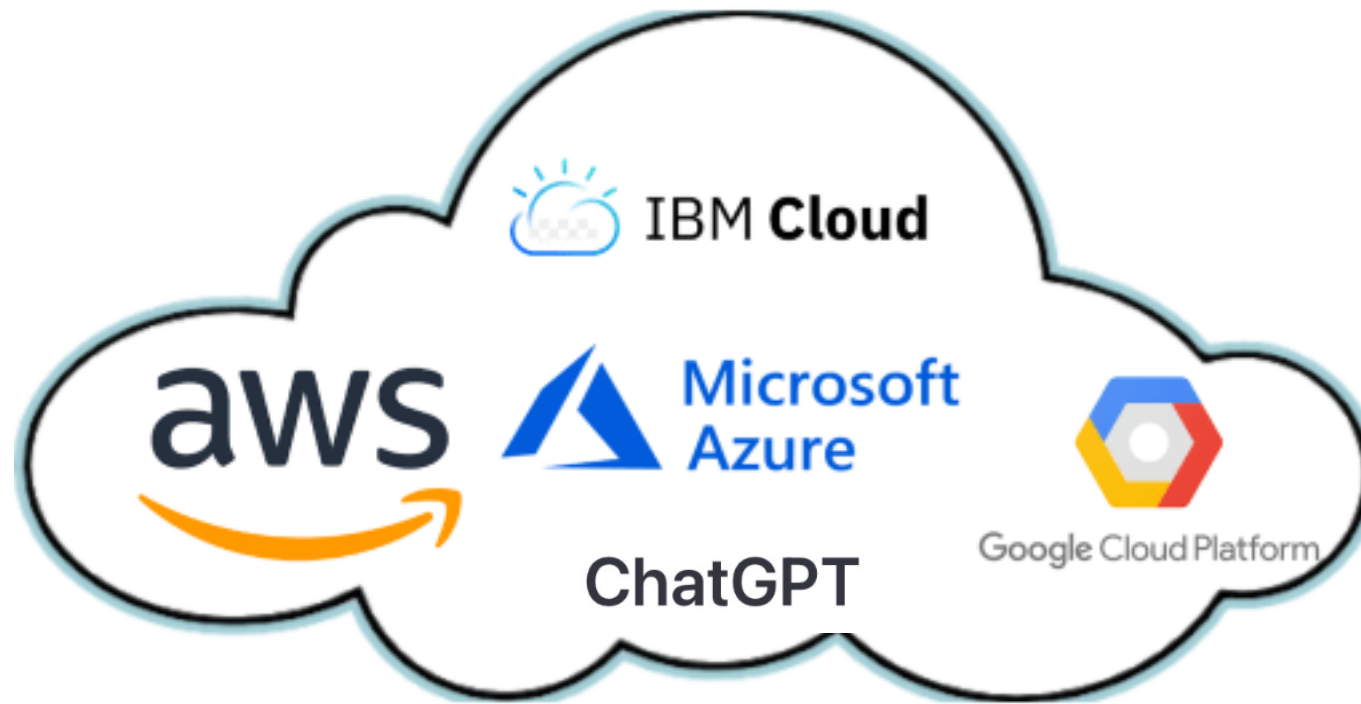


Homomorphic Evaluation of Convolutional Neural Networks

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October 25th, Università di Padova

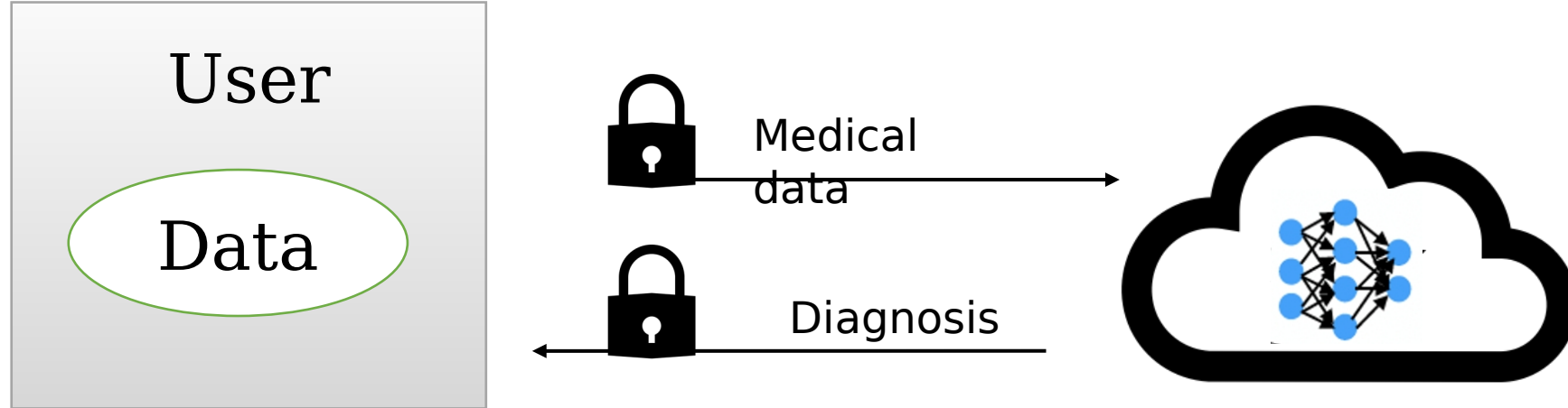
Machine Learning As a Service



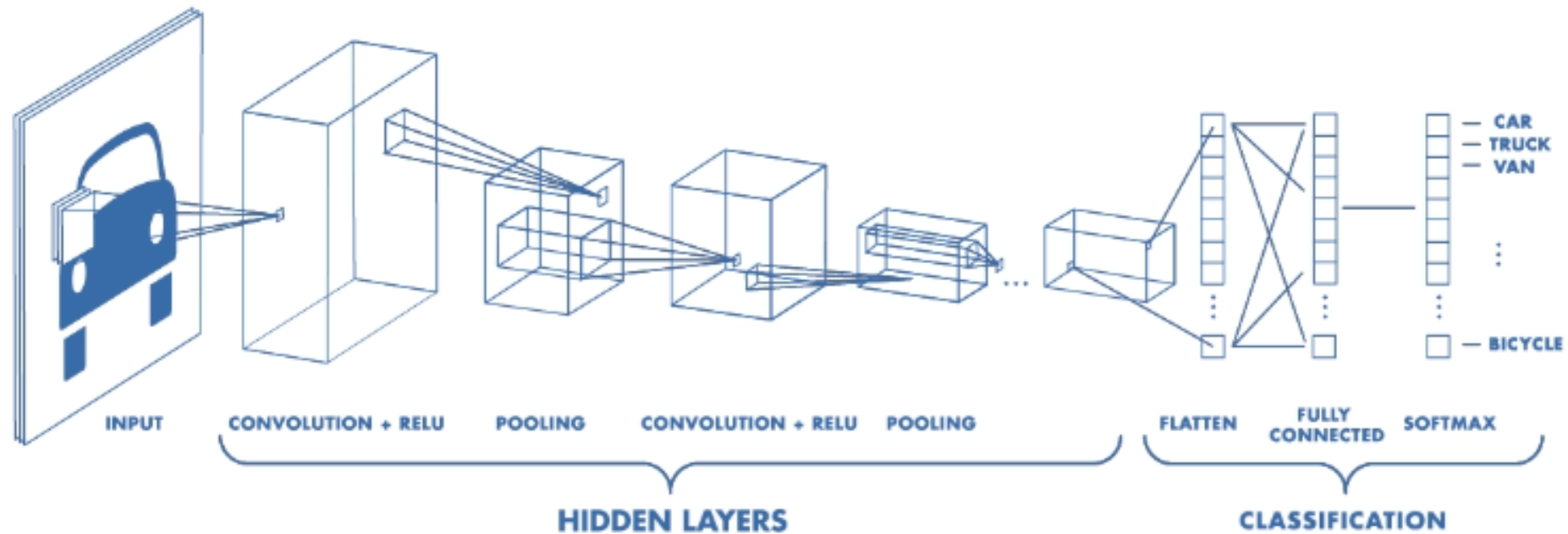
\$1.0 billion in 2019 □ \$8.48 billion by 2025*

**<https://neptune.ai/blog/machine-learning-as-a-service-what-it-is-when-to-use-it-and-what-are-the-best-tools-out-there>*

Privacy-Preserving Machine Learning



CNN



Activation function: ReLU, Max, sign, Sigmoid, etc.

Fully Homomorphic Encryption (FHE)

Given encrypted_data and a computation F , there exists an alternative F' s.t.

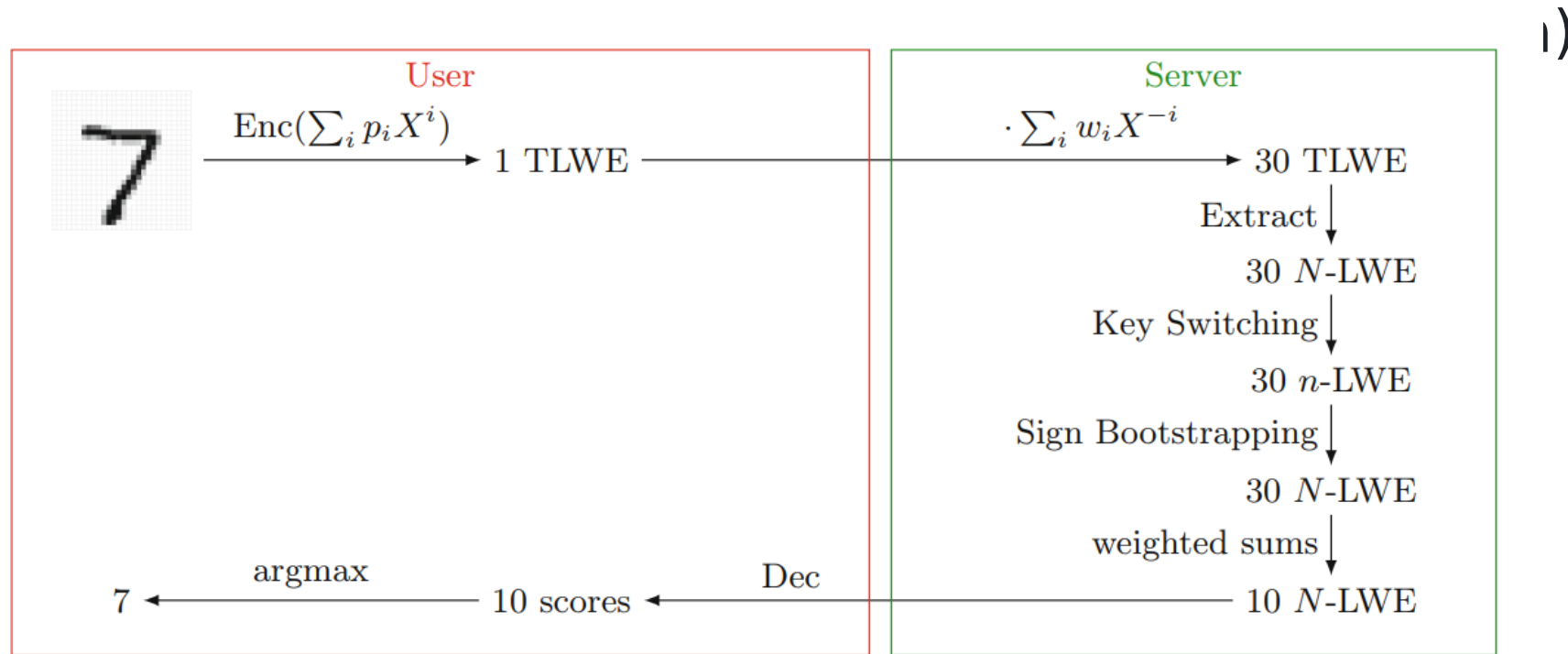


Fig. 1: homomorphic evaluation of a 784:30:10 neural network with activation function sign [Crypto 2018]

Prior Frameworks Are Not the Best

- From the activation function side
 - Only evaluate the sign function
 - Others are converted to polynomials
- From the message space side
 - Limited to 4-5 bits (eg. $[0,128] \rightarrow -1$, $[128,255] \rightarrow 1$)
- Batch
 - Not SIMD, only SISD

We Propose a New Framework

	Activation Func.	Large MSG Space (# of Boot, if yes)	Batch
[BMMP, Crypt`18]	Sign	✗	✗
[LMP, Asiacrypt`22]	Sign	✓ (2)	✗
[LW, EUROCRYPT`2 3]	Sign	✗	✓ (msg: 0/1)
Our work	Sign/Max/ReLU	✓ (1)	✓

Learning With Errors (LWE)

RSA: (discrete logarithm problem)

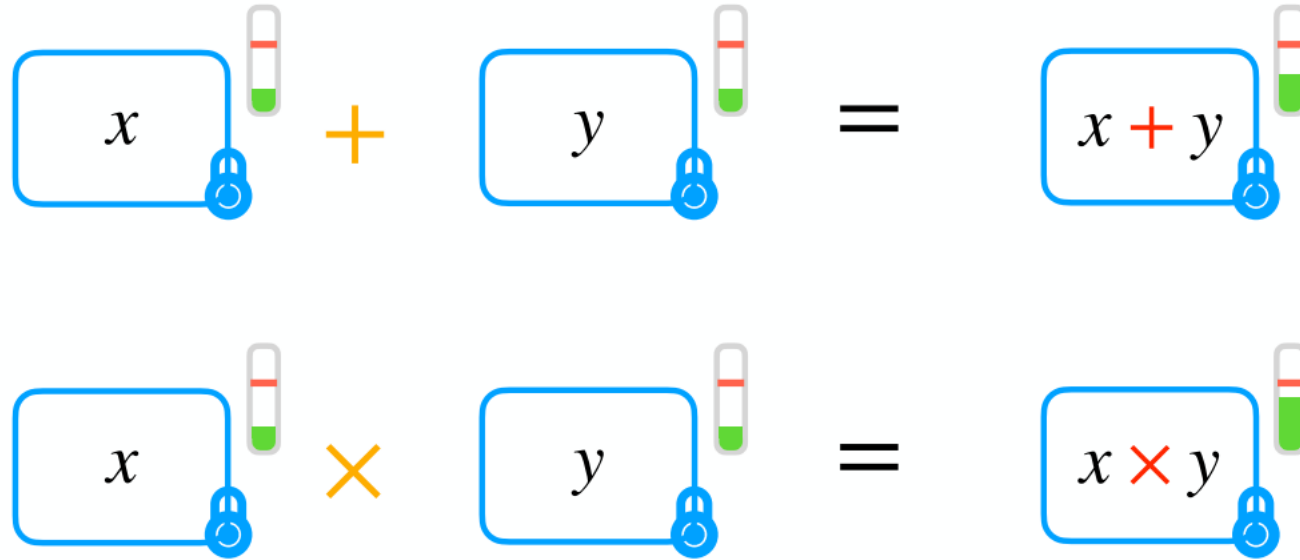
LWE hardness:

LWE encryption: $\text{mod } q$, msg space

decryption: $\text{mod } q$

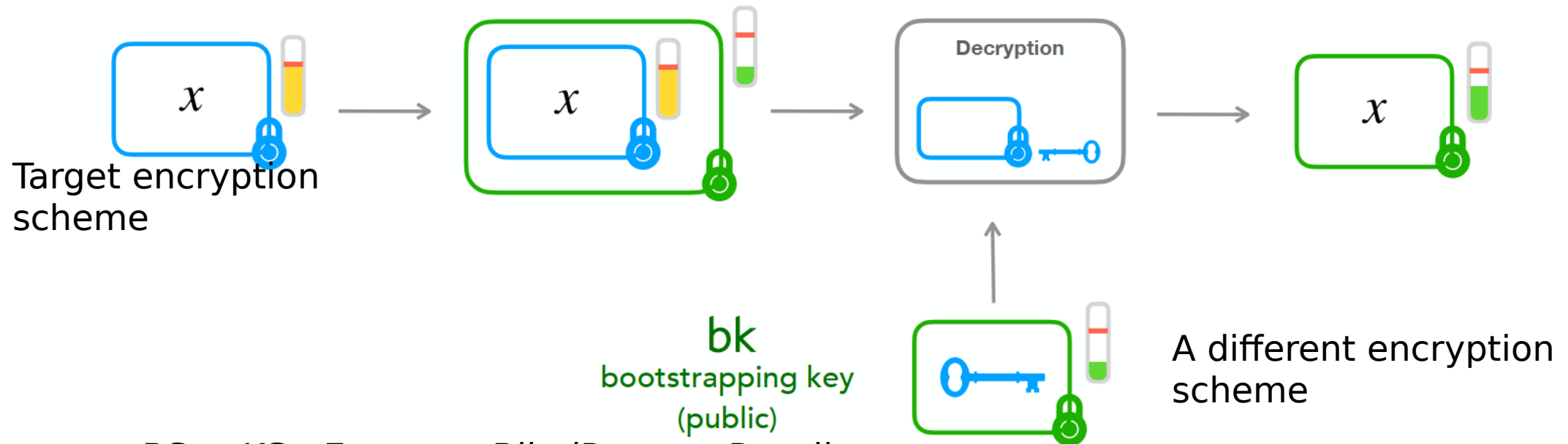
addition homomorphism:

Errors Increased After Homomorphic Operations



Noise grows too much 🌡️ \Rightarrow decryption incorrect 🚨

Bootstrapping [Gen09]



$BS = KS \circ Extract \circ BlindRotate$, Recall
BlindRotate - Linear part: with input
(*msb*)*Extract* - Nonlinear part: