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Social Network Analysis for Computer Scientists — Course paper

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ABSTRACT KEYWORDS

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1 INTRODUCTION

Graphs are mathematical objects that can model complex relationships on non-Eucildean space. They are widely used in multiple domains such as molecular structure modelling, social network analysis, recommender systems, etc. To leverage the information contained in graphs, it is essential to develop efficient techniques for representing graph-structured data numerically.

Traditional statistical and machine learning methods are designed for extracting features from structured data on Eucildean space. For example, principal component analysis(PCA), uniform manifold approximation and projection (UMAP), and t-distributed stochastic neighbor embedding (T-SNE) are common techniques to reduce dimensions and capture features of data. Although these methods have achieved satisfactory performance on structured-data, they are hard to be generalized to graph-structured data, because they highly depend on properties of Eucildean space.

This challenge led to the development of techniques specifically for graph-based representation. There are two main types of these techniques: shallow embedding method and deep embedding method [8]. Shallow embedding methods use shallow encoder functions to map the original graph structure onto a Euclidean space and obtain the embedding matrix. If data is labelled, we can apply supervised learning algorithms, e.g. label propagation, to extract embeddings later used in a supervised task. However, labels are not available or only partly available in most cases, where we need unsupervised learning or semi-supervised learning to distill information about graph structure. These methods can be divided into distance-based method and outer product method further [8]. Generally, distance-based methods select a metric function that indicates distances between any pairs of nodes and optimize the

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function to generate embeddings. Representative distance-based methods include multi-dimensional scaling and laplacian eigenmaps. Outer product-based methods use matrix operations to evaluate the similarity between nodes. Most of early studies in graph embedding field adopt matrix factorization to reduce dimensionality of data while preserve the structure information [2]. Another mainstream outer product-based method is inspired by the development in natural language processing. Existing research generalizes the skip-gram word embedding framework to capture the graph embeddings, which has been proved to be efficient on many graph related tasks [9][10]. Node2vec [4], one of algorithms addressed in this paper, is also a variation of skip-gram-based method.

Node2vec is a semi-supervised algorithm whose goal is learning features from networks [4]. It transforms the graph embedding learning into a maximum likelihood optimization problem in a similar way to skip-gram architecture of word embedding learning. Likelihood calculation requires a clear definition of the neighborhood. Textual data has the intrinsic semantic order that can be naturally employed as word neighborhoods. However, graph-structured data has no explicit neighborhoods. Node2vec introduces the idea of the second-order random walk into graph neighborhood sampling strategy. The emphasis of node2vec model is easy to switch between breadth-first sampling (BFS) and depth-first sampling (DFS) by adjusting hyperparameters. Moreover, its computational complexity is less than classical BFS and DFS strategies. Because of its efficiency and great performance on graph embedding learning task, node2vec is an ideal choice among shallow embedding methods.

In recent years, a lot of studies have focused more on deep embedding method rather than the shallow one. Deep embedding method usually refers to algorithms that learn graph features via graph neural networks (GNN). The GNN is a class of artificial neural networks constructed for graph-structured data. Inspired by the success of convolutional neural networks (CNN) on grid data, many GNN architectures have been proposed to generalize the convolution operation on graphs. In this paper, we mainly focus on a method called graph convolutional networks (GCN) [6]. GCNs defines the graph convolution based on the graph Laplacian spectrum. It has achieved state-of-the-art performance on common graph related tasks, such as node classification, link prediction, etc.

We propose a novel method to extract embeddings from graphs in this paper. Our method is based on node2vec and GCNs. Motivated by the concept of meta learning, we regard the embeddings returned by node2vec as the meta information for GCNs. This prior knowledge helps to improve the quality of final graph embeddings, and therefore enhances the model performance in various tasks.

The rest of the paper is organized as follows. Section 2 reviews related works on graph embedding learning methods. We illustrate

basic task notations and framework in Section 3. And then we describe approaches in detail in Section 4. Section 5 is an introduction to five open source data sets we use in the project. After that, we present our experimental set-up and results in Section 6. The paper ends with a conclusion section.

2 RELATED WORK

Our project draws inspiration both from the skip-gram-based shallow embedding method and the deep embedding method. The following will briefly review existing works related to these methods.

Skip-gram-based methods optimize graph embeddings to predict nodes in the defined context. Actually, this kind of methods leverages the matrix factorization technique implicitly [8]. Compared to early works that explicitly use matrix factorization, skipgram-based methods are usually more computationally efficient. Deepwalk [9], an algorithm proposed in 2014, is one of pioneering studies that generalizes the idea of skip-gram model in language processing to graph embedding learning field. Deepwalk models the context of nodes by truncated random walks, which is analogous to sentences in textual data. It utilizes the local information obtained from random walks and learns a latent space that corresponds to features of vertices. Following the Deepwalk, LINE algorithm [10] is proposed to address the preservation of network properties and applicability on large-scale networks. The neighborhood sampling strategy of LINE is firstly simulating a BFS-style search for half of the feature dimensions and then a DFS-style search for remaining dimensions. Both Deepwalk and LINE are restricted to a specific sampling strategy of neighborhoods. Node2vec [4] algorithm provides a more flexible option. It introduces a return parameter and an in-out parameter during second-order random walks that enables users to adjust the style of sampling. Its workflow is similar to Deepwalk and can be considered as a generalization.

GNNs have been extensively researched these years. Learning graph embeddings is one of the important applications of GNNs. According to [8], GNN models used to devise graph embeddings are called deep embedding methods. A main challenge in designing GNNs is finding an efficient and easy-to-train filter to process graph signals. One solution is applying graph Fourier transform to define the convolution operation on graphs. However, using a filter directly based on graph Laplacian matrix is computationally expensive. Defferrard et al. [3] suggest to approximate the filter by the k-order Chebyshev polynomial, which has a practical computational complexity. Kipf and Welling [6] propose GCN model that simplifies the approximation further. GCNs limit the order Chebyshev polynomial to one and assume the coefficients in polynomial are equal. Besides, GCNs consider the self-loops in the graph and intrduce the renormalization trick, which improves the quality of learned graph embeddings. So far, GCNs have achieved the great performance on different graph related tasks.

Based on these works, we make the following contributions in the project.

(1) We propose a novel method to learn graph embeddings, inspired by meta learning concept. Our method fully utilizes the information from node2vec and the power of GCN architecture. We test our model on node classification and link prediction task. (2) We evaluate node2vec, GCN, and our proposed method on five real-word data sets. In node classification task, we use additional metrics to assess the model performance, i.e. accuracy, recall, and weighted f1-score, while the original paper of node2vec only reports macro f1-score.

3 PRELIMINARIES

3.1 Feature Learning Framework

Feature learning in networks is regarded as a a maximum likelihood optimization problem[4]. We represent the given network as G = (V, E), where V and E are nodes set and edges set respectively. Feature Learning task aims to find a projection $f: V \to \mathbb{R}^d$, such that f optimizes the following objective function:

$$\max_{f} \sum_{u \in V} \log Pr(N_{s}(u)|f(u))$$

Projection f allocates each node an embedding vector with length d. In other words, projection f can be formulated as a matrix of size $|V| \times d$. $N_s(u) \subset V$ defines network neighborhood for a node u with neighborhood sampling strategy S. Please be aware, this network neighborhood is not equivalent to the commonly used concept local neighborhood which only is determined by the graph structure. On the contrary, network neighborhood is generated based on both network structure and sampling strategy. Therefore, the above formula aims to maximize the log-probability of observing a network neighborhood $N_s(u)$ for a node u conditioned on its feature embedding representation, given by projection f.

To simplify the above optimization formula and task, two standard assumptions are made. One is conditional independence, which means observing a neighborhood node is independent of observing any other neighborhood node. Then according to the property of independent event, the formula in the objective function above can be written in the form of multiplication:

$$Pr(N_s(u)|f(u)) = \prod_{n_i \in N_s(u)}^{N} Pr(n_i|f(u))$$

The other is symmetry in feature space, which means each source node and its neighborhood node have a symmetric effect over each other in feature space. In the reference [4], the conditional likelihood of each (source node, neighbor node) pair in the network neighborhood is formulated as a softmax function:

$$Pr(n_i|f(u)) = \frac{exp(f(n_i) \cdot f(u))}{\sum_{v \in V} exp(f(v) \cdot f(u))}$$

Finally, the objective function can be rewritten using the above two assumptions in the form of:

$$\max_{f} \sum_{u \in V} [-log \sum_{u \in V} exp(f(u) \cdot f(v)) + \sum_{n_i \in N_s(u)} f(n_i) \cdot f(u)]$$

The first half of this formula $-log \sum_{u \in V} exp(f(u) \cdot f(v))$ is very expensive in computing. Therefore, a negative sampling method is applied to calculate it approximately [7]. For this objective function, stochastic gradient decent is applied to optimize it and obtain the projection f.

With a good designed network neighborhood sampling strategy S, the above optimization process could help to find projection f which makes the nodes embedding equipped with homophily

and structural equivalence information [5], which could be taken advantage of in the downstream task.

The sampling strategy *S* is the most important part of feature learning framework. In this paper, second order random walk, the key point of *Node2Vec*, is applied as the sampling strategy. Before we dive into the details of *Node2Vec* and second order random walk in section 4.1, let us have a glance to two commonly used downstream tasks, nodes classification and link prediction, which can be used to measure the performance of the nodes embedding generated by *Node2Vec*.

3.2 Downstream Task

Nodes embedding is widely used in many common tasks of networks, such as nodes classification and link prediction. These tasks, which take advantage of information from nodes embedding, are called downstream tasks. Therefore, the best way to examine whether the nodes embedding generated by Feature Learning Framework, such as *Node2Vec*, is to check the performance of nodes embedding on such downstream task.

In this paper, two downstream tasks are used.

Nodes Classification. Given a graph G = (E, V) with category labels of part of nodes, nodes classification task aims to classify the rest of nodes without labels into their category correctly.

Link prediction. Given a subgraph G' = (V', E) of the entire graph G = (V, E), where $V' \subset V$ and the rest of edges are missing. Link prediction task aims to predict these missing edges correctly.

Nodes classification and link prediction are two basic but very important tasks in network analysis area. Therefore, it's of much importance to examine *Node2Vec* whether works well in these two tasks.

The downstream tasks also need a model, such as a classifier like Logistic Regression Classifier or Graph Neural Network. Determining which downstream model is better is not our focus in this paper. In this paper, we mainly care about whether the nodes embedding generated from *Node2Vec* can make downstream model work better. Therefore, in experiments section, we will experimentally show the performance improvement gained by applying GCN with nodes embedding from *node2vec* comparing to GCN without nodes embedding.

4 APPROACH

4.1 Node2vec

In section 3.1, we discussed feature learning framework. And node2vec is such a feature learning model with special designed sampling strategy *S*. There are two classic search algorithms, BFS and DFS, can be naively used as network neighborhood sampling strategy *S*. However, according to the reference [4], directly applying BFS as network neighborhood sampling strategy leads the nodes embedding to fully learn structural equivalence of networks. On the contrary, directly applying DFS as network neighborhood sampling strategy leads the nodes embedding to fully learn homophily of networks. Since structural equivalence and homophily are both important similarities for nodes [7], it's definitely not a good way to throw away one of them. Therefore, we should use a method

to combine the features of BFS and DFS, and make the sampling strategy capture these two similarities at the same time.

Inspired by random walk, the reference [4] comes up a second order bias random walk method, which combines the features from both BFS and DFS, as the network neighborhood sampling strategy of node2vec.

The basic random walk procedure with length l is formulated as following [4]. Given a source node u and let Let c_i denote the i-th node in the walk, starting with $c_0 = u$. Nodes c_i are generated by the following distribution:

$$p(c_i = x | c_{i-1} = v) = \begin{cases} \frac{\pi_{vx}}{Z} & if (v, x) \in E \\ 0 & otherwise \end{cases}$$

where π_{vx} is the unnormalized transition probability between nodes v and x, and Z is the normalizing constant. In weighted graph, π_{vx} is usually set to the edge weight between node v and x, namely w_{vx} . In unweighted graph, $w_{vx} = 1$, that's to say, the next nodes to walk is generated with equal possibility in the local neighborhood. However, the basic random walk is still not enough to capture both structural equivalence and homophily similarities.

Therefore, a second order bias random walk method is proposed by the reference [4]. Consider a baisc random walk process just traversed edge (t,v) and now resides at node v. Now the walk process wants to decide the nodes to visit in the next step. So the unnormalized transition probability $\pi_{v,x}$ on edge (v,x) will be calculated. Particularly, the unnormalized transition probability is set as $\pi_{v,x} = \alpha_{pq}(t,x) \cdot w_{vx}$, where

$$\alpha_{pq}(t,x) = \begin{cases} \frac{1}{p} & \text{if } d_{tx} = 0\\ 1 & \text{if } d_{tx} = 1\\ \frac{1}{q} & \text{if } d_{tx} = 2 \end{cases}$$

p and q are two key hyperparameters introduced in this method, and d_{tx} represents the smallest distance between node t and node x. Notice that for each two step, d_{tx} can only be three possible values: 0, 1 and 2. When $d_{tx} = 0$, it means the possible next step node xwill lead the process to walk back to node t again. When $d_{tx} = 1$, it means the possible next step node x will lead the process to walk to the nodes which are the other direct local neighbor of node t. When $d_{tx} = 2$, it means the possible next step node x will lead the process to walk to the new node and get rid of node t's ego network. Hyperparameters p and q are called return parameter and in-out parameter. p controls the possibility for the walk immediately step back to the previous node, and q controls the possibility for the walk to go out of the previous node's ego network. That's easy to find, when applying small p and large q, the walk process will prefer staying in the previous node's ego network, which means the walk process is more similar to BFS. On the contrary, when applying large p and small q, the walk process will prefer stepping out of the previous node's ego network, which means the walk process is more similar to DFS. Therefore, by well tuning p and q, we can obtain a method that can take advantage of the features from both DFS and BFS, and then can capture both structural equivalence and homophily similarities.

Up to now, the second order bias random walk has been formulated. Them, we should apply it in the features learning framework as the network neighborhood sampling strategy. In each walk from source node u with length L, we will obtain L network neighborhood nodes of u. And use that network neighborhood in the features learning framework to do obtain the optimized projection f. Then node2vec will output embedding vectors for each nodes in the graph.

Then the nodes embedding vectors can be used in the downstream tasks. When using nodes embedding in nodes-related tasks, such as nodes classification, nodes embedding can be directly applied in the downstream model. For example, in reference [4], the authors use one-vs-rest logistic regression classifier, using these nodes embedding vectors as input.

However, in edges-related tasks, such as link prediction, we need to use edges' features rather than nodes' features. Therefore, we should apply an operation to transform the nodes embedding vectors obtained by *node2vec* into edges' features.

remaining to be finished......

5 DATA

We evaluate node2vec, GCN, and our proposed model on five open source data sets. Three data sets, i.e. AIFB, MUTAG, and PubMed, are used in node classification task. Meanwhile, the goal of FB15K-237 and WordNet18RR data is link prediction. We apply built-in preprocessing APIs in Pytorch Geometric to convert the raw data into the desired format. The following is an overview of data sets.

AIFB. AIFB is a directed network modelling relationships among staff, research groups, and publications in AIFB research institute. The data set is firstly published for mining knowledge about instances with machine learning [1]. AFIB network has 8,285 nodes, 58,086 edges, and 4 node classes. The original data can be downloaded from https://data.dgl.ai/dataset/aifb.tgz.

MUTAG. MUTAG is a benchmark dataset for node classification task. It contains a collection of chemical compounds. We use the version provided by Deep Graph Library. It is a directed network with 23,644 nodes, 148,454 edges, and 2 node classes. The download link is https://data.dgl.ai/dataset/mutag.tgz.

PubMed. PubMed is a directed citation network in biomedical field provided by paper [11]. In the network, nodes represent documents, while edges denote citation links. It contains 19,717 nodes, 88,648 edges, and 3 node classes. The original data is on https://github.com/kimiyoung/planetoid/tree/master/data.

FB15K-237. FB15K-237 contains knowledge relationships sourced from the Freebase database. It is a modified version of FB15K dataset. FB15K-237 network is directed, including 14,541 nodes and 544,230 edges. The link of the original data is https://github.com/MichSchli/RelationPrediction/tree/master/data/FB-Toutanova.

WordNet18RR. WordNet18RR is an improved version of WordNet18 dataset, which is a large lexical database of English. The network is directed. It contains 40,943 nodes and 93,003 edges. The original data can be found on https://github.com/villmow/datasets_knowledge_embedding/tree/master/WN18RR/original.

Table 1 summarizes the data sets used in our experiments.

Table 1: Summary of Data Sets

Data	Nodes	Edges	Classes
AIFB	8,285	58,086	4
MUTAG	23,644	148,454	2
PubMed	19,717	88,648	3
FB15K-237	14,541	544,230	-
WordNet18RR	40,943	93,003	-

6 EXPERIMENTS

7 CONCLUSION

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