

Derivatives

Contents

1	Useful Derivatives	1
2	Differentiation of Vector/Matrix	1
3	Differentiation of natural log	1

1 Useful Derivatives

From "Another Walkthrough of Variational Bayes".

$$\begin{aligned}\frac{d}{dx}x &= 1 \\ \frac{d}{dx}\log(x) &= \frac{1}{x} \\ \frac{\partial}{\partial q} \int q(x)dx &= 1 \\ \frac{\partial}{\partial q} \int \log q(x)dx &= \frac{1}{q(x)}\end{aligned}$$

2 Differentiation of Vector/Matrix

2.1 PRML Math Book p.77

$$\frac{\partial}{\partial \mu} \left(-\frac{1}{2}(x - \mu)^T \Sigma^{-1}(x - \mu) \right) = \Sigma^{-1}(x - \mu)$$

3 Differentiation of natural log

$$(e^{kx})' = (kx)' e^{kx}$$

Use the chain rule of differentiation (合成関数の微分)