

Tools used: [SageMath](#)

```
def test_encryption(self):
    plaintext = input('Plaintext: ').strip()

    m = int(plaintext, 16)
    cs = []

    while m:
        c = pow(m, self.e, self.n)
        cs.append(c)
        m //= self.n

    if len(cs) > 1:
        return 'Too many messages!'

    return 'Thanks for the message!'
```

Summary:

```
m < n => Thanks for the message!
m >= n => Too many messages!
```

The binary search can take few mins:

```
from pwn import *

p = remote("134.122.105.9", 31644)
reply = p.recvuntil(b'Option: ')

def getOne():
    p.sendline(b"1")
    reply = p.recvuntil(b'Option: ')
    print(reply)
    guess()

def guess():
    lower, upper = 10**616, 10**618
    actualKnown = 1
    while (upper - lower != 1):
        knownNumbers = 618 - len(str(upper - lower))
        if (knownNumbers > actualKnown):
            actualKnown = knownNumbers
            print(str(upper)[:knownNumbers - 2] + (618 - knownNumbers) * "-")

        p.sendline(b"2")
        reply = p.recvuntil(b'Plaintext: ')
        p.sendline(bytes(hex((lower + upper) // 2), "utf-8"))
        reply = p.recvuntil(b'Option: ')
        if ("Too many messages" in str(reply)):
            upper = (lower + upper) // 2
        elif ("Thanks for the message!" in str(reply)):
            lower = (lower + upper) // 2

    print("Done ! n=", upper)
```

```
getOne()
```

[https://gchq.github.io/CyberChef/#recipe=From_Base\(16\)&input=MHg4Y2U3YTcyN2M0YTcwNDcwYWZlZDZiODcyZjgyZWYyNmM4ZmY1Yzc4MjBkNTc5MGFhNTNIOWRiZDFkOWYzMjhjODg0N2lyNjg4MTNjOWMxYmNhNTRjM2E4OTJjOWE4NDhlOTVmMzdiYjNjNDY3OTcxYWYzYTl5YTJlYTcwNmRkZTY2MmNhYTU5NTcyOGZmMDk0YjZjM2M2NmJkZGRjNjczM2Y0MjhjNWl4MGVmODFjMGRiZmE3ZjQ0MTlmMDhjYzZjZDZGUzMGRmMjAwNGZmODAzN2JhZjM2NDdjZjE4MTNjNTc3Y2ExMzAzZmI5MmYzMTk0MThlM2VhNGYzNmRjNDlkMzNlN2Q5MjQ3MWE1M2FIMmMwMjIjZGZhMmI5MMDM0YTzYjhmM2I0NjhmOTE1NGE2NzU1YWZmMTNkOTIzYmQ3ZTZkNDlkMmU4ZGZlYjM0YjYxMzU2NzVkMWExMTIzNmU3Yzg2NDE3MTZjNTRmZTkxZGM5NjY3NzlwMDIzMmJhYWU4YTlkNTI5MzEwOWQ3MzMzMmYyMzlkOWE4OTA1YzdhMWI4MWFhYzU3ZDNkZjU1ZjMzMDJjMGNkZGJjZDc0MmVhMzAyYzExNTdmYTdiMTEzOGZlNmFjZDgyY2Q3MzE0Mml0ZmJmMjYwOTkxNTM2MTZjZDBkMjQ0ZGVhMmUxYw](https://gchq.github.io/CyberChef/#recipe=From_Base(16)&input=MHg4Y2U3YTcyN2M0YTcwNDcwYWZlZDZiODcyZjgyZWYyNmM4ZmY1Yzc4MjBkNTc5MGFhNTNIOWRiZDFkOWYzMjhjODg0N2lyNjg4MTNjOWMxYmNhNTRjM2E4OTJjOWE4NDhlOTVmMzdiYjNjNDY3OTcxYWYzYTl5YTJlYTcwNmRkZTY2MmNhYTU5NTcyOGZmMDk0YjZjM2M2NmJkZGRjNjczM2Y0MjhjNWl4MGVmODFjMGRiZmE3ZjQ0MTlmMDhjYzZjZDZGUzMGRmMjAwNGZmODAzN2JhZjM2NDdjZjE4MTNjNTc3Y2ExMzAzZmI5MmYzMTk0MThlM2VhNGYzNmRjNDlkMzNlN2Q5MjQ3MWE1M2FIMmMwMjIjZGZhMmI5MMDM0YTzYjhmM2I0NjhmOTE1NGE2NzU1YWZmMTNkOTIzYmQ3ZTZkNDlkMmU4ZGZlYjM0YjYxMzU2NzVkMWExMTIzNmU3Yzg2NDE3MTZjNTRmZTkxZGM5NjY3NzlwMDIzMmJhYWU4YTlkNTI5MzEwOWQ3MzMzMmYyMzlkOWE4OTA1YzdhMWI4MWFhYzU3ZDNkZjU1ZjMzMDJjMGNkZGJjZDc0MmVhMzAyYzExNTdmYTdiMTEzOGZlNmFjZDgyY2Q3MzE0Mml0ZmJmMjYwOTkxNTM2MTZjZDBkMjQ0ZGVhMmUxYw)

Coppersmith's small public RSA exponent attack with partially known message

Since we know all the beginning of the message we can use this attack.

Then we implement this attack from <https://latticehacks.cr.yp.to/rsa.html>

```
class univariate_coppersmith:
    def __init__(self, f, N, X):
        self.f = f
        self.N = N
        self.X = X
        self.R = QQ['x']

    def gen_lattice(self, t=1, k=1):
        d = self.f.degree()
        dim = k*d+t
        A = matrix(IntegerRing(), dim, dim)
        x = self.R.0
        X = self.X

        monomial_list = [x^i for i in range(dim)]
        for i in range(k):
            for j in range(d):
                g = self.f(X*x)^i*(X*x)^j*self.N^(k-i)
                A[d*i+j] = [g.monomial_coefficient(mon) for mon in monomial_list]
        for j in range(t):
            g = self.f(X*x)^k*(X*x)^j
            A[k*d+j] = [g.monomial_coefficient(mon) for mon in monomial_list]

        weights = [X^i for i in range(dim)]
        def getf(M, i):
            return sum(self.R(b/w)*mon for b, mon, w in zip(M[i], monomial_list, weights))
        return A, getf

    def solve(self, t=1, k=1):
        A, getf = self.gen_lattice(t, k)
        B = A.LLL()
        roots = []
        for r, multiplicity in getf(B, 0).roots():
            if mod(self.f(r), self.N) == 0:
                roots.append(r)
        return roots

    def gen_random_coppersmith(a, rlen=150, d=3):
```

```

N = 217...

c = 177...

x = ZZ['x'].0
f = (x+a)^d-c
X = 2^rlen
return (f,N,X)

def test_coppersmith():
    for length in range(50):
        a = int(("Hey! This is my secret... it is secure because RSA is extremely strong and very
hard to break... Here you go: HTB{"+"0"*length)).encode("utf-8").hex(),16)
        (f,N,X) = gen_random_coppersmith(a)
        u = univariate_coppersmith(f,N,X)
        solutions=u.solve()
        if(len(solutions)>0):
            print(bytes.fromhex(hex(a+solutions[0])[2:]))

test_coppersmith()

```

We get the flag:

```

Hey! This is my secret... it is secure because RSA is extremely strong and very hard to break...
Here you go: HTB{*4*_L*_r*4*_S*?*!}

```