

# **DESIGN AND ANALYSIS OF ALGORITHM**

## **IMP**

Based on the frequency and weightage of the questions in the provided past papers, here's a prioritized study plan for "Design and Analysis of Algorithms (BTCOC401)":

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### **High Priority Topics (Guaranteed to Appear & High Marks)**

These topics consistently appear across all provided papers and often carry significant marks. Master these first.

#### **1. Asymptotic Notations:**

- Define and explain Big O, Big Omega, and Big Theta notations with expressions and neat graphs.
- Proving relationships between functions using asymptotic notations (e.g.,  $f(n)=\sqrt{n}$  and  $g(n)=n$ , prove  $f(n)$  is  $O(g(n))$ ).
- This is fundamental and usually asked in Q.1.

#### **2. Recurrence Relations (Master Method):**

- Solve recurrence relations using the Master Theorem (e.g.,  $T(n)=4T(n/2)+n$ ,  $T(n)=4T(n/2)+n^2$ ,  $T(n)=4T(n/2)+n^3$ ,  $T(n)=16T(n/4)+n$ ,  $T(n)=T(2n/3)+1$ ,  $T(n)=3T(n/4)+n\log n$ ).
- Verify solutions using the substitution method.
- Another core topic for Q.1.

#### **3. Merge Sort:**

- Algorithm description and finding its time complexity.
- Applying Merge Sort to a given array (e.g.,  $A=5\ 1\ 2\ 6\ 3\ 7\ 4$ ,  $A=\{5\ 2\ 4\ 7\ 3\ 2\ 6\}$ ,  $A=\{13,4,22,1,16,9,0,2\}$ ).
- Best case and worst case time complexity.
- Very frequent in Q.2.

#### **4. Strassen's Matrix Multiplication:**

- Algorithm description and its time complexity.
- Apply the algorithm to multiply two  $2 \times 2$  matrices (e.g.,  $(6574)(1324)$ ,  $A=(1111)$ ,  $B=(2222)$ ,  $A=(1221)$ ,  $B=(5667)$ ,  $A=(2236)$ ,  $B=(6487)$ ).
- A common application-based question in Q.2.

#### **5. Huffman Coding:**

- Huffman Coding algorithm and elements of greedy strategy.
- Obtain Huffman tree and codes for given character frequencies (e.g., a:50, b:25, c:15, d:40, e:75; a:6, b:11, c:19, d:35, e:50; a:45, b:13, c:12, d:16, e:9, f:5).
- Frequently asked in Q.3.

#### 6. Longest Common Subsequence (LCS):

- Compute LCS using Dynamic Programming approach for given sequences (e.g.,  $X=\{A,B,C,B,D,A,B\}$  and  $Y=\{B,D,C,A,B,A\}$ ;  $X=\langle x,m,j,y,a,u,z \rangle$  and  $Y=\langle m,z,j,a,w,x,u \rangle$ ).
- State the length of the LCS.
- A recurring question in Q.4.

#### 7. 4-Queens Problem (Backtracking):

- Solve the 4-Queens problem using the backtracking approach and draw the state space tree.
- Consistently asked in Q.3 or Q.5.

#### 8. P, NP, NP-Complete Problems:

- Explain the concepts of P, NP, and NP-Complete classes and show the relationship between them.
- A theoretical question often found towards the end (Q.4 or Q.5).

#### 9. Fractional Knapsack Problem:

- Solve the fractional knapsack problem given objects' profits/weights and knapsack capacity.
- This is a common application of the greedy approach. (Q.4)

#### 10. Floyd Warshall Algorithm:

- Analyze or apply Floyd's Warshall Algorithm for all-pairs shortest path.
- Important dynamic programming application (Q.5 or Q.4).

### Medium Priority Topics (Likely to Appear, Important)

These topics are also important but might appear slightly less frequently or as part of a broader question.

#### 1. Algorithm Basics:

- Define Algorithm and state its main characteristics/criteria.

- Need for algorithm analysis and factors affecting runtime of an algorithm.
  - Often combined with other basic questions in Q.1.
  - 2. Quick Sort:**
    - Algorithm and its best/worst case analysis with examples.
    - Time complexity. (Q.2)
  - 3. Dynamic Programming vs. Greedy Approach vs. Divide and Conquer:**
    - Differentiate between these algorithm design paradigms.
    - Often asked as a comparative question (Q.2 or Q.5).
  - 4. Job Sequencing with Deadlines:**
    - Solve problems using this greedy approach.
    - A specific application of greedy strategy. (Q.4)
  - 5. Travelling Salesman Problem (TSP) using Branch and Bound:**
    - Apply Branch and Bound technique to solve TSP for a given matrix/graph.
    - A key application of Branch and Bound (Q.3 or Q.5).
  - 6. Graph Coloring Problem:**
    - Describe with a suitable example. (Q.3)
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### **Lower Priority Topics (May Appear, Good to Know)**

These are less frequent but could still be part of a question or asked as a standalone if other high-priority topics are covered differently.

- 1. Binary Search:**
  - Algorithm and its time complexity. (Q.2)
- 2. Max and Min Heap:**
  - Define and write algorithm to insert into a heap. (Q.1)
- 3. Bellman Ford Algorithm:**
  - Find the shortest path for a given graph. (Q.4)
- 4. State Space Tree:**
  - General concept and its use (e.g., for sum of subsets or 15-puzzle). (Q.5)
- 5. Red-Black Tree:**

- Properties and potential operations (insertion/deletion justification). (Q.6 in older papers)
6. **B-Tree:**
- Insertion of keys and configurations. (Q.6 in older papers)
7. **Minimum Cost Spanning Tree:**
- Explanation with a suitable example. (Q.4)
8. **Polynomial Time Reduction:**
- Explain with an example. (Q.6 in older papers)

## **CHAPTER 2**

- A) Write algorithm for Binary Search and calculate its time complexity.
- B) Explain Quick Sort algorithm with its performance analysis.
- C) Explain Strassen's Matrix Multiplication with example.
- D) Describe an algorithm for Merge Sort and find its time complexity.
- E) Distinguish between Divide and Conquer and Dynamic programming approach.

