.

NEED OF FIND & UNION OPERATIONS

- TO DETECT CYCLE.

DETECT CYCLE USING IN KRUSKAL'S

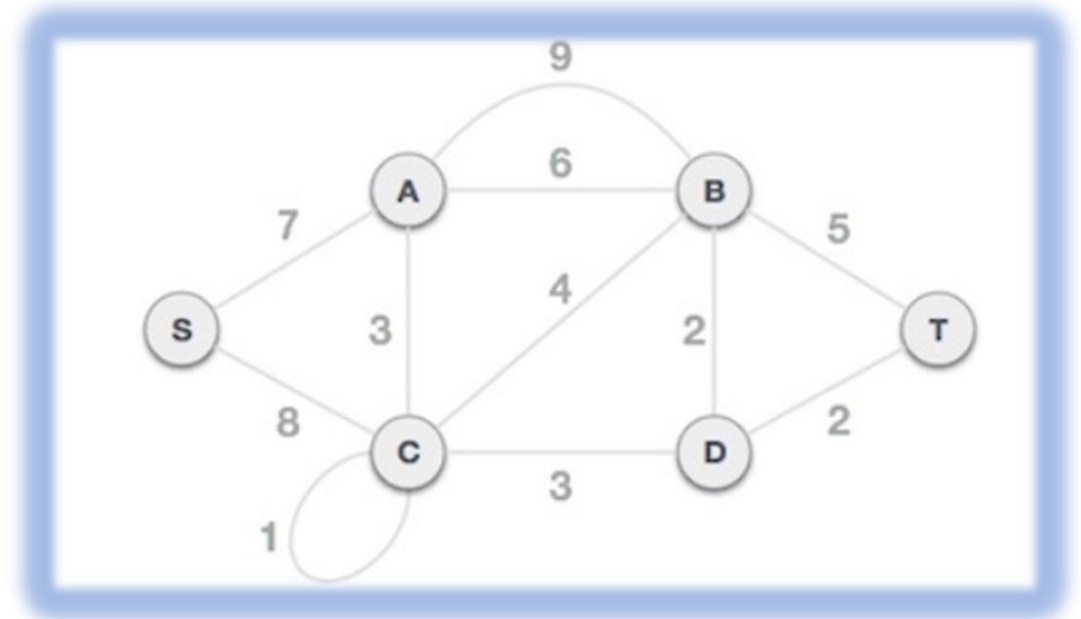
UNIVERSAL SET(U) {S,A,C,B,D,T}

Edge BD find(B)- B find(D)-D union (B,D) E1-{B,D}
 Edge DT find(D)- E1 find(T)-U union(D,T) E2- B,D,T
 Edge AC find(A)- A find(C)-C union(A,C) E3- A,C
 Edge CD find(C)- E3 find(D)-E2 union(C,D) E4- A,B,C,D,T

Edge BC find(B)- E4 find(C)- E4 **CYCLE DETECTION**

Edge BT find(B)- E4 find(T)- E4 **CYCLE DETECTION**
 Edge AB find(A)- E4 find(B)- E4 **CYCLE DETECTION**

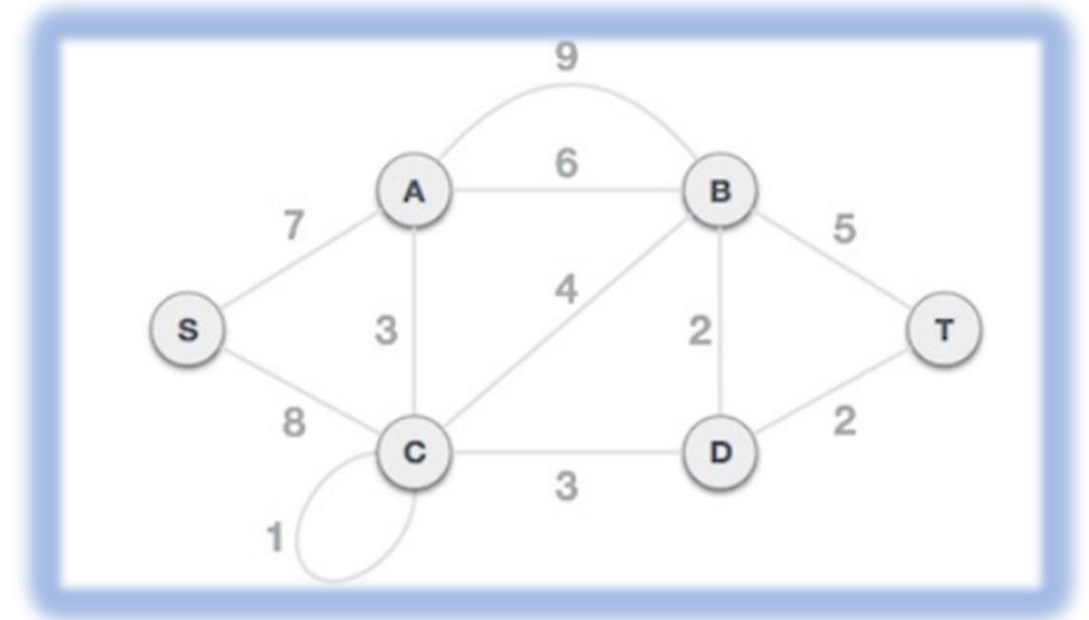
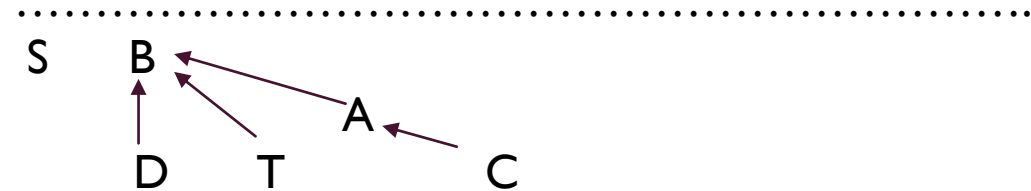
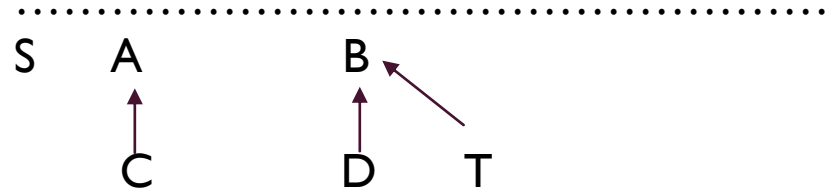
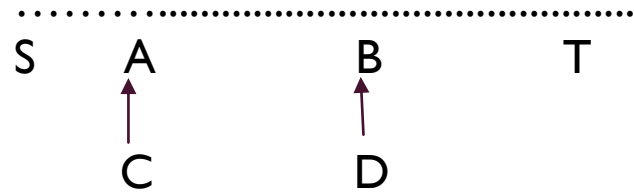
Edge AS find(A)- E4 find(S)- S union(A,S) E5-A, B, C, D, T, S



B, D	D, T	A, C	C, D	C, B	B, T	A, B	S, A	S, C
2	2	3	3	4	5	6	7	8

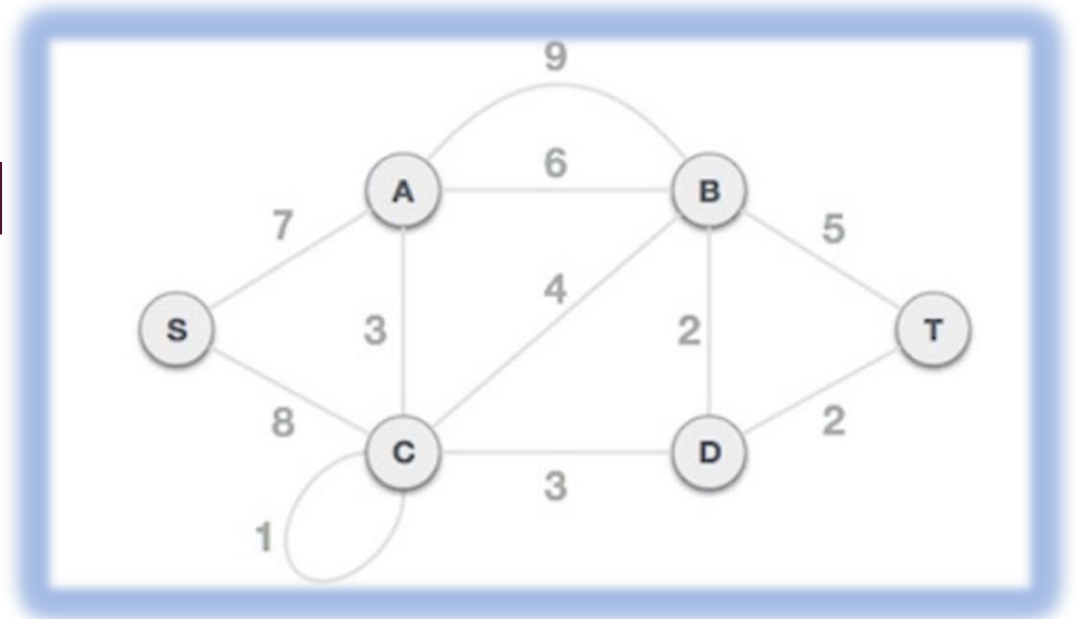
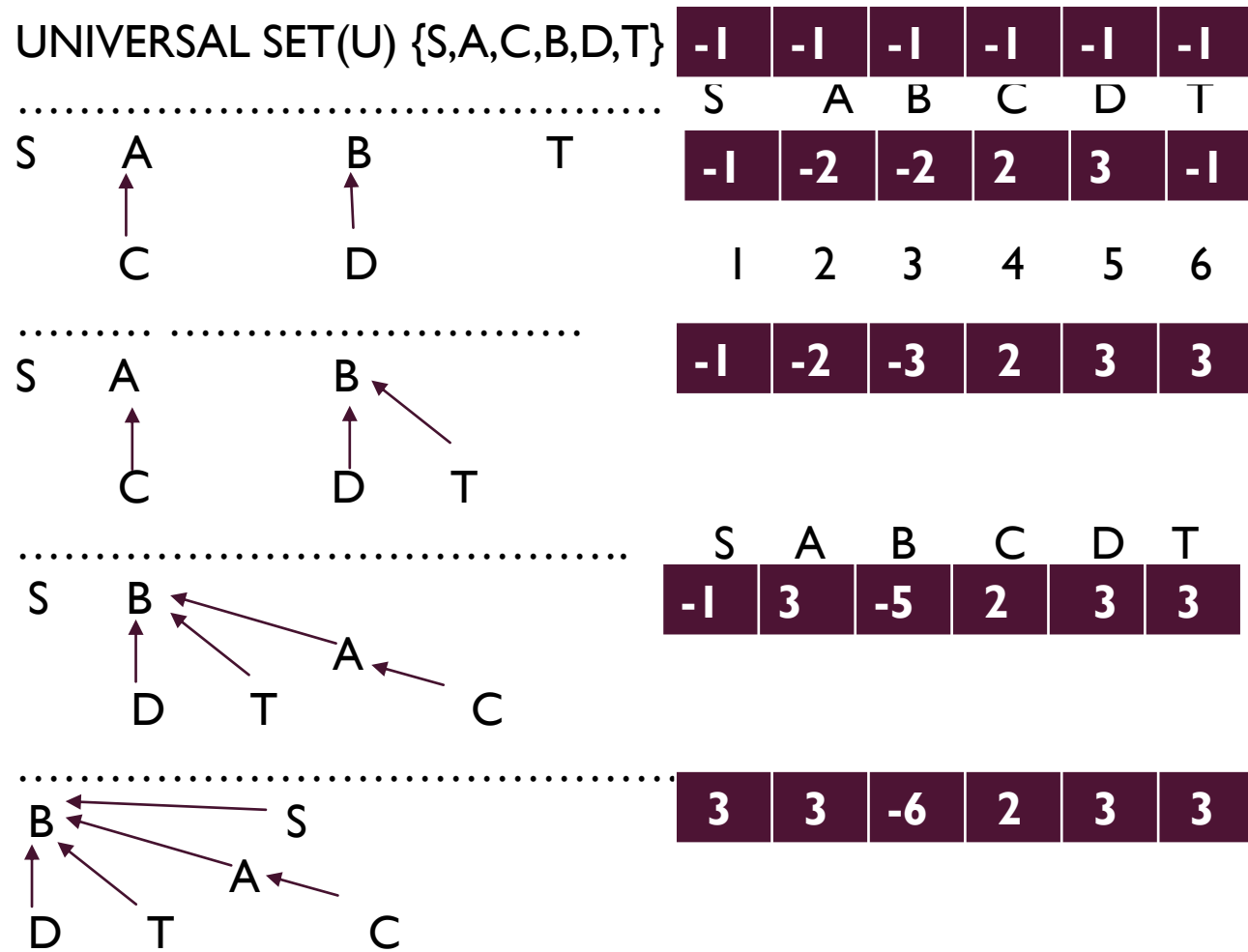
GRAPHICAL REPRESENTATION

UNIVERSAL SET(U) {S,A,C,B,D,T}



B, D	D, T	A, C	C, D	C, B	B, T	A, B	S, A	S, C
2	2	3	3	4	5	6	7	8

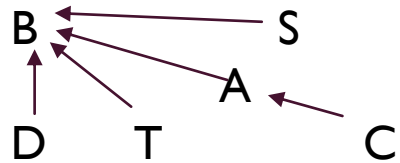
GRAPHICAL & ARRAY REPRESENTATION



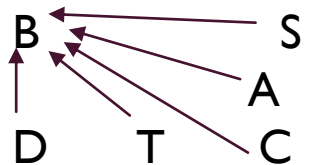
B, D	D, T	A, C	C, D	C, B	B, T	A, B	S, A	S, C
2	2	3	3	4	5	6	7	8

WEIGHTED UNION & COLLAPSING FIND

UNIVERSAL SET (U) {S,A,C,B,D,T}

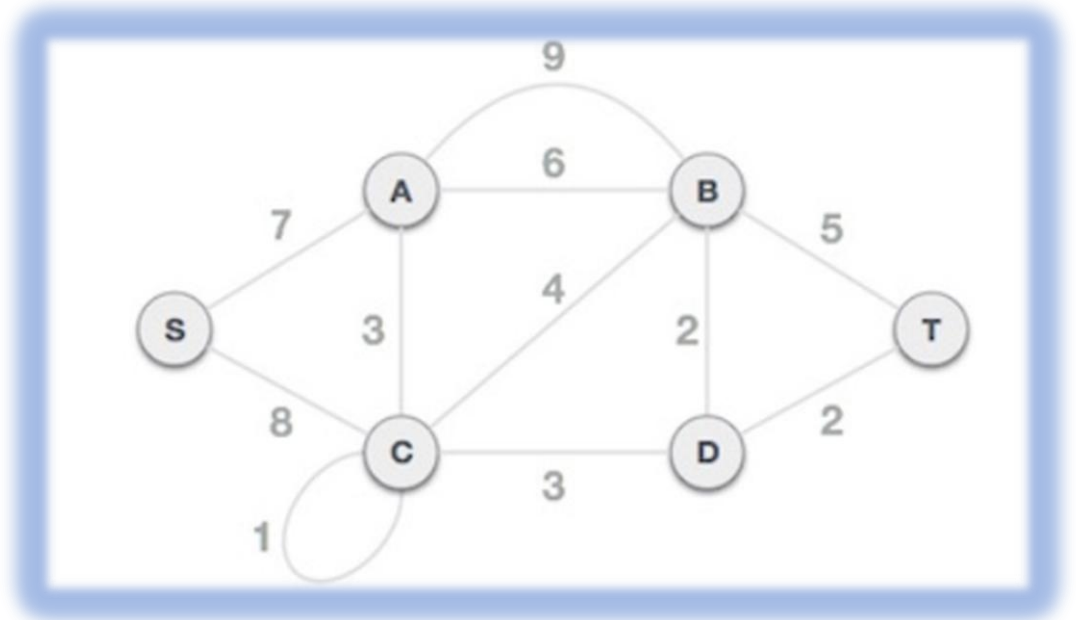


	S	A	B	C	D	T
1	-1	-1	-1	-1	-1	-1
2	3	3	-6	2	3	3
3						
4						
5						
6						



	S	A	B	C	D	T
1	-1	-1	-1	-1	-1	-1
2	3	3	-6	2	3	3
3						
4						
5						
6						

Find() takes constant time



B, D	D, T	A, C	C, D	C, B	B, T	A, B	S, A	S, C
2	2	3	3	4	5	6	7	8

NEXT CLASS

- Single Source Shortest Path Problem / Dijkstra's Algorithm