

*Heaven's Light is Our Guide*

# Rajshahi University of Engineering & Technology



## Department of Electrical & Computer Engineering

Course No : ECE 4124

Course Title : Digital Signal Processing Sessional

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## Experiment No: 05

**Experiment Name:** Experiment on finding the Z-transform and inverse Z-transform of a function.

### Theory:

A mathematical technique called the Z-transform is used to translate differential equations in the time domain into algebraic equations in the z-domain.

The Z-transform formula-

$$X(z) = \sum_{n=-\infty}^{\infty} x[n]z^{-n}$$

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The method of determining the time domain signal  $x(n)$  from its Z-transform  $X(z)$  is known as the inverse Z-transform. The symbol for the inverse Z-transform is-

$$x(n) = Z^{-1}[X(z)]$$

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$$x_n = \frac{1}{2\pi j} \int_c X(z) z^{n-1} dz$$

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### Code:

**Z-transform and inverse Z-transform of right-side signal:**

```
1. clc;
2. close all;
3. clear all;
4.
5. syms n;
6. x = [1 2 3 4 5];
7. l = length(x);
8.
9. trans = 0;
10. z = sym('z');
11. for i=0:l-1
12. trans=trans+x(i+1).*z^(-i);
13. end
14.
15. disp('Z-transform: ');
16. disp(trans);
17.
18. f=iztrans(trans);
19. disp('Inverse Z-transform:');
20. disp(f);
```

### **Z-transform and inverse Z-transform of left-side signal:**

```
1. clc;
2. close all;
3. clear all;
4.
5. syms n;
6. x = [1 2 3 4 5];
7. y = fliplr(x);
8. l = length(y);
9.
10. trans = 0;
11. z = sym('z');
12. for i=0:l-1
13. trans=trans+y(i+1).*z^(i);
14. end
15.
16. disp('Z-transform:');
17. disp(trans);
18.
19. f=iztrans(trans);
20. disp('Inverse Z-transform:');
21. disp(f);
```

### **Z-transform and inverse Z-transform of non-causal signal:**

```
1. clc;
2. close all;
3. clear all;
4.
5. syms n;
6. x = [1 2 3 4 5 6 7];
7. n = length(x);
8.
9. k=input('Enter zero index:');
10. p=[];
11. for i=0:k
12. p(i+1)=x(i+1);
13. end
14.
15. h=fliplr(p);
16. u=length(h);
17.
18. trans = 0;
19. z = sym('z');
20. for i=0:u-1
21. trans=trans+h(i+1).*z^(i);
22. end
23.
24. q=[];
25. for i=0:(n-k-2)
26. q(i+1)= x(i+k+2);
27. end
```

```

28.
29. v=length(q);
30. for i=0:v-1
31. trans=trans+q(i+1).*z^(-(i+1));
32. end
33.
34. disp('Z-transform:');
35. disp(trans);
36. f=iztrans(trans);
37. disp('Inverse Z-transform:');
38. disp(f);

```

### Output:

#### Z-transform and inverse Z-transform of right-side signal:

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Z-transform:

$$2/z + 3/z^2 + 4/z^3 + 5/z^4 + 1$$

Inverse Z-transform:

$$2*\text{kroneckerDelta}(n-1, 0) + 3*\text{kroneckerDelta}(n-2, 0) + 4*\text{kroneckerDelta}(n-3, 0) + 5*\text{kroneckerDelta}(n-4, 0) + \text{kroneckerDelta}(n, 0)$$

#### Z-transform and inverse Z-transform of right-side signal:

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Z-transform:

$$z^4 + 2*z^3 + 3*z^2 + 4*z + 5$$

Inverse Z-transform:

$$5*\text{kroneckerDelta}(n, 0) + 3*\text{iztrans}(z^2, z, n) + 2*\text{iztrans}(z^3, z, n) + \text{iztrans}(z^4, z, n) + 4*\text{iztrans}(z, z, n)$$

#### Z-transform and inverse Z-transform of non-causal signal:

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Enter zero index:4

Z-transform:

$$4*z + 6/z + 7/z^2 + 3*z^2 + 2*z^3 + z^4 + 5$$

Inverse Z-transform:

$$6*\text{kroneckerDelta}(n-1, 0) + 7*\text{kroneckerDelta}(n-2, 0) + 5*\text{kroneckerDelta}(n, 0) + 3*\text{iztrans}(z^2, z, n) + 2*\text{iztrans}(z^3, z, n) + \text{iztrans}(z^4, z, n) + 4*\text{iztrans}(z, z, n)$$

### Discussion:

In this experiment, we have worked with Z-transform and inverse Z-transform of three types of signals – right side signal, left side signal and both sided that is non-causal signal. In right side signal we found the power of z as negative and in case of left side signal those power of z was positive which was matched with our theoretical explanations also.

For inverse z-transform, we used a function ‘iztrans’ which worked correctly to find out the inverse of the Z-transform of the functions.

**Conclusion:** The code was executed successfully and no errors were found.

