

Ques: Find a unit vector that makes an angle of $90^\circ, 135^\circ, 45^\circ$ with positive X, Y and Z axis respectively.

Soln : Given,

$$\alpha = 90^\circ,$$

$$\beta = 135^\circ,$$

$$\gamma = 45^\circ.$$

$$\text{i.e } l = \cos 90^\circ = 0, m = \cos 135^\circ = \frac{-1}{\sqrt{2}},$$

$$n = \cos 45^\circ = \frac{1}{\sqrt{2}}$$

$$\Rightarrow \vec{m} = \cos 90^\circ \cos 135^\circ \cos 45^\circ \quad (1)$$

Also, we know that,

$$\vec{m} = \frac{\vec{m}}{\|\vec{m}\|}$$

$$\|\vec{m}\| = \sqrt{0^2 + \left(\frac{-1}{\sqrt{2}}\right)^2 + \left(\frac{1}{\sqrt{2}}\right)^2}$$

$$\Rightarrow \|\vec{m}\| = 1 \quad (2)$$

Hence, from (1) and (2) we have the unit vector:

$$\vec{m} = 0 \frac{-1}{\sqrt{2}} \frac{1}{\sqrt{2}}$$