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5-E
1BM22CS275

A* ALGORITHM - MISPLACED TILES

```python
import heapq

# Define the goal state for the 8 puzzle
GOAL_STATE = [1, 2, 3, 8, 0, 4, 7, 6, 5]        # 0 represents the blank space

# Find the index of the blank space (0)
def find_blank(state):
    return state.index(0)

# Define valid moves based on the blank's position
def possible_moves(blank_index):
    moves = []
    # Move blank up (swap with element above)
    if blank_index > 2:
        moves.append(blank_index - 3)
    # Move blank down (swap with element below)
    if blank_index < 6:
        moves.append(blank_index + 3)
    # Move blank left (swap with element to the left)
    if blank_index % 3 > 0:
        moves.append(blank_index - 1)
    # Move blank right (swap with element to the right)
    if blank_index % 3 < 2:
        moves.append(blank_index + 1)
    return moves

# Swap blank space (0) with the target position
def swap(state, blank_index, target_index):
    new_state = state[:]
    new_state[blank_index], new_state[target_index] = new_state[target_index], new_state[blank_index]
    return new_state
```

```python
# Heuristic function: Count the number of misplaced tiles
def heuristic(state):
    return sum([1 if state[i] != GOAL_STATE[i] and state[i] != 0 else 0
for i in range(9)])

# A* Search Algorithm
def a_star(start_state):
    open_list = [] # priority queue to maintain nodes to be explored
    closed_list = set() # to store already explored nodes

    # Initial state setup
    g = 0 # Cost to reach the current node (depth/level)
    h = heuristic(start_state) # Heuristic (misplaced tiles)
    f=g+h        #Totalcost(f=g+h)

    heapq.heappush(open_list, (f, g, h, start_state, []))        # Add initial
node to open list

    while open_list:
        # Get the node with the lowest f value
        f, g, h, current_state, path = heapq.heappop(open_list)

        # If current state is the goal, return the solution path
        if current_state == GOAL_STATE:
            return path + [(current_state, g, h)]

        # Add current state to the closed list
        closed_list.add(tuple(current_state))

        # Find blank's position and generate all possible moves
        blank_index = find_blank(current_state)
        for move in possible_moves(blank_index):
            new_state = swap(current_state, blank_index, move)

            # If the new state is already explored, skip it
            if tuple(new_state) in closed_list:
                continue

            # Calculate g, h, and f for the new state
            new_g = g + 1
```

```python
            new_h = heuristic(new_state)
            new_f = new_g + new_h

            # Add the new state to the open list
            heapq.heappush(open_list, (new_f, new_g, new_h, new_state,
path + [(current_state, g, h)]))

    return None  # If no solution is found

# Example usage
start_state = [2,8,3,1,6,4,7,0,5]          # Start state of the puzzle
solution = a_star(start_state)

if solution:
    print("Solution found:")
    for state_info in solution:
        state, g, h = state_info
        for i in range(0, 9, 3):
            print(state[i:i+3])
        print(f"Level (g): {g}, Heuristic (h): {h}, Total Cost (f = g +
h): {g + h}\n")
else:
    print("No solution exists.")
```

OUTPUT:

```
Solution found:
[2, 8, 3]
[1, 6, 4]
[7, 0, 5]
Level (g): 0, Heuristic (h): 4, Total Cost (f = g + h): 4

[2, 8, 3]
[1, 0, 4]
[7, 6, 5]
Level (g): 1, Heuristic (h): 3, Total Cost (f = g + h): 4

[2, 0, 3]
[1, 8, 4]
[7, 6, 5]
Level (g): 2, Heuristic (h): 3, Total Cost (f = g + h): 5

[0, 2, 3]
[1, 8, 4]
[7, 6, 5]
Level (g): 3, Heuristic (h): 2, Total Cost (f = g + h): 5

[1, 2, 3]
[0, 8, 4]
[7, 6, 5]
Level (g): 4, Heuristic (h): 1, Total Cost (f = g + h): 5

[1, 2, 3]
[8, 0, 4]
[7, 6, 5]
Level (g): 5, Heuristic (h): 0, Total Cost (f = g + h): 5
```