

Time Series Analysis

Fall 2017

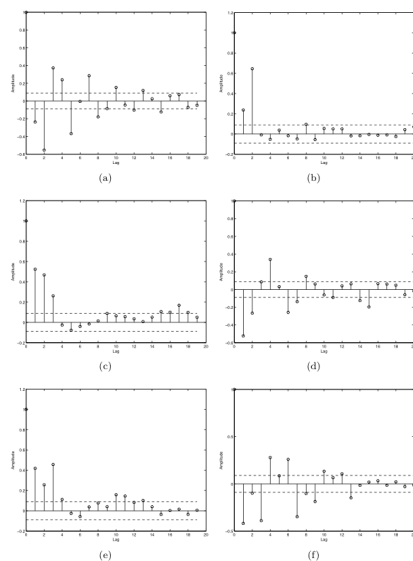
Andreas Jakobsson

Identification

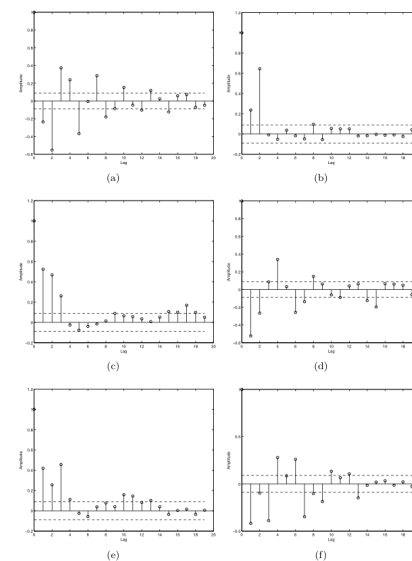
Characteristics for the autocorrelation functions:

	ACF $\rho(k)$	PACF ϕ_{kk}
$AR(p)$	Damped exponential and/or sine functions	$\phi_{kk} = 0$ for $k > p$
$MA(q)$	$\rho(k) = 0$ for $k > q$	Dominated by damped exponential and or/sine functions
$ARMA(p, q)$	Damped exponential and/or sine functions after lag $q - p$	Dominated by damped exponential and/or sine functions after lag $p - q$

Identification



Identification



AR(2)

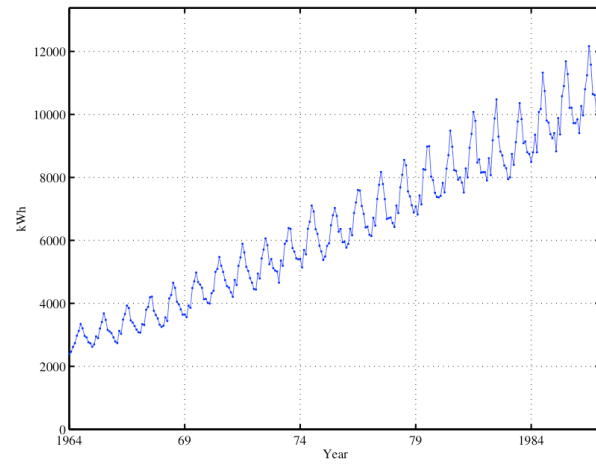
MA(3)

ARMA(1,4)



Time series analysis

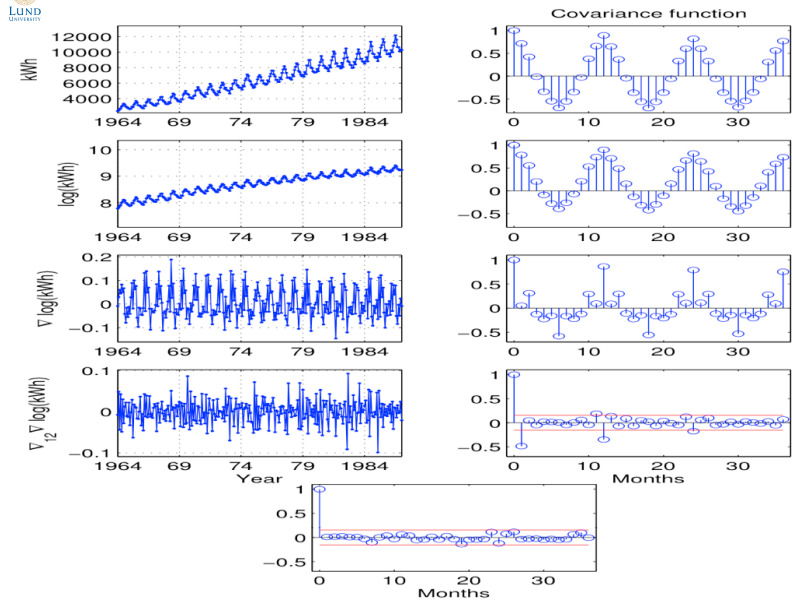
Electricity consumption in Australia



$$\nabla_{12} \nabla \log y_t = (1 - 0.71B)(1 - 0.67B^{12})e_t$$

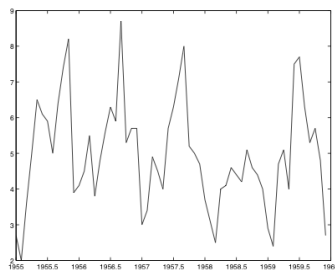


Time series analysis



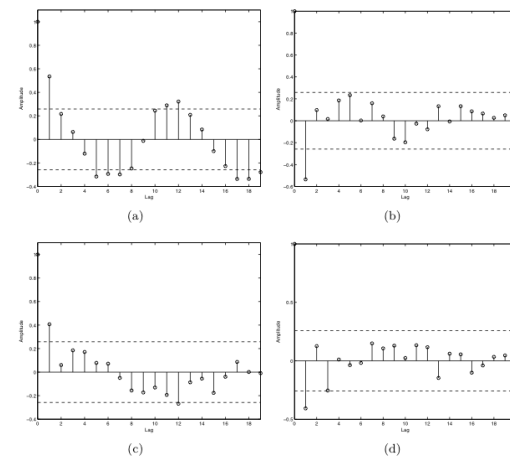
Time series analysis

Oxidant levels in Los Angeles

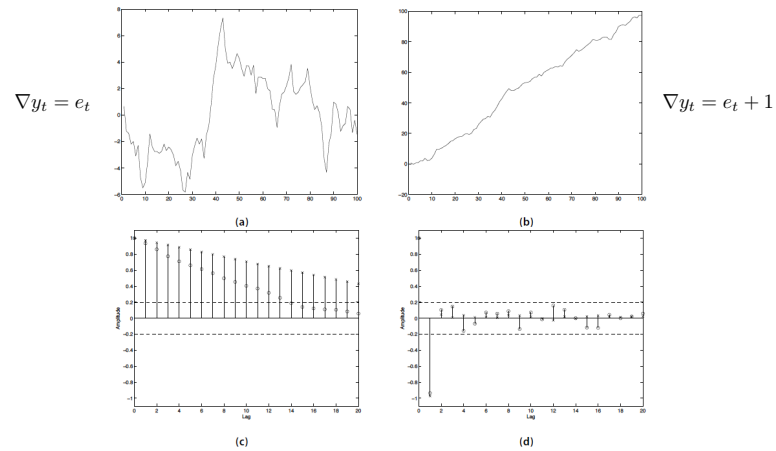


Time series analysis

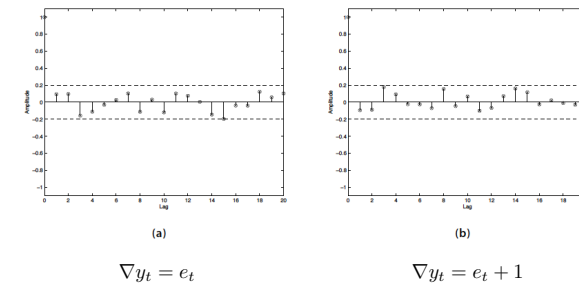
Oxidant levels in Los Angeles



Testing for a non-zero mean



Testing for a non-zero mean

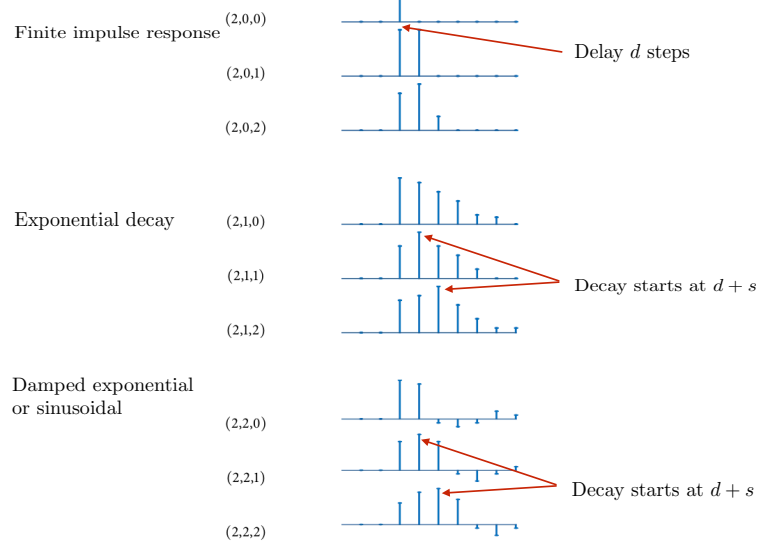


Reject the hypothesis that $m_y = \hat{m}_y$, with significance α , if

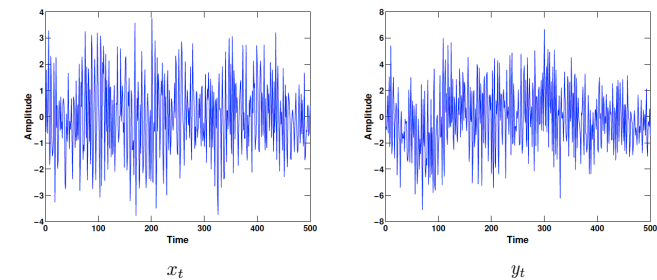
$$N(\hat{m}_y - m_y) \hat{\sigma}_y^{-2} (\hat{m}_y - m_y) > t_{N-1}^2(\alpha/2)$$

Use the provided function `testMean`.

(d, r, s) Typical impulse weights

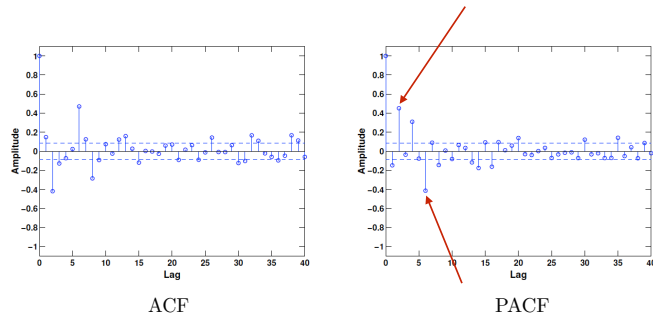


Identifying a Box-Jenkins model



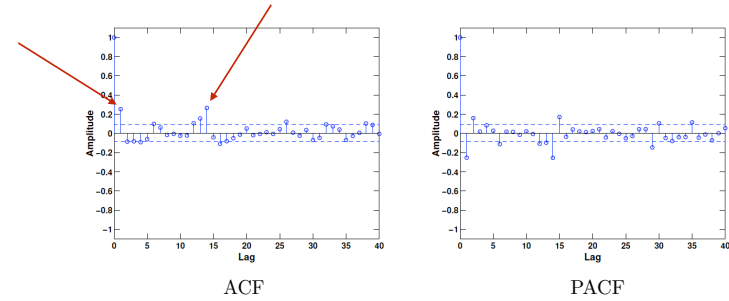
Input and output of the simulated process in Example 4.21.

Begin by modeling the input signal, x_t .



There seems to be strong dependencies for order 2 and 6, as well as, perhaps, at 4. In order to have a simple model, we begin with trying

$$A_3(z) = 1 + a_2 z^{-2} + a_6 z^{-6}$$

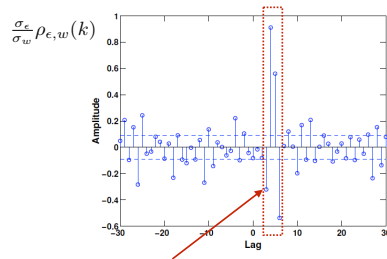


We estimate the parameters of this model and examine the ACF and PACF of the residual (above). Looking at the ACF, there seems to be strong dependencies at lag 1 and 14. We thus modify our model to

$$A_3(z) = 1 + a_2 z^{-2} + a_6 z^{-6}$$

$$C_3(z) = 1 + c_1 z^{-1} + c_{14} z^{-14}$$

We re-estimating *all* parameters and examine the residuals. These are now deemed to be white.



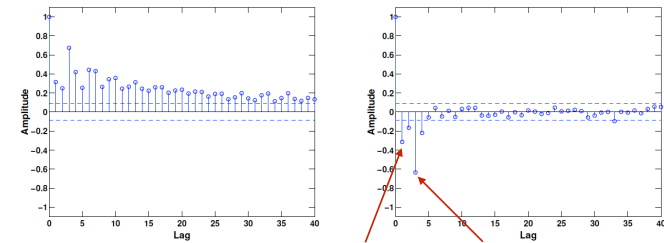
We form the "white" input signal and the corresponding output

$$w_t = \frac{A_3(z)}{C_3(z)} x_t \quad \text{and} \quad \epsilon_t = \frac{A_3(z)}{C_3(z)} y_t$$

and then estimate the transfer function from w_t to ϵ_t as

$$h_k = \frac{\sigma_\epsilon}{\sigma_w} \rho_{\epsilon,w}(k)$$

The delay suggests $d = 3$. The impulse response seems to "ring", so we try $r = 2$. There seems to be 4 dominant components, i.e., $s = 3$.



We pretend that the additive noise is white, and estimate the parameters detailing the model

$$y_t = \frac{B(z)z^{-d}}{A_2(z)} x_t + \tilde{\epsilon}_t$$

where $B(z)$ and $A_2(z)$ are of order s and r , respectively. We then compute the ACF and PACF of the residual $\tilde{\epsilon}_t$ (above).

We form a model of the residual, beginning with using just a_1 and a_3 . Examining the resulting residual suggest that we also needs c_1 . This yields a white residual. Finally, we *re-estimate* all coefficients.



This week

We will cover

- Identification. Estimation.
- Reading instructions: Ch. 4, 5.1-5.2
- Problems: 4.1-4.4