

Module No : 01

Number system

Number system:-

* A Number system is method to represent the numbers *

* The number system is used for representing a quantity or information in digital electronics.

Digit :- In any number system, every symbol in the numbers is called a digit.

MSD (Most significant Digit) :-

The Leftmost digit of the number has the greatest positional weight among the remaining digit in number. It is called as Most significant digit in number. It is called as Most Significant Digit (MSD)

LSD [Least Significant Digit] :-

The rightmost digit of the number has the least positional weight among the digit in numbers. It is called as Least significance Digit (LSD).

$$\begin{array}{r}
 \text{MLSB} \\
 \frac{+}{+} \quad 2 \quad 8 \quad . \quad 1 \quad 4 \\
 \frac{1}{1} \times 10^2 \quad \frac{1}{2} \times 10^1 \quad \frac{1}{8} \times 10^0 \quad \frac{1}{1} \times 10^{-1} \quad \frac{1}{4} \times 10^{-2}
 \end{array}$$

Base / Radix :-

The base or radix (b) of the number system is the total number of digit used in that number system.

example:- Binary system $\rightarrow (0, 1)$

Base / Radix = 2

Types of number system:-

1) Binary number system

The number system with Base / Radix is 2, then it is called as binary number system.

A number system where a number system

Types of Number system

Binary :- (0, 1) [Base = 2]

Octal (0, 1, 2, 3, 4, 5, 6, 7) [Base = 8]

Decimal (0, 1, 2, 3, 4, 5, 6, 7, 8, 9) [Base = 10]

Hexa (0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F) [Base = 16]

→ Decimal

$$\begin{array}{r} & 2 \leftarrow \text{Quotient} \\ \text{Base } \rightarrow 2) & 4 \\ & -4 \\ & 0 \leftarrow \text{remainder} \end{array}$$

(Noted that)

Noted that

Base	Quotient	Remainder
2	199	
2	99 → 1	
2	49 → 1	
2	24 → 1	
2	12 → 0	
2	6 → 0	
2	3 → 0	
2	1 → 1	

* Take calculator

* Divided that number $2 \div 13 = 0.\overline{15}$

* multiply that number $0.\overline{15} \times 2 = 1.0 \rightarrow ①$

2	13	↓ 0
2	(06)	↓ 01

④

* fractional part में 4 बारा multiplication
करना चाहते हैं।

Universal college of
Rutile Bodice
div-A

Conversion :-

A) Decimal to Binary

$$① (8)_{10} \rightarrow (?)_2$$

2	8	
2	4 → 0	↑ LSB
2	2 → 0	
2	1 → 0	
	0 → 1	MSB

$$② (19.32)_{10} \rightarrow (?)_2$$

2	19	↓ 1	↑ LSB
2	9 → 1		
2	4 → 0		
2	2 → 0		
2	1 → 0		
	0 → 1	MSB	

$$③ 0.35 \times 2$$

$$= 0.70 \rightarrow 0$$

$$④ 0.70 \times 2$$

$$= 1.40 \rightarrow 1$$

$$⑤ 0.40 \times 2$$

$$= 0.80 \rightarrow 0$$

$$⑥ 0.80 \times 2$$

$$= 1.60 \rightarrow 1$$

Note that :-
In fractional part, you
can calculate only
4x times

b) Decimal to octal conversion:-

$$0.1 \rightarrow (151.33)_{10} \rightarrow (?)_8$$

Ans:-

8 151
8 18 → 7 LSB
8 2 → 2 ↑
8 0 → 2 ↑
0 → 2 MSB

$$0.33 \times 8 = 2.64 \rightarrow 2 \text{ MSB}$$

$$0.64 \times 8 = 5.12 \rightarrow 5$$

$$0.12 \times 8 = 0.96 \rightarrow 0$$

$$0.96 \times 8 = 7.68 \rightarrow 7 \text{ LSB}$$

$$\boxed{\text{ANS: } (27.2507)_8}$$

c) Decimal to Hexadecimal conversion

$$(151.33)_{10} \rightarrow (?)_{16}$$

16 151	LSB
16 9	→ 7 ↑
0	→ 8 MSB

$$0.33 \times 16 = 5.28 \rightarrow 5 \text{ MSB}$$

$$0.28 \times 16 = 4.48 \rightarrow 4$$

$$0.48 \times 16 = 7.68 \rightarrow 7$$

$$0.68 \times 16 = 10.88 \rightarrow 10 \text{ A} \text{ LSB}$$

$$0.88 \times 16 = 14.08 \rightarrow 14$$

ANS:-

$$(151.33)_{10} \rightarrow (97.547E)_{16}$$

$$(151.33)_{10} \rightarrow (97.547AAE)_{16}$$

2

a) Binary to Decimal conversion

$$\begin{aligned}
 & \text{Given: } (1001.0101)_2 \rightarrow (?)_{10} \\
 & n=4 \\
 & n=3 \\
 & = 1 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 + 0 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3} \\
 & \quad + 1 \times 2^{-4} \\
 & = 8 + 0 + 0 + 1 + 0 + \frac{1}{2^2} + 0 \frac{1}{2^4} \\
 & = (8.3125)_{10}
 \end{aligned}$$

ANS:- $(1001.0101) \rightarrow (8.3125)_{10}$

b) Binary to octal conversion

For 3 bit	For 4 bit
4 2 1	8 4 2 1

$$\begin{array}{r}
 ① (010\ 110\ 010\ 101)_2 \\
 \downarrow \downarrow \downarrow \downarrow \\
 (2\ 6\ 2\ 5)_8
 \end{array}$$

Ans:- $(010\ 110\ 010\ 101)_2 \rightarrow (2625)_8$

a) Binary to Hexadecimal conversion

$$\begin{array}{r}
 ② (1101\ 1011\ 0101)_2 \rightarrow (DB5)_{16} \\
 \downarrow \downarrow \downarrow \\
 13\ 14\ 5 \\
 D\ B
 \end{array}$$

b) Octal to Binary conversion

$$\begin{array}{r}
 ③ (726)_8 \rightarrow (11010110)_2 \\
 \downarrow \downarrow \downarrow \\
 111\ 010\ 110
 \end{array}$$

b) Octal to Decimal conversion

$$\begin{array}{r}
 ④ (254)_8 \rightarrow (?)_{10} \\
 n=3 \\
 (n-1)=2 \\
 = (2 \times 8^2) + (5 \times 8^1) + (4 \times 8^0)
 \end{array}$$

c) Octal to Hexadecimal conversion

$$\begin{array}{r}
 ⑤ (670.17)_8 \rightarrow (?)_{10} \\
 \text{make 3 group} \\
 \text{make 4 group} \\
 1\ 3\ 8\ :\ 3\ C \\
 \text{Ans: } (670.17)_8 \rightarrow (188.3)_{16}
 \end{array}$$

Hexadecimal to Binary

$$\textcircled{1} \quad (3A9D)_{16} \rightarrow (?)_2$$

↓ ↓ ↓ ↓
 0011 1010 1001 1101

Ans: - $3A9D \rightarrow 0011\ 1010\ 1001\ 1101$

Hexadecimal to Octal

$$\textcircled{1} \quad (B\ C\ 2.4C)_{16} \rightarrow (?)_8$$

↓ ↓ ↓ ↓
 1011 1100 0010 0100
 5 7 0 2 . 3 0

Ans: - $(B\ C\ 2.4C)_{16} \rightarrow (5702.230)_8$

\textcircled{3} Hexadecimal to Decimal

$$(4C8.2)_{16} \rightarrow (?)_{10}$$

$$= (4 \times 16^2) + (8 \times 16^1) + (8 \times 16^0) + (2 \times 16^{-1})$$

$$= 1024 + 192 + 8 + 0.125$$

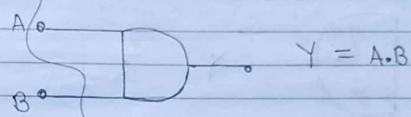
$$= 1224 + 0.125$$

$$= 1224.125$$

[(4C8.2)16 → (1224.125)8]

* Logic gate *

AND function



Input		Output
A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

Logic gate

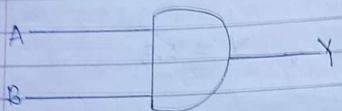
Basic gate
eg. AND, OR, gate

Universal gate
eg. NAND, NOR

derived gate

Eg. EX-OR, PN-NOR

AND Function:-

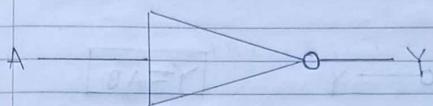


Input	Output	
A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

Truth table

$$Y = A \times B \\ = A \cdot B \\ [Y = AB]$$

NOT function



Input	Output
A	Y
0	1
1	0

$$Y = \bar{A}$$

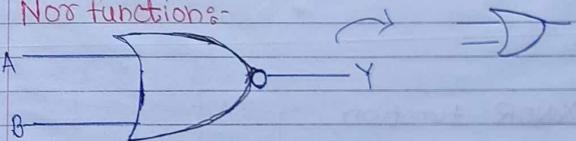
OR function:-



Input	Output	
A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

$$Y = A + B$$

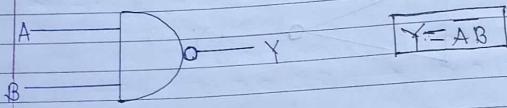
Nor function:-



Input	Output	
A	B	Y
0	0	1
0	1	1
1	0	1
1	1	0

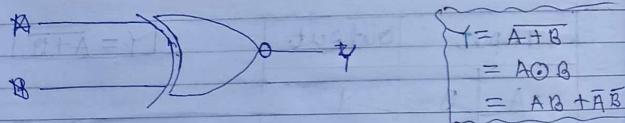
$$Y = \bar{A} + \bar{B}$$

NAND Function :-



Input	Output	
A	B	Y
0	0	1
0	1	1
1	0	0
1	1	0

XNOR function



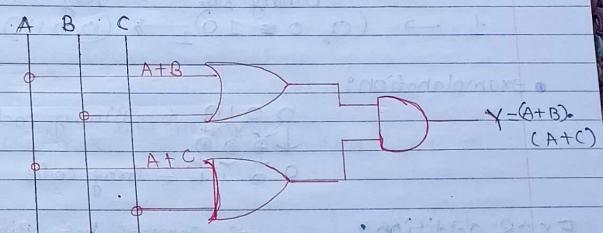
Truth table

Input	Output	
A	B	$Y = A \oplus B$
0	0	0
0	1	1
1	0	1
1	1	0

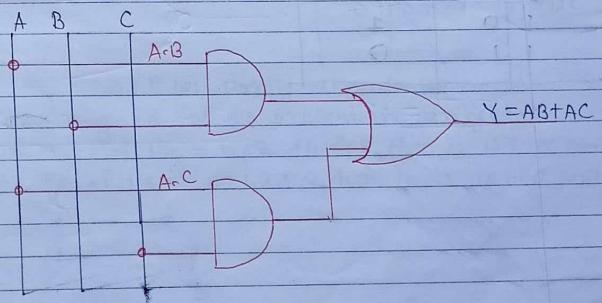
* Problem *

Draw the combination circuit using Basic Gates

① $Y = (A+B) \cdot (A+C)$



② $Y = AB + AC$



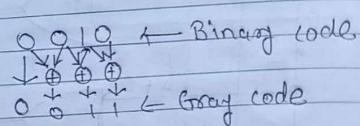
Hamming

* Gray Code :-

$$1 \rightarrow (0 \ 0 \ 1 \ 0)_2 \rightarrow (0 \ 0 \ 1 \ 1)_2$$

Binary No. Gray code.

* explanation :-



Ex OR addition :-

- * convert into Binary code
- * first written 1st no
- as it is or same in Gray code
- * Add with each other

A	B	$y = A \oplus B$
0	0	0
0	1	1
1	0	1
1	1	0

* FROM DETECTING AND CORRECTING CODES *

Parity checking using Hamming code
Even parity Odd parity

* Parity checking :-

Receivers] \leftarrow 4 bit data [Transmitter]

Even Parity :- n= 2, 4, 6, 8

00101
original signal parity bit

Odd Parity :- n= 1, 3, 5, 7

00100 parity bit
original signal
01001 parity bit

* Bit odd/even parity depends upon the how many no. of 1's present in parity boxes

- * if no. of 1's = n= 2, 4, 6, 8, then it is even parity
- * If no. of 1's is n= 1, 3, 5, 7, then it is odd parity

It is the simplest technique for detecting and correcting error. The MSB of an 8-bit word is used as the parity bit and the remaining 7 bits are used as data or message bits. The parity of 8 bits transmitted word can be either even parity or odd parity.

MSB	P	d ₆	d ₅	d ₄	d ₃	d ₂	d ₁	LSB

Even:

* Binary Arithmetic

① Binary Addition :-

Rule:- $B1 + 1 = 0$ and carry = 1

other addition like normal math

$$\text{Eg. } (00101100)_2 + (10110101)_2 = (?)_2$$

Ans:-

$$\begin{array}{r}
 0^1 0^1 1^1 0^0 \\
 + 1^0 1^1 0^1 0^1 \\
 \hline
 1^1 10 0001
 \end{array}$$

② Binary Subtraction :-

Rule:- $0 - 1 = 1$ and carry = 1

and $1 - 1 = 0$
other subtraction like normal math

10 digit consider as 2 in decimal form

$$\text{Eg } (10101.100)_2 - (00111.000)_2$$

$$\begin{array}{r}
 1^0 1^0 1^1 . 1^0 0 \\
 - 0^0 1^1 1^1 . 0^0 0 \\
 \hline
 0^1 1^1 0^0 . 1^0 0
 \end{array}$$

It is the simplest technique for detecting and correcting error. The MSB of an 8-bit word is used as the parity bit and the remaining 7 bits are used as data or message bits. The parity of 8 bits transmitted word can be either even parity or odd parity.

MSB	LSB						
P	d ₆	d ₅	d ₄	d ₃	d ₂	d ₁	d ₀

Even :

* Binary Arithmetic

① Binary Addition :-

Rule :- $0+1=1$ and $1+1=0$ and carry = 1

other addition like normal math

$$\text{Eg. } (00101100)_2 + (10110101)_2 = (?)_2$$

Ans:-

$$\begin{array}{r} 0 \ 0 \ 1 \ 0 \ 1 \ 1 \ 0 \ 0 \\ + 1 \ 0 \ 1 \ 1 \ 0 \ 1 \ 0 \ 1 \\ \hline 1 \ 1 \ 1 \ 0 \ 0 \ 0 \ 1 \end{array}$$

② Binary Subtraction :-

Rule :- $0-1=1$ and carry = 1
and $1-1=0$

other subtraction like normal math
and

10 digit consider as 2 in decimal form

$$\text{Eg } (10101.100)_2 - (00111.000)_2$$

$$\begin{array}{r} 1 \ 0 \ 1 \ 0 \ 1 . \ 1 \ 0 \ 0 \\ - 0 \ 0 \ 1 \ 1 \ 1 . \ 0 \ 0 \ 0 \\ \hline 0 \ 1 \ 1 \ 1 0 . \ 1 \ 0 0 \end{array}$$

* Representation of signed number *

1) Sign magnitude form

2) Complement form

a) 1's complement:

The 1's complement of a binary number is obtained by complementing every bit of number i.e. a 0 is changed to 1 and vice-versa.

Rule :- 0 changed \rightarrow 1
1 changed \rightarrow 0

e.g. Given number $\rightarrow (0101100)_2$

1's complement $\rightarrow \begin{array}{cccccc} \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ (1101001)_2 \end{array}$

2) 2's complement

Rule \rightarrow * Take 1's complement
 \rightarrow * Add 1

e.g. Given no. $\begin{array}{cccccc} 1 & 0 & 1 & 0 & 1 & 0 & 0 \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 0 & 1 & 0 & 1 & 0 & 1 & 0 \end{array}$
1's complement of no. $\begin{array}{cccccc} 0 & 1 & 0 & 1 & 0 & 1 \\ + 1 & & & & & \\ \hline 0 & 1 & 0 & 1 & 1 & 0 \end{array}$ (2)

* Law of Boolean Algebra

1) Complementation Law

$$A = 0 \text{ then } \bar{A} = 1$$

$$A = 1, \text{ then } \bar{A} = 0$$

2) Commutative Law

$$\textcircled{i} A \cdot B = B \cdot A$$

$$\textcircled{ii} A + B = B + A$$

A	B	$A \cdot B$	A	B	$A + B$
0	0	0	0	0	0
0	1	0	0	1	1
1	0	0	1	0	1
1	1	1	1	1	1

3) Associative Laws

$$\textcircled{i} A + (B + C) = (A + B) + C$$

$$\textcircled{ii} A \cdot (B \cdot C) = (A \cdot B) \cdot C$$

4) Distributive Laws

$$\textcircled{i} A(B+C) = AB+AC$$

$$\textcircled{ii} A+B(C = (A+B)(A+C))$$

⇒ AND Law

$$\text{i) } A \cdot 0 = 0$$

$$\text{ii) } A \cdot 1 = A$$

$$\text{iii) } A \cdot A = A$$

$$\text{iv) } A \cdot \bar{A} = 0$$

⇒ OR Law

$$\text{i) } A + 0 = A$$

$$\text{ii) } A + 1 = 1 \cdot A$$

$$\text{iii) } A + A = A$$

$$\text{iv) } A + \bar{A} = 1$$

⇒ Inversion Law

$$\bar{\bar{A}} = A$$

Problem based on Laws

$$\text{i) } A\bar{B} + \bar{A}\bar{B} + AB + \bar{A}\bar{B} = 1$$

$$A\bar{B} + B(\bar{A} + A) + \bar{A}\bar{B}$$

$$A\bar{B} + B + \bar{A}\bar{B}$$

$$B(A + \bar{A}) + B$$

$$\bar{B} + B = 1$$

$$\text{ii) } A + AB = A$$

$$= A(1+B)$$

$$= A \cdot 1 = A$$

$$\text{iii) } (A+B)(A+C) = A+BC$$

$$\text{iv) } A+AB+AB=A+B$$

$$= AA + AC + BA + BC$$

$$= A + B(C\bar{A} + A)$$

$$= A^2 + AC + AB^2 + BC$$

$$= A + B$$

$$= A(1+C) + AB + BC$$

$$= A + AB + BC$$

$$= A(1+B) + BC$$

$$= A + BC$$

$$\text{v) } \bar{AB} = A + \bar{B}$$

← 1st De Morgan's Theorem

A	B	\bar{A}	\bar{B}	\bar{AB}	$A + B$
0	0	1	1	1	1
0	1	1	0	1	1
1	0	0	1	1	1
1	1	0	0	0	0

(23)

2nd De Morgan's theorems :-

$$\textcircled{6} \quad A + B = \overline{A} \cdot \overline{B}$$

A	B	\overline{A}	\overline{B}	$\overline{A} + \overline{B}$	$\overline{A} \cdot \overline{B}$
0	0	1	1	1	1
0	1	1	0	0	0
1	0	0	1	0	0
1	1	0	0	0	0

* Codes *

→ Binary codes :-

Encoding the data :-

When the data or information is coded, the numbers, letters or words are represented by a specific group of symbols. The process of coding these symbols is called as encoding the data.

Code :- The group of symbols is called as code.

Binary code :-

The digital data is represented, stored and transmitted in the form of a stream (group) of binary 0's and 1's. This group of binary bits is also called as binary code.

(24)

Classification of codes

→ 1. Weighted code :-

Each position has fixed weight

(OR)

In weighted codes, each digit position of the number represents a specific weight.

e.g. $8 \ 4 \ 2 \ 1$ \Rightarrow weight
 $n_3 \ n_2 \ n_1, n_0$ \Rightarrow position

2. Non-weighted code :-

(25)

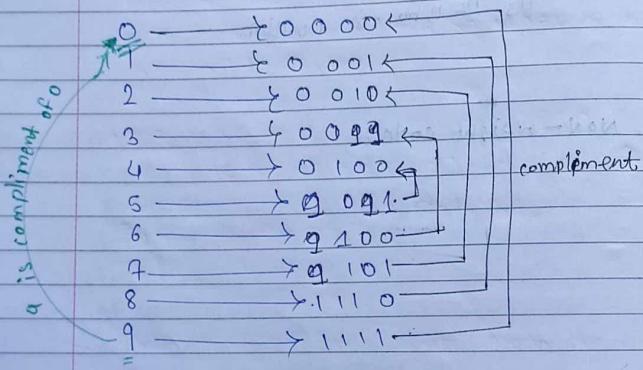
3) Reflective code :-

It is self complimenting code.

In that code 9 is complement of 0

8	→ 1	→ 11 → 1
7	→ 11	→ 11 → 2
6	→ 11	→ 11 → 3
5	→ 11	→ 11 → 4

Decimal 2 4 2 1



4) Sequential code :-

Next data will increment by 1 or difference between successive code is 1

e.g. 0 → 0 000 diff = 0 - 1 = 1
 1 → 0 001 =

5) Alphanumeric codes

↓ →
 (ASCII) . (EBCDIC)

6) Error detecting and correcting codes

BCD code :-

- ① In this code, Each decimal digit represented by 4 bits binary code
- ② In decimal, digit are ranging from 0 to 9, which we will represent in 4 bit binary by BCD code

e.g. Decimal 8 4 2 1
 No 0 → 0 000 + BCD code
 1 → 0 001

Excess 3 code :-

Decimal → 8 4 2 1 Add 0 0 1 1 → Excess 3
 No BCD code

e.g. 4 1 1 1 → 0 1 0 0 → 0 1 0 0
 0 0 1 1 Excess 3

* ERROR DETECTION AND CORRECTING CODES.

- i) Parity bit are the extra bit/bits added to the data being transmitted for detecting the error in data transmission.
- ii) The MSB of an 8-bits word is used as the parity bit and the remaining 7 bits used as data or message bits. The parity of 8-bits transmitted word can be either even parity or odd parity.

Even Parity :- Even parity means the number of 1's in the given word including the parity bits should be even (2, 4, 6, ...).

Odd Parity :- odd parity means the number of 1's in the given word including of 1's the parity bit should be odd (1, 3, 5)

Use of Parity Bit:-

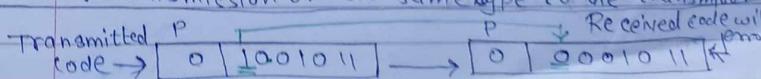
- ① The parity bit can be set 0 and 1 depending on the type of the parity required

② For even parity, this bit is set to 1 or 0 such that no. of "1 bits" in the entire word is even. shown in fig (a).

0	1	00	1011	↑ Parity	
				11	001011

③ for odd parity, the bit is set to 1 or 0 which Such that the no. of 1's or "1 bits" in the entire Word is odd. shown in fig (b)

How does parity checking detect error
Parity checking at the receivers can detect the presence of an error if the parity of receiver signal is different from the expected parity. That means, if it is known the parity of the transmitted signal is always going to be "even" and if the received signal has an odd parity, then the receiver can conclude that receiver signal is not correct. If an error is detected, then the receiver will ignore the received byte and request for retransmission of the same type to the transmitter.



Hamming codes

① It is developed by R.W. HAMMING, it is easy to implement 7 bit hamming code we use mostly

② Data Bit $\Rightarrow 4$

Parity Bit $\Rightarrow 2 \rightarrow 2^n$

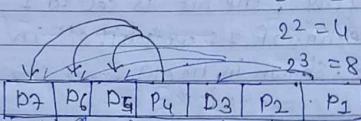
$$n = 0, 1, 2, 3, \dots, h$$

$$2^0 = 1$$

$$2^1 = 2$$

$$2^2 = 4$$

$$2^3 = 8$$



$$P_1 = D_3 D_5 D_7$$

$$P_2 = D_8 D_6 D_7$$

$$P_4 = D_5 D_6 D_7$$

7	6	5	4	3	2	1
D ₇	D ₆	D ₅	P ₄	D ₃	P ₂	P ₁

$$P_1 \rightarrow P_1, D_3, D_5, D_7 \rightarrow (1, 3, 5, 7)$$

$$P_2 \rightarrow P_2, D_3, D_6, D_7 \rightarrow (2, 3, 6, 7)$$

$$P_4 \rightarrow P_4, D_5, D_6, D_7 \rightarrow$$

Difference between computer architecture and computer organization

Computer Architecture

⑥ All the high-level design issue are handled by the computer architecture.

⑦ Computer architecture deals with high-level design issue.

⑧ Actors in computer architecture are hardware part.

⑨ Computer architecture is also called as instruction set architecture.

⑩ All the low-level design issue are handled by the computer organization.

⑪ Computer organization deals with low-level design issue.

⑫ Actor in computer organization is performance.

⑬ Computer organization is frequently called as micro architecture.