

RV College of Engineering[®] Mydete Roled RV Vidyaniki ton Post, Bengaluro - 000039 Kamataka India

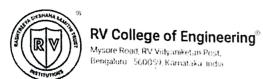
DEPARTMENT OF MATHEMATICS

Course: Fundamentals of Linear Algebra, Calculus	CIE-2	Maximum marks: 10+50
and Statistics	First semester 2024-2025	2 00 PM 4 00 PM
Course code: MA211TC	Chemistry Cycle Branch: CI, BT, CD, CS, CY, IS	Time: 2.00 PM - 4.00 PM Date: 11/12/2024

	Dianch. Ci, Di, Co,				
	Answer all questions	М	вт	со)
,	PART A				
.1	The Cartesian form of the polar curve $r = 2(\sin \theta - \cos \theta)$ is	2	1	1	Ĺ
.2	The radius of curvature at (x, y) of the curve $y = \frac{c}{2} \left(e^{x/c} + e^{-x/c} \right)$ is	2	2	2	
.3	The coefficient of $\left(x - \frac{\pi}{2}\right)^2$ in the Taylor's series expansion of $\cos x$ about the point $x = \frac{\pi}{2}$ is	2	1	2	2
.4	If $z = x^2y$ where $x = at$, $y = 2at$ then $\frac{dz}{dt} =$	2	1		1
1.5	Given that $\cos^y x = \sin^x y$, then $\frac{dy}{dx} = $	2	1		1
	PART B				
1	Determine the angle of intersection of the pair of curves $r = \frac{a\theta}{1+\theta}$ and $r = \frac{a}{1+\theta^2}$.	10) 2	2	2
2	Show that the circle of curvature at the origin of the curve $x + y = ax^2 + by^2 + cx^3$ is	10) 3	3	3
	$(a+b)(x^2+y^2) = 2(x+y).$				
3a	Obtain the angle between the radius vector and tangent for the curve $r \cos^2\left(\frac{\theta}{2}\right) = a^2$ at $\theta = \frac{2\pi}{3}$.	4		2	1
3t		6		2	-
4	Use Maclaurin series up to fourth degree term to evaluate the approximate value of the integral	1	0	3	7
	$\int_0^1 e^{x \sin x} \ dx.$				
5	ia If $f(x,y) = x e^{xy}$, then verify that $f_{xy} = f_{yx}$.		5	2	
5	The temperature function for a bird in flight is given by		5	4	
	$T(x,y,z) = 0.09x^2 + 1.4xy + 95z^2.$				
	Use differential dT to approximate change in temperature when head wind x increases from	1			
	meter per second to 2 meters per second, bird heart rate y increases from 50 beats per minute t	0			
	55 beats per minute and flapping rate z increases from 3 flaps per second to 4 flaps per second.				

BT-Blooms Taxonomy, CO-Course Outcomes, M-Marks

Marks Distribution	Partic	ulars	CO1	CO2	CO3	CO4	LI	1.2	L3	L4	L5	L6
	Test	Max Marks	4	21	20	5	0	25	20	5	-	-
	Quiz	Max Marks	6	4			8	2				



DEPARTMENT OF MATHEMATICS

Course: Fundamentals of Linear Algebra, Calculus		
and Statistics Course code: MA211TC	CIE-1 First semester 2024-2025	Maximum marks: 50+10
Course code, MAZITIC	Chemistry Cycle Branch: CI, BT, CD, CS, CY, IS	Time: 2.00PM - 4.00PM Date: 04/11/2024

	Dianent Ci, B1, CD, CS, CY, IS Date: 04/1	1/202	.4	
Q.No	Answer all questions	М	ВТ	СО
	PART A	141	ы	CO
1.1	If the matrix $B = \begin{bmatrix} 1 & 2 & 3 \\ 0 & 6 & 9 \\ 0 & 2 & 4 \end{bmatrix}$, then the rank of its transpose is	2	1	1
1.2	Rank of a matrix of order 6 × 7 whose all minors of order 6 are zero is			
1.3		1	1	1
1.4	By Gauss Jordan method the augmented matrix $\begin{bmatrix} 1 & 1 : & 3 \\ 2 & 3 : & 2 \end{bmatrix}$ reduces to	2	1	2
	If A is an invertible matrix of order 5×5 and X is matrix of unknowns of order 5×1 , then the system $AX = 0$ has solution.	1	1	1
1.5	The solution of the given system of equations $x + y + z = 0$, $y - z = 0$, $x + 2y = 0$ is	2	2	2
1.6	If $\begin{bmatrix} \frac{4}{3} \\ 1 \end{bmatrix}$ is the eigenvector of $\begin{bmatrix} 2 & 4 \\ 3 & 1 \end{bmatrix}$. The associated eigenvalue is	2	2	2
	PART B			
1a)	Find the values of b such that the rank of the matrix $A = \begin{bmatrix} 1 & 5 & 4 \\ 0 & 3 & 2 \\ b & 13 & 10 \end{bmatrix}$ is 2.	4	2	1
1b)	Investigate for what values of λ and μ the system of simultaneous equations $x + y + z = 6$, $2x + 4y + 6z = 20$, $3x + 6y + \lambda z = \mu$ has (i) no solution (ii) unique solution (iii) infinite number of solutions,	6	3	3
2	Solve the following system of linear equations by Gauss-Elimination method	10		_
	$4x_1 - x_2 + 2x_3 - x_4 = 2$, $x_1 - 2x_2 - 3x_3 + x_4 = 4$, $x_1 + 4x_2 - x_3 + x_4 = 2$, $x_2 - 4x_3 - 0$	10	2	2
3	$4x_1 - x_2 + 2x_3 - x_4 = 2, x_1 - 2x_2 - 3x_3 + x_4 = 4, x_1 + 4x_2 - x_3 + x_4 = 2, x_2 - 4x_4 = 0.$ Apply Gauss Jordan method to find the inverse of the matrix $=\begin{bmatrix} 3 & 0 & 1 \\ -2 & 1 & 0 \\ -1 & 2 & 4 \end{bmatrix}$. Hence solve the system of equation AX $=$ B where B $=\begin{bmatrix} 1 \\ 2 \\ -1 \end{bmatrix}$.	10	3	3
4(a)	The current in the branches of an electrical network follows the system of linear equations of the form $5i_1 + 2i_2 + 12i_3 = 36$, $10i_1 - 3i_2 + 2i_3 = 10$, $3i_1 + 11i_2 - i_3 = 23$. Find an approximate solution for the above system of equations using Gauss-Seidel method. Perform 3 iterations (consider four decimal places).	5	3	4
4(b)	Find the eigenvalues and the corresponding eigenvectors of the Matrix $B = \begin{bmatrix} 1 & -2 \\ -5 & 4 \end{bmatrix}$.	5	1	2
5	In analysing connectivity between pages, Google's PageRank algorithm uses eigenvalues and eigenvectors to determine the importance of pages. For a simplified network analysis, identify the dominant eigenvalue and corresponding eigenvector of the matrix $A = \begin{bmatrix} 3 & 1 & 0 \\ 1 & 2 & 1 \\ 0 & 1 & 3 \end{bmatrix}$ by Rayleigh's power method with the initial approximation $\begin{bmatrix} 1 & 0 & 0 \end{bmatrix}^T$. Perform 5 iterations.	10	2	4

BT-Blooms Taxonomy, CO-Course Outcomes, M-Marks

	Particula	rs	C01	CO2	СОЗ	CO4	Li	1.2	1.3	L4	L5	L6
Marks Distribution	Test	Max Marks	4	15	16	15	6	23	21	-		-
	Quiz	Max Marks	4	6			6	4				

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RV COLLEGE OF ENGINEERING®

(An Autonomous Institution Affiliated to VTU)

I Semester B. E. Regular / Supplementary Examinations Feb/Mar-2025 Common to AIML / BT / CS / CY / CD / IS

FUNDAMENTALS OF LINEAR ALGEBRA, CALCULUS AND STATISTICS

Time: 03 Hours

Maximum Marks: 100

Instructions to candidates:

- 1. Answer all questions from Part A. Part A questions should be answered in first three pages of the answer book only.
- 2. Answer FIVE full questions from Part B. In Part B question number 2 is compulsory. Answer any one full question from 3 and 4, 5 and 6, 7 and 8, 9 and 10.
- 3. Use of Handbook of Mathematics is permitted

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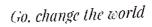
M BT CO

1 1 1	TIL TO			
1.1	The Trace and determinant of matrix whose eigen values are 7,1,9,			
	respectively and	02	1	1
1.2	The coefficient of x^3 in Maclaurin series of $\sin(2x)$ is	02	2	2
1.3	The curvature of the function $f(x) = x^2 + 2x + 1$ at $x = 0$ is	02	1	2
1.4	[1 2 3]			
	The rank of the matrix $\begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 3 & 7 \end{bmatrix}$ is			
		02	1	1
1.5	If $f(x, y) = x \sin y$, then value of f_{xy} at (0,1) is	02	2	2
1.6	For the implicit function, $x^3 + y^3 - 3xy + y^2 = 0$, find $\frac{dy}{dx}$ using			
	partial differentiation.	02	2	2
1.7	Evaluate the integral $\int_0^1 \int_0^2 \int_0^3 dx dy dz$.	02	1	1
1.8	Sketch the domain of integral $\int_0^1 \int_{x^2}^x f(x,y) dy dx$.		1	1
		02	3	3
1.9	If $r = 0.8$, $b_{xy} = 0.32$, then the value of b_{yx} is	02	1	1
1.10	If $\mu_2 = 8$, $\mu_3 = 50$ and $\mu_4 = 199$, then $\beta_1 =$ and $\beta_2 =$.	02	1	1

PART-B

2	a ·	Examine the consistency and solve the system of equations			
		x - y + z = 4			
		2x + y - 3z = 0			
		x + y + z = 0	05	2	2
	b	Solve following system of equations by Gauss Seidel method			
		10x + y + z = 9			
		x - 10y + 3z = 8			
		2x + y - 10z = 3			
		By taking initial approximation $X(0) = \begin{bmatrix} 0 & 0 & 0 \end{bmatrix}^T$. Perform			
		4 iterations.	05	2	2
	С	Find the dominant eigen value and the corresponding eigen vector			
		of the matrix. $A = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \end{bmatrix}$ by power method by taking the			
		of the matrix. $A = \begin{bmatrix} -2 & 3 & -1 \\ 2 & 3 & 1 \end{bmatrix}$ by power method by taking the			
		initial eigen vector as $\begin{bmatrix} 1 & -1 & 3 \end{bmatrix}$. Perform four iterations.	06	3	3
		initial eigen vector as [1 1 1]. Ferform four iterations.	100	-	3
		Show that the pair of curves intersect each other orthogonally.			
3	а	Show that the pair of curves intersect each other orthogonally. $r^2 \sin(2\theta) = a^2$, $r^2 \cos(2\theta) = b^2$	08	2	2
		Show that the radius of curvature of the curve $r^n = a^n \cos n\theta$		4	4
	b	Show that the radius of curvature of the curve $r = u \cos n\theta$	08	3	2
		varies inversely as r^{n-1} .	00		4
		J. C.			

4	а	Find the circle of curvature at the point $(3/2, 3/2)$ of the curve			
	•	$ x^3 + y^3 = 3xy$.	00	3	2
	b	Expand $\tan^{-1} x$ in powers of $(x-1)$ upto the term containing			
		fourth degree.	08	2	2
5	a	If $v = e^{a\theta} cos(a \log r)$ prove that			
	-	$\frac{\partial^2 v}{\partial x^2} = \frac{\partial^2 v}{\partial$			
	h	$\frac{\partial^2 v}{\partial r^2} + \frac{1}{r} \frac{\partial v}{\partial r} + \frac{1}{r^2} \frac{\partial^2 v}{\partial \theta^2} = 0$	08	2	1
	b	The temperature 'T' at any point (x, y, z) in space is $T = 400 \text{ xyz}^2$.			
		Find the highest temperature at the surface of the unit sphere. $x^2 + y^2 + z^2 = 1$.			
		OR CONTRACTOR	08	4	4
6					
0	а	If $Z = f(x, y)$ where $x = r \cos \theta$, $y = r \sin \theta$. Show that $\left(\frac{\partial z}{\partial x}\right)^2 + \left(\frac{\partial z}{\partial y}\right)^2 = \left(\frac{\partial z}{\partial r}\right)^2 + \frac{1}{r^2} \left(\frac{\partial z}{\partial \theta}\right)^2$.			
		$\left(\frac{\partial z}{\partial x}\right)^{2} + \left(\frac{\partial z}{\partial y}\right)^{2} = \left(\frac{\partial z}{\partial r}\right)^{2} + \frac{1}{r^{2}} \left(\frac{\partial z}{\partial \theta}\right)^{2}.$	00		
	b	If $x = r \sin \theta \cos \phi$, $y = r \sin \theta \sin \phi$, $z = r \cos \theta$. Show that	08	2	1
		$\frac{\partial(x,y,z)}{\partial(r,\theta,\phi)} = r^2 \sin\theta.$			
			08	4	4
7	а	Evaluate $\int_0^1 \int_0^{\sqrt{1-x^2}} \int_0^{\sqrt{1-x^2-y^2}} \frac{dz dy dx}{\sqrt{1-x^2-y^2-z^2}}$.			
	b	Y = J 2	08	2	2
		Change the order of integration and evaluate $\int_0^\infty \int_x^\infty \frac{e^{-y}}{y} dy dx$.	08	3	3
		OR			
8	а	Evaluate $\iint xy \ dx \ dy$ over the region bounded by x-axis, ordinate			
	1.	$x^{2} = 2a$ and the curve $x^{2} = 4av$	08	2	2
	b	Find the area enclosed by the cardiod $r = a(1 + \cos\theta)$ between		2	
		$\theta = 0$ and $\theta = \pi$, using double integration.	80	3	3
9	а	If F is the force required to lift a load W , by means of a pulley, fit a			
		linear expression $F = a + bW$ against the following data			
		W 50 70 100 120 140 180			
		Also find the force at the load $W = 130$.	`		
	b	Various doses of medical substances were given to groups of 25	08	2	2
		mice and the following results were observed.			
		Dose mg (x) 4 6 8 10 12 14 16			
		No. of recoveries (y) 1 3 6 8 14 16 20		1	
		i) Find the equation of regression line of y on x which fits			
		the data best.			
		ii) Estimate the number of recoveries in a group of 25 mice			
-		who received the doses of $7 mg$.	08	2	3
		OR			2
10	а	Calculate the first four central moments of the following			
		distribution.			
		Wages 1.5 - 2.5 2.5 - 3.5 3.5 - 4.5 4.5 - 5.5 5.5 - 6.5 f 1 3 7 3 1	00		
	b	Fit a curve of the form $y = ab^x$ for the data and hence find the	80	2	2
		estimation for 'y' when $x = 8$.			
		x 1 2 3 4 5 6 7			
		y 87 97 113 129 202 195 193	80	2	3





Department of Mathematics Academic Year 2024-2025 (Odd Semester 2024)

			2:00 PM to	A DM
Date	02/01/2025	Time		
Test	Improvement CIE (Quiz & Test)	Maximum Marks	10+50=	
Course Title	Fundamentals of linear Algebra, Calculu	is and Statistics	Course Code	MA211TC
Semester	I	Programs	B.E. (AIML, BT, CD,	CS, CY, IS)

PART - A

	FARI - A			
S.No.	Questions	M	BT	CO
1	Let $x = r \cos \theta$ and $y = r \sin \theta$. Then Jacobian of x, y with respect to r, θ is	2	1	1
2	Given the data points $(1, 2)$, $(3, 5)$ and $(7, 11)$. The slope of the line $y = mx$ that fits the data is	2	1	1
3	The following data regarding the heights (y) and the weights (x) of twelve college students are given $\sigma_x = 16.8$, $\sigma_y = 10.8$, $\sum (x - \bar{x})(y - \bar{y}) = 2020$. For the given data the regression coefficient of x on y is	2	2	2
4	Given $f(x,y) = x^3 + y^3 - 63(x+y) + 12xy$, $f_{xx} = 6x$, $f_{yy} = 6y$ and $f_{xy} = 12$. Which of the critical points $(-7, -7)$ and $(-1, 5)$ are saddle points?	2	1	1
5	In a partially destroyed laboratory record of an analysis of a correlation data, the following results were noted: variance of $x = 9$, equations of lines of regression of y on x is $4x - 5y + 33 = 0$ and x on y is $20x - 9y = 107$. For the given data the value of correlation coefficient is and the standard deviation of y is	2	2	2

PART - B

SI.No.	Questions	M	BT	СО
la	Calculate $\frac{\partial(x,y,z)}{\partial(u,v,w)}$ if $u = \frac{2yz}{x}$, $v = \frac{3zx}{y}$ and $w = \frac{4xy}{z}$.	5	2	2
16	Using the concept of Jacobians, determine whether the following functions are functionally dependent or not. If functionally dependent, find the functional relation between them. $u = x_1 + x_2 - x_3, v = x_1 - x_2 + x_3, w = x_1^2 + x_2^2 + x_3^2 - 2x_2x_3$	5	2	2
2	 For the given function, f(x, y) = x² + y² - 4x - 4y. Determine the following: i) The extreme values of f(x, y). ii) The extreme values of f(x, y) on the circle x² + y² = 9. iii) The extreme values of f(x, y) on the open disk x² + y² < 9. 	10	2	3
3a	A rectangular box without a lid is to be made from $12m^2$ of cardboard. Find the maximum volume of such a box using Lagrange's multiplier method.	6	3	4
3b	Use the method of least squares to fit the data points, $(1, 1.8)$, $(2, 5.1)$, $(3, 8.9)$ and $(4, 14.1)$ to a straight line of the form $y = mx + c$.	4	1	1
5	The following pair of observations was noted in an experimental work on cosmic rays. Find by the method of least squares the best values of a and b for the equation $y = ax^b$ which fits the following data. Also extrapolate the value of y when $x = 7$. x <td>10</td> <td>3</td> <td>3</td>	10	3	3
3	Marks obtained by 6 students in mathematics papers are given below: Paper I 60 65 68 70 75 85 Paper II 62 64 65 70 74 88 i) Determine the equations of lines of regressions and hence the coefficient of correlation for the given data. ii) Obtain the angle between the lines of regression.	10	2	2

				DIOOIII3 I	anonomy,	CO-Cours	e Outcome	es, M-Mark	S			
	Particulars		COI	CO2	CO3	CO4	L1	L2	L3	I.4	L5	L6
Marks Distribution	Test	Max Marks	4	20	20	6	4	30	16	-	-	-
	Quiz	Max Marks	6	4	T.	<u>:</u>	6	4			-	