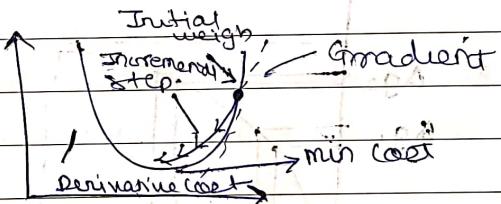


Machine Learning

① Gradient Descent.

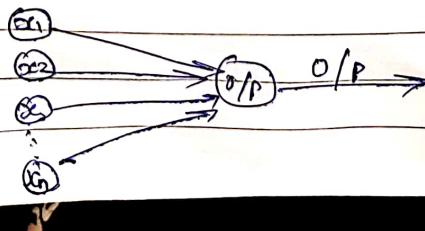
- - One of the most commonly used iterative optimization algorithms of ML to train ML & DL models.
- helps in finding the local minimum of a function.
- If we move towards a negative gradient or away from the gradient at current point it will give the local minimum.
- If we move towards a positive gradient or toward the gradient from at current point it will give the local maximum.



- Objective of Gradient descent is to minimize the cost function using iterations.

② Hebbian Learning Rule.

- - Hebbian network is a single layer neural network which consist of one input layer with many input units & one output layer with one output unit.
- Architecture used for pattern classification.
- Works by updating the weights between neurons for each training sample.



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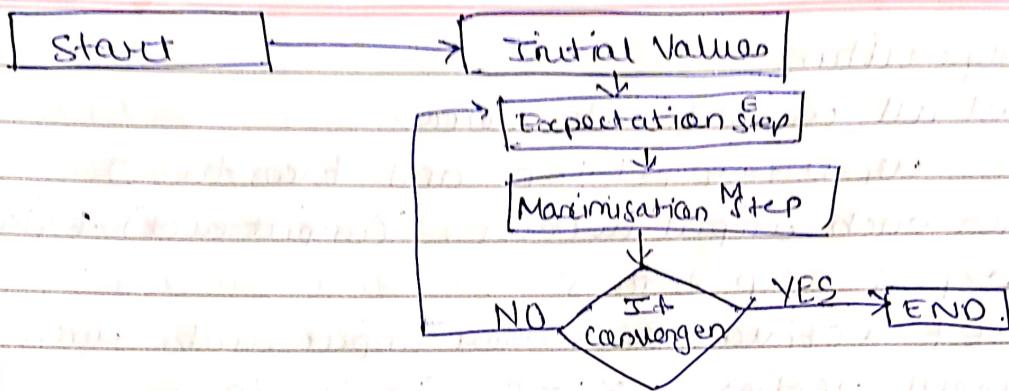
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Algorithm:

- (1) Set all weights to zero.
 $w_i = 0$ for $i=1$ to n and bias to 0
- (2) For each input vector, S (input vect) + Target of next repeat step 3 to 5.
- (3) set activations for input units with the input vector $x_i = s_i$ for $i=1$ to n
- (4) set the corresponding o/p value to o/p neurons
 $y = \text{activation}$
- (5) Apply weights by & bias by applying Hebb rule for $i=1$ to n :
 $w_{i(\text{new})} = w_{i(\text{old})} + s_i y$
 $b_{(\text{new})} = b_{(\text{old})} + y$

⑭ Expectation - Maximization Algorithm:

- Performs maximum likelihood expectation
 - Used to find the latent variables whose value is derived from other variables
 - Basic for many unsupervised clustering algorithms.
- Steps in EM algorithm:
1. Initially a set of initial values are considered
- A set of incomplete data is given to system.
 2. Next - Step - Expectation step - E-step
Here, we use observed data to estimate or guess the values of missing/incomplete data.
 3. Maximisation step / M-step
Here, we use the complete data generated in preceding e-step to update the values.
 4. We check if values are converging or not
If converging - stop
Otherwise repeat step 2 and 3 till convergence occurs.



* Purpose of EM:

- In ML P.S., we obtain many relevant feature to build model, but only few are observable (Non-observable features are latent features)

* Applications of EM:

- Use to calculate Gaussian density function
- Helps in filling the missing data of sample
- Used in NLP, CV
- Image reconstruction in medical & structural engineering
- Used to estimate parameters of mixed model

* Advantages:

- Guaranteed that likelihood will increase in each iter
- The E-step & M-step are easy to implement
- Solution to the M-steps exist in closed form

* Disadvantages:

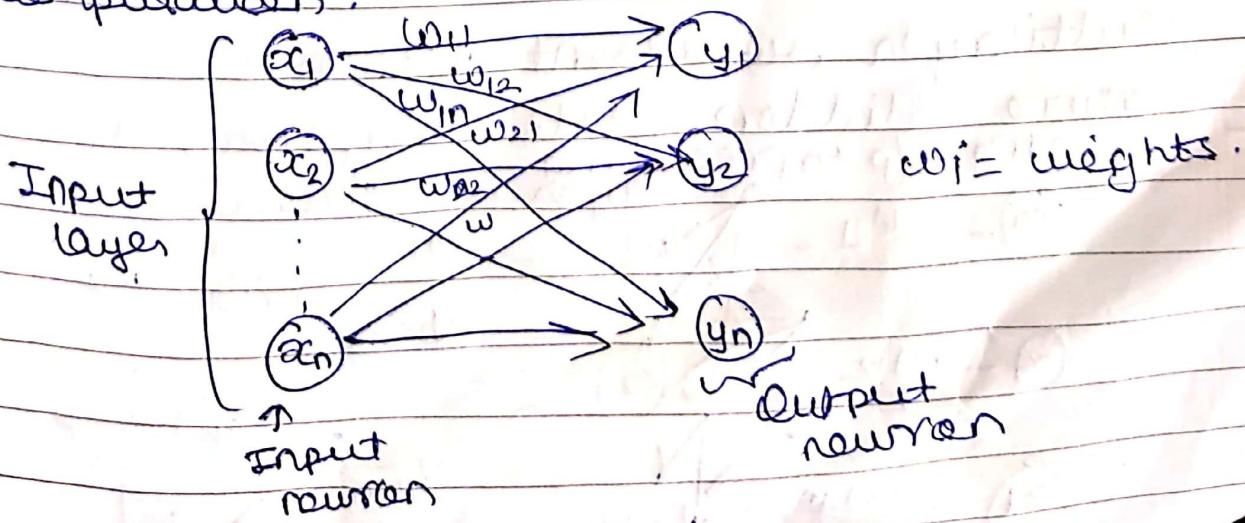
- Slow convergence
- Makes convergence to local optimal only.
- Requires both the probabilities, forward & backward.

⑥ (21) Different types of neural network. Comparison b/w BNN & ANN.

	ANN	BNN
Processing	Sequential & centralised	Parallel & distributed
Rate	Process info in faster pace	Slow in processing information
Size	Small	Large
Complexity	Incapable to perform pattern recog.	Enormous size & complexity of connections
Fault tolerance	Intolerance to failure	Implicitly fault tolerant
Control unit	Central unit monitors computer activities	All the processing is centrally controlled
Feedback	Not provided	Provided

11. ⑥ Different types of neural networks.

- Five basic types of neural network archi ~
- 1. Single layer feed-forward network:
- Two layers: Input layers receives input signals
Output layers receive output signal
- Synaptic links carrying weights connect i/p_1 to o/p_n but not conversely.
- Called as single layer as output layer performs computation.



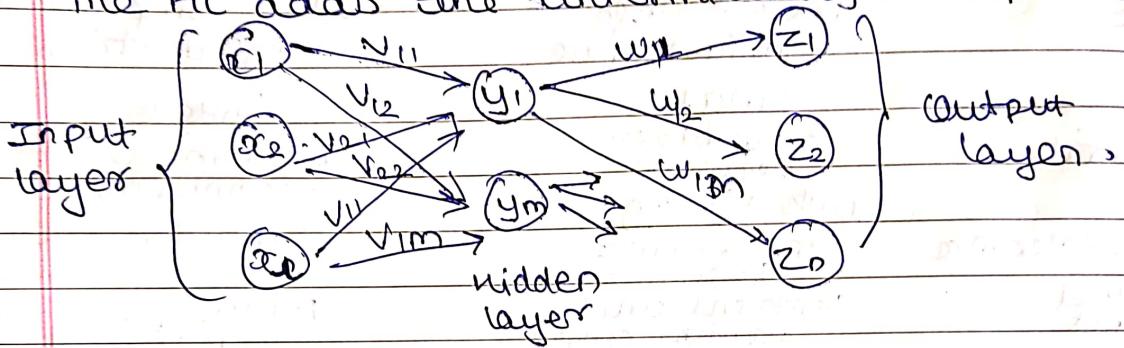
2. Multilayer feedforward.

- Made up of multiple layers.

- Intermediary layers beside i/o & o/p
Called as hidden layer.

- Computational units of h.l are called neurons

- The HL adds the intermediary computation.

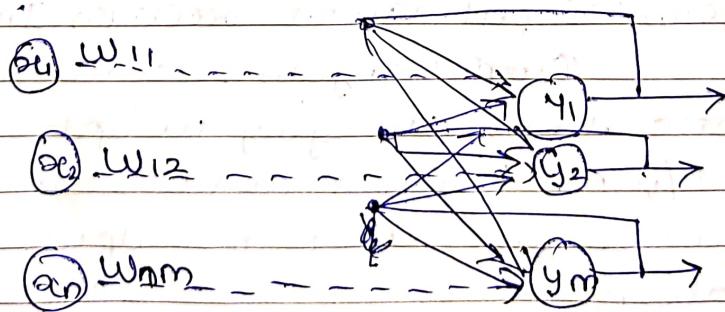


3. Single node with its own feedback.

- Output directs back as input to the same layer or preceding layer, results in feedback network.

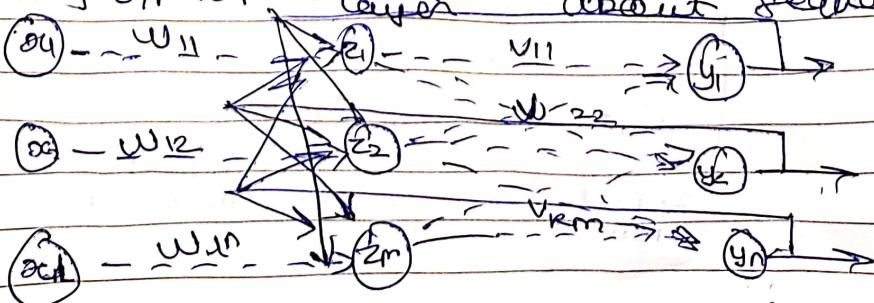
4. Single layer recurrent network.

- Recurrent network \rightarrow feedback net with closed loop.



5. Multilayer recurrent network.

- Feature: Hidden state \rightarrow captures information about sequence



(7) Diff b/w single layer feed forward & multilayer feed forward

Single layer FF

- Formation of layer is done by processing & combining elements
- link b/w i/p & o/p
- Not efficient

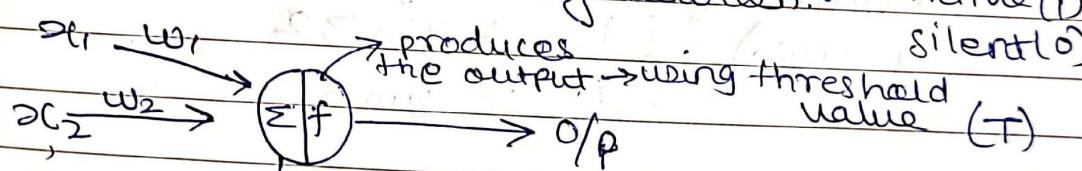
Multilayer FF

- Interconnectors of several layers

- take middle layers hidden layers
- Efficient as complexity from HL

(8) McCulloch Pitts model

- First mathematical model of a biological neuron
- Basic building block of neural network
- Directed weight graph is used for connecting
- Two possible states of neuron. \rightarrow Active (1) silent (0)



Aggregates the weighted input into single value

$$\sum x_i w_i + x_2 w_2 + x_n w_n] X$$

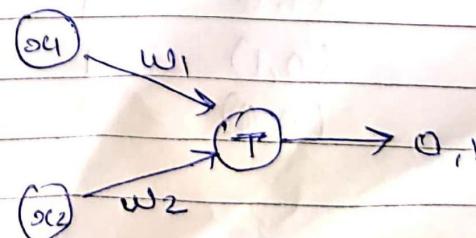
$$O/P = \begin{cases} 1 & \text{if } X > T \\ 0 & \text{if } X \leq T \end{cases}$$

Bias / threshold: Minimum value of weighted active i/p for a neuron to fire if effective i/p is larger than T.
 - then o/p \rightarrow 1 else 0

GATES:

OR Gate:

x_1	x_2	y
0	0	0
0	1	1
1	0	1
1	1	1



$$w_1 = +1, w_2 = +1$$

$$(0,0) \Rightarrow \sum x_i w_i = 0$$

$$(0,1) \Rightarrow \sum x_i w_i = +1$$

$$(1,0) \Rightarrow \sum x_i w_i = +1$$

$$(1,1) \Rightarrow \sum x_i w_i = +2$$

Assume threshold as +1 ($T=1$)

\therefore Output of neuron y will be

$$y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} \geq 1 \\ 0 & \text{if } y_{in} < 1 \end{cases}$$

AND GATE:

$$(w_1 = 1) \quad (w_2 = 1)$$

$$(1, 1) \Rightarrow \sum \alpha_i w_i = 2$$

$$(1, 0) \Rightarrow \sum \alpha_i w_i = 1$$

$$(0, 1) \Rightarrow \sum \alpha_i w_i = 0$$

$$(0, 0) \Rightarrow \sum \alpha_i w_i = 0$$

Assume threshold val +2 i.e. $T=2$

Output of neuron y will be

$$y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} \geq 2 \\ 0 & \text{if } y_{in} < 2 \end{cases}$$

*

BIG:

$$\sum \alpha_i w_i \leq y_{out}$$

$$\begin{array}{c|cc} & \alpha_1 & \alpha_2 \\ \hline 1 & 1 & 0 \\ 1 & 0 & 1 \end{array}$$

$$\begin{array}{ccc} 0 & \text{and} & 1 \\ 0 & & 0 \end{array}$$

$$w_1 = 1; w_2 = -1$$

$$(1, 1) = 0$$

$$(1, 0) = 1$$

$$(0, 1) = -1$$

$$(0, 0) = 0$$

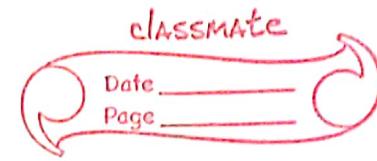
$$\text{Threshold } T = 2$$

$$\cancel{\begin{array}{c} 0 \\ 1 \end{array}} \leq 2 \leq 3 = 0$$

$$\text{Threshold} = 1$$

$$\text{when } w_1 = 1, w_2 = -1$$

-4
-2
-2
0



1
0
1
-1
0

NAND:

~~or~~ y, x_1 , x_2 , y

1 1 0

1 0 1

$w_1 = -2$ $w_2 = -2$

0 1 1

~~1~~
~~0~~
~~1~~
~~1~~

$T = -3$

0 0 1

~~T~~

$T=2$

NOR:

x_1 , x_2 , y

1 1 0

$w_1 = -1$ $w_2 = -1$

1 0 0

$T = -1$

0 1 0

0 0 1