Untitled

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#The standard error of the mean (SEM): described as the

[]: #question 1

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#"standard deviation of the distribution of bootstrapped means,
     #" captures the variability of the sample mean when repeatedly drawing samples.
     #It reflects how much the sample mean would fluctuate if you repeatedly
     #resampled and calculated new means, indicating the precision of the sample_
      →mean as an estimate of the true population mean.
     #the standard deviation (SD) of the original data measures
     #the spread of individual data points around the mean, reflecting
     #the variability within the dataset itself. It shows how much
     #the values differ from the average.
[ ]: | #question 2
     #1. Start with the sample mean: Calculate the mean of your sample data.
     #2. Use the SEM: Multiply the SEM by 1.96 (the approximate z-value for 95%)
     ⇔confidence under a normal distribution).
     #3. Calculate the interval:
     #Lower bound = Sample Mean - (1.96 × SEM)
     #Upper bound = Sample Mean + (1.96 × SEM)
[ ]: | #question 3
     import numpy as np
     # Assuming original dataset
     data = np.array([...])
     # Number of bootstrap samples
     B = 1000
     # Initialize an array to store bootstrapped means
     bootstrapped_means = np.zeros(B)
     # Generate bootstrapped samples and calculate means
     for i in range(B):
         sample = np.random.choice(data, size=len(data), replace=True)
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bootstrapped_means[i] = np.mean(sample)
# Calculate the 95% confidence interval (2.5th and 97.5th quantiles)
ci_lower = np.quantile(bootstrapped_means, 0.025)
ci_upper = np.quantile(bootstrapped_means, 0.975)
print(f"95% Confidence Interval: ({ci_lower}, {ci_upper})")
#explaination
#To calculate a 95% confidence interval (CI) for the mean using bootstrapping,
#you repeatedly sample from your dataset with replacement to create many
#new datasets (bootstrap samples). For each sample, you calculate the
#mean, then store all the means in an array. To find the 95% CI,
#you use `np.quantile()` to get the 2.5th and 97.5th percentiles
#of the bootstrapped means. These percentiles give the lower and
#upper bounds of the CI, meaning that 95% of the time, the true
#mean will lie within this range in repeated samples.
#Using np.quantile() to calculate the 2.5th and 97.5th percentiles
#of bootstrapped means gives us a 95% confidence interval,
#making it a robust method for non-parametric confidence
#interval estimation.
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[1]: #question 4
     # step 1: collect data
     import plotly.express as px
     import plotly.graph_objects as go
     import pandas as pd
     import numpy as np
     df = pd.read csv("https://raw.githubusercontent.com/rfordatascience/tidytuesday/
      42e9bd5a67e09b14d01f616b00f7f7e0931515d24/data/2020/2020-07-07/coffee ratings.
     ⇔csv")
     df = df.rename(columns={'country_of_origin': 'origin', 'total_cup_points':__
      df = df[df['points']>65] # ignore some very low scores
     df = df[~df['origin'].isna()] # remove rows with unknown origin
     df['origin'] = df['origin'].str.replace("?","'") # fix character encoding issue
     df['origin_original'] = df.origin.copy().values # save original (corrected)
      \hookrightarrownames
     df.shape
```

[1]: (1335, 44)

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[5]: # step2: loop
    N = 1000
     boot_median = np.zeros(N)
     for i in range(N):
         boot_sample = np.random.choice(df['points'], size=len(df['points']),__
      →replace=True)
         boot_median[i] = np.median(boot_sample)
[7]: #step3: draw histagram
     import plotly.express as px
     import pandas as pd
     # Assuming boot median has been calculated correctly
     fig = px.histogram(pd.DataFrame({"x": boot_median}), x="x")
     fig.show()
[8]: #stepcalculate
     # Calculate the 2.5th and 97.5th percentiles
     quantiles = np.quantile(boot_median, [0.025, 0.975])
     # Extract lower and upper bounds from the result
     ci_lower, ci_upper = quantiles
     print(f"95% Confidence Interval: ({ci_lower}, {ci_upper})")
    95% Confidence Interval: (82.42, 82.67)
[]: # question 5
     #Distinguishing between the population parameter and the sample
     #statistic is essential because the population parameter represents
     #the true value we want to estimate, while the sample statistic is
     #derived from our sample data. Confidence intervals provide a
     #range of plausible values for the population parameter based
     #on the sample statistic, reflecting the uncertainty due to
     #sampling variability. This distinction helps us understand
     #the reliability of our estimates and the potential error in
     #inferring population characteristics from a sample.
[]:  # question 6
     # question: What is the process of bootstrapping?
```

#of the statistic. # question: What is the main purpose of bootstrapping? #The main purpose of bootstrapping is to assess the reliability #of your estimates, like averages or medians. It helps you create #confidence intervals, showing a range of values where the true #population parameter might lie. #question: How could you use bootstrapping to assess whether your quess about, → the average is plausible? #If you have a quess about the average (like 10), #you can take a sample from your data and use bootstrapping #to generate many averages. If most of these averages are close #to your guess, it suggests your guess is plausible; if not, #it may need reconsideration. []: #question 7 #When a confidence interval (CI) includes zero, it means there is #a plausible range of values for the effect, including no effect #(zero). This suggests that the observed data is consistent with #the possibility that the drug has no effect on average. As a result, #we "fail to reject the null hypothesis," which assumes no effect. #To reject the null hypothesis, the CI must not include zero. #This would indicate that the observed sample mean is significantly #different from zero, suggesting that the drug likely has an effect.

[14]: # question 8 #problem introduction: #An explaination of the meaning of a Null Hypothesis of "no effect" in thisuscontext # null hypotheses: there is no different, no relationship, or impact in theuscontext being studied # alternative hypothesis: there is different, relationship or impact in theuscontext being studied #Data Visualization # we can ilustrate the comparison of initial and final heath scores, a box plotusor bar graph can be used. import pandas as pd # Define the data as a list of dictionaries data = { "PatientID": [1, 2, 3, 4, 5, 6, 7, 8, 9, 10],

```
"Age": [45, 34, 29, 52, 37, 41, 33, 48, 26, 39],

"Gender": ['M', 'F', 'M', 'F', 'M', 'F', 'M', 'F'],

"InitialHealthScore": [84, 78, 83, 81, 81, 80, 79, 85, 76, 83],

"FinalHealthScore": [86, 86, 80, 86, 84, 86, 82, 83, 84]

# Create the DataFrame

df = pd.DataFrame(data)

# Display the DataFrame

df ["d"] = df.FinalHealthScore - df.InitialHealthScore

print(df)
```

```
PatientID Age Gender InitialHealthScore FinalHealthScore d
0
              45
                                                        86 2
          1
                     Μ
                                       84
1
          2
             34
                     F
                                       78
                                                        86 8
2
          3 29
                     M
                                       83
                                                        80 -3
          4 52
                     F
3
                                       81
                                                        86 5
4
          5 37
                                                        84 3
                     Μ
                                       81
          6 41
5
                     F
                                       80
                                                        86 6
          7
6
              33
                                       79
                                                        86 7
                     Μ
7
          8 48
                     F
                                       85
                                                        82 -3
8
          9
              26
                                       76
                                                        83 7
                     Μ
9
         10
              39
                     F
                                       83
                                                        84 1
```

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[3]: import numpy as np
     import pandas as pd
     import plotly.express as px
     # Re-create the DataFrame for completeness
     data = {
         "PatientID": [1, 2, 3, 4, 5, 6, 7, 8, 9, 10],
         "Age": [45, 34, 29, 52, 37, 41, 33, 48, 26, 39],
         "Gender": ['M', 'F', 'M', 'F', 'M', 'F', 'M', 'F', 'M', 'F'],
         "InitialHealthScore": [84, 78, 83, 81, 81, 80, 79, 85, 76, 83],
         "FinalHealthScore": [86, 86, 80, 86, 84, 86, 86, 82, 83, 84]
     }
     df = pd.DataFrame(data)
     df["d"] = df["FinalHealthScore"] - df["InitialHealthScore"]
     # Bootstrapping
     N = 1000
     boot_mean = np.zeros(N)
     for i in range(N):
```

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boot_sample = np.random.choice(df["d"], size=len(df), replace=True)
 →Corrected here
   boot_mean[i] = np.mean(boot_sample)
# Calculate confidence intervals
ci lower = np.percentile(boot mean, 2.5)
ci_upper = np.percentile(boot_mean, 97.5)
# Creating histogram
fig = px.histogram(pd.DataFrame({"x": boot_mean}), x="x", title="Bootstrapped_

→Mean Differences")
fig.show()
# Print confidence intervals
print(f"95% Confidence Interval for the Mean Difference: [{ci_lower:.2f},__

⟨ci_upper:.2f⟩]")
# Step 4: Supporting Visualization - Histogram of bootstrapped means
fig = px.histogram(pd.DataFrame({"Mean Difference": boot_mean}),
                   x="Mean Difference",
                   title="Bootstrapped Mean Differences",
                   labels={'Mean Difference': 'Mean Difference in Health_

Scores'

fig.add_vline(x=ci_lower, line_color='red', line_dash='dash',__
 →annotation_text='Lower CI', annotation_position="bottom right")
fig.add_vline(x=ci_upper, line_color='green', line_dash='dash',
 →annotation_text='Upper CI', annotation_position="top right")
fig.show()
```

95% Confidence Interval for the Mean Difference: [0.90, 5.60]

```
# discussion
# The confidence interval does include zero,
#we fail to reject the null hypothesis, which indicating
#that the vaccine not have a significant effect on health outcomes.

#Further Considerations
#Sample Size: Future studies should aim for larger samples for more
#reliable results.
#Longitudinal Studies: Assessing long-term effects could provide
#deeper insights.
#Additional Variables: Investigating other factors
#(e.g., comorbidities) may help understand the vaccine's impact better.
```

[]: #chatbox: https://chatgpt.com/share/66ff1b1d-5974-8002-9e50-347bbe4a25ed