

$$\begin{aligned}
 (A) \quad \Sigma &= L L^T = \begin{pmatrix} l_{11} & l_{12} \\ l_{21} & l_{22} \end{pmatrix} \begin{pmatrix} l_{11}^T & l_{21}^T \\ l_{12}^T & l_{22}^T \end{pmatrix} \\
 &= \begin{pmatrix} l_{11} l_{11}^T + l_{12} l_{12}^T & l_{11} l_{21}^T + l_{12} l_{22}^T \\ l_{21} l_{11}^T + l_{22} l_{12}^T & l_{21} l_{21}^T + l_{22} l_{22}^T \end{pmatrix} = \begin{pmatrix} \Sigma_{11} & \Sigma_{12} \\ \Sigma_{21} & \Sigma_{22} \end{pmatrix}
 \end{aligned}$$

$$X = L Z + \mu$$

$$\begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = \begin{pmatrix} l_{11} & l_{12} \\ l_{21} & l_{22} \end{pmatrix} \begin{pmatrix} z_1 \\ z_2 \end{pmatrix} + \begin{pmatrix} \mu_1 \\ \mu_2 \end{pmatrix} = \begin{pmatrix} l_{11} z_1 + l_{12} z_2 + \mu_1 \\ l_{21} z_1 + l_{22} z_2 + \mu_2 \end{pmatrix}$$

$$\text{So } x_1 = l_{11} z_1 + l_{12} z_2 + \mu_1$$

$$M_{x_1}(t) = E[\exp(t^T(l_{11} z_1 + l_{12} z_2 + \mu_1))]$$

$$= e^{t^T \mu_1} E(e^{t^T l_{11} z_1}) E(e^{t^T l_{12} z_2})$$

$$= \exp\left[t^T \mu_1 + \frac{1}{2} t^T l_{11} l_{11}^T t + \frac{1}{2} t^T l_{12} l_{12}^T t\right]$$

$$= \exp\left[t^T \mu_1 + \frac{1}{2} t^T (l_{11} l_{11}^T + l_{12} l_{12}^T) t\right]$$

$$= \exp(t^T \mu_1 + \frac{1}{2} t^T \Sigma_{11} t)$$

$$\text{So } x_1 \sim N(\mu_1, \Sigma_{11})$$