Hello and welcome to decision trees!

Decision trees are often pretty effect learning algorithms, and certainly serve as an interesting technical exercise in data preprocessing and recursion. This notebook will walk you through some of the basic notions of how the implementation should be executed, and also give you a chance to write some of your own code.

Suggested reading before you start:

https://www.cs.princeton.edu/courses/archive/spring07/cos424/papers/mitchell-dectrees.pdf (https://www.cs.princeton.edu/courses/archive/spring07/cos424/papers/mitchell-dectrees.pdf)

Throughout the notebook you'll see TODO tags in the comments. This is where you should insert your own code to make the functions work! If you get stuck, we encourage you to come to office hours. You can also try to look at APIs and documentation online to try to get a sense how certain methods work. If you take inspiration from any source online other than official documentation, please be sure to cite the resource! Good luck!

```
In [64]: import pandas as pd import scipy.io import numpy as np
```

We will be using decision trees to classify if a banknote is fradulent (class 1) or not fradulent (class 0). Download data from https://archive.ics.uci.edu/ml/datasets/banknote+authentication# (https://archive.ics.uci.edu/ml/datasets/banknote+authentication#)

Import data

```
In [65]:
         # TODO YOUR CODE HERE
          def import data(split = 0.8, shuffle=False):
              """Read in the data, split it by split percentage into train and t
              and return X_train, y_train, X test, y test as numpy arrays"""
              # TODO
              df = pd.read csv('./data banknote authentication.txt',
                                names = ['vairance', 'skewness', 'curtosis', 'entrop'
          y','class'])
              df array = np.array(df)
              #shuffle data
              np.random.shuffle(df array)
              train = df array[:round(split*len(df array))]
              test = df array[round(split*len(df array)):]
              X train = train[:,0:4]
              y train = train[:,-1].astype(int)
              X \text{ test} = \text{test}[:,0:4]
              y \text{ test} = \text{test}[:,-1].astype(int)
              print("data imported")
              return X train, y train, X test, y test
```

```
In [66]: class Node:
             """Each node of our decision tree will hold values such as left an
         d right children,
             the data and labels being split on, the threshold value & index in
         the dataframe for a particular feature,
             and the uncertainty measure for this node"""
             def init (self, data, labels, depth):
                 data: X data
                 labels: y data
                 depth: depth of tree
                 self.left = None
                 self.right = None
                 self.data = data
                 self.labels = labels
                 self.depth = depth
                 self.threshold = None # threshold value
                 self.threshold index = None # threshold index
                 self.feature = None # feature as a NUMBER (column number)
                 self.label = None # y label
                 self.uncertainty = None # uncertainty value
```

In [67]: class DecisionTree:

```
def __init__(self, K=5, verbose=False):
        K: number of features to split on
        self.root = None
        self.K = K
        self.verbose = verbose
    def buildTree(self, data, labels, metric ='entropy'):
        """Builds tree for training on data. Recursively called build
Tree"""
        self.root = Node(data, labels, 0)
        if self.verbose:
            print("Root node shape: ", data.shape, labels.shape)
        self. buildTree(self.root, metric)
   def buildTree(self, node, metric ='entropy'):
        # get uncertainty measure and feature threshold
        node.uncertainty = self.get uncertainty(node.labels)
        self.get feature threshold(node, metric)
        index = node.data[:, node.feature].argsort() # sort feature f
or return
        node.data = node.data[index]
        node.labels = node.labels[index]
        # check label distribution.
        label distribution = np.bincount(node.labels)
        majority label = node.labels[0] if len(label distribution) ==
1 else np.argmax(label distribution)
        if self.verbose:
            print("Node uncertainty: %f" % node.uncertainty)
        # Split left and right if threshold is not the min or max of t
he feature or every point has the
        # same label.
        if node.threshold index == 0 or node.threshold index == node.d
ata.shape[0] or \
            len(label distribution) == 1:
            node.label = majority label
        else:
            node.left = Node(node.data[:node.threshold index], node.la
bels[:node.threshold index], node.depth + 1)
            node.right = Node(node.data[node.threshold index:], node.l
abels[node.threshold index:], node.depth + 1)
            node.data = None
            node.labels = None
```

```
# If in last layer of tree, assign predictions
            if node.depth == self.K:
                if len(node.left.labels) == 0:
                    node.right.label = np.argmax(np.bincount(node.righ
t.labels))
                    node.left.label = 1 - node.right.label
                elif len(node.right.labels) == 0:
                    node.left.label = np.argmax(np.bincount(node.left.
labels))
                    node.right.label = 1 - node.left.label
                else:
                    node.left.label = np.argmax(np.bincount(node.left.
labels))
                    node.right.label = np.argmax(np.bincount(node.righ
t.labels))
                return
            else: # Otherwise continue training the tree by calling b
uildTree
                self. buildTree(node.left)
                self. buildTree(node.right)
    def predict(self, data pt):
        return self. predict(data pt, self.root)
    def predict(self, data pt, node):
        feature = node.feature
        threshold = node.threshold
        if node.label is not None:
            return node.label
        elif data pt[node.feature] < node.threshold:</pre>
            return self. predict(data pt, node.left)
        elif data_pt[node.feature] >= node.threshold:
            return self. predict(data pt, node.right)
    def get feature threshold(self, node, metric ='entropy'):
        Find the feature that gives the largest information gain.
        Update node.threshold, node.threshold index, and node.feature
(a number representing the feature. e.g. 2nd column feature would be 1
        Make sure to sort the columns of data before you try to find t
he threshold index (look at numpy argsort) and set the values
        for node.threshold, node.threshold index, and node.feature
        return: None
        11 11 11
        node.threshold = 0
        node.threshold index = 0
        node.feature = 0
        # TODO YOUR CODE HERE
```

```
n = node.data.shape[0]
        n feature = node.data.shape[1]
        info gain = 0
        for i in range(n feature):
            sort = np.argsort(node.data[:,i])
            node.data = node.data[sort]
            node.labels = node.labels[sort]
            for j in range(n-1):
                gain = self.getInfoGain(node, j+1, metric)
                if info gain == 0:
                    info gain = gain
                    node.threshold = node.data[j+1,i]
                    node.threshold index = j+1
                    node.feature = i
                elif gain > info gain:
                    info gain = gain
                    node.threshold = node.data[j+1,i]
                    node.threshold index = j+1
                    node.feature = i
    def getInfoGain(self, node, split index, metric = 'entropy'):
        TODO Get information gain using the variables in the parameter
s, \
        split_index: index in the feature column that you are splittin
q the classes on
        return: information gain (float)
        # TODO YOUR CODE HERE
        Q = self.get uncertainty(node.labels, metric)
        Q r = self.get uncertainty(node.labels[0:split index], metric)
        Q l = self.get uncertainty(node.labels[split index:], metric)
        gain = Q - (Q 1 * (split index)/node.labels.shape[0]
                    + Q r * (1-(split index/node.labels.shape[0])))
        return gain
    def get uncertainty(self, labels, metric="entropy"):
        TODO Get uncertainty. Implement entropy AND gini index metrics
        np.bincount(labels) and labels.shape might be useful here
        return: uncertainty (float)
        11 11 11
        if labels.shape[0] == 0:
            return 1
```

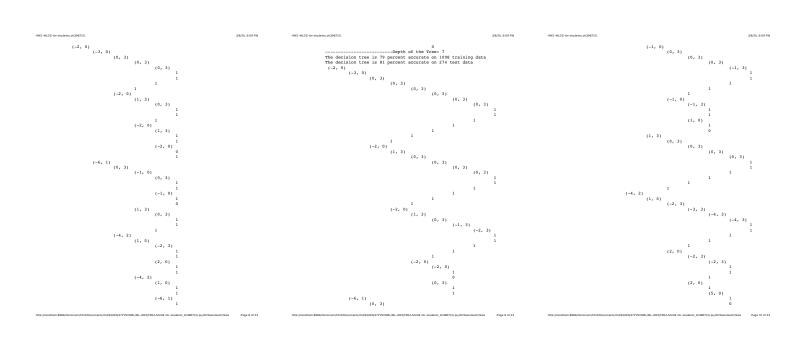
```
# TODO YOUR CODE HERE
        else:
            O = 0
            p_mk = (1/labels.shape[0]) * np.bincount(labels)[0] #np.bi
ncount(labels)[0] output majority of type
            if metric == 'entropy':
                if p_mk !=1 and p_mk !=0:
                    Q = p_mk * np.log(p_mk) + (1-p_mk) * np.log(p_mk)
            if metric == 'gini':
                Q = p mk*(1-p mk)*2
        return 0
    def printTree(self):
        """Prints the tree including threshold value and feature name"
11 11
        self. printTree(self.root)
    def printTree(self, node):
        if node is not None:
            if node.label is None:
                print("\t" * node.depth, "(%d, %d)" % (node.threshold,
node.feature))
            else:
                print("\t" * node.depth, node.label)
            self. printTree(node.left)
            self. printTree(node.right)
    def homework evaluate(self, X train, labels, X test, y test):
        n = X train.shape[0]
        count = 0
        for i in range(n):
            if self.predict(X train[i]) == labels[i]:
                count += 1
        print("The decision tree is %d percent accurate on %d training
data" % ((count / n) * 100, n))
        n = X_test.shape[0]
        count = 0
        for i in range(n):
            if self.predict(X_test[i]) == y_test[i]:
                count += 1
        print("The decision tree is %d percent accurate on %d test dat
```

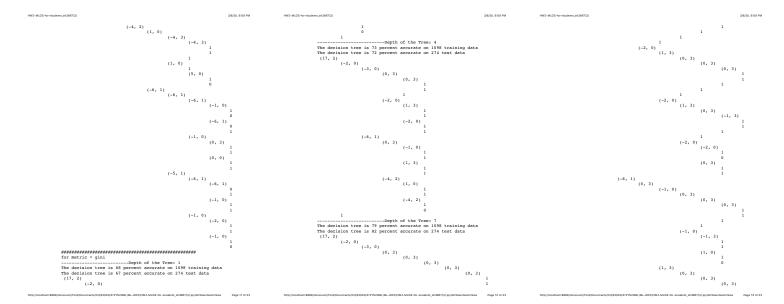
```
a" % ((count / n) * 100, n))
    return count / n
```

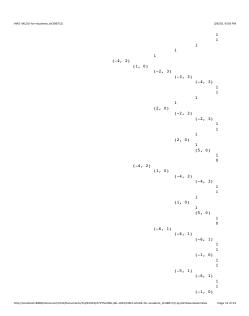
Run the tree

Try different values of K (depth of tree a.k.a. number of features the tree will split on) and compare the performance. Which feature gives the largest information gain? Which feature is the least useful for the decision tree?

```
In [68]: X train, y train, X test, y test = import data(split=0.8)
        data imported
In [70]: | print('for metric = entropy')
        for k in range(1,10,3):
            print('-----Depth of the Tree:', k)
            tree = DecisionTree(K=k, verbose=False)
            tree.buildTree(X train, y train, metric = 'entropy')
            tree.homework evaluate(X train, y train, X test, y test)
            tree.printTree()
        print('###############")
        print('for metric = gini')
        for k = n  range(1,10,3):
            print('-----Depth of the Tree:', k)
            tree = DecisionTree(K=k, verbose=False)
            tree.buildTree(X_train, y_train, metric = 'gini')
            tree.homework evaluate(X train, y train, X test, y test)
            tree.printTree()
        for metric = entropy
        -----Depth of the Tree: 1
        The decision tree is 72 percent accurate on 1098 training data
        The decision tree is 71 percent accurate on 274 test data
         (-2, 0)
                (-3, 0)
                 (-6, 1)
               -----Depth of the Tree: 4
        The decision tree is 75 percent accurate on 1098 training data
        The decision tree is 74 percent accurate on 274 test data
```







1

1

- For both metric, the accuracy of decision tree model increase by adding more depth.
- By observing printed tree, 0 is the feature appears most frequently, while 3 is the least frequent feature. Therefore, feature 0 provides largest information gain. Feature 3 is the least useful for the tree.
- Model performance does't vary a lot provided different uncertainty metric, gini and entropy. The reason is that both of the two metric are measuring impurity with similar methods. The two function change in same direction. Therefore, the output is similar

Optional Decision Tree Exercise

This section is designed to give you some exposure to typical preprocessing and allow you to run your decision tree code on another example.

All of the preprocessing has been done for you — there's nothing you need to fill in, but it may be worthwhile to tinker with some of the pieces to make sure you understand how everything fits together.

Otherwise, if your decision tree code works on the bank notes example, you should be able to run through this straight away.

Step 1: Data Preprocessing

To start, you'll need to download the data files from https://archive.ics.uci.edu/ml/machine-learning-databases/breast-cancer/). The file <code>breast-cancer.data</code> contains the actual data you'll need and the file <code>breast-cancer.names</code> gives some information about the researchers and the data types (it's probably worth looking at to give you a sense of what's going on).

Note: If you try to open <code>breast-cancer.data</code> or <code>breast-cancer.names</code> directly, your computer might not know how to handle the file format. To view them, you need to change the file types from .data and .names to .txt — this can be accomplished by simply changing the file name from <code>breast-cancer.txt</code>

Now let's load the data file into the notebook. All you need to do is put it in the same directory as the notebook and the cell below should locate the appropriate file.

```
In [48]: import os
    current_directory = os.listdir()

try:
    cancer_files = [file for file in current_directory if 'cancer' in fi
le]
    data_file = [file for file in cancer_files if 'names' not in file][0
]
except IndexError:
    print('The breast cancer files were not found. Please upload again.'
)
    data_file = None

if data_file:
    print(f'The data file has been located as {data_file}.')
```

The data file has been located as breast-cancer.data.

!! If the cell above returned a file that you don't recognize as the correct data file, you must go back to the upload step and ensure you have successfully uploaded your files before proceeding. !!

Now we'll try to read the sample into our environment:

```
In [49]: samples = []

with open(data_file, 'r') as file:
    samples = file.readlines()

samples = [sample.split(',') for sample in samples]

print(f'There are {len(samples)} samples in the dataset')
```

There are 286 samples in the dataset

We can now start defining how we want to map our sample values to numeric features that can be used in the decision tree algorithm below. Let's first store our samples in a pandas DataFrame so that it'll be easier to view and work with.

Out[50]:

	class	age	menopause	tumor- size	inv- nodes	node- caps	deg- malig	breast	breast- quad	irradiat	
0	no- recurrence- events	30- 39	premeno	30-34	0-2	no	3	left	left_low	no	
1	no- recurrence- events	40- 49	premeno	20-24	0-2	no	2	right	right_up	no	
2	no- recurrence- events	40- 49	premeno	20-24	0-2	no	2	left	left_low	no	
3	no- recurrence- events	60- 69	ge40	15-19	0-2	no	2	right	left_up	no	
4	no- recurrence- events	40- 49	premeno	0-4	0-2	no	2	right	right_low	no	
281	recurrence- events	30- 39	premeno	30-34	0-2	no	2	left	left_up	no	
282	recurrence- events	30- 39	premeno	20-24	0-2	no	3	left	left_up	yes	
283	recurrence- events	60- 69	ge40	20-24	0-2	no	1	right	left_up	no	
284	recurrence- events	40- 49	ge40	30-34	3-5	no	3	left	left_low	no	
285	recurrence- events	50- 59	ge40	30-34	3-5	no	3	left	left_low	no	

286 rows × 10 columns

Our DataFrame looks great! Now that we have the raw data stored in an interpretable way, it's good practice to make a copy before trying to encode everything — if something goes wrong, it'll be easy to just come back up here and reset the encoded DataFrame.

```
In [51]: encoded_samples_df = samples_df.copy()
```

In the following few cells, we're going to define the different types of variables that exist in our dataset and make sure we assign the appropriate type of encoding.

To start, we'll define our binary variables (0,1) and create Python dictionaries to map the string labels to binary integer values.

It's also helpful to store all of the columns and dictionaries in two lists so that we can easily reference them later on.

```
In [52]: binary_cols = ['class', 'breast', 'irradiat']

class_map = {'no-recurrence-events': 0, 'recurrence-events': 1}
breast_map = {'left': 0, 'right': 1}
irrad_map = {'yes': 1, 'no': 0}

binary_maps = [class_map, breast_map, irrad_map]
```

Next, we've defined our ordinal variables (those that have obvious ordered structure). Instead of hard-coding the maps here, it's nice to have a function that can take any number of ordinal columns and instantly create all of the corresponding maps. The code below does that exactly, relying on the integer value of the first number in the range (i.e. '50-65') as the sorting key.

```
In [53]: ordinal_cols = ['age', 'tumor-size', 'inv-nodes', 'deg-malig']

def first_val(x):
    return eval(x.split('-')[0].replace("'", ''))

ordinal_maps = {}

for col in ordinal_cols:
    uniques = sorted(list(encoded_samples_df[col].unique()), key=first_v al)
    val_map = {}
    i = 1

for val in uniques:
    val_map[val] = i
    i += 1

ordinal_maps[col] = val_map
```

Finally, we have several columns that take n > 2 discrete values. Binary encoding won't work here, so we'll use one-hot encoding. Just like in the cell immediately above, we'll use a function here to take an arbitrary number of columns and encode their unique values as one-hot vectors.

```
In [54]: one_hot_cols = ['menopause', 'breast-quad', 'node-caps']
    one_hot_maps = {}

    def    one_hot_map(col, df):
        one_hot = {}
        unique_vals = list(df[col].unique())
        one_hot_vecs = np.identity(len(unique_vals))

    for i in range(len(unique_vals)):
        one_hot[unique_vals[i]] = one_hot_vecs[i]

    return one_hot

    for col in one_hot_cols:
        one_hot_maps[col] = one_hot_map(col, encoded_samples_df)
```

Now that we have all of our encoding maps set up, we'll zip them all up into a master dictionary so that we can easily iterate through them on our encoded samples df DataFrame.

```
In [55]: all_maps = dict(one_hot_maps, **ordinal_maps)
for col, val_map in zip(binary_cols, binary_maps):
    all_maps[col] = val_map
```

Before proceeding, let's double check to make sure you've captured all of the columns:

```
In [56]: if len(all_maps) != len(columns):
    print("You're missing a map! Go back and double check that you didn'
    t miss a column.")
    else:
        print("Looks like you successfully created all the maps! Nice work!"
    )
```

Looks like you successfully created all the maps! Nice work!

And now the moment of truth! Let's apply all of our encoding maps on the DataFrame to turn everything into useable features for our decision trees algorithm.

```
In [57]: for col in columns:
    encoded_samples_df[col] = encoded_samples_df[col].map(all_maps[col])
    encoded_samples_df
```

HW2-MLDS-for-students_sh3967(2) 3/8/20, 6:09 PM

Out[57]:

	class	age	menopause	tumor- size	inv- nodes	node- caps	deg- malig	breast	breast-quad	irradiat
0	0	2	[1.0, 0.0, 0.0]	7	1	[1.0, 0.0, 0.0]	3	0	[1.0, 0.0, 0.0, 0.0, 0.0, 0.0]	0
1	0	3	[1.0, 0.0, 0.0]	5	1	[1.0, 0.0, 0.0]	2	1	[0.0, 1.0, 0.0, 0.0, 0.0, 0.0]	0
2	0	3	[1.0, 0.0, 0.0]	5	1	[1.0, 0.0, 0.0]	2	0	[1.0, 0.0, 0.0, 0.0, 0.0, 0.0]	0
3	0	5	[0.0, 1.0, 0.0]	4	1	[1.0, 0.0, 0.0]	2	1	[0.0, 0.0, 1.0, 0.0, 0.0, 0.0]	0
4	0	3	[1.0, 0.0, 0.0]	1	1	[1.0, 0.0, 0.0]	2	1	[0.0, 0.0, 0.0, 1.0, 0.0, 0.0]	0
281	1	2	[1.0, 0.0, 0.0]	7	1	[1.0, 0.0, 0.0]	2	0	[0.0, 0.0, 1.0, 0.0, 0.0, 0.0]	0
282	1	2	[1.0, 0.0, 0.0]	5	1	[1.0, 0.0, 0.0]	3	0	[0.0, 0.0, 1.0, 0.0, 0.0, 0.0]	1
283	1	5	[0.0, 1.0, 0.0]	5	1	[1.0, 0.0, 0.0]	1	1	[0.0, 0.0, 1.0, 0.0, 0.0, 0.0]	0
284	1	3	[0.0, 1.0, 0.0]	7	2	[1.0, 0.0, 0.0]	3	0	[1.0, 0.0, 0.0, 0.0, 0.0, 0.0]	0
285	1	4	[0.0, 1.0, 0.0]	7	2	[1.0, 0.0, 0.0]	3	0	[1.0, 0.0, 0.0, 0.0, 0.0, 0.0]	0

286 rows × 10 columns

Double check your encoded_samples_df here to make sure everything passes the sniff test!

Assuming it all looks good, the final step is to break up our DataFrame into individual samples, unpack the nested arrays into their constituent values, and concatenate everything together into a final sample vector...

```
In [58]: sample_list = list(encoded_samples_df.to_numpy())
```

```
In [59]: def unpack_nested_arrays(vec):
    final_vec = np.array([])

    for e in vec:
        if isinstance(e, int):
            e = np.array([e])
            final_vec = np.concatenate((final_vec, e))

        return final_vec

In [60]: final_vecs = []
    for e in sample list:
```

```
In [60]: final_vecs = []
for e in sample_list:
    final_vecs.append(unpack_nested_arrays(e))

final_vecs = np.array(final_vecs, dtype=int)
```

Great! The final_vecs variable should now point to a 286x19 numpy.ndarray containing all of our samples. Let's finally move on to the machine learning!

Step 2: Decision Tree

We'll run the decision tree process here again.

```
In [61]: def import_cancer_data(split=0.8, shuffle=True, CUTOFF=0, bins = 256):
    if shuffle:
        np.random.shuffle(final_vecs)

    num_samples = final_vecs.shape[0]
    num_train_samples = int(num_samples*split)

    train_data, test_data = final_vecs[:num_train_samples, :], final_vecs[num_train_samples:, :]

    X_train = train_data[:, 1:]
    y_train = train_data[:, 0]
    X_test = test_data[:, 1:]
    y_test = test_data[:, 0]

    print(X_train.shape)
    print(y_train.shape)
    return X_train, y_train, X_test, y_test
```

Here's the final fit/evaluation code again, but this time using the breast cancer data. You should get somewhere around 0.75 accuracy for the decision tree on this dataset — not 100%, but not too bad for the humble decision tree!

In [62]:	<pre>X_train, y_train, X_test, y_test = import_cancer_data(split=0.8)</pre>							
	<pre>tree = DecisionTree(K=3, verbose=False) tree.buildTree(X_train, y_train)</pre>							
	<pre>tree.homework_evaluate(X_train, y_train, X_test, y_test)</pre>							
	(228, 18) (228,) The decision tree is 63 percent accurate on 228 training data The decision tree is 77 percent accurate on 58 test data							
Out[62]:	0.7758620689655172							
In []:								
In []:								
In []:								