MovieLens Reccomender System Project

HarvardX PH125.9x Data Science: Capstone

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1 Introduction

The goal of this project is to use the MovieLens dataset to create a recommender system.

The version of the Movielens dataset that we will use in this final project contains about 10 milion movie evaluations, divided into 9 milion for training (edx) and 1 milion for validation (validation). The training dataset contains 70,000 users and 10,500 different movies, divided into 20 genres such as Drama, Comedy, Action, and Romance.

We first perform data exploration to understand an overview of the model building process. The training data set is further divided into two parts and the resulting test set is used to evaluate the recommendation system. We select a model with a small Root Mean Squared Error (RMSE) and evaluate it using the validation test set, which is below the target of **0.8649**.

$$RMSE = \sqrt{\frac{1}{N} \sum_{u,i} (\hat{y}_{u,i} - y_{u,i})}$$

As a FINAL model, the Matrix Factorization - recosystem reached a RMSE of 0.7825.

```
# Define Root Mean Squared Error (RMSE)
RMSE <- function(true_ratings, predicted_ratings){
   sqrt(mean((true_ratings - predicted_ratings)^2))
}</pre>
```

2 Data Preprocessing and Explanatory Data Analysis

2.1 Initial Data Preprocessing

The version of the movielens dataset we use contains about 10 milion movie evaluations, divided into 9 milion for training (edx) and 1 milion for validation (validation).

edx dataset contains 9,000,000 rows with 70,000 Users, 10,500 Movies and 797 Genres conbination. There is no missing values.

```
# Data Exploaration
head(edx) %>% kable()
```

userId	${\rm movie Id}$	rating	timestamp	title	genres
1	122	5	838985046	Boomerang (1992)	Comedy Romance
1	185	5	838983525	Net, The (1995)	Action Crime Thriller
1	292	5	838983421	Outbreak (1995)	Action Drama Sci-Fi Thriller
1	316	5	838983392	Stargate (1994)	Action Adventure Sci-Fi
1	329	5	838983392	Star Trek: Generations (1994)	Action Adventure Drama Sci-Fi
1	355	5	838984474	Flintstones, The (1994)	${\bf Children} {\bf Comedy} {\bf Fantasy}$

```
str(edx)
```

```
## Classes 'data.table' and 'data.frame': 9000055 obs. of 6 variables:
## $ userId : int 1 1 1 1 1 1 1 1 1 1 ...
## $ movieId : num 122 185 292 316 329 355 356 362 364 370 ...
```

[1] 0

summary(edx) %>% kable()

userId	movieId	rating	timestamp	title	genres
 Min. : 1	Min. : 1	Min. :0.500	Min. :7.897e+08	Length:9000055	Length:9000055
1st	1st Qu.: 648	1st	1st	Class:character	Class :character
Qu.:18124		Qu.:3.000	Qu.:9.468e+08		
Median	Median:	Median	Median	Mode :character	Mode :character
:35738	1834	:4.000	:1.035e+09		
Mean $:35870$	Mean: 4122	Mean $:3.512$	Mean $:1.033e+09$	NA	NA
3rd	3rd Qu.:	3rd	3rd	NA	NA
Qu.:53607	3626	Qu.:4.000	Qu.:1.127e+09		
Max. :71567	Max. :65133	Max. :5.000	Max. :1.231e+09	NA	NA

n_users	n_movies	n_genres
69878	10677	797

The data is difficult to process because of the timestamp, which is difficult for humans to understand, and the concatenation of the title and the year of airing. We perform data formatting. The training set is further divided into 9:1 and a test set is prepared for use in the modeling process.

```
# Convert timestamp to a human readable date
edx$date <- as.POSIXct(edx$timestamp, origin="1970-01-01")
validation$date <- as.POSIXct(validation$timestamp, origin="1970-01-01")

# Extract the year of Rate in both data sets
edx$year_Rate <- as.integer(format(edx$date,"%Y"))
validation$year_Rate <- as.integer(format(validation$date,"%Y"))</pre>
```

```
# Extract the year of release for each movie in both data set
# edx dataset
edx <- edx %>%
 mutate(title = str_trim(title)) %>%
  extract(title,
          c("titleTemp", "release"),
          regex = "^(.*) \\(([0-9 \\-]*)\\)$",
          remove = F) %>%
 mutate(release = if_else(str_length(release) > 4,
                            as.integer(str_split(release, "-",
                                                 simplify = T)[1]),
                            as.integer(release))
 ) %>%
  mutate(title = if_else(is.na(titleTemp),
                         title,
                         titleTemp)
  ) %>%
  select(-titleTemp)
# validation data set
validation <- validation %>%
  mutate(title = str trim(title)) %>%
  extract(title,
          c("titleTemp", "release"),
          regex = "^(.*) \\(([0-9 \\-]*)\\)$",
          remove = F) %>%
  mutate(release = if_else(str_length(release) > 4,
                            as.integer(str_split(release, "-",
                                                  simplify = T)[1]),
                            as.integer(release))
  ) %>%
  mutate(title = if_else(is.na(titleTemp),
                         title,
                         titleTemp)
 ) %>%
 select(-titleTemp)
# Preparation test and train data set for model selection
set.seed(1, sample.kind="Rounding")
test_index <- createDataPartition(y = edx$rating, times = 1, p = 0.1, list = FALSE)</pre>
train_set <- edx[-test_index,]</pre>
temp <- edx[test_index,]</pre>
# Make sure userId and movieId in test set are also in train set
test_set <- temp %>%
 semi_join(train_set, by = "movieId") %>%
  semi_join(train_set, by = "userId")
# Add rows removed from test set back into train set
removed <- anti_join(temp, test_set)</pre>
train_set <- rbind(train_set, removed)</pre>
```

2.2 Explanatory Data Analysis (EDA)

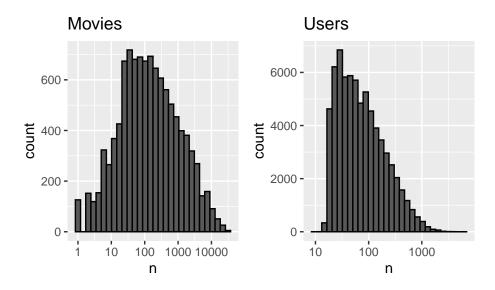
2.2.1 Whole count distribution

According to the histograms, we can see that the distributions are not uniform respectively.

```
# Whole count distribution
p_c1 <- edx %>%
    dplyr::count(movieId) %>%
    ggplot(aes(n)) +
    geom_histogram(bins = 30, color = "black") +
    scale_x_log10() +
    ggtitle("Movies")

p_c2 <- edx %>%
    dplyr::count(userId) %>%
    ggplot(aes(n)) +
    geom_histogram(bins = 30, color = "black") +
    scale_x_log10() +
    ggtitle("Users")

# compare count distribution by movie and user
p_c1 + p_c2
```



2.2.2 Whole rating distribution

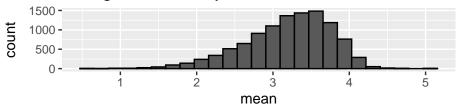
The graph below shows the distribution of the average Rating by Movie and by User. The rating distribution by year shows that before 2002, the rating was based on integer values only, while after 2003, the rating method of half stars was added. The year of Rate is considered in the model construction.

```
# Whole rating distribution
p_d1 <- edx %>% group_by(movieId) %>%
    summarise(mean = mean(rating)) %>%
    ggplot(aes(mean)) + geom_histogram(bins = 25,col="black") +
    ggtitle("Rating distribution by Movie")

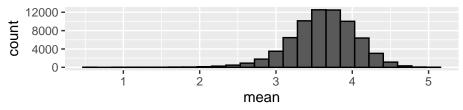
p_d2 <- edx %>% group_by(userId) %>%
    summarise(mean = mean(rating)) %>%
    ggplot(aes(mean)) + geom_histogram(bins = 25,col="black") +
    ggtitle("Rating distribution by User")

# compare rating distribution by movie and user
p_d1 / p_d2
```

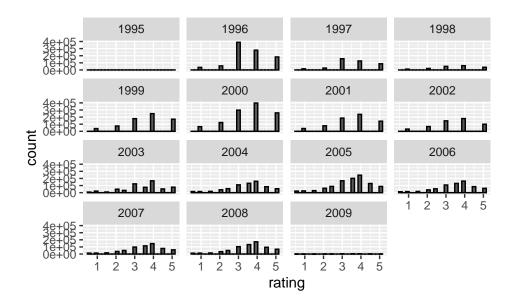
Rating distribution by Movie



Rating distribution by User



```
# rating distribution by year of Rating
edx %>% ggplot(aes(rating)) +
  geom_histogram(bins = 25,col="black") +
  facet_wrap(~year_Rate)
```



2.2.3 Genres

There are 797 genres, but they are composed of multiple combinations. Each of them is sorted into rows to check the overall number and relationship.

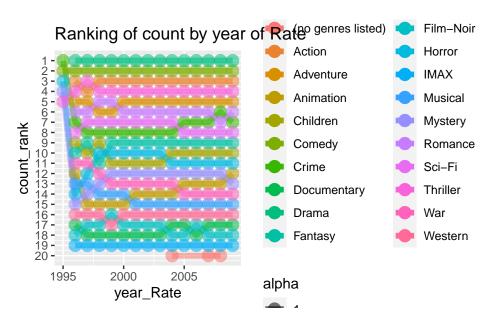
We used a ranking system to check whether the year of evaluation would affect the confirmed genres. The 20 genres were found to show generally the same ranking trends throughout the period of the data set.

```
# Genres
edx %>% group_by(genres) %>%
  summarise(n=n()) %>%
 head()
## # A tibble: 6 x 2
##
     genres
                                                             n
     <chr>>
##
                                                          <int>
## 1 (no genres listed)
                                                              7
## 2 Action
                                                         24482
## 3 Action|Adventure
                                                          68688
## 4 Action|Adventure|Animation|Children|Comedy
                                                          7467
## 5 Action|Adventure|Animation|Children|Comedy|Fantasy
                                                            187
## 6 Action|Adventure|Animation|Children|Comedy|IMAX
                                                            66
# Separate genres and rating distribution by genres
edx %>%
  separate_rows(genres, sep = "\\|") %>%
  select(genres, rating) %>%
  group_by(genres) %>%
  summarize(count = n(), mean = mean(rating)) %>% kable()
```

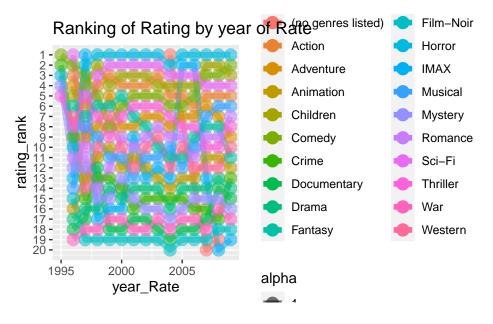
genres	count	mean
(no genres listed)	7	3.642857

genres	count	mean
Action	2560545	3.421405
Adventure	1908892	3.493544
Animation	467168	3.600644
Children	737994	3.418715
Comedy	3540930	3.436908
Crime	1327715	3.665925
Documentary	93066	3.783487
Drama	3910127	3.673131
Fantasy	925637	3.501946
Film-Noir	118541	4.011625
Horror	691485	3.269815
IMAX	8181	3.767693
Musical	433080	3.563305
Mystery	568332	3.677001
Romance	1712100	3.553813
Sci-Fi	1341183	3.395743
Thriller	2325899	3.507676
War	511147	3.780813
Western	189394	3.555918

```
# Identify trends in the time period being evaluated focusing ranking.
genresByYear <- edx %>%
  separate_rows(genres, sep = "\\|") %>%
  select(movieId, year_Rate, genres, rating) %>%
  group_by(year_Rate, genres) %>%
 filter(!is.na(rating)) %>%
  summarise(count = n(),
           rating_avg = mean(rating)) %>%
 mutate(count_rank = row_number(desc(count)),
        rating_rank = row_number(rating_avg))
# Create the graph count ranking
p_genre1 <- genresByYear %>% #filter(year_Rate>=1993) %>%
  ggplot(aes(x = year_Rate, y= count_rank, group=genres))+
  geom_line(aes(color = genres, alpha = 1), size = 2) +
 geom_point(aes(color = genres, alpha = 1), size = 4) +
  scale_y_reverse(breaks = 1:nrow(genresByYear)) +
  guides(color=guide_legend(ncol=2)) +
  ggtitle("Ranking of count by year of Rate")
p_genre1
```



```
# Create the graph rating ranking
p_genre2 <- genresByYear %>% #filter(year_Rate>=1993) %>%
ggplot(aes(x = year_Rate, y= rating_rank, group=genres))+
geom_line(aes(color = genres, alpha = 1), size = 2) +
geom_point(aes(color = genres, alpha = 1), size = 4) +
scale_y_reverse(breaks = 1:nrow(genresByYear)) +
guides(color=guide_legend(ncol=2)) +
ggtitle("Ranking of Rating by year of Rate")
p_genre2
```



```
# Extract the genres name
genre_name <- unique(genresByYear$genres)</pre>
```

3 Methods and Analysis

3.1 Regression Models and Regularized Models

In order to build a linear model, we start from a simple mean model and add each variable identified in the previous chapter to build the models.

3.1.1 Mean model

$$Y_{u,i} = \mu + \epsilon_{u,i}$$

We start by building the simplest possible recommendation system, mean model. A model that assumes the same rating $(\hat{\mu})$ for all movies and users with all the differences explained by random variation $(\epsilon_{u,i})$. $\hat{\mu}$ can be calculated as the average whole rating value.

3.1.2 Movie effects

$$Y_{u,i} = \mu + b_i + \epsilon_{u,i}$$

We can extend the previous model by adding terms, b_i . It represents the movie effect of movie_i. As an approximation (\hat{b}_i) can be calculated as the average value by **movieId** after subtracting the average value from each Rating.

3.1.3 User effects

$$Y_{u,i} = \mu + b_i + b_u + \epsilon_{u,i}$$

As we saw in the previous chapter, there are differences in Rating for each user. We can extend the model by incorporating differences between users. Since it is difficult to calculate with lm() function due to the environment of computing resources, we compute an approximation by computing $\hat{\mu}$ and \hat{b}_i and estimating \hat{b}_u as the average of $y_{u,i} - \hat{\mu} - \hat{b}_i$.

3.1.4 year of Rate effects

$$Y_{u,i} = \mu + b_i + b_u + f(year_{u,i}) + \epsilon_{u,i}$$

We extend the model with the yearly impact of Rating. We use $f(year_{u,i})$ to more accurately represent the year-to-year impact. However, there is a major change in the evaluation methodology as identified in the previous chapter. To simplify the model, we express the impact in years as b_y , and as in previous models, we compute an approximation by computing $\hat{\mu}$, \hat{b}_i and \hat{b}_u and estimating \hat{b}_y as the average of $y_{u,i} - \hat{\mu} - \hat{b}_i - \hat{b}_u$.

This implies that a further improvement to our model may be:

$$Y_{u,i} = \mu + b_i + b_u + b_y + \epsilon_{u,i}$$

3.1.5 Genre Effect

$$Y_{u,i} = \mu + b_i + b_u + b_y + \sum_{k=1}^{K} x_{u,i}^k \beta_k + \epsilon_{u,i}, \quad with \ x_{u,i}^k = 1 \quad if \ g_{u,i} \ is \ genre \ k$$

We extend the model with the Genre effect. We use $\sum_{k=1}^{K} x_{u,i}^k \beta_k$ to more accurately represent the each genre impact. As we saw in the previous chapters, there are 20 genres. On the other hand, the number of genre combinations is approximately 800, which is sufficiently small compared to the number of 10500 movies and

9 million total data. As in the previous model, in order to simplify the model, we represent the effect of genre by b_g and perform the calculation as the combination of genres. We compute an approximation by computing $\hat{\mu}$, \hat{b}_i , \hat{b}_u and \hat{b}_y and estimating \hat{b}_g as the average of $y_{u,i} - \hat{\mu} - \hat{b}_i - \hat{b}_u - \hat{b}_y$.

This implies that a further improvement to our model may be:

$$Y_{u,i} = \mu + b_i + b_u + b_u + b_a$$

Note: $\sum_{k=1}^{K} x_{u,i}^k \beta_k$ incorporated into the modeling in the Gradient Boosting section below.

3.1.6 Regularized Models

In order to avoid over training, we consider minimizing the model equation by adding a penalty (λ) to the models we have created. We consider minimization for Movie+User effect model and 4 effect model.

This implies that a further improvement to our model may be:

$$\sum_{u,i} (y_{u,i} - \mu - b_i - b_u)^2 + \lambda \left(\sum_i b_i^2 + \sum_u b_u^2 \right)$$
$$\sum_{u,i} (y_{u,i} - \mu - b_i - b_u - b_y - b_g)^2 + \lambda \left(\sum_i b_i^2 + \sum_u b_u^2 + \sum_{u,i} b_y^2 + \sum_{u,i} b_g^2 \right)$$

3.2 Matrix-factorization

The main function of the recommender system is to predict the unknown values of the evaluation matrix based on the observed values. We consider m users and n items. The users will be represented by an n-dimensional vector, which we aim to transform by dimensionality reduction to k dimensions where m > k > 0. This can be approximated as follows by considering a $k \ddot{O} m$ matrix P and a $k \ddot{O} n$ matrix Q representing the user elements for an $m\ddot{O} n$ matrix R representing the evaluation values.

$$R \approx P^T Q$$

As a method to perform matrix factorization using R, we use A Matrix-factorization Library for Recommender Systems, LIBMF, developed and published by W.-S. Chin et al. The evaluation value of item v evaluated by user u can be expressed as p_u, q_v . Matrix Factorization is to learn p_u and q_v for each user and each item from the known evaluation values. P and Q that satisfy the following equation are derived from the training data by using the library.

$$min_{P,Q} \sum_{(u,v) \in R} ((r_{u,v} - \boldsymbol{p}_u^T \boldsymbol{q}_i)^2 + \lambda_P ||\boldsymbol{p}_u||^2 + \lambda_Q ||\boldsymbol{p}_v||^2$$

where ||.|| is the Euclidean norm, $(u, v) \in R$ indicates that rating $r_{u,v}$ is available, λ_P and λ_Q are regularization coefficients for avoiding over-fitting.

3.3 Gradient Boosting

We consider the simplification of $\sum_{k=1}^{K} x_{u,i}^k \beta_k$ when building the regression models. In order to examine the impact of each genre, the matrix is extended to include whether or not the corresponding movie has 20 genres. Since it has a huge dimension with 20 additional columns, we model it using XGBoost, one of the Gradient Boosting commonly used in machine learning of table data. In addition to building a recommendation model for this Project, we also build a model excluding user and/or movie data for new users and/or movies.

Gradient boosting is a machine learning method for tasks such as regression and classification that generates a predictive model in the form of an ensemble of weak prediction models (usually decision trees).

4 Results

4.1 Model Selection

We builded each model using the Train and Test datasets created by splitting the edx dataset. We selected the model that achieves the target RMSE, and finally validated it using the Validation set.

```
# Creating the Target
result <- data.frame(Method = "Target", RMSE = 0.8649)</pre>
```

4.1.1 Regression Models and Regularized Models

4.1.1.1 Mean model The mean value alone showed a large RMSE.

Method	RMSE
Target	0.864900
Mean	1.060054

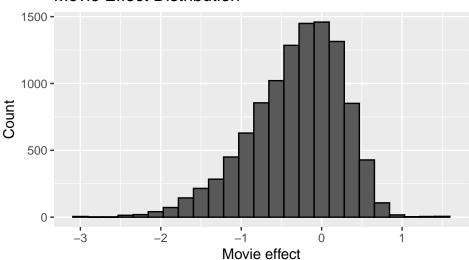
4.1.1.2 Movie effects Improvements were seen by adding movie effects.

```
# Add Movie Effect(bi) -----
# Movie effects (bi)
bi <- train_set %>%
  group_by(movieId) %>%
  summarize(b_i = mean(rating - mu))
head(bi) %>% kable()
```

movieId	b_i
1	0.4150040
2	-0.3064057
3	-0.3613952
4	-0.6372808
5	-0.4416058
6	0.3018943

```
# Confirm the Movie effects distribution
bi %>% ggplot(aes(x = b_i)) +
  geom_histogram(bins=25, col = I("black")) +
  ggtitle("Movie Effect Distribution") +
  xlab("Movie effect") +
  ylab("Count")
```

Movie Effect Distribution



Method	RMSE
Target	0.8649000
Mean	1.0600537
Mean + bi	0.9429615

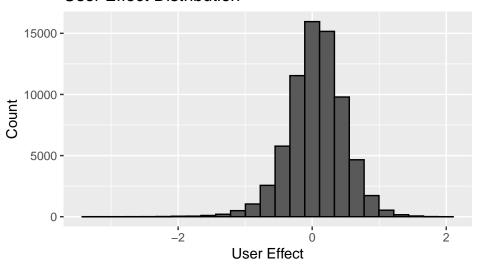
4.1.1.3 User effects Further improvement was seen by adding user-specific effects.

```
# Add User Effect(bu) -----
# User effect (bu)
bu <- train_set %>%
  left_join(bi, by = "movieId") %>%
```

```
group_by(userId) %>%
summarize(b_u = mean(rating - mu - b_i))

# Confirm the User effects distribution
bu %>% # filter(n()>=100) %>%
ggplot(aes(b_u)) +
geom_histogram(bins=25,color = "black") +
ggtitle("User Effect Distribution") +
xlab("User Effect") +
ylab("Count")
```

User Effect Distribution



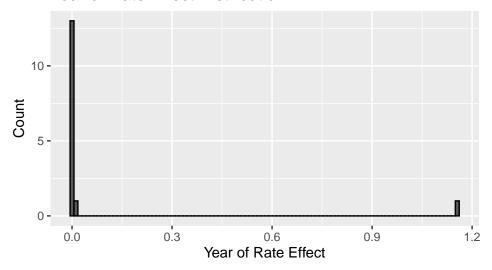
Method	RMSE
Target	0.8649000
Mean	1.0600537
Mean + bi	0.9429615
Mean + bi + bu	0.8646843

4.1.1.4 year of Rate effects The addition of the RATE year showed little improvement.

```
# Add year of Rate Effect(by) -----
# year of Rate effect (by)
by <- train_set %>%
  left_join(bi, by = "movieId")%>%
  left_join(bu, by="userId") %>%
  group_by(year_Rate) %>%
  summarize(b_y = mean(rating - mu - b_i - b_u))

# Confirm the year of Rate effects distribution
by %>%
  ggplot(aes(b_y)) +
  geom_histogram(bins=100,color = "black") +
  ggtitle("Year of Rate Effect Distribution") +
  xlab("Year of Rate Effect") +
  ylab("Count")
```

Year of Rate Effect Distribution



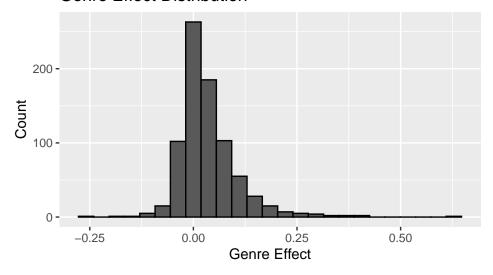
Method	RMSE
Target	0.8649000
Mean	1.0600537
Mean + bi	0.9429615
Mean + bi + bu	0.8646843
Mean + bi + bu + by	0.8646811

4.1.1.5 Genre Effect Even a simple addition of a genre showed some improvement.

```
# Add Genre Effect(bg) ------
# Genre Rate effect (bg)
bg <- train_set %>%
  left_join(bi, by = "movieId")%>%
  left_join(bu, by="userId") %>%
  left_join(by, by="year_Rate") %>%
  group_by(genres) %>%
  summarize(b_g = mean(rating - mu - b_i- b_u - b_y))

# Confirm the Genre effects distribution
bg %>%
  ggplot(aes(b_g)) +
  geom_histogram(bins=25,color = "black") +
  ggtitle("Genre Effect Distribution") +
  xlab("Genre Effect") +
  ylab("Count")
```

Genre Effect Distribution

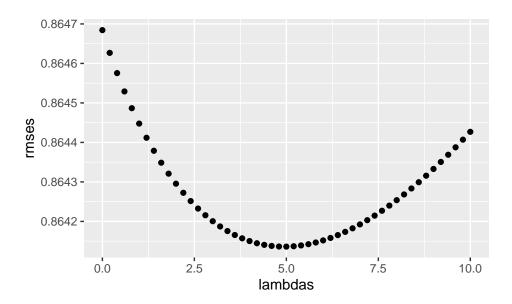


```
# Prediction
y_hat_bi_bu_by_bg <- test_set %>%
left_join(bi, by="movieId") %>%
left_join(bu, by="userId") %>%
left_join(by, by="year_Rate") %>%
left_join(bg, by="genres") %>%
```

Method	RMSE
Target	0.8649000
Mean	1.0600537
Mean + bi	0.9429615
Mean + bi + bu	0.8646843
Mean + bi + bu + by	0.8646811
Mean + bi + bu + by + bg	0.8643201

4.1.1.6 Regularized Models By regularizing each model, further improvement over the original model was observed. The obtained lambda value ($\lambda = 5$) was used for validation.

```
# Regularization----
# Movie + User (Same methods the course)
lambdas \leftarrow seq(0, 10, 0.2)
rmses <- sapply(lambdas, function(l){</pre>
  mu <- mean(train_set$rating)</pre>
  bi <- train_set %>%
    group_by(movieId) %>%
    summarize(b_i = sum(rating - mu)/(n()+1))
  bu <- train_set %>%
    left_join(bi, by = "movieId") %>%
    group_by(userId) %>%
    summarize(b_u = sum(rating - mu - b_i)/(n()+1))
  predicted_ratings <-</pre>
    test_set %>%
    left_join(bi, by = "movieId") %>%
    left_join(bu, by = "userId") %>%
    mutate(pred = mu + b_i + b_u) %>%
    pull(pred)
 return(RMSE(predicted_ratings, test_set$rating))
})
# Check the lambdas
qplot(lambdas,rmses)
```



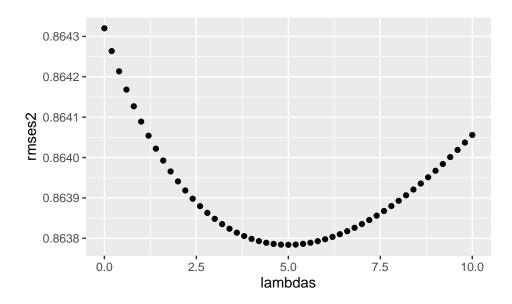
```
lambda <- lambdas[which.min(rmses)]
lambda</pre>
```

[1] 5

Method	RMSE
Target	0.8649000
Mean	1.0600537
Mean + bi	0.9429615
Mean + bi + bu	0.8646843
Mean + bi + bu + by	0.8646811
Mean + bi + bu + by + bg	0.8643201
Regularized Movie + User Effect	0.8641362

```
# Movie + User + Year of Rate + Genre (new one, regularization with 4 biases)
lambdas <- seq(0, 10, 0.2)
rmses2 <- sapply(lambdas, function(1){
  mu <- mean(train_set$rating)
  bi <- train_set %>%
    group_by(movieId) %>%
    summarize(b_i = sum(rating - mu)/(n()+1))
  bu <- train_set %>%
    left_join(bi, by = "movieId") %>%
    group_by(userId) %>%
```

```
summarize(b_u = sum(rating - mu - b_i)/(n()+1))
  by <- train_set %>%
   left_join(bi, by = "movieId")%>%
   left_join(bu, by="userId") %>%
   group_by(year_Rate) %>%
    summarize(b_y = sum(rating - mu - b_i - b_u)/(n()+1))
  bg <- train_set %>%
   left_join(bi, by = "movieId")%>%
   left_join(bu, by="userId") %>%
   left_join(by, by="year_Rate") %>%
   group_by(genres) %>%
   summarize(b_g = sum(rating - mu - b_i - b_u - b_y)/(n()+1))
  predicted_ratings <-</pre>
   test_set %>%
   left_join(bi, by = "movieId") %>%
   left_join(bu, by = "userId") %>%
   left_join(by, by="year_Rate") %>%
   left_join(bg, by="genres") %>%
   mutate(pred = mu + b_i + b_u + b_y + b_g) \%
   pull(pred)
 return(RMSE(predicted_ratings, test_set$rating))
})
# Check the lambdas
qplot(lambdas,rmses2)
```



```
lambda <- lambdas[which.min(rmses2)]
lambda</pre>
```

[1] 5

```
# Calculate the RMSE and update result
result <- bind_rows(result,</pre>
```

Method	RMSE
Target	0.8649000
Mean	1.0600537
Mean + bi	0.9429615
Mean + bi + bu	0.8646843
Mean + bi + bu + by	0.8646811
Mean + bi + bu + by + bg	0.8643201
Regularized Movie + User Effect	0.8641362
Regularized Movie + User + Year of Rate + Genre Effect	0.8637838

4.1.2 Matrix-factorization

Significant improvement was observed by using the recosystem library.

```
# Matrix Factorization----
set.seed(1, sample.kind = "Rounding")
# Convert "train" and "test" sets to recosystem input format
train_reco <- with(train_set, data_memory(user_index = userId,</pre>
                                            item_index = movieId,
                                            rating = rating))
test_reco <- with(test_set, data_memory(user_index = userId,</pre>
                                           item_index = movieId,
                                           rating = rating))
# Create the model object
reco <- recosystem::Reco()</pre>
# Tune the parameters
opts <- reco$tune(train_reco, opts = list(dim = c(10, 20, 30),
                                            lrate = c(0.1, 0.2),
                                            costp_12 = c(0.01, 0.1),
                                            costq_12 = c(0.01, 0.1),
                                            nthread = nc, niter = 10))
# Train the model
reco$train(train_reco, opts = c(opts$min, nthread = nc, niter = 20))
```

```
## iter
            tr_rmse
                            obj
##
     0
             0.9828
                    1.1036e+07
##
     1
             0.8761 8.9945e+06
             0.8432 8.3549e+06
##
     2
##
     3
             0.8203 7.9576e+06
##
     4
             0.8035 7.6873e+06
             0.7910 7.4922e+06
##
     5
```

```
##
      6
              0.7806
                       7.3497e+06
##
      7
              0.7720
                       7.2297e+06
##
     8
              0.7648
                      7.1367e+06
     9
              0.7585
                       7.0564e+06
##
##
     10
              0.7532
                       6.9938e+06
##
              0.7482
                      6.9367e+06
     11
##
     12
              0.7440
                      6.8875e+06
              0.7402
                      6.8453e+06
##
     13
##
     14
              0.7366
                       6.8087e+06
##
     15
              0.7331
                       6.7741e+06
##
     16
              0.7302
                       6.7444e+06
##
     17
              0.7274
                       6.7189e+06
                       6.6934e+06
##
     18
              0.7247
              0.7223
                       6.6715e+06
##
     19
```

Method	RMSE
Target	0.8649000
Mean	1.0600537
Mean + bi	0.9429615
Mean + bi + bu	0.8646843
Mean + bi + bu + by	0.8646811
Mean + bi + bu + by + bg	0.8643201
Regularized Movie + User Effect	0.8641362
Regularized Movie + User + Year of Rate + Genre Effect	0.8637838
Matrix Factorization - recosystem	0.7860689

4.2 Validation

Through the analysis using the training set, the Matrix factorization model that showed the best results was selected as the final model and evaluated using the Validation set. As a FINAL model, **the Matrix Factorization - recosystem** reached a RMSE of **0.7825**.

```
item_index = movieId,
                                          rating = rating))
# Create the model object
reco_final <- recosystem::Reco()</pre>
# Tune the parameters
opts_final <- reco_final$tune(edx_reco, opts = list(dim = c(10, 20, 30),
                                           lrate = c(0.1, 0.2),
                                           costp_12 = c(0.01, 0.1),
                                           costq_12 = c(0.01, 0.1),
                                           nthread = nc, niter = 10))
# Train the model
reco_final$train(edx_reco, opts = c(opts_final$min, nthread = nc, niter = 20))
## iter
             tr_rmse
                              obj
##
                       1.2016e+07
      0
              0.9730
##
      1
              0.8718
                       9.8723e+06
##
      2
              0.8382
                      9.1711e+06
##
      3
              0.8164
                      8.7462e+06
##
                       8.4686e+06
      4
              0.8011
##
      5
              0.7896
                       8.2776e+06
##
      6
                       8.1203e+06
              0.7797
##
     7
              0.7713
                     8.0002e+06
##
              0.7642
                      7.9010e+06
     8
     9
                       7.8212e+06
##
              0.7581
     10
              0.7529
                      7.7515e+06
##
##
     11
              0.7482
                     7.6922e+06
##
     12
              0.7441
                       7.6425e+06
##
     13
              0.7405
                       7.6007e+06
##
     14
              0.7371
                      7.5618e+06
##
     15
              0.7340
                      7.5279e+06
##
     16
              0.7312
                      7.4978e+06
##
                      7.4682e+06
     17
              0.7285
##
     18
              0.7261
                       7.4447e+06
##
              0.7239
                      7.4230e+06
     19
# Calculate the prediction
y_hat_final_reco <- reco_final$predict(valid_reco, out_memory())</pre>
# Update the result table
result <- bind_rows(result,</pre>
                    data.frame(Method = "[FINAL model] Matrix Factorization - recosystem",
                               RMSE = RMSE(validation$rating, y_hat_final_reco)))
# Show the RMSE improvement
result %>% kable()
```

Method	RMSE
Target	0.8649000

Method	RMSE
Mean	1.0600537
Mean + bi	0.9429615
Mean + bi + bu	0.8646843
Mean + bi + bu + by	0.8646811
Mean + bi + bu + by + bg	0.8643201
Regularized Movie + User Effect	0.8641362
Regularized Movie + User + Year of Rate + Genre Effect	0.8637838
Matrix Factorization - recosystem	0.7860689
[FINAL model] Matrix Factorization - recosystem	0.7824372

As a reference, the obtained lambda was used to validate the Regularized 4 Effects model. We also achieved our target of 0.8649.

```
# Reference: What is the RMSE of regularized 4 effects
# With edx and validation data sets
# Movie + User + Year of Rate + Genre (new one, regularization with 4 biases)
lambda <- 5
# Attention: Validation data set cannot be used for select the model
rmse_v <- sapply(lambda, function(1){</pre>
 mu <- mean(edx$rating)</pre>
  bi <- edx %>%
   group_by(movieId) %>%
   summarize(b_i = sum(rating - mu)/(n()+1))
  bu <- edx %>%
   left_join(bi, by = "movieId") %>%
   group_by(userId) %>%
    summarize(b_u = sum(rating - mu - b_i)/(n()+1))
  by <- edx %>%
   left_join(bi, by = "movieId")%>%
   left_join(bu, by="userId") %>%
   group_by(year_Rate) %>%
   summarize(b_y = sum(rating - mu - b_i - b_u)/(n()+1))
  bg <- edx %>%
   left_join(bi, by = "movieId")%>%
   left_join(bu, by="userId") %>%
   left_join(by, by="year_Rate") %>%
   group_by(genres) %>%
   summarize(b_g = sum(rating - mu - b_i - b_u - b_y)/(n()+1))
  predicted_ratings <-</pre>
   validation %>%
   left_join(bi, by = "movieId") %>%
   left_join(bu, by = "userId") %>%
   left_join(by, by="year_Rate") %>%
   left_join(bg, by="genres") %>%
   mutate(pred = mu + b_i + b_u + b_y + b_g) \%
   pull(pred)
  return(RMSE(predicted_ratings, validation$rating))
})
# Update result
```

Method	RMSE
Target	0.8649000
Mean	1.0600537
Mean + bi	0.9429615
Mean + bi + bu	0.8646843
Mean + bi + bu + by	0.8646811
Mean + bi + bu + by + bg	0.8643201
Regularized Movie + User Effect	0.8641362
Regularized Movie + User + Year of Rate + Genre Effect	0.8637838
Matrix Factorization - recosystem	0.7860689
[FINAL model] Matrix Factorization - recosystem	0.7824372
Reference Regularized 4 Effects with Lambda=5	0.8644116

4.3 Additional: Gradient Boosting

We performed the analysis using XGBoost, but due to the performance of the PC (amount of memory), we could not perform the desired analysis with the edx data set. Therefore, a smaller dataset, Movielens100K, was used for the analysis.

The same model construction as for the edx set was used for each analysis. Due to the small amount of data, not much improvement was observed in the recosystem, but good results were obtained in XGBoost. Also, although we did not get good scores for new users, we did get some scores for new movies.

```
# For Discussion
data("movielens")
# Preparation test and train data set
set.seed(1, sample.kind="Rounding")
test_index <- createDataPartition(y = movielens$rating, times = 1, p = 0.1, list = FALSE)
train_small <- movielens[-test_index,]</pre>
temp <- movielens[test_index,]</pre>
# Make sure userId and movieId in test set are also in train set
test_small <- temp %>%
  semi_join(train_small, by = "movieId") %>%
  semi_join(train_small, by = "userId")
# Add rows removed from test set back into train set
removed <- anti_join(temp, test_small)</pre>
train_small <- rbind(train_small, removed)</pre>
rm(test_index, temp, removed)
# To compare, targeted same value: 0.8649
```

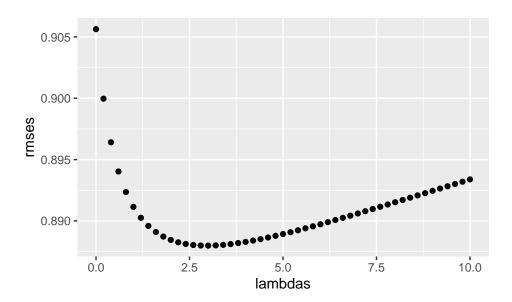
Method	RMSE
Target	0.864900
Mean	1.054766

Method	RMSE
Target	0.8649000
Mean	1.0547663
Mean + bi	0.9860457

```
# Add User Effect(bu) -----
# User effect (bu)
bu <- train_small %>%
  left_join(bi, by = 'movieId') %>%
  group_by(userId) %>%
  summarize(b_u = mean(rating - mu - b_i))
# Prediction
```

Method	RMSE
Target	0.8649000
Mean	1.0547663
Mean + bi	0.9860457
Mean + bi + bu	0.9056371

```
# Regularization----
lambdas \leftarrow seq(0, 10, 0.2)
rmses <- sapply(lambdas, function(l){</pre>
  mu <- mean(train_small$rating)</pre>
  b_i <- train_small %>%
    group_by(movieId) %>%
    summarize(b_i = sum(rating - mu)/(n()+1))
  b_u <- train_small %>%
    left_join(b_i, by="movieId") %>%
    group_by(userId) %>%
    summarize(b_u = sum(rating - b_i - mu)/(n()+1))
  predicted_ratings <-</pre>
    test_small %>%
    left_join(b_i, by = "movieId") %>%
    left_join(b_u, by = "userId") %>%
    mutate(pred = mu + b_i + b_u) %>%
    .$pred
  return(RMSE(predicted_ratings, test_small$rating))
qplot(lambdas,rmses)
```



```
lambda <- lambdas[which.min(rmses)]
lambda</pre>
```

[1] 3

Method	RMSE
Target	0.8649000
Mean	1.0547663
Mean + bi	0.9860457
Mean + bi + bu	0.9056371
Regularized Movie + User Effect	0.8879858

```
reco <- recosystem::Reco()</pre>
# Tune the parameters
opts <- reco\u00a9tune(train_reco, opts = list(\u00ddim = c(10, 20, 30),
                                            lrate = c(0.1, 0.2),
                                            costp_12 = c(0.01, 0.1),
                                            costq_12 = c(0.01, 0.1),
                                            nthread = nc, niter = 10)) # nc is depended on PC
# Train the model
reco$train(train_reco, opts = c(opts$min, nthread = nc, niter = 20))
## iter
             tr_rmse
                               obj
##
      0
                       2.2591e+05
              1.3033
##
      1
              0.9283
                       1.4616e+05
      2
                       1.3873e+05
##
              0.8957
##
      3
              0.8724
                       1.3391e+05
##
      4
              0.8477
                       1.2953e+05
##
      5
              0.8198
                      1.2513e+05
##
      6
              0.7900
                      1.2104e+05
##
      7
              0.7632
                      1.1743e+05
##
      8
              0.7388
                       1.1459e+05
##
     9
              0.7146
                      1.1172e+05
##
     10
              0.6952
                      1.0966e+05
              0.6770
                      1.0765e+05
##
     11
     12
              0.6604
                      1.0595e+05
##
##
     13
              0.6468
                      1.0475e+05
##
     14
              0.6333 1.0344e+05
##
     15
              0.6217
                       1.0230e+05
##
     16
              0.6123
                       1.0155e+05
##
              0.6041
                       1.0084e+05
     17
##
     18
              0.5957
                       1.0010e+05
              0.5873
                       9.9320e+04
##
     19
# Calculate the prediction
y_hat_final_reco <- reco$predict(test_reco, out_memory())</pre>
# Update the result small table
result_small <- bind_rows(result_small,</pre>
                           data.frame(Method = "Matrix Factorization - recosystem",
                                      RMSE = RMSE(test_small$rating, y_hat_final_reco)))
# Show the RMSE improvement
result_small
##
                                 Method
                                             RMSE
## 1
                                 Target 0.8649000
## 2
                                   Mean 1.0547663
## 3
                             Mean + bi 0.9860457
## 4
                        Mean + bi + bu 0.9056371
## 5
       Regularized Movie + User Effect 0.8879858
## 6 Matrix Factorization - recosystem 0.9307754
```

```
# Xqboost-----
# genres is same as edx data set
genre_name
## [1] "Comedy"
                              "Crime"
                                                   "Horror"
## [4] "Mystery"
                              "Thriller"
                                                   "Action"
## [7] "Adventure"
                              "Animation"
                                                   "Children"
## [10] "Documentary"
                              "Drama"
                                                    "Fantasy"
                              "IMAX"
## [13] "Film-Noir"
                                                   "Musical"
## [16] "Romance"
                             "Sci-Fi"
                                                   "War"
## [19] "Western"
                              "(no genres listed)"
# Copy the modify data sets
train_small2 <- train_small</pre>
test_small2 <- test_small</pre>
# To use Xgboost, modify genres such like one-hot encoding(but not same)
for (n in genre_name){
  train_small2 <- train_small2 %>%
    mutate(!!n := if_else(str_detect(genres,n),1,0))
}
for (n in genre_name){
  test_small2 <- test_small2 %>%
    mutate(!!n := if_else(str_detect(genres,n),1,0))
}
train_small2 %>% select(-c(title, genres)) %>%
  mutate_all(~ifelse(is.na(.), median(., na.rm = TRUE), .)) -> train_small2
test_small2 %>% select(-c(title, genres)) %>%
  mutate_all(~ifelse(is.na(.), median(., na.rm = TRUE), .)) -> test_small2
# Note: it took 45 minutes!!
# Xgboost Linear model
set.seed(1, sample.kind = "Rounding")
system.time(
  modelXgboostLinear <- train(</pre>
    rating ~ .,
    data = train_small2,
    method = "xgbLinear",
    preProcess = c('center', 'scale'),
    trControl = trainControl(method = "cv"),
    tuneLength = 4)
)
##
      user system elapsed
##
     41.87
              1.17 2667.94
print(modelXgboostLinear)
```

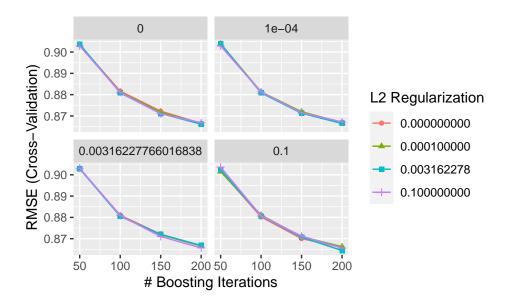
eXtreme Gradient Boosting

```
##
  90324 samples
      24 predictor
##
##
##
  Pre-processing: centered (24), scaled (24)
   Resampling: Cross-Validated (10 fold)
   Summary of sample sizes: 81292, 81291, 81291, 81291, 81292, 81292, ...
   Resampling results across tuning parameters:
##
##
     lambda
                   alpha
                                 nrounds
                                           RMSE
                                                       Rsquared
                                                                  MAE
##
     0.00000000
                   0.00000000
                                  50
                                           0.9033259
                                                       0.2773919
                                                                  0.7030091
##
     0.00000000
                   0.00000000
                                 100
                                           0.8816748
                                                       0.3083933
                                                                  0.6821762
##
     0.00000000
                   0.00000000
                                 150
                                           0.8722778
                                                       0.3216070
                                                                  0.6725054
##
     0.00000000
                   0.00000000
                                 200
                                           0.8665554
                                                       0.3299025
                                                                  0.6668118
##
     0.00000000
                   0.000100000
                                  50
                                           0.9035868
                                                       0.2769350
                                                                  0.7032041
##
     0.00000000
                   0.000100000
                                 100
                                           0.8811419
                                                       0.3093070
                                                                  0.6817493
##
                                 150
     0.00000000
                   0.000100000
                                           0.8718377
                                                       0.3223293
                                                                  0.6721066
##
     0.00000000
                   0.000100000
                                 200
                                                       0.3291055
                                                                  0.6670052
                                           0.8670754
##
     0.00000000
                                  50
                                           0.9029278
                                                                  0.7025638
                   0.003162278
                                                       0.2780996
##
     0.00000000
                   0.003162278
                                 100
                                           0.8810435
                                                       0.3094610
                                                                  0.6816991
##
     0.00000000
                   0.003162278
                                 150
                                           0.8721130
                                                      0.3220075
                                                                  0.6726284
##
     0.00000000
                   0.003162278
                                 200
                                           0.8666518
                                                       0.3297934
                                                                  0.6667293
##
                   0.100000000
                                  50
                                                       0.2801151
     0.00000000
                                           0.9017776
                                                                  0.7014335
##
     0.00000000
                   0.100000000
                                 100
                                           0.8802022
                                                       0.3109638
                                                                  0.6810510
##
     0.00000000
                   0.100000000
                                 150
                                           0.8700321
                                                       0.3253341
                                                                  0.6708925
##
     0.00000000
                   0.100000000
                                 200
                                           0.8658326
                                                       0.3310694
                                                                  0.6662852
##
     0.000100000
                   0.00000000
                                  50
                                           0.9034021
                                                       0.2772511
                                                                  0.7030066
##
     0.000100000
                   0.00000000
                                 100
                                           0.8812461
                                                       0.3091676
                                                                  0.6818602
##
     0.000100000
                   0.00000000
                                 150
                                           0.8718582
                                                       0.3223190
                                                                  0.6723818
                                                                  0.6666269
##
                   0.00000000
                                 200
     0.000100000
                                           0.8663824
                                                       0.3301983
##
     0.000100000
                   0.000100000
                                  50
                                           0.9038936
                                                       0.2764973
                                                                  0.7033419
##
     0.000100000
                   0.000100000
                                 100
                                           0.8812972
                                                       0.3091649
                                                                  0.6818719
##
     0.000100000
                   0.000100000
                                 150
                                           0.8719905
                                                       0.3221804
                                                                  0.6724858
                                 200
##
                                                       0.3294634
     0.000100000
                   0.000100000
                                           0.8668708
                                                                  0.6668299
##
                                  50
                                                                  0.7025651
     0.000100000
                   0.003162278
                                           0.9029283
                                                       0.2780985
                                                      0.3098372
##
     0.000100000
                   0.003162278
                                 100
                                           0.8808295
                                                                  0.6815315
##
     0.000100000
                   0.003162278
                                 150
                                           0.8718726
                                                       0.3224277
                                                                  0.6726806
##
                                 200
     0.000100000
                   0.003162278
                                           0.8665699
                                                       0.3299198
                                                                  0.6667882
##
     0.000100000
                   0.100000000
                                  50
                                           0.9015018
                                                       0.2805396
                                                                  0.7011845
##
                   0.100000000
                                 100
     0.000100000
                                           0.8810965
                                                       0.3094385
                                                                  0.6815910
##
     0.000100000
                   0.100000000
                                 150
                                           0.8709849
                                                       0.3237860
                                                                  0.6716801
##
                                 200
     0.000100000
                   0.100000000
                                           0.8662541
                                                       0.3303684
                                                                  0.6665060
##
     0.003162278
                   0.00000000
                                  50
                                           0.9037230
                                                       0.2766631
                                                                  0.7032327
##
                                 100
     0.003162278
                   0.00000000
                                           0.8808332
                                                       0.3098966
                                                                  0.6817866
##
     0.003162278
                   0.00000000
                                 150
                                           0.8711504
                                                       0.3235381
                                                                  0.6719729
##
                                 200
     0.003162278
                   0.00000000
                                           0.8661562
                                                       0.3306033
                                                                  0.6665590
##
     0.003162278
                   0.000100000
                                  50
                                           0.9038861
                                                       0.2763494
                                                                  0.7032469
##
     0.003162278
                   0.000100000
                                 100
                                           0.8808483
                                                       0.3098413
                                                                  0.6818832
##
     0.003162278
                   0.000100000
                                 150
                                           0.8712561
                                                       0.3233605
                                                                  0.6721923
##
     0.003162278
                   0.000100000
                                 200
                                           0.8664764
                                                       0.3301022
                                                                  0.6668395
##
                                  50
     0.003162278
                   0.003162278
                                           0.9028207
                                                       0.2781904
                                                                  0.7028330
##
     0.003162278
                   0.003162278
                                 100
                                           0.8804793
                                                       0.3103928
                                                                  0.6813900
##
                                 150
                                           0.8719943
                                                       0.3220154
                                                                  0.6723424
     0.003162278
                   0.003162278
##
     0.003162278
                   0.003162278
                                 200
                                           0.8668322
                                                      0.3294580
                                                                  0.6672339
```

##

```
##
     0.003162278
                  0.100000000
                                 50
                                          0.9024158
                                                     0.2789113
                                                                 0.7017852
##
                  0.100000000
                                100
     0.003162278
                                          0.8806475
                                                     0.3103430
                                                                 0.6813528
##
     0.003162278
                  0.100000000
                                150
                                          0.8707192
                                                     0.3242720
                                                                 0.6714503
                                200
##
     0.003162278
                  0.100000000
                                          0.8644279
                                                     0.3333085
                                                                 0.6654507
##
     0.10000000
                  0.00000000
                                 50
                                          0.9028645
                                                     0.2781094
                                                                 0.7023696
                  0.00000000
                                100
##
     0.100000000
                                          0.8810723
                                                     0.3095378
                                                                 0.6813761
                   0.00000000
                                                                 0.6718570
##
     0.100000000
                                150
                                          0.8710416
                                                     0.3237279
                                200
##
     0.100000000
                  0.00000000
                                          0.8668150
                                                     0.3295844
                                                                 0.6673573
##
     0.100000000
                   0.000100000
                                 50
                                          0.9028619
                                                      0.2781144
                                                                 0.7023675
##
     0.100000000
                  0.000100000
                                100
                                          0.8812441
                                                      0.3092454
                                                                 0.6816132
##
     0.100000000
                  0.000100000
                                150
                                          0.8715205
                                                     0.3229700
                                                                 0.6722319
##
                  0.000100000
                                200
                                          0.8671735
                                                     0.3290032
                                                                 0.6678042
     0.100000000
##
     0.100000000
                  0.003162278
                                 50
                                          0.9030585
                                                     0.2778794
                                                                 0.7024823
                                          0.8808579
##
     0.100000000
                  0.003162278
                                100
                                                     0.3099648
                                                                 0.6815566
                                                                 0.6714864
##
     0.100000000
                  0.003162278
                                150
                                          0.8710348
                                                     0.3238341
##
     0.10000000
                   0.003162278
                                200
                                          0.8656673
                                                      0.3313997
                                                                 0.6660079
##
                                 50
     0.100000000
                  0.100000000
                                          0.9036062
                                                     0.2768013
                                                                 0.7033907
##
     0.100000000
                  0.100000000
                                100
                                          0.8807416
                                                      0.3099968
                                                                 0.6815187
##
     0.100000000
                  0.100000000
                                150
                                                     0.3234925
                                          0.8711901
                                                                 0.6716861
##
     0.100000000
                  0.100000000
                                200
                                          0.8655786
                                                     0.3315022
                                                                 0.6657733
##
## Tuning parameter 'eta' was held constant at a value of 0.3
## RMSE was used to select the optimal model using the smallest value.
   The final values used for the model were nrounds = 200, lambda =
    0.003162278, alpha = 0.1 and eta = 0.3.
```

ggplot(modelXgboostLinear)



```
# Note: it took 30 minutes!!
# Xgboost Tree model
set.seed(1, sample.kind = "Rounding")
system.time(
  modelXgboostTree <- train(
    rating ~ .,</pre>
```

```
data = train_small2,
    method = "xgbTree",
    preProcess = c('center', 'scale'),
    trControl = trainControl(method = "cv"),
    tuneLength = 4)
)
##
      user
            system elapsed
##
              0.69 1717.75
     34.71
print(modelXgboostTree)
## eXtreme Gradient Boosting
## 90324 samples
##
      24 predictor
##
## Pre-processing: centered (24), scaled (24)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 81292, 81291, 81291, 81291, 81292, 81292, ...
## Resampling results across tuning parameters:
##
##
     eta max_depth colsample_bytree
                                         subsample
                                                    nrounds
                                                              RMSE
                                                                         Rsquared
##
     0.3 1
                      0.6
                                         0.5000000
                                                     50
                                                              1.0226586
                                                                         0.07301263
##
     0.3 1
                      0.6
                                         0.5000000
                                                    100
                                                              1.0139590
                                                                         0.08842350
##
     0.3 1
                      0.6
                                         0.5000000
                                                    150
                                                              1.0079665
                                                                         0.09889056
##
     0.3
         1
                      0.6
                                         0.5000000
                                                    200
                                                              1.0035463
                                                                         0.10595198
##
     0.3
         1
                      0.6
                                                     50
                                                              1.0231373
                                                                         0.07251672
                                         0.6666667
##
     0.3
         1
                      0.6
                                         0.6666667
                                                     100
                                                              1.0144425
                                                                          0.08815203
##
     0.3
                      0.6
                                                    150
                                                                         0.09847579
                                         0.6666667
                                                              1.0086808
         1
##
     0.3
                                                    200
          1
                      0.6
                                         0.6666667
                                                              1.0043692
                                                                         0.10529285
##
     0.3
                      0.6
                                                     50
                                                              1.0233018
                                                                         0.07239859
         1
                                         0.8333333
##
     0.3
                      0.6
                                         0.8333333
                                                    100
         1
                                                              1.0148741
                                                                         0.08736482
##
     0.3 1
                      0.6
                                         0.8333333
                                                    150
                                                              1.0091881
                                                                         0.09797547
##
     0.3 1
                      0.6
                                         0.8333333
                                                    200
                                                              1.0051008
                                                                         0.10434956
                                                              1.0235645
##
     0.3 1
                      0.6
                                                     50
                                                                         0.07195906
                                         1.0000000
##
     0.3 1
                      0.6
                                         1.0000000
                                                    100
                                                              1.0154284
                                                                         0.08684681
     0.3 1
##
                      0.6
                                         1.0000000
                                                    150
                                                              1.0100389
                                                                         0.09670124
##
     0.3 1
                      0.6
                                         1.0000000
                                                    200
                                                              1.0060408
                                                                         0.10350381
##
     0.3 1
                      0.8
                                         0.5000000
                                                     50
                                                              1.0227364
                                                                         0.07248407
##
     0.3 1
                      0.8
                                         0.5000000
                                                    100
                                                              1.0136712
                                                                         0.08902322
##
     0.3
         1
                      0.8
                                         0.5000000
                                                    150
                                                              1.0075308
                                                                         0.09973745
##
     0.3 1
                      0.8
                                                    200
                                         0.5000000
                                                              1.0031699
                                                                         0.10684651
##
     0.3
         1
                      0.8
                                         0.666667
                                                     50
                                                              1.0229547
                                                                          0.07279690
##
     0.3
         1
                      0.8
                                         0.6666667
                                                    100
                                                              1.0142443
                                                                         0.08844710
##
     0.3
                      0.8
                                         0.6666667
                                                    150
                                                              1.0083209
                                                                         0.09909485
          1
##
     0.3
                      0.8
                                                    200
         1
                                         0.6666667
                                                              1.0041183
                                                                         0.10585721
                                                     50
##
     0.3
                      0.8
                                         0.8333333
                                                                         0.07242248
         1
                                                              1.0231819
     0.3 1
                                                    100
##
                      0.8
                                         0.8333333
                                                              1.0147366
                                                                         0.08778523
##
     0.3 1
                      0.8
                                                    150
                                                              1.0091582
                                         0.8333333
                                                                         0.09779421
##
     0.3 1
                      0.8
                                                    200
                                                              1.0049514
                                                                         0.10478427
                                         0.8333333
##
     0.3 1
                      0.8
                                         1.0000000
                                                     50
                                                              1.0235224
                                                                         0.07214455
##
     0.3
                      0.8
                                         1.0000000
                                                    100
                                                              1.0154089
                                                                         0.08721944
```

1

##	0.3	1	0.8	1.0000000	150	1.0099037	0.09701929
##	0.3	1	0.8	1.0000000	200	1.0060069	0.10356107
##	0.3	2	0.6	0.5000000	50	0.9913098	0.13049824
##	0.3	2	0.6	0.5000000	100	0.9721928	0.16199941
##	0.3	2	0.6	0.5000000	150	0.9593136	0.18362174
##	0.3	2	0.6	0.5000000	200	0.9489554	0.20105492
##	0.3	2	0.6	0.6666667	50	0.9918613	0.12947764
##	0.3	2	0.6	0.6666667	100	0.9728922	0.16097853
##	0.3	2	0.6	0.6666667	150	0.9595068	0.18380980
##	0.3	2	0.6	0.6666667	200	0.9497022	0.19994126
##	0.3	2	0.6	0.8333333	50	0.9916226	0.13059517
##	0.3	2	0.6	0.8333333	100	0.9718795	0.16372098
##	0.3	2	0.6	0.8333333	150	0.9582546	0.18647535
##	0.3	2	0.6	0.8333333	200	0.9485624	0.20239685
##	0.3	2	0.6	1.0000000	50	0.9912467	0.13211399
##	0.3	2	0.6	1.0000000	100	0.9720915	0.16396284
##	0.3	2	0.6	1.0000000	150	0.9585410	0.18677985
	0.3	2	0.6	1.0000000	200		0.20364174
##		2				0.9482124	
##	0.3		0.8	0.5000000	50	0.9908643	0.13140139
##	0.3	2	0.8	0.5000000	100	0.9715190	0.16340815
##	0.3	2	0.8	0.5000000	150	0.9583088	0.18537171
##	0.3	2	0.8	0.5000000	200	0.9484260	0.20168339
##	0.3	2	0.8	0.6666667	50	0.9899833	0.13311195
##	0.3	2	0.8	0.6666667	100	0.9709379	0.16468827
##	0.3	2	0.8	0.6666667	150	0.9581689	0.18612636
##	0.3	2	0.8	0.6666667	200	0.9479141	0.20317884
##	0.3	2	0.8	0.8333333	50	0.9910132	0.13121180
##	0.3	2	0.8	0.8333333	100	0.9713712	0.16444170
##	0.3	2	0.8	0.8333333	150	0.9582220	0.18643236
##	0.3	2	0.8	0.8333333	200	0.9480158	0.20318484
##	0.3	2	0.8	1.0000000	50	0.9903050	0.13344275
##	0.3	2	0.8	1.0000000	100	0.9711208	0.16554438
##	0.3	2	0.8	1.0000000	150	0.9573179	0.18885716
##	0.3	2	0.8	1.0000000	200	0.9472731	0.20545718
##	0.3	3	0.6	0.5000000	50	0.9663615	0.17416709
##	0.3	3	0.6	0.5000000	100	0.9432569	0.21194254
##	0.3	3	0.6	0.5000000	150	0.9284151	0.23566845
##	0.3	3	0.6	0.5000000	200	0.9188407	0.25049630
##	0.3	3	0.6	0.6666667	50	0.9670342	0.17412210
##	0.3	3	0.6	0.6666667	100	0.9428536	0.21325247
##	0.3	3	0.6	0.6666667	150	0.9276743	0.23759264
##	0.3	3	0.6	0.6666667	200	0.9176376	0.25310712
##	0.3	3	0.6	0.8333333	50	0.9676080	0.17304467
##	0.3	3	0.6	0.8333333	100	0.9425071	0.21393836
##	0.3	3	0.6	0.8333333	150	0.9274053	0.23810143
##	0.3	3	0.6	0.8333333	200	0.9176075	0.25332029
##	0.3	3	0.6	1.0000000	50	0.9664128	0.17531185
##	0.3	3	0.6	1.0000000	100	0.9415729	0.21645826
##	0.3	3	0.6	1.0000000	150	0.9260892	0.24100800
##	0.3	3	0.6	1.0000000	200	0.9159702	0.25674400
##	0.3	3	0.8	0.5000000	50	0.9651945	0.17598704
##	0.3	3	0.8	0.5000000	100	0.9406283	0.21643763
##	0.3	3	0.8	0.5000000	150	0.9257588	0.24012330
##	0.3	3	0.8	0.5000000	200	0.9157725	0.25561365

		_				0.0010510	
##	0.3	3	0.8	0.6666667	50	0.9648512	0.17787305
##	0.3	3	0.8	0.6666667	100	0.9400060	0.21779421
##	0.3	3	0.8	0.6666667	150	0.9255038	0.24080938
##	0.3	3	0.8	0.666667	200	0.9156093	0.25625647
##	0.3	3	0.8	0.8333333	50	0.9650391	0.17745935
##	0.3	3	0.8	0.8333333	100	0.9396638	0.21892017
##	0.3	3	0.8	0.8333333	150	0.9240639	0.24394312
##	0.3	3	0.8	0.8333333	200	0.9141749	0.25924324
##	0.3	3	0.8	1.0000000	50	0.9651812	0.17760262
##	0.3	3	0.8	1.0000000	100	0.9400907	0.21881042
##	0.3	3	0.8	1.0000000	150	0.9246857	0.24310654
##	0.3	3	0.8	1.0000000	200	0.9139225	0.26007741
##	0.3	4	0.6	0.5000000	50	0.9460461	0.20855817
##	0.3	4	0.6	0.5000000	100		
						0.9209968	0.24763946
##	0.3	4	0.6	0.5000000	150	0.9075960	0.26786933
##	0.3	4	0.6	0.5000000	200	0.8975508	0.28324098
##	0.3	4	0.6	0.6666667	50	0.9442277	0.21244097
##	0.3	4	0.6	0.6666667	100	0.9192758	0.25107722
##	0.3	4	0.6	0.6666667	150	0.9044217	0.27378541
##	0.3	4	0.6	0.6666667	200	0.8947473	0.28835905
##	0.3	4	0.6	0.8333333	50	0.9445529	0.21216773
##	0.3	4	0.6	0.8333333	100	0.9182173	0.25353547
##	0.3	4	0.6	0.8333333	150	0.9030972	0.27668103
##	0.3	4	0.6	0.8333333	200	0.8934993	0.29097217
##	0.3	4	0.6	1.0000000	50	0.9451715	0.21135954
##	0.3	4	0.6	1.0000000	100	0.9173691	0.25558565
##	0.3	4	0.6	1.0000000	150	0.9028785	0.27755107
##	0.3	4	0.6	1.0000000	200	0.8927868	0.29265808
##	0.3	4	0.8	0.5000000	50	0.9439029	0.21157761
##	0.3	4	0.8	0.5000000	100	0.9186932	0.25105801
##	0.3	4	0.8	0.5000000	150	0.9051516	0.27155098
##	0.3	4	0.8	0.5000000	200	0.8956893	0.28590485
	0.3	4		0.6666667			0.21677989
##			0.8		50	0.9414719	
##	0.3	4	0.8	0.6666667	100	0.9155339	0.25726304
##	0.3	4	0.8	0.6666667	150	0.9011375	0.27921352
##	0.3	4	0.8	0.6666667	200	0.8916175	0.29323088
##	0.3	4	0.8	0.8333333	50	0.9420563	0.21589567
##	0.3	4	0.8	0.8333333	100	0.9155500	0.25745161
##	0.3	4	0.8	0.8333333	150	0.9008521	0.27984193
##	0.3	4	0.8	0.8333333	200	0.8913117	0.29414604
##	0.3	4	0.8	1.0000000	50	0.9426137	0.21575900
##	0.3	4	0.8	1.0000000	100	0.9148319	0.25945077
##	0.3	4	0.8	1.0000000	150	0.9007632	0.28050207
##	0.3	4	0.8	1.0000000	200	0.8910541	0.29503040
##	0.4	1	0.6	0.5000000	50	1.0189689	0.07882919
##	0.4	1	0.6	0.5000000	100	1.0089763	0.09700781
##	0.4	1	0.6	0.5000000	150	1.0029902	0.10683366
##	0.4	1	0.6	0.5000000	200	0.9989367	0.11306656
##	0.4	1	0.6	0.6666667	50	1.0193276	0.07827531
##	0.4	1	0.6	0.6666667	100	1.0098156	0.09601805
##	0.4	1	0.6	0.6666667	150	1.0037565	0.10597329
##	0.4	1	0.6	0.6666667	200	0.9995994	0.11239676
##	0.4	1	0.6	0.8333333	50	1.0195218	0.11239070
##	0.4	1	0.6	0.8333333	100	1.0104173	0.09518175

##	0.4	1	0.6	0.8333333	150	1.0045551	0.10488608
##	0.4	1	0.6	0.8333333	200	1.0005353	0.11135912
##	0.4	1	0.6	1.0000000	50	1.0197306	0.07796894
##	0.4	1	0.6	1.000000	100	1.0109129	0.09489080
##	0.4	1	0.6	1.0000000	150	1.0053328	0.10426218
##	0.4	1	0.6	1.0000000	200	1.0013430	0.11057779
##	0.4	1	0.8	0.5000000	50	1.0185344	0.07953627
##	0.4	1	0.8	0.5000000	100	1.0086960	0.09782798
##	0.4	1	0.8	0.5000000	150	1.0024671	0.10816057
##	0.4	1	0.8	0.5000000	200	0.9984382	0.11395498
##	0.4	1	0.8	0.6666667	50	1.0189571	0.07891660
##	0.4	1	0.8	0.6666667	100	1.0095001	0.09659283
##	0.4	1	0.8	0.6666667	150	1.0035771	0.10640017
##	0.4	1	0.8	0.6666667	200	0.9996006	0.11254525
##	0.4	1	0.8	0.8333333	50	1.0194859	0.07840170
##	0.4	1	0.8	0.8333333	100	1.0100813	0.09601060
##	0.4	1	0.8	0.8333333	150	1.0041828	0.10613759
##	0.4	1	0.8	0.8333333	200	1.0003141	0.11172359
##	0.4	1	0.8	1.0000000	50	1.0196963	0.07834468
##	0.4	1	0.8	1.0000000	100	1.0108806	0.09481781
##	0.4	1	0.8	1.0000000	150	1.0051775	0.10488646
##	0.4	1	0.8	1.0000000	200	1.0013996	0.11058599
##	0.4	2	0.6	0.5000000	50	0.9843692	0.13999545
##	0.4	2	0.6	0.5000000	100	0.9634702	0.17537362
##	0.4	2	0.6	0.500000	150	0.9506807	0.19676895
##	0.4	2	0.6	0.5000000	200	0.9415710	0.21155595
##	0.4	2	0.6	0.6666667	50	0.9844019	0.14073691
##	0.4	2	0.6	0.666667	100	0.9640274	0.17461690
##	0.4	2	0.6	0.6666667	150	0.9499603	0.19849180
##	0.4	2	0.6	0.6666667	200	0.9405238	0.21372931
##	0.4	2	0.6	0.8333333	50	0.9845405	0.14083097
##	0.4	2	0.6	0.8333333	100	0.9625604	0.17803080
##	0.4	2	0.6	0.8333333	150	0.9487538	0.20067059
##	0.4	2	0.6	0.8333333	200	0.9389626	0.21688310
##	0.4	2	0.6	1.0000000	50	0.9854163	0.13937484
##	0.4	2	0.6	1.0000000	100	0.9629799	0.17766168
##	0.4	2	0.6	1.0000000	150	0.9485134	0.20177288
##	0.4	2	0.6	1.0000000	200	0.9381386	0.21886944
##	0.4	2	0.8	0.5000000	50	0.9825286	0.14383005
##	0.4	2	0.8	0.5000000	100	0.9632099	0.17579214
##	0.4	2	0.8	0.5000000	150	0.9510462	0.19577604
##	0.4	2	0.8	0.5000000	200	0.9407088	0.21301451
##	0.4	2	0.8	0.6666667	50	0.9826008	0.14418568
##	0.4	2	0.8	0.6666667	100	0.9617236	0.17910095
##	0.4	2	0.8	0.6666667	150	0.9485898	0.20062933
##	0.4	2	0.8	0.6666667	200	0.9385085	0.20002933
##	0.4	2	0.8	0.8333333	50	0.9830164	0.14344730
##	0.4	2	0.8	0.8333333	100	0.9621000	0.17890601
##	0.4	2	0.8	0.8333333	150	0.9478686	0.20260125
##	0.4	2	0.8	0.8333333	200	0.9376887	0.21927548
##	0.4	2	0.8	1.0000000	50	0.9825976	0.14517317
##	0.4	2	0.8	1.0000000	100	0.9605538	0.18227242
##	0.4	2	0.8	1.0000000	150	0.9465222	0.20547818
##	0.4	2	0.8	1.0000000	200	0.9367238	0.22152204

		_					
##	0.4	3	0.6	0.5000000	50	0.9585270	0.18484961
##	0.4	3	0.6	0.5000000	100	0.9341938	0.22444539
##	0.4	3	0.6	0.5000000	150	0.9203762	0.24648533
##	0.4	3	0.6	0.5000000	200	0.9116180	0.26013009
##	0.4	3	0.6	0.6666667	50	0.9570624	0.18827898
##	0.4	3	0.6	0.666667	100	0.9322731	0.22842050
##	0.4	3	0.6	0.6666667	150	0.9181098	0.25081205
##	0.4	3	0.6	0.6666667	200	0.9088855	0.26523788
##	0.4	3	0.6	0.8333333	50	0.9580447	0.18695520
##	0.4	3	0.6	0.8333333	100	0.9320863	0.22935372
##	0.4	3	0.6	0.8333333	150	0.9178930	0.25179863
##	0.4	3	0.6	0.8333333	200	0.9080176	0.26716413
##	0.4	3	0.6	1.0000000	50	0.9569041	0.18921401
##	0.4	3	0.6	1.0000000	100	0.9314507	0.23083158
##	0.4	3	0.6	1.0000000	150	0.9171739	0.25326638
##	0.4	3	0.6	1.0000000	200	0.9071175	0.26894475
##	0.4	3	0.8	0.5000000	50	0.9561116	0.18884886
	$0.4 \\ 0.4$	3	0.8	0.5000000	100		0.22623525
##						0.9330781	
##	0.4	3	0.8	0.5000000	150	0.9202267	0.24659220
##	0.4	3	0.8	0.5000000	200	0.9111325	0.26065681
##	0.4	3	0.8	0.6666667	50	0.9565786	0.18848980
##	0.4	3	0.8	0.6666667	100	0.9309716	0.23038507
##	0.4	3	0.8	0.6666667	150	0.9172275	0.25201827
##	0.4	3	0.8	0.6666667	200	0.9073751	0.26740778
##	0.4	3	0.8	0.8333333	50	0.9548307	0.19229987
##	0.4	3	0.8	0.8333333	100	0.9296925	0.23299231
##	0.4	3	0.8	0.8333333	150	0.9148094	0.25660047
##	0.4	3	0.8	0.8333333	200	0.9052594	0.27136696
##	0.4	3	0.8	1.0000000	50	0.9557951	0.19102336
##	0.4	3	0.8	1.0000000	100	0.9296872	0.23351761
##	0.4	3	0.8	1.0000000	150	0.9148125	0.25700235
##	0.4	3	0.8	1.0000000	200	0.9051817	0.27188397
##	0.4	4	0.6	0.5000000	50	0.9362683	0.22215174
##	0.4	4	0.6	0.5000000	100	0.9131063	0.25797071
##	0.4	4	0.6	0.5000000	150	0.9003427	0.27765861
##	0.4	4	0.6	0.5000000	200	0.8926253	0.28928974
##	0.4	4	0.6	0.6666667	50	0.9361923	0.22246840
##	0.4	4	0.6	0.6666667	100	0.9117656	0.26078599
##	0.4	4	0.6	0.6666667	150	0.8986247	0.28085332
##	0.4	4	0.6	0.6666667	200	0.8895069	0.29468213
##	0.4	4	0.6	0.8333333	50	0.9342998	0.22612092
##	0.4	4	0.6	0.8333333	100	0.9086924	0.26602283
##	0.4	4	0.6	0.8333333	150	0.8954275	0.28624076
##	0.4	4	0.6	0.8333333	200	0.8867860	0.29933403
##	0.4	4	0.6	1.0000000	50	0.9327059	0.22957478
##	0.4	4	0.6	1.0000000	100	0.9065250	0.27055617
##	0.4	4	0.6	1.0000000	150	0.8923694	0.29211660
##	0.4	4	0.6	1.0000000	200	0.8837402	0.30491113
##	0.4	4	0.8	0.5000000	50	0.9327488	0.22726976
##	0.4	4	0.8	0.5000000	100	0.9114542	0.26009068
##	0.4	4	0.8	0.5000000	150	0.9003549	0.27704090
##	0.4	4	0.8	0.5000000	200	0.8918439	0.29023061
##	0.4	4	0.8	0.6666667	50	0.9333663	0.22669310
##	0.4	4	0.8	0.6666667	100	0.9084342	0.26581873
		-			•		

##	0.4 4	0.8	0.6666667	150	0.8960290	0.28473599
##	0.4 4	0.8	0.6666667	200	0.8878913	0.29704618
##	0.4 4	0.8	0.8333333	50	0.9326909	0.22884030
##	0.4 4	0.8	0.8333333	100	0.9067255	0.26925376
##	0.4 4	0.8	0.8333333	150	0.8932442	0.28975303
##	0.4 4	0.8	0.8333333	200	0.8851745	0.30177643
##	0.4 4	0.8	1.0000000	50	0.9309782	0.23195682
##	0.4 4	0.8	1.0000000	100	0.9046510	0.27339980
##	0.4 4	0.8	1.0000000	150	0.8914355	0.29334555
##	0.4 4	0.8	1.0000000	200	0.8836294	0.30482324
##	MAE					
##	0.8187048					
##	0.8096154					
##	0.8031344					
##	0.7980205					
##	0.8192679					
##	0.8102477					
##	0.8039038					
##	0.7991864					
##	0.8194361					
##	0.8106379					
##	0.8046295					
##	0.7999392					
##	0.8197890					
##	0.8113216					
##	0.8056354					
##	0.8011423					
##	0.8189655					
##	0.8093410					
##	0.8025122					
##	0.7976579					
##	0.8190924					
##	0.8100287					
##	0.8035628					
##	0.7987578					
##	0.8192757					
##	0.8105688					
##	0.8045182					
##	0.7998662					
##	0.8197399					
##	0.8114065					
##	0.8055367					
##	0.8011328					
##	0.7858054					
##	0.7660084					
##	0.7535924					
##	0.7437937					
##	0.7864832					
##	0.7670141					
##	0.7538235					
##	0.7446152					
##	0.7862627					
##	0.7664174					
##	0.7531327					

- 0.7436605 ##
- ## 0.7857111
- ## 0.7665214
- ## 0.7535599
- ## 0.7437154
- ## 0.7854258
- ## 0.7660667
- ## 0.7528638
- ## 0.7436481
- ## 0.7843756
- ## 0.7651121
- ## 0.7528587
- ## 0.7430303
- ## 0.7855704
- 0.7659992 ##
- ## 0.7531711
- ## 0.7432056
- ## 0.7848004
- 0.7656250 ##
- ## 0.7525684
- ## 0.7427621
- ## 0.7612074
- ## 0.7391796
- ## 0.7254844
- ## 0.7163780
- ## 0.7622497
- ## 0.7387341
- ## 0.7244059
- ## 0.7147572
- 0.7623226 ##
- ## 0.7381641 ##
- 0.7241507 ##
- 0.7148549
- ## 0.7616182
- ## 0.7377001 0.7230659 ##
- ## 0.7136649
- ## 0.7604038
- ## 0.7367736
- ## 0.7228744
- ## 0.7135501
- ## 0.7599792
- ## 0.7359167
- ## 0.722255
- ## 0.7128236
- ## 0.7600218
- ## 0.7361497
- ## 0.7214788
- ## 0.7121588
- ## 0.7605940 ##
- 0.7365432 ## 0.7221821
- ## 0.7119955
- ## 0.7417163

- 0.7181615 ##
- ## 0.7052370
- ## 0.6958611
- ## 0.7401781
- ## 0.7163628
- ## 0.7025855
- ## 0.6935395
- 0.7405391 ##
- ## 0.7158025
- ## 0.7015380
- ## 0.6926252
- ##
- 0.7410062
- ## 0.7152498
- ## 0.7017142
- ## 0.6922600
- ## 0.7400522
- ## 0.7164426
- ## 0.7037909
- ## 0.6947512
- ## 0.7380946
- ## 0.7136365
- ## 0.7005137
- ## 0.6914281
- ## 0.7388941
- ## 0.7140466
- ## 0.7004829
- ## 0.6915602 ## 0.7391161
- ## 0.7134443
- ## 0.7000713
- ## 0.6909557
- ## 0.8148917
- ## 0.8041480
- ## 0.7975060
- ## 0.7926960
- ## 0.8152024
- ## 0.8053482
- ## 0.7984288
- ## 0.7936127
- ##
- 0.8155115 ## 0.8060191
- ## 0.7992693
- ##
- 0.7946719
- ## 0.8157912
- ## 0.8065836 ## 0.8002670
- ## 0.7957354
- ##
- 0.8143362 ## 0.8038822
- ## 0.7969262
- ## 0.7922085
- ## 0.8148210
- ## 0.8049768
- ## 0.7982792

- 0.7936089 ##
- ## 0.8155048
- ## 0.8056044
- ## 0.7989754
- ## 0.7944587
- ## 0.8157233
- ## 0.8065123
- ## 0.8001753
- ## 0.7957834
- ## 0.7775425
- ## 0.7570102
- ## 0.7445209
- ## 0.7359705
- ## 0.7781646
- ## 0.7579205
- ## 0.7444542
- ## 0.7357474
- ## 0.7784995
- 0.7567893 ##
- 0.7433983 ##
- ## 0.7340795
- ## 0.7792842
- ## 0.7572692
- ## 0.7432023
- ##
- 0.7332621
- ## 0.7769017
- ## 0.7569755
- ## 0.7453241
- ## 0.7356823
- ## 0.7768657
- ## 0.7555923
- 0.7432081 ##
- ## 0.7337915
- ## 0.7768324
- ## 0.7560525
- 0.7425484 ##
- ## 0.7328058
- ## 0.7765734
- ## 0.7551907 ##
- 0.7414111 ## 0.7321878
- ## 0.7528467
- ## 0.7294874
- ## 0.7167354
- ## 0.7084404
- ## 0.7515054
- ## 0.7283356
- ## 0.7152461
- ## 0.7064329
- ## 0.7533013
- ## 0.7281895
- ## 0.7149175
- ## 0.7058665 ## 0.7519173

```
0.7276993
##
##
     0.7142684
     0.7046890
##
##
     0.7502392
##
     0.7283329
##
     0.7162500
##
     0.7077888
     0.7511541
##
##
     0.7267153
##
     0.7135526
##
     0.7047620
##
     0.7496017
##
     0.7258436
##
     0.7121405
     0.7031407
##
##
     0.7506579
##
     0.7262294
     0.7121964
##
     0.7031102
##
     0.7321511
##
##
     0.7099759
##
     0.6980793
##
     0.6910041
##
     0.7325958
##
     0.7093285
##
     0.6966933
     0.6880165
##
##
     0.7305312
##
     0.7062984
##
     0.6941173
##
     0.6859043
##
     0.7288383
##
     0.7044627
     0.6913016
##
     0.6831407
##
     0.7286127
##
##
     0.7082546
##
     0.6981311
##
     0.6903308
##
     0.7295579
##
     0.7061566
     0.6940746
##
##
     0.6866793
##
     0.7292102
##
     0.7051451
##
     0.6921615
##
     0.6847352
##
     0.7279803
##
     0.7034129
##
     0.6911057
##
     0.6837324
##
## Tuning parameter 'gamma' was held constant at a value of 0
## Tuning
```

Method	RMSE
Target	0.8649000
Mean	1.0547663
Mean + bi	0.9860457
Mean + bi + bu	0.9056371
Regularized Movie + User Effect	0.8879858
Matrix Factorization - recosystem	0.9307754
XGboostLinear	0.8676153

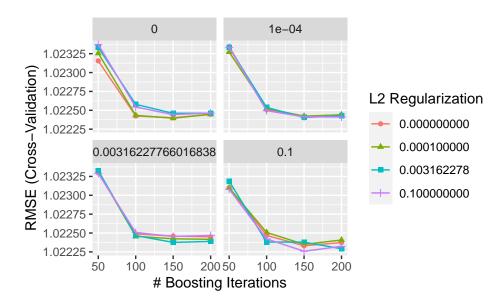
Method	RMSE
Target 0.8	649000
Mean 1.0	547663
Mean + bi 0.9	860457
Mean + bi + bu 0.96	056371
Regularized Movie + User Effect 0.8	879858
Matrix Factorization - recosystem 0.93	307754
XGboostLinear 0.8	676153
XGboostTree 0.8	868028

```
# To make a model for new user / new movie (ONLY genre selection)
train_small2 %>% select(-c(movieId, year, userId, timestamp)) %>%
mutate_all(~ifelse(is.na(.), median(., na.rm = TRUE), .)) -> train_small3
```

```
test_small2 %>% select(-c(movieId, year, userId, timestamp)) %>%
 mutate_all(~ifelse(is.na(.), median(., na.rm = TRUE), .)) -> test_small3
# Note: it took 40 minutes!!
# Xgboost Linear model for new user/movie
set.seed(1, sample.kind = "Rounding")
system.time(
 modelXgboostLinear_new <- train(</pre>
   rating ~ .,
   data = train_small3,
   method = "xgbLinear",
   preProcess = c('center', 'scale'),
   trControl = trainControl(method = "cv"),
   tuneLength = 4)
)
##
     user
           system elapsed
##
    29.58
             1.25 2290.09
print(modelXgboostLinear_new)
## eXtreme Gradient Boosting
##
## 90324 samples
##
     20 predictor
##
## Pre-processing: centered (20), scaled (20)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 81292, 81291, 81291, 81291, 81292, 81292, ...
## Resampling results across tuning parameters:
##
##
    lambda
                 alpha
                             nrounds
                                      RMSE
                                                Rsquared
                                                            MAE
##
                 0.00000000
                              50
    0.000000000
                                      1.023155
                                                0.06564875
                                                           0.8124933
##
    0.000000000
                 0.000000000
                                      1.022425
                             100
                                                ##
    0.000000000
                 0.000000000
                             150
                                      1.022400
                                                ##
    0.000000000
                 0.000000000
                              200
                                      1.022447
                                                0.06746456
                                                           0.8107015
##
    0.00000000
                 0.000100000
                              50
                                      1.023343 0.06532308 0.8125872
##
    0.000000000
                 0.000100000
                             100
                                      1.022507 0.06705514 0.8112632
                                      1.022417
##
                 0.000100000
                                                0.06738914   0.8108207
    0.000000000
                             150
##
    0.000000000
                 0.000100000
                             200
                                      1.022440
                                                0.06747727 0.8106731
##
    0.000000000
                 0.003162278
                              50
                                      1.023298 0.06541659 0.8125052
##
    0.000000000
                 0.003162278
                             100
                                      1.022488 0.06707666 0.8111424
##
    0.000000000
                 0.003162278
                             150
                                      1.022459
                                                ##
                             200
                                      1.022449
                                                0.000000000
                 0.003162278
##
    0.000000000
                 0.100000000
                              50
                                      1.023099
                                                0.06577150 0.8123362
##
    0.000000000
                 0.100000000
                             100
                                      1.022468
                                                0.06713222  0.8112222
##
    0.000000000
                 0.100000000
                             150
                                      1.022331
                                                0.06754676
                                                           0.8108081
##
                             200
    0.000000000
                 0.100000000
                                      1.022374
                                                0.06758450
                                                          0.8106259
##
    0.000100000
                 0.00000000
                              50
                                      1.023255 0.06546429
                                                          0.8125892
##
    0.000100000
                 0.000000000
                             100
                                      1.022433 0.06716289 0.8111902
```

```
##
     0.000100000
                  0.00000000
                                150
                                          1.022395
                                                    0.06741537
                                                                 0.8107977
##
                                200
     0.000100000
                  0.00000000
                                          1.022447
                                                    0.06744828
                                                                 0.8106707
##
     0.000100000
                  0.000100000
                                 50
                                          1.023273
                                                    0.06545203
                                                                 0.8125506
##
                                          1.022524
     0.000100000
                  0.000100000
                                100
                                                    0.06702677
                                                                 0.8112781
##
     0.000100000
                  0.000100000
                                150
                                          1.022423
                                                    0.06738114
                                                                 0.8108159
                                          1.022439
##
     0.000100000
                  0.000100000
                                200
                                                    0.06747570
                                                                 0.8106739
##
     0.000100000
                  0.003162278
                                 50
                                          1.023314
                                                    0.06539103
                                                                 0.8125366
##
     0.000100000
                  0.003162278
                                100
                                          1.022457
                                                    0.06713394
                                                                 0.8111387
##
     0.000100000
                  0.003162278
                                150
                                          1.022423
                                                    0.06737839
                                                                 0.8108287
##
     0.000100000
                  0.003162278
                                200
                                          1.022416
                                                    0.06751742
                                                                 0.8106028
##
     0.000100000
                  0.100000000
                                 50
                                          1.023099
                                                    0.06577153
                                                                 0.8123361
##
     0.000100000
                  0.100000000
                                100
                                          1.022508
                                                    0.06705907
                                                                 0.8112685
##
     0.000100000
                  0.100000000
                                150
                                          1.022350
                                                    0.06751041
                                                                 0.8108405
                  0.100000000
##
     0.000100000
                                200
                                          1.022407
                                                    0.06752274
                                                                 0.8106861
##
     0.003162278
                  0.00000000
                                 50
                                          1.023333
                                                    0.06534837
                                                                 0.8125681
##
     0.003162278
                  0.00000000
                                100
                                          1.022578
                                                    0.06692002
                                                                 0.8113101
##
                  0.00000000
                                150
                                          1.022460
                                                    0.06731398
     0.003162278
                                                                 0.8108859
##
     0.003162278
                  0.00000000
                                 200
                                          1.022461
                                                    0.06742994
                                                                 0.8106930
##
     0.003162278
                  0.000100000
                                 50
                                          1.023333
                                                    0.06534844
                                                                 0.8125681
##
     0.003162278
                  0.000100000
                                100
                                          1.022539
                                                    0.06698221
                                                                 0.8112863
##
     0.003162278
                  0.000100000
                                150
                                          1.022405
                                                    0.06740218
                                                                 0.8108115
                  0.000100000
                                          1.022427
##
     0.003162278
                                200
                                                    0.06748961
                                                                 0.8106304
##
     0.003162278
                  0.003162278
                                 50
                                          1.023326
                                                    0.06536710
                                                                 0.8125555
##
     0.003162278
                  0.003162278
                                100
                                          1.022466
                                                    0.06712004
                                                                 0.8111428
##
     0.003162278
                  0.003162278
                                150
                                          1.022376
                                                    0.06746516
                                                                 0.8108000
##
     0.003162278
                  0.003162278
                                200
                                          1.022389
                                                    0.06755095
                                                                 0.8105908
##
     0.003162278
                                          1.023186
                  0.100000000
                                 50
                                                    0.06563675
                                                                 0.8124563
##
     0.003162278
                  0.100000000
                                100
                                          1.022380
                                                    0.06726178
                                                                 0.8111882
##
     0.003162278
                  0.100000000
                                150
                                          1.022379
                                                    0.06743415
                                                                 0.8108675
##
     0.003162278
                  0.100000000
                                200
                                          1.022291
                                                    0.06770342
                                                                 0.8106115
##
     0.100000000
                  0.00000000
                                 50
                                          1.023372
                                                    0.06529482
                                                                 0.8126703
##
     0.100000000
                  0.00000000
                                100
                                          1.022543
                                                    0.06700449
                                                                 0.8112986
##
     0.100000000
                  0.00000000
                                150
                                          1.022443
                                                    0.06734986
                                                                 0.8109165
                                200
##
     0.100000000
                  0.00000000
                                          1.022464
                                                    0.06743071
                                                                 0.8107428
##
     0.100000000
                  0.000100000
                                 50
                                          1.023334
                                                    0.06536177
                                                                 0.8126644
##
     0.100000000
                  0.000100000
                                100
                                          1.022495
                                                    0.06709115
                                                                 0.8112536
##
     0.100000000
                  0.000100000
                                150
                                          1.022414
                                                    0.06740032
                                                                 0.8108715
##
                  0.000100000
                                200
                                          1.022412
     0.100000000
                                                    0.06751516
                                                                 0.8107056
##
                  0.003162278
                                          1.023289
     0.100000000
                                 50
                                                    0.06543406
                                                                 0.8125539
##
                                                                 0.8112550
     0.100000000
                  0.003162278
                                100
                                          1.022507
                                                    0.06706731
##
     0.100000000
                  0.003162278
                                150
                                          1.022454
                                                    0.06732874
                                                                 0.8109118
##
                                200
                                          1.022468
                                                    0.06743602
     0.100000000
                  0.003162278
                                                                 0.8107397
##
     0.100000000
                  0.100000000
                                 50
                                          1.023081
                                                    0.06580730
                                                                 0.8123527
##
                  0.100000000
                                100
                                          1.022422
     0.100000000
                                                    0.06720006
                                                                 0.8111909
##
     0.100000000
                  0.100000000
                                150
                                          1.022259
                                                    0.06765055
                                                                 0.8107862
##
     0.100000000
                  0.100000000
                                200
                                          1.022324
                                                    0.06764578
                                                                 0.8106414
##
   Tuning parameter 'eta' was held constant at a value of 0.3
   RMSE was used to select the optimal model using the smallest value.
   The final values used for the model were nrounds = 150, lambda = 0.1, alpha
    = 0.1 and eta = 0.3.
##
```

ggplot(modelXgboostLinear_new)



RMSE .8649000
8649000
.0043000
.0547663
.9860457
.9056371
.8879858
.9307754
.8676153
.8868028
.0147697

```
# Again, to make a model for new user (KEEP the movieId)
train_small2 %>% select(-c(year, userId, timestamp)) %>%
   mutate_all(~ifelse(is.na(.), median(., na.rm = TRUE), .)) -> train_small4

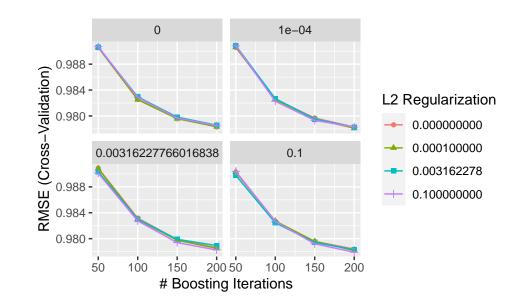
test_small2 %>% select(-c(year, userId, timestamp)) %>%
   mutate_all(~ifelse(is.na(.), median(., na.rm = TRUE), .)) -> test_small4

# Note: it took 35 minutes!!
# Xgboost Linear model for new user/movie
```

```
set.seed(1, sample.kind = "Rounding")
system.time(
  modelXgboostLinear_newUser <- train(</pre>
    rating ~ .,
   data = train_small4,
   method = "xgbLinear",
   preProcess = c('center', 'scale'),
    trControl = trainControl(method = "cv"),
    tuneLength = 4)
)
##
      user
            system elapsed
##
     44.10
              0.89 1986.98
print(modelXgboostLinear newUser)
## eXtreme Gradient Boosting
##
## 90324 samples
##
      21 predictor
##
## Pre-processing: centered (21), scaled (21)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 81292, 81291, 81291, 81291, 81292, 81292, ...
## Resampling results across tuning parameters:
##
##
     lambda
                  alpha
                                        RMSE
                                                    Rsquared
                                                               MAE
                               nrounds
##
                                                    0.1252092
     0.00000000
                  0.00000000
                                50
                                         0.9905718
                                                               0.7818742
##
     0.00000000
                  0.00000000
                               100
                                         0.9825392 0.1384463
                                                               0.7729092
##
     0.000000000
                  0.00000000
                               150
                                         0.9797368 0.1432080
                                                               0.7691322
                               200
##
     0.000000000
                  0.00000000
                                         0.9782981
                                                    0.1460119
                                                               0.7669334
##
     0.000000000
                  0.000100000
                                50
                                         0.9905718 0.1252092 0.7818742
##
                                         0.9825851 0.1383726
     0.000000000
                  0.000100000
                               100
                                                              0.7729963
##
     0.00000000
                  0.000100000
                               150
                                         0.9796785
                                                    0.1433102 0.7691285
##
     0.000000000
                  0.000100000
                               200
                                         0.9782857
                                                    0.1460369
                                                               0.7669162
##
                                50
     0.000000000
                  0.003162278
                                         0.9908884 0.1245655
                                                               0.7823068
##
     0.000000000
                  0.003162278
                               100
                                         0.9831837 0.1373276
                                                              0.7737418
##
     0.000000000
                  0.003162278
                               150
                                         0.9798573 0.1430094
                                                               0.7694102
##
     0.000000000
                  0.003162278
                               200
                                         0.9786080 0.1454886
                                                              0.7672619
##
     0.000000000
                  0.100000000
                                50
                                         0.9902436 0.1258803
                                                              0.7815445
##
     0.000000000
                  0.100000000
                               100
                                         0.9826899 0.1382200
                                                              0.7730423
##
     0.000000000
                  0.100000000
                               150
                                         0.9795823
                                                    0.1435174
                                                               0.7689600
##
                               200
     0.000000000
                  0.100000000
                                         0.9783889 0.1459059
                                                               0.7669422
##
     0.000100000
                  0.00000000
                                50
                                         0.9906263
                                                   0.1251272
                                                               0.7819922
##
     0.000100000
                  0.00000000
                               100
                                         0.9825156
                                                   0.1385047
                                                               0.7729141
##
     0.000100000
                  0.00000000
                               150
                                         0.9795706
                                                    0.1434990
                                                               0.7689973
##
                               200
     0.000100000
                  0.00000000
                                         0.9783347
                                                   0.1459635
                                                               0.7669137
##
                  0.000100000
     0.000100000
                                50
                                         0.9906264
                                                    0.1251271
                                                               0.7819922
                  0.000100000
##
     0.000100000
                               100
                                         0.9825157
                                                    0.1385045
                                                               0.7729143
##
     0.000100000
                  0.000100000
                               150
                                         0.9795185
                                                    0.1435908
                                                               0.7690359
##
     0.000100000
                  0.000100000
                               200
                                         0.9781091
                                                    0.1463480
                                                               0.7667518
##
     0.000100000
                  0.003162278
                                50
                                         0.9908348 0.1246694
                                                               0.7822129
##
     0.000100000
                  0.003162278
                               100
                                         0.9829611 0.1377242 0.7735969
```

```
##
    0.000100000 0.003162278
                              150
                                       0.9797469 0.1431856 0.7693683
##
    0.000100000
                 0.003162278
                              200
                                       0.9785213 0.1456040
                                                             0.7673675
                 0.100000000
                                                             0.7814686
##
    0.000100000
                               50
                                       0.9903146 0.1257455
##
                 0.100000000
    0.000100000
                              100
                                       0.9827267 0.1381826
                                                             0.7730890
##
    0.000100000
                 0.100000000
                              150
                                       0.9795718 0.1435487
                                                             0.7689951
##
    0.000100000
                 0.100000000
                              200
                                       0.9781626 0.1463143 0.7668421
##
    0.003162278
                 0.00000000
                                       0.9906079 0.1250642 0.7820176
                               50
                 0.000000000
                                       0.9829593 0.1377122 0.7733981
##
    0.003162278
                              100
##
    0.003162278
                 0.00000000
                              150
                                       0.9798241 0.1430850
                                                             0.7693851
##
                 0.000000000
                              200
                                       0.9785649 0.1456147
    0.003162278
                                                             0.7673183
##
    0.003162278
                 0.000100000
                               50
                                       0.9908694 0.1246199
                                                             0.7822843
##
    0.003162278
                 0.000100000
                              100
                                       0.9826822 0.1382051 0.7732123
##
    0.003162278
                 0.000100000
                              150
                                       0.9795268 0.1435710 0.7692177
    0.003162278
##
                 0.000100000
                              200
                                       0.9782727 0.1460837
                                                             0.7671844
##
    0.003162278
                 0.003162278
                               50
                                       0.9903269 0.1256178 0.7815567
##
    0.003162278
                 0.003162278
                              100
                                       0.9830016 0.1376637
                                                             0.7734435
##
    0.003162278
                 0.003162278
                              150
                                       0.9799047 0.1429209
                                                             0.7693579
                              200
##
    0.003162278
                 0.003162278
                                       0.9789373 0.1449654
                                                             0.7673970
##
    0.003162278
                 0.100000000
                               50
                                       0.9897787 0.1267296
                                                            0.7813190
##
    0.003162278
                 0.100000000
                              100
                                       0.9824438 0.1386684
                                                            0.7729609
##
    0.003162278
                 0.100000000
                              150
                                       0.9794072 0.1438220 0.7689269
##
    0.003162278
                 0.100000000
                              200
                                       0.9783025 0.1460663
                                                             0.7668465
##
    0.100000000
                 0.00000000
                               50
                                       0.9907131 0.1250247
                                                             0.7820704
##
    0.100000000
                 0.00000000 100
                                       0.9828633 0.1379342
                                                             0.7733804
##
    0.100000000
                 0.000000000
                              150
                                       0.9796847 0.1433170 0.7693557
##
    0.100000000
                 0.000000000
                              200
                                       0.9785007 0.1456319 0.7674193
##
    0.100000000
                 0.000100000
                               50
                                       0.9908137 0.1248435 0.7820966
    0.100000000
                 0.000100000 100
                                       0.9822745 0.1389785
##
                                                            0.7729065
##
                 0.000100000
                                       0.9793120 0.1439612 0.7689832
    0.100000000
                              150
                 0.000100000
                                       0.9782890 0.1460394 0.7671353
##
    0.100000000
                              200
                 0.003162278
##
    0.100000000
                               50
                                       0.9901168 0.1261836 0.7815049
##
    0.100000000
                 0.003162278 100
                                       0.9827509 0.1381070 0.7731920
##
                              150
                                       0.9793874 0.1437917
    0.100000000
                 0.003162278
                                                             0.7689444
##
    0.100000000
                 0.003162278
                              200
                                       0.9782592 0.1460406
                                                            0.7670333
##
    0.100000000
                 0.100000000
                               50
                                       0.9904147 0.1256314
                                                             0.7818342
##
    0.100000000
                 0.10000000 100
                                       0.9826503 0.1383127
                                                             0.7729789
##
    0.100000000
                 0.100000000
                              150
                                       0.9792085 0.1441337
                                                             0.7687148
##
    0.100000000
                 0.100000000 200
                                       0.9779021 0.1466735 0.7666347
##
## Tuning parameter 'eta' was held constant at a value of 0.3
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were nrounds = 200, lambda = 0.1, alpha
   = 0.1 and eta = 0.3.
```

ggplot(modelXgboostLinear_newUser)



Method	RMSE
Target	0.8649000
Mean	1.0547663
Mean + bi	0.9860457
Mean + bi + bu	0.9056371
Regularized Movie + User Effect	0.8879858
Matrix Factorization - recosystem	0.9307754
XGboostLinear	0.8676153
XGboostTree	0.8868028
XGboostLinear for New User/Movie	1.0147697
XGboostLinear for New User	0.9728732

```
# Once more, to make a model for new movie (KEEP the userId)
train_small2 %>% select(-c(year, movieId, timestamp)) %>%
   mutate_all(~ifelse(is.na(.), median(., na.rm = TRUE), .)) -> train_small5

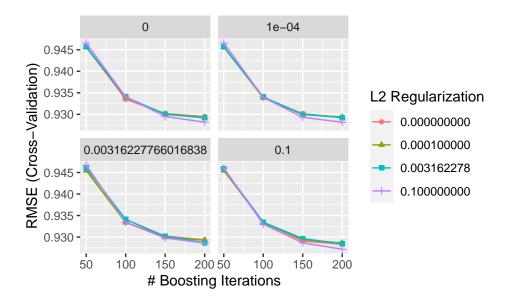
test_small2 %>% select(-c(year, movieId, timestamp)) %>%
   mutate_all(~ifelse(is.na(.), median(., na.rm = TRUE), .)) -> test_small5

# Note: it took 35 minutes!!
```

```
# Xgboost Linear model for new user/movie
set.seed(1, sample.kind = "Rounding")
system.time(
  modelXgboostLinear_newMovie <- train(</pre>
    rating ~ .,
    data = train_small5,
   method = "xgbLinear",
   preProcess = c('center', 'scale'),
    trControl = trainControl(method = "cv"),
    tuneLength = 4)
)
##
           system elapsed
##
     39.50
              0.91 2084.00
print(modelXgboostLinear_newMovie)
## eXtreme Gradient Boosting
##
## 90324 samples
##
      21 predictor
##
## Pre-processing: centered (21), scaled (21)
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 81292, 81291, 81291, 81291, 81292, 81292, ...
## Resampling results across tuning parameters:
##
##
                                                               MAE
     lambda
                  alpha
                               nrounds
                                        RMSE
                                                    Rsquared
##
     0.00000000
                  0.00000000
                                50
                                         0.9456368
                                                   0.2050042
                                                               0.7394535
##
     0.000000000
                  0.00000000
                                        0.9334930 0.2226497
                               100
                                                               0.7265766
     0.000000000
                  0.00000000
##
                               150
                                        0.9301666
                                                   0.2276977
                                                               0.7223797
##
     0.00000000
                  0.00000000
                               200
                                        0.9294869 0.2292551
                                                               0.7207675
##
                                        0.9456505 0.2049876
     0.000000000
                  0.000100000
                                                              0.7395026
##
                               100
     0.00000000
                  0.000100000
                                        0.9338877
                                                   0.2219811
                                                               0.7268404
##
     0.000000000
                  0.000100000
                               150
                                        0.9301310
                                                   0.2277544
                                                               0.7222199
##
                               200
                                        0.9292987 0.2295448
     0.000000000
                  0.000100000
                                                              0.7205373
##
     0.000000000
                  0.003162278
                                50
                                        0.9455125 0.2052888
                                                              0.7395488
##
     0.000000000
                  0.003162278
                               100
                                        0.9334305 0.2227722
                                                              0.7266116
##
     0.000000000
                  0.003162278
                               150
                                        0.9302448 0.2275659
                                                              0.7225952
##
     0.000000000
                  0.003162278
                               200
                                        0.9293659 0.2294233
                                                              0.7208566
##
     0.000000000
                  0.100000000
                                50
                                        0.9454969 0.2054991
                                                               0.7392016
##
     0.000000000
                  0.100000000
                               100
                                        0.9333471
                                                   0.2229396
                                                               0.7265349
##
     0.000000000
                  0.100000000
                               150
                                        0.9290986 0.2294539
                                                               0.7216903
##
     0.000000000
                  0.100000000
                               200
                                         0.9283141
                                                   0.2310321
                                                               0.7199741
##
     0.000100000
                  0.00000000
                                50
                                        0.9456335
                                                   0.2050569
                                                               0.7396036
##
     0.000100000
                  0.00000000
                               100
                                         0.9338389
                                                   0.2220710
                                                               0.7268325
##
     0.000100000
                  0.000000000
                               150
                                        0.9301123 0.2277949
                                                              0.7222712
                  0.00000000
                                                   0.2295662
##
     0.000100000
                                        0.9292860
                                                              0.7205707
##
     0.000100000
                  0.000100000
                                50
                                        0.9456334
                                                   0.2050572 0.7396036
##
                               100
     0.000100000
                  0.000100000
                                        0.9338380
                                                   0.2220726
                                                               0.7268306
##
     0.000100000
                  0.000100000
                               150
                                        0.9299700
                                                   0.2280324
                                                               0.7220791
                               200
##
     0.000100000
                  0.000100000
                                        0.9293743 0.2294265
                                                              0.7205305
##
     0.000100000
                  0.003162278
                                50
                                        0.9454596 0.2053874 0.7394779
```

```
##
     0.000100000
                  0.003162278
                               100
                                        0.9333765 0.2228972
                                                              0.7266376
##
     0.000100000
                               150
                  0.003162278
                                        0.9299682
                                                   0.2280354
                                                               0.7224897
                               200
                                                               0.7207442
##
     0.000100000
                  0.003162278
                                        0.9292565
                                                   0.2296006
##
     0.000100000
                  0.100000000
                                50
                                        0.9454880 0.2054719
                                                              0.7392963
##
     0.000100000
                  0.100000000
                               100
                                        0.9333020 0.2230091
                                                               0.7265240
##
     0.000100000
                  0.100000000
                               150
                                        0.9294058 0.2289393
                                                              0.7218420
##
                  0.100000000
                               200
                                        0.9286062 0.2305687
     0.000100000
                                                               0.7201968
                  0.00000000
##
     0.003162278
                                50
                                        0.9457237
                                                   0.2048777
                                                               0.7395789
##
     0.003162278
                  0.00000000
                               100
                                        0.9340330
                                                   0.2217273
                                                               0.7269491
##
     0.003162278
                  0.00000000
                               150
                                        0.9300138 0.2279451
                                                               0.7223617
##
     0.003162278
                  0.00000000
                               200
                                        0.9292036 0.2296660
                                                              0.7210091
##
     0.003162278
                  0.000100000
                                50
                                        0.9457236 0.2048779
                                                              0.7395788
##
     0.003162278
                  0.000100000
                               100
                                        0.9340328 0.2217278
                                                              0.7269490
                  0.000100000
                                        0.9300134 0.2279458
##
                                                              0.7223616
     0.003162278
                               150
##
     0.003162278
                  0.000100000
                               200
                                        0.9292378 0.2296133
                                                              0.7209882
##
     0.003162278
                  0.003162278
                                50
                                        0.9461039
                                                   0.2043235
                                                               0.7399164
##
                                        0.9341140 0.2216154
     0.003162278
                  0.003162278
                               100
                                                               0.7269243
##
     0.003162278
                  0.003162278
                               150
                                        0.9301847 0.2276601
                                                               0.7223270
##
     0.003162278
                  0.003162278
                               200
                                        0.9286841 0.2304862
                                                              0.7202667
##
     0.003162278
                  0.100000000
                                50
                                        0.9458931 0.2047508
                                                              0.7395238
##
     0.003162278
                  0.100000000
                               100
                                        0.9334431 0.2228081
                                                              0.7267514
##
     0.003162278
                  0.100000000
                               150
                                        0.9296563 0.2285458
                                                              0.7224768
##
     0.003162278
                  0.100000000
                               200
                                        0.9284234 0.2308997
                                                               0.7204987
##
     0.100000000
                  0.00000000
                                        0.9465615
                                                   0.2035480
                                50
                                                               0.7402912
##
                                        0.9340568 0.2217650
     0.100000000
                  0.000000000
                               100
                                                              0.7274988
##
     0.100000000
                  0.000000000
                               150
                                        0.9295094 0.2287799
                                                              0.7223541
##
     0.100000000
                  0.00000000
                               200
                                        0.9281779 0.2312318
                                                              0.7203746
     0.100000000
                  0.000100000
                                        0.9465607 0.2035489
##
                                50
                                                              0.7402896
##
     0.100000000
                  0.000100000
                               100
                                        0.9339316 0.2219768 0.7274960
##
     0.100000000
                  0.000100000
                               150
                                        0.9293187 0.2290974
                                                              0.7222441
                  0.000100000
##
     0.100000000
                               200
                                        0.9281561
                                                   0.2312669
                                                               0.7203711
##
     0.100000000
                  0.003162278
                                50
                                        0.9466990 0.2033827
                                                               0.7401534
##
     0.100000000
                  0.003162278
                               100
                                        0.9334074 0.2229166
                                                              0.7264732
                  0.003162278
##
                                        0.9297704 0.2283653
                                                              0.7224056
     0.100000000
                               150
##
     0.100000000
                  0.003162278
                               200
                                        0.9286298
                                                   0.2305179
                                                               0.7201823
##
     0.100000000
                  0.100000000
                                        0.9460278 0.2043751
                                50
                                                              0.7390793
##
     0.100000000
                  0.100000000
                               100
                                        0.9329931
                                                   0.2235792
                                                              0.7260371
##
     0.100000000
                  0.100000000
                               150
                                        0.9286647
                                                   0.2301933
                                                               0.7212111
##
     0.100000000
                  0.100000000
                               200
                                        0.9271721 0.2328562 0.7191945
##
## Tuning parameter 'eta' was held constant at a value of 0.3
  RMSE was used to select the optimal model using the smallest value.
  The final values used for the model were nrounds = 200, lambda = 0.1, alpha
##
   = 0.1 and eta = 0.3.
```

ggplot(modelXgboostLinear_newMovie)



Method	RMSE
Target	0.8649000
Mean	1.0547663
Mean + bi	0.9860457
Mean + bi + bu	0.9056371
Regularized Movie + User Effect	0.8879858
Matrix Factorization - recosystem	0.9307754
XGboostLinear	0.8676153
XGboostTree	0.8868028
XGboostLinear for New User/Movie	1.0147697
XGboostLinear for New User	0.9728732
XGboostLinear for New Movie	0.9282118

5 Conclusion

As a result of training various models, it is clear that movieId and userId contribute more to the prediction than genre and year of Rate (timestamp). The results of the analysis using recosystem showed that with a large data size, only two pieces of information, movieId and userId, are highly accurate.

Although we were not able to run it on the target data set, we were able to build a model with movieId and userId missing and find a possibility for improvement. We did multiple machine learning runs, but not

enough studies with tuning. Since there are many places where default values are used, Future work is to tune the parameters in an environment where faster calculations can be done.

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