

# WAVE MOTION & DOPPLER'S EFFECT

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## NEET SYLLABUS

Wave motion. Longitudinal and transverse waves, speed of wave motion. Displacement relation for a progressive wave. Principle of superposition of waves, reflection of waves, standing waves in strings and organ pipes, fundamental mode and harmonics. Beats. Doppler effect.

### **CHRISTIAN DOPPLER (1803 - 1853)**

Christian Doppler was an Austrian mathematician and physicist best known for articulating a principle known as the 'Doppler effect'. Christian Andreas Doppler was born on November 29, 1803, in Salzburg, Austria. Doppler studied philosophy in Salzburg, and mathematics and physics at the Vienna University of Technology and the University of Vienna. In 1842, Doppler gave a presentation at the Royal Bohemian Society of Sciences. The paper theorized that since the pitch of sound from a moving source varies for a stationary observer, the color of the light from a star should alter according to the star's velocity relative to Earth. This principle came to be known as the "Doppler effect". The Doppler effect has been used to support the Big Bang Theory and is often referenced in weather forecasting, radar and navigation.



### **PIERRE-SIMON LAPLACE (1749 - 1827)**

He was born on March 23, 1749 at Beaumont-en-Auge, Normandy, France. Pierre-Simon Laplace was a prominent French mathematical physicist and astronomer of the 19<sup>th</sup> century, who made crucial contributions in the arena of planetary motion by applying Sir Isaac Newton's theory of gravitation to the entire solar system. His work regarding the theory of probability and statistics is considered pioneering and has influenced a whole new generation of mathematicians. Laplace in 1816 was the first to point out that the speed of sound in air depends on the heat capacity ratio. Newton's original theory gave too low a value, because it does not take account of the adiabatic compression of the air which results in a local rise in temperature and pressure.



# WAVE THEORY, SOUND WAVES AND DOPPLER'S EFFECTS

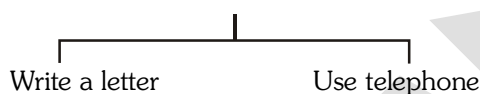
## 1. WAVE AND ITS CHARACTERISTICS

### 1.1 Introduction of Waves

**What is wave motion ?**

- When a particle moves through space, it carries KE with itself. Wherever the particle goes, the energy goes with it. (One way of transport energy from one place to another place).
- There is another way (wave motion) to transport energy from one part of space to other without any bulk motion of material together with it. Sound is transmitted in air in this manner.

**Ex.** You (in Kota) want to communicate your friend (in Delhi)



1<sup>st</sup> option involves the concept of particle & the second choice involves the concept of wave.

**Ex.** When you say "Namaste" to your friend no material particle is ejected from your lips to fall on your friend's ear. Basically you create some disturbance in the part of the air close to your lips. Energy is transferred to these air particles either by pushing them ahead or pulling them back. The density of the air in this part temporarily increases or decreases. These disturbed particles exert force on the next layer of air, transferring the disturbance to that layer. In this way, the disturbance proceeds in air and finally the air near the ear of the listener gets disturbed.

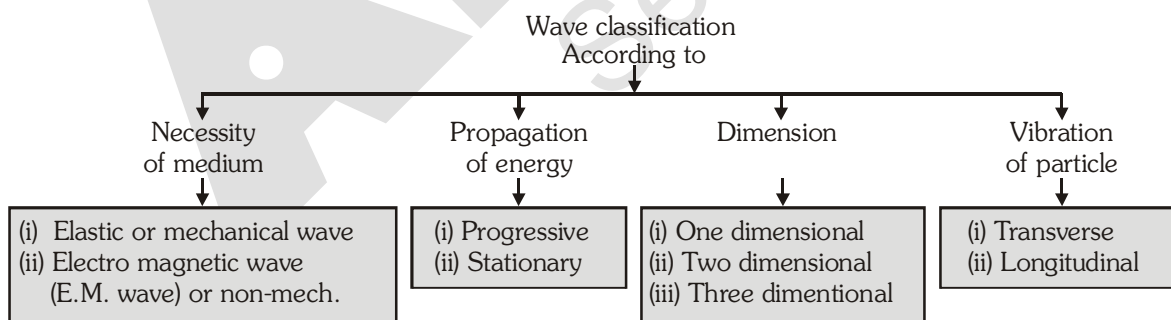
**Note :-** In the above example air itself does not move.

A **wave** is a disturbance that propagates in space, transports energy and momentum from one point to another without the transport of matter.

**Few examples of waves :**

The ripples on a pond (water waves), the sound we hear, visible light, radio and TV signals etc.

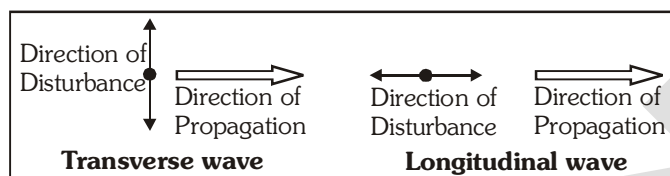
### 1.2 Classification of waves



- (i) Based on medium necessity :-** A wave may or may not require a medium for its propagation. The waves which do not require medium for their propagation are called non-mechanical, e.g. light, heat (infrared), radio waves etc. On the other hand the waves which require medium for their propagation are called mechanical waves. In the propagation of mechanical waves elasticity and density of the medium play an important role therefore mechanical waves are also known as **elastic waves**.

**Example :** Sound waves in water, seismic waves in earth's crust.

- (ii) **Based on energy propagation** :- Waves can be divided into two parts on the basis of energy propagation (i) Progressive wave (ii) Stationary waves. The progressive wave propagates with constant velocity in a medium. In stationary waves particles of the medium vibrate with different amplitude but energy does not propagate.
- (iii) **Based on direction of propagation** :- Waves can be one, two or three dimensional according to the number of dimensions in which they propagate energy. Waves moving along strings are one-dimensional. Surface waves or ripples on water are two dimensional, while sound or light waves from a point source are three dimensional.
- (iv) **Based on the motion of particles of medium** :



Waves are of two types on the basis of motion of particles of the medium.

- (i) Longitudinal waves
- (ii) Transverse waves

In the transverse wave the direction associated with the disturbance (i.e. motion of particles of the medium) is at right angle to the direction of propagation of wave while in the longitudinal wave the direction of disturbance is along the direction of propagation.

### 1.3 Transverse Wave Motion

Mechanical transverse waves are produced in such type of medium which have shearing property, so they are known as shear wave or S-wave

**Note** :- Shearing is the property of a body by which it changes its shape on application of force.

⇒ Mechanical transverse waves are generated

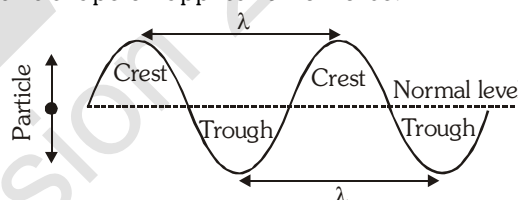
only in solids and surface of liquid.

Individual particles of the medium execute

SHM about their mean position in direction perpendicular to the direction of propagation of wave.

A **crest** is a portion of the medium, which is raised temporarily above the normal position of rest of particles of the medium, when a transverse wave passes.

A **trough** is a portion of the medium, which is depressed temporarily below the normal position of rest of particles of the medium, when a transverse wave passes.

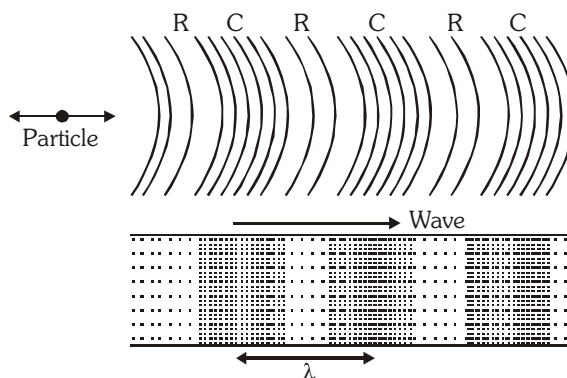


### 1.4 Longitudinal Wave Motion

In this type of waves, oscillatory motion of the medium particles produces regions of compression (high pressure) and rarefaction (low pressure) which propagated in space with time (see figure).

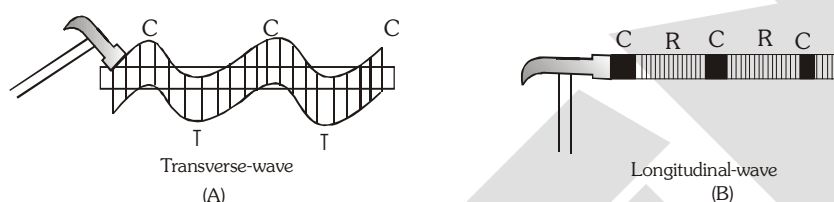
**Note** : The regions of high particle density are called compressions and regions of low particle density are called rarefactions.

The propagation of sound waves in air is visualized as the propagation of pressure or density fluctuations. The pressure fluctuations are of the order of 1 Pa, whereas atmospheric pressure is  $10^5$  Pa.



## 1.5 Mechanical Waves in Different Media

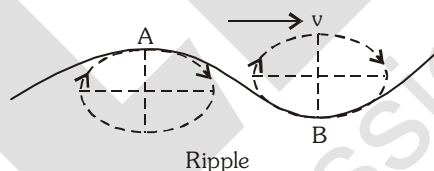
- A mechanical wave will be transverse or longitudinal depending on the nature of medium and mode of excitation.
- In strings, mechanical waves are always transverse when string is under a tension. In the bulk of gases and liquids mechanical waves are always longitudinal e.g. sound waves in air or water. This is because fluids cannot sustain shear.
- In solids, mechanical waves (may be sound) can be either transverse or longitudinal depending on the mode of excitation. The speed of the two waves in the same solid are different. (Longitudinal waves travels faster than transverse waves). e.g., if we struck a rod at an angle as shown in fig. (A) the waves in the rod will be transverse while if the rod is struck at the side as shown in fig. (B) or is rubbed with a cloth the waves in the rod will be longitudinal. In case of vibrating tuning fork waves in the prongs are transverse while in the stem are longitudinal.



Further more in case of seismic waves produced by Earthquakes both S (shear) and P (pressure) waves are produced simultaneously which travel through the rock in the crust at different speeds

$[v_s \cong 5 \text{ km/s while } v_p \cong 9 \text{ km/s}]$  S-waves are transverse while P-waves are longitudinal.

Some waves in nature are neither transverse nor longitudinal but a combination of the two. These waves are called 'ripple' and waves on the surface of a liquid are of this type. In these waves particles of the medium vibrate up and down and back and forth simultaneously describing ellipses in a vertical plane.



## 1.6 Characteristics of wave motion

- In wave motion, the disturbance travels through the medium due to repeated periodic oscillations of the particles of the medium about their mean positions.
- The energy is transferred from one place to another without any actual transfer of the particles of the medium.
- Each particle receives disturbance a little later than its preceding particle i.e., there is a regular phase difference between one particle and the next.
- The velocity with which a wave travels is different from the velocity of the particles with which they vibrate about their mean positions.
- The wave velocity remains constant in a given medium while the particle velocity changes continuously during its vibration about the mean position. It is maximum at mean position and zero at extreme position.
- For the propagation of a mechanical wave, the medium must possess the properties of inertia, elasticity and minimum friction among its particles.

## 1.7 Some important terms connected with wave motion

- **Wavelength ( $\lambda$ ) [length of one wave]**

Distance travelled by the wave during the time interval in which any one particle of the medium completes one cycle about its mean position. We may also define wavelength as the distance between any two nearest particles of the medium, vibrating in the same phase.

- **Frequency ( $n$ )** : Number of cycle (number of complete wavelengths) completed by a particle in unit time.

- **Time period ( $T$ )** : Time taken by wave to travel a distance equal to one wavelength.

- **Amplitude ( $A$ )** : Maximum displacement of vibrating particle from its equilibrium position.

- **Angular frequency ( $\omega$ )** : It is defined as  $\omega = \frac{2\pi}{T} = 2\pi n$

- **Phase** : Phase is a quantity which contains all information related to any vibrating particle in a wave. For equation  $y = A \sin (\omega t - kx)$ ;  $(\omega t - kx) = \text{phase}$ .

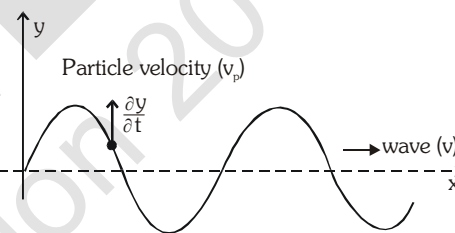
- **Angular wave number or propagation constant ( $k$ )** : It is defined as  $k = \frac{2\pi}{\lambda}$

- **Wave number ( $\bar{\nu}$ )** : It is defined as  $\bar{\nu} = \frac{1}{\lambda} = \frac{k}{2\pi} = \text{number of waves in unit length of the wave pattern}$ .

- **Particle velocity, wave velocity and particle's acceleration** : In plane progressive harmonic wave particles of the medium oscillate simple harmonically about their mean position. Therefore, all the formulae that we studied in SHM apply to the particles here also. For example, maximum particle velocity is  $\pm A\omega$  at mean position and it is zero at extreme positions. Similarly maximum particle acceleration is  $\pm \omega^2 A$  at extreme positions and zero at mean position. However the wave velocity is different from the particle velocity. This depends on certain characteristics of the medium. Unlike the particle velocity which oscillates simple harmonically (between  $+A\omega$  and  $-A\omega$ ) the wave velocity is constant for given characteristics of the medium.

- **Particle velocity in wave motion :**

The individual particles which make up the medium do not travel through the medium with the waves. They simply oscillate about their equilibrium positions. The instantaneous velocity of an oscillating particle of the medium, through which a wave is travelling, is known as "particle velocity".



- **Wave velocity** : The velocity with which the disturbance, or planes of equal phase (wave front), travel through the medium is called wave (or phase) velocity.

- **Relation between particle velocity and wave velocity :**

Wave equation :-  $y = A \sin (\omega t - kx)$ , Particle velocity  $v_p = \frac{\partial y}{\partial t} = A\omega \cos (\omega t - kx)$ .

$$\text{Wave velocity} = V = \frac{\lambda}{T} = \lambda \frac{\omega}{2\pi} = \frac{\omega}{k}, \quad \frac{\partial y}{\partial x} = -Ak \cos (\omega t - kx) = -\frac{A}{\omega} \omega k \cos (\omega t - kx) = -\frac{1}{V} \frac{\partial y}{\partial t} \Rightarrow \boxed{\frac{\partial y}{\partial x} = -\frac{1}{V} \frac{\partial y}{\partial t}}$$

**Note :**  $\frac{\partial y}{\partial x}$  represents the slope of the string (wave) at the point  $x$ .

Particle velocity at a given position and time is equal to negative of the product of wave velocity with slope of the wave at that point at that instant.

- **Particle velocity ( $v_p$ ) and acceleration ( $a_p$ ) in a sinusoidal wave :**

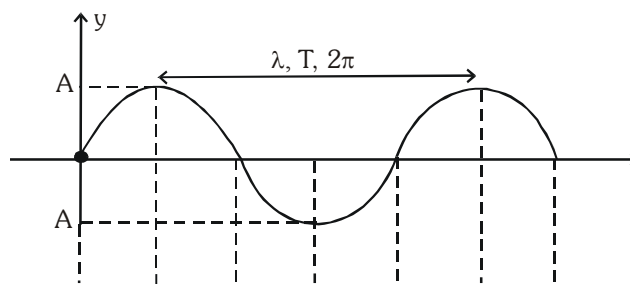
The acceleration of the particle is the second partial derivative of  $y(x, t)$  with respect to  $t$ ,

$$\therefore a_p = \frac{\partial^2 y(x, t)}{\partial t^2} = -\omega^2 A \sin(\omega t - kx) = -\omega^2 y(x, t)$$

i.e., the acceleration of the particle equals  $-\omega^2$  times its displacement, which is the same result we obtained for SHM. Thus,  $a_p = -\omega^2 (\text{displacement})$



• Relation between Phase difference, Path difference & Time difference



<b>Phase difference (<math>\Delta\phi</math>)</b>	0	$\frac{\pi}{2}$	$\pi$	$\frac{3\pi}{2}$	$2\pi$	$\frac{5\pi}{2}$	$3\pi$
<b>Path difference (<math>\Delta\lambda</math>)</b>	0	$\frac{\lambda}{4}$	$\frac{\lambda}{2}$	$\frac{3\lambda}{4}$	$\lambda$	$\frac{5\lambda}{4}$	$\frac{3\lambda}{2}$
<b>Time difference (<math>\Delta t</math>)</b>	0	$\frac{T}{4}$	$\frac{T}{2}$	$\frac{3T}{4}$	$T$	$\frac{5T}{4}$	$\frac{3T}{2}$

$$\Rightarrow \frac{\Delta\phi}{2\pi} = \frac{\Delta\lambda}{\lambda} = \frac{\Delta t}{T} \Rightarrow \text{Path difference} = \left( \frac{\lambda}{2\pi} \right) \text{Phase difference}$$

**GOLDEN KEY POINTS**

- A wave motion is a kind of disturbance which travels through a medium due to repeated periodic motion of the particles of the medium about their mean position, the motion being transferred continuously from particle to particle.
- Mechanical waves transmit energy but not the matter.
- The transmission of energy is possible due to two properties of the medium, the elasticity and the inertia.
- Material medium is necessary for the propagation of mechanical waves :
- If we generate waves in a medium continuously, the particles of the medium oscillate continuously. In this situation, the disturbance produced in the medium is called a progressive wave.
- When a progressive waves propagates in a medium, then, at any instant all the particles of the medium oscillate in the same way but the phase of oscillation changes from particle to particle.
- Equation of a plane progressive simple harmonic wave :  $y = a \sin \frac{2\pi}{\lambda} (Vt - x) = a \sin 2\pi \left( \frac{t}{T} - \frac{x}{\lambda} \right)$

Where  $V$  is the velocity of wave,  $\lambda$  is the wavelength of wave,  $a$  is the amplitude of the oscillation of particles of the medium and  $y$  is the instantaneous displacement of the particle located at  $x$  at instant  $t$ .

- Phase difference between two medium particle having a path difference  $\Delta\lambda$  is :

$$\Delta\phi = \frac{2\pi}{\lambda} \times \Delta\lambda \quad \text{If } \Delta\lambda = \lambda \quad \text{Then } \Delta\phi = 2\pi$$

- Also  $\Delta\phi = \frac{2\pi}{T} \times \Delta t \quad \text{If } \Delta t = T \quad \text{Then } \Delta\phi = 2\pi$

That is after one time period the phase of oscillation of a particle becomes the same as in the beginning.

## Illustrations

## Illustration 1.

Given below are some examples of wave motion. State in each case the wave motion is transverse, longitudinal or a combination of both :

- Motion of kink in a long coil spring produced by displacing one end of the spring side ways.
- Waves produced in a cylinder containing a liquid by moving its piston back and forth.
- Waves produced by a motorboat sailing in water.
- Ultrasonic waves in air produced by a vibrating quartz crystal.

## Solution

- |                                 |                  |
|---------------------------------|------------------|
| (a) Transverse and longitudinal | (b) Longitudinal |
| (c) Transverse and longitudinal | (d) Longitudinal |

## Illustration 2.

A progressive wave of frequency 500 Hz is travelling with a velocity of 360 m/s. How far apart are two points  $60^\circ$  out of phase.

## Solution

We know that for a wave  $v = f \lambda$  So  $\lambda = \frac{v}{f} = \frac{360}{500} = 0.72$  m

Phase difference  $\Delta\phi = 60^\circ = (\pi/180) \times 60 = (\pi/3)$  rad,

so path difference  $\Delta\lambda = \frac{\lambda}{2\pi} (\Delta\phi) = \frac{0.72}{2\pi} \times \frac{\pi}{3} = 0.12$  m

## Illustration 3.

On the average a human heart is found to beat 75 times in a minute. Calculate its beat frequency of heart and period.

## Solution

The beat frequency of heart =  $\frac{75}{60} = 1.25 = 1.25$  Hz

The time period  $T = \frac{1}{1.25} = 0.8$  s.

## Illustration 4.

A man generates a symmetrical pulse in a string by moving his hand up and down. At  $t = 0$  the point in his hand moves downward. The pulse travels with speed of 3 m/s on the string & his hands passes 6 times in each second from the mean position. Then the point on the string at a distance 3m will reach its upper extreme first time at time  $t =$

- (1) 1.25 sec.                      (2) 1 sec                      (3)  $\frac{13}{12}$  sec                      (4) none

## Solution

Ans. (1)

Frequency of wave =  $\frac{6}{2} = 3 \Rightarrow T = \frac{1}{3}$  s;  $\lambda = VT = (3) \left( \frac{1}{3} \right) = 1$  m

Total time taken =  $\frac{3}{3} + \frac{3T}{4} = 1.25$  sec

## BEGINNER'S BOX-1

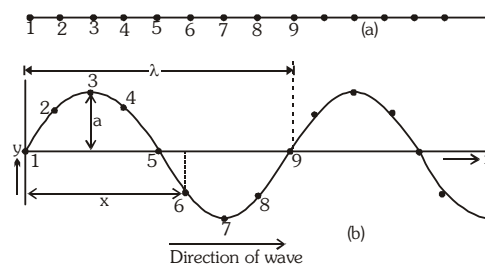
- A wave has a speed of 300 m/sec and frequency 500 Hz. The phase difference between two adjacent points is  $\pi/3$  radian. What will be the path difference between them ?
- A stone dropped from the top of a tower of height 300 m high splashes into the water of a pond near the base of the tower. When is the splash heard at the top, given that the speed of sound in air is  $340 \text{ m s}^{-1}$  ? ( $g = 9.8 \text{ ms}^{-2}$ )



## 2. PROGRESSIVE WAVE ON STRING

### 2.1 Equation of a Plane Progressive Wave

If, during propagation of wave in a medium, the particles of the medium perform simple harmonic motion then the wave is called a 'simple harmonic progressive wave'. Suppose, a simple harmonic progressive wave is propagating in a medium along the positive direction of the  $x$ -axis (from left to right). In fig. (a) the equilibrium positions of the particles 1, 2, 3 ..... are shown.



When the wave propagates, these particles oscillate about

their equilibrium positions. In Fig. (b) the instantaneous positions of these particles at a particular instant are shown. The curve joining these positions represents the wave. Let the time be counted from the instant when the particle 1 situated at the origin starts oscillating. If  $y$  be the displacement of this particle after  $t$  seconds, then  $y = a \sin \omega t \dots (i)$

where  $a$  is the amplitude of oscillation and  $\omega = 2\pi n$ , where  $n$  is the frequency. As the wave reaches the particles beyond the particle 1, the particles start oscillating. If the speed of the wave be  $v$ , then it will reach particle 6, distant  $x$  from the particle 1, in  $x/v$  sec. Therefore, the particle 6 will start oscillating  $x/v$  sec after the particle 1. It means that the displacement of the particle 6 at a time  $t$  will be the same as that of the particle 1 at a time  $x/v$  sec earlier i.e. at time  $t - (x/v)$ . The displacement of particle 1 at time  $t - (x/v)$  is equal to particle 6, distant  $x$  from the origin (particle 1), at time  $t$  which is given by

$$y = a \sin \omega \left( t - \frac{x}{v} \right) \quad \text{But } \omega = 2\pi n, y = a \sin (\omega t - kx) \quad \left( k = \frac{\omega}{v} \right) \dots (ii)$$

$$y = a \sin \left[ \frac{2\pi}{T} t - \frac{2\pi}{\lambda} x \right] \quad \text{Also } k = \frac{2\pi}{\lambda} \dots (iii) \quad y = a \sin 2\pi \left[ \frac{t}{T} - \frac{x}{\lambda} \right] \dots (iv)$$

This is the equation of a simple harmonic wave travelling along  $+x$  direction. If the wave is travelling along the  $-x$  direction, then there will be plus sign instead of minus sign inside the brackets in the above equations. For example, equation (iv) will be of the following form :  $y = a \sin 2\pi \left( \frac{t}{T} + \frac{x}{\lambda} \right)$ . If  $\phi$  be the initial phase difference between the above wave travelling along  $+x$  direction and an other wave, then the equation of other wave will be

$$y = a \sin \left\{ 2\pi \left( \frac{t}{T} - \frac{x}{\lambda} \right) \pm \phi \right\}$$

### 2.2 Velocity of Transverse Mechanical Waves

Velocity of a transverse wave propagating along a string having tension  $T$  and mass per unit length  $m$ , is given by  $V = \sqrt{\frac{T}{m}}$

If  $D$  is the diameter of the string,  $\ell$  is its length and  $\rho$  is its density, then

$$\Rightarrow m = \frac{\pi \left( \frac{D}{2} \right)^2 \ell \rho}{\ell} = \frac{\pi D^2 \rho}{4} \Rightarrow V = \sqrt{\frac{T}{\frac{\pi D^2 \rho}{4}}} = \frac{2}{D} \sqrt{\frac{T}{\pi \rho}}$$

**Wave always travel with respect to medium (not w.r.t. ground). Therefore any expression derived for the velocity of wave always gives velocity w.r.t. medium not w.r.t. ground.**

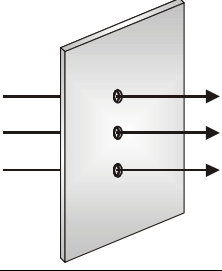
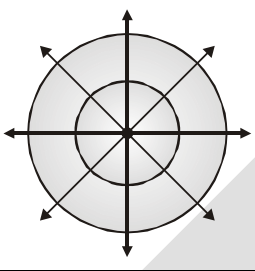
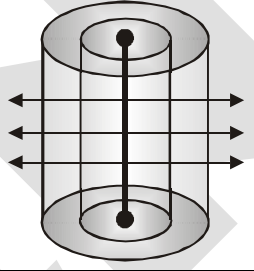
## 2.3 Intensity of Waves :

When waves incident perpendicularly on an imaginary surface (wavefront) then the max. energy of waves per unit area, per unit time is known as intensity of waves.

$$I = \frac{1}{2} \rho w^2 A^2 v \quad \frac{w}{m^2} \text{ or } \frac{J}{s - m^2}$$

when medium is fixed then  $I \propto w^2 A^2$

**Wave front** → An imaginary surface on which waves incident perpendicular & in same phase.

Wave front	Plane	Spherical	Cylindrical
			
Source	Source at infinite distance Sun, Torch, loud speaker	Point source (Bulb, small siren)	Linear source (tubelight)
Area of wavefront	$A = \ell \times b$ $A = \text{const.}$	$A = 4\pi r^2$ $A \propto r^2$	$A = 2\pi r \ell$ $A \propto r$
$I \propto \frac{1}{\text{Area}} \propto a^2$	$I = \text{constant}$	$I \propto \frac{1}{r^2} \propto a^2$	$I \propto \frac{1}{r} \propto a^2$
Variation during propagation	$a = \text{constant}$	$a \propto \frac{1}{r}$	$a \propto \frac{1}{\sqrt{r}}$
Equation	$y = a \sin(\omega t - kx)$  Plane progressive wave	$y = \frac{c}{r} \sin(\omega t - kr)$  Spherical progressive wave	$y = \frac{c'}{\sqrt{r}} \sin(\omega t - kr)$  Cylindrical progressive wave

## GOLDEN KEY POINTS

- Equation  $y = a \sin(\omega t - kx)$  represents displacement of all medium particles at any time 't', in other words it can give us displacement of any specific particle at each and every time so it is called as equation of progressive wave.
- Negative sign between  $\omega t$  and  $kx$  indicates that direction of propagation is positive.
- Positive sign between  $\omega t$  and  $kx$  indicates that direction of propagation is negative.

- For a plane progressive wave  $y = a \sin(\omega t - kx)$  producing transverse vibration show that  $\frac{\partial y}{\partial x} = -\frac{1}{V} \times \frac{\partial y}{\partial t}$   
**i.e. velocity of particle at a given point = (-) wave velocity  $\times$  slope of wave at that point.** (Slope of wave is also called as wave strain) and  $\frac{\partial^2 y}{\partial x^2} = \frac{1}{V^2} \frac{\partial^2 y}{\partial t^2}$  is known as differential equation of wave motion.

- Differential equation of harmonic progressive waves :**

$$\frac{\partial^2 y}{\partial t^2} = -A\omega^2 \sin(\omega t - kx) \Rightarrow \frac{\partial^2 y}{\partial x^2} = -Ak^2 \sin(\omega t - kx) \Rightarrow \frac{\partial^2 y}{\partial x^2} = \frac{1}{V^2} \frac{\partial^2 y}{\partial t^2}$$

- Relations :-**  $\omega = 2\pi n$ ,  $V = n\lambda$ ,  $k = \frac{2\pi}{\lambda}$ ,  $\omega = Vk$

- Intensity of wave (I) :-**

$$I = 2\pi^2 n^2 a^2 V \rho$$

$\rho \rightarrow$  density of medium

For Interference  $\rightarrow I \propto a^2$

For Beats  $\rightarrow I \propto n^2 a^2$

**Energy density (U) :-** Maximum wave energy per unit volume of medium

$$U = \frac{E_{\max}}{\text{vol}} = \frac{\frac{1}{2} M v_{\max}^2}{\text{vol}} = \frac{\frac{1}{2} \text{vol} \times \rho \times v_{\max}^2}{\text{vol}} = 2\pi^2 n^2 a^2 \rho \Rightarrow I = V \times U$$

## Illustrations

### Illustration 5.

The equation of a wave is,  $y(x, t) = 0.05 \sin \left[ \frac{\pi}{2} (10x - 40t) - \frac{\pi}{4} \right] \text{m}$

- Find :**
- The wavelength, the frequency and the wave velocity
  - The particle velocity and acceleration at  $x=0.5 \text{ m}$  and  $t=0.05 \text{ s}$ .

### Solution

- The equation may be rewritten as,  $y(x, t) = 0.05 \sin \left( 5\pi x - 20\pi t - \frac{\pi}{4} \right) \text{m}$

Comparing this with equation of plane progressive harmonic wave,

$y(x, t) = A \sin(kx - \omega t + \phi)$  we have,

$$\text{wave number } k = \frac{2\pi}{\lambda} = 5\pi \text{ rad/m} \quad \therefore \lambda = 0.4 \text{m}$$

$$\text{The angular frequency is, } \omega = 2\pi f = 20\pi \text{ rad/s} \quad \therefore f = 10 \text{Hz}$$

The wave velocity is,

$$V = f \lambda = \frac{\omega}{k} = 4 \text{ms}^{-1} \text{ in } +x \text{ direction}$$

- The particle velocity and acceleration are,

$$v_p = \frac{\partial y}{\partial t} = -(20\pi)(0.05) \cos \left( \frac{5\pi}{2} - \pi - \frac{\pi}{4} \right) = 2.22 \text{m/s}$$

$$a_p = \frac{\partial^2 y}{\partial t^2} = -(20\pi)^2 (0.05) \sin \left( \frac{5\pi}{2} - \pi - \frac{\pi}{4} \right) = 140 \text{ m/s}^2$$

**Illustration 6.**

For the travelling harmonic wave  $y(x, t) = 2 \cos 2\pi(10t - 0.0080x + 0.35)$

where  $x$  and  $y$  are in cm and  $t$  in s. Calculate the phase difference between oscillatory motion of two points separated by a distance of

- (a) 4m (b) 0.5m  
(c) half of wavelength (d) Third fourth of the wavelength

**Solution**

Given equation  $y = 2 \cos 2\pi(10t - 0.008x + 0.35) = 2 \cos(20\pi t - 0.016\pi x + 0.7\pi)$

compare with standard equation  $y = a \cos(\omega t - kx + \phi)$

$$k = 0.016\pi \text{ cm}^{-1}, \omega = 20\pi \text{ s}^{-1},$$

(a) When  $x = 4\text{m} = 400 \text{ cm}$  then phase difference  $= 0.016\pi \times 400 = 6.4\pi \text{ rad.}$

(b) When  $x = 0.5\text{m} = 50 \text{ cm}$  then phase difference  $= 0.016\pi \times 50 = 0.8\pi \text{ rad.}$

(c) When  $x = \frac{\lambda}{2}$  then phase difference  $= kx = \frac{2\pi}{\lambda} \times \frac{\lambda}{2} = \pi \text{ rad.}$

(d) When  $x = \frac{3\lambda}{4}$  then phase difference  $= kx = \frac{2\pi}{\lambda} \times \frac{3\lambda}{4} = \frac{3\pi}{2} \text{ rad.}$

**Illustration 7.**

Which of the following functions represent a travelling wave ?

- (a)  $(x - vt)^2$  (b)  $\ln(x + vt)$  (c)  $e^{-(x-vt)^2}$  (d)  $\frac{1}{x + vt}$

**Solution**

Although all the four functions are written in the form  $f(ax \pm bt)$ , only (c) among the four functions is finite everywhere at all times. Hence only (c) represents a travelling wave.

**Illustration 8.**

A progressive wave having amplitude 5 m and wavelength 3 m. If the maximum average velocity of particle in half time period is 5 m/s and wave is moving in the positive  $x$ -direction then find which may be the **correct** equation(s) of the wave? [where  $x$  in meter]

(1)  $5 \sin\left(\frac{2\pi}{5}t - \frac{2\pi}{3}x\right)$

(2)  $4 \sin\left(\frac{\pi t}{2} - \frac{2\pi}{3}x\right) + 3 \cos\left(\frac{\pi t}{2} - \frac{2\pi}{3}x\right)$

(3)  $5 \sin\left(\frac{\pi t}{2} - \frac{2\pi}{3}x\right)$

(4)  $3 \cos\left(\frac{2\pi}{5}t - \frac{2\pi}{3}x\right) - 4 \sin\left(\frac{2\pi}{5}t - \frac{2\pi}{3}x\right)$

**Solution**

**Ans. (2,3)**

$$\because \lambda = 3\text{m} \therefore k = \frac{2\pi}{\lambda} = \frac{2\pi}{3}$$

Maximum displacement in half time period  $= 2a = 10 \text{ m}$

$$\text{So maximum average velocity} = \frac{10}{T/2} = 5 \Rightarrow T = 4 \text{ s} \Rightarrow \omega = \frac{2\pi}{T} = \frac{2\pi}{4} = \frac{\pi}{2}$$

Illustration 9.

Two mechanical waves,  $y_1 = 2 \sin 2\pi (50t - 2x)$  &  $y_2 = 4 \sin 2\pi (ax + 100t)$  propagate in a medium with same speed.

- (1) The ratio of their intensities is 1 : 16  
(2) The ratio of their intensities is 1 : 4  
(3) The value of 'a' is 4 units  
(4) The value of 'a' is 2 units

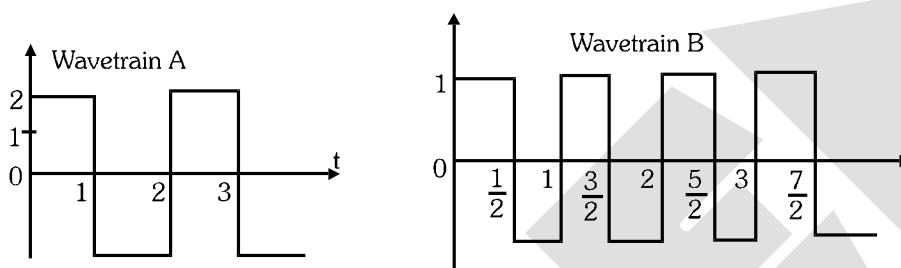
**Solution**

**Ans. (1,3)**

$$I = \frac{1}{2} \rho v \omega^2 A^2 \text{ and velocity} = \frac{\omega}{k}$$

Illustration 10.

Calculate the ratio of intensity of wavetrain A to wavetrain B.



**Solution**

$$\therefore I \propto a^2 n^2 \therefore \frac{I_A}{I_B} = \frac{a_A^2 n_A^2}{a_B^2 n_B^2} = \left(\frac{2}{1}\right)^2 \times \left(\frac{1}{2}\right)^2 = 1$$

Illustration 11.

A steel wire has a length of 12.0 m and a mass of 2.10 kg. What should be the tension in the wire so that speed of a transverse wave on the wire equals the speed of sound in dry air at  $20^\circ\text{C} = 343 \text{ ms}^{-1}$ .

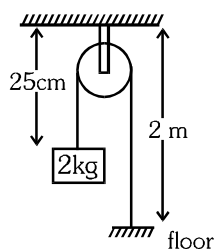
**Solution**

$$m = \frac{2.10}{12} = 0.175 \text{ kgm}^{-1} \quad \therefore \sqrt{\frac{T}{m}} = 343 \text{ ms}^{-1} \Rightarrow T = (343)^2 \times 0.175 = 2.06 \times 10^4 \text{ N}$$

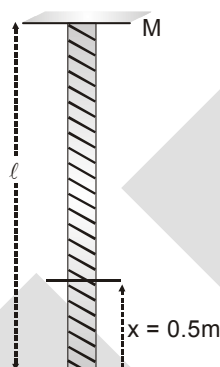
**BEGINNER'S BOX-2**

1. A travelling wave in stretched string is given by the equation :  $y = 40 \cos(3x - 5t)$  cm where t is in sec. Determine the maximum speed of particles of medium.
2. The displacement produced by a simple harmonic wave is  $y = \frac{10}{\pi} \sin\left(200\pi t - \frac{\pi x}{17}\right)$ . Then find the time period and maximum velocity of the particle. ( $x \rightarrow \text{m}$ ,  $y \rightarrow \text{cm}$ ,  $t \rightarrow \text{sec.}$ )
3. You have learnt that a travelling wave in one dimension is represented by a function  $y = f(x, t)$  where x and t must appear in the combination  $x - vt$  or  $x + vt$ , i.e.  $y = F(x \pm vt)$ . Is the converse true? Examine if the following functions for y can possibly represent a travelling wave :
  - (a)  $(x - vt)^2$
  - (b)  $\log [(x + vt)/x_0]$
  - (c)  $\exp [-(x + vt)/x_0]$
  - (d)  $1/(x + vt)$

4. In the given figure the string has mass 4.5 g. Find the time taken by a transverse pulse produced at the floor to reach the pulley. ( $g = 10 \text{ ms}^{-2}$ ).



5. A wave moves with speed  $300 \text{ ms}^{-1}$  on a wire which is under a tension of 500 N. Find how much the tension must be changed to increase the speed to  $360 \text{ ms}^{-1}$ .
6. A string of mass 2.50 kg is under a tension of 200 N. The length of the stretched string is 20.0 m. If the transverse jerk is struck at one end of the string, how long does the disturbance take to reach the other end?
7. A uniform rope of mass 0.1 kg and length 2.45 m hangs from a ceiling as shown in diagram.



- (a) find speed of transverse wave in the rope at a point 0.5 m distance from the lower end.
- (b) Calculate time taken by a transverse wave to travel the full length of rope.

### 3. SOUND WAVES & ITS CHARACTERISTICS

#### 3.1 Ultrasonic, Infrasonic and Audible Sound

Sound waves can be classified in three groups according to their range of frequencies.

##### Infrasonic Waves

Longitudinal waves having frequencies below 20 Hz are called infrasonic waves. They cannot be heard by human beings. They are produced during earthquakes. Infrasonic waves can be heard by snakes.

##### Audible Waves

Longitudinal waves having frequencies lying between 20-20,000 Hz are called audible waves.

##### Ultrasonic Waves

Longitudinal waves having frequencies above 20,000 Hz are called ultrasonic waves. They are produced and heard by bats. They have a large energy content.

##### Applications of Ultrasonic Waves

Ultrasonic waves have a large range of applications. Ultrasonic waves can be used –

- |  |   |
|--|---|
| (i) to detect fine internal cracks in metal.               | (ii) for determining the depth of the sea, lakes etc. |
| (iii) to detect submarines, icebergs etc.                  | (iv) to clean clothes, fine machinery parts etc.      |
| (v) to kill smaller animals like rats, fish and frogs etc. |   |

### • Equations of sound wave

A longitudinal mechanical wave can be described in two ways :

(A) Displacement wave form (B) Pressure wave form

**(A) Displacement wave form :-** When sound wave is described in term of longitudinal displacement suffered by particles of the medium, it is called displacement wave.

Which can be given by  $y = A \sin(\omega t - kx)$

**(B) Pressure wave form :-** When sound wave is described in term of excess pressure generated due to compression and rarefaction called pressure wave.

Which can be given by  $\Delta P = P_0 \cos(\omega t - kx)$

$P_0 = ABK$  where  $A$  = displacement of amplitude,  $B$  = Bulk modulus,  
 $K$  = propagation constant,  $P_0$  = Amplitude of pressure wave  
 $P$  = Pressure in sound wave

• The phase difference between pressure wave form and displacement wave form is  $90^\circ$  and path diff is  $\lambda/4$ . Displacement will be maximum when pressure is minimum and vice versa.

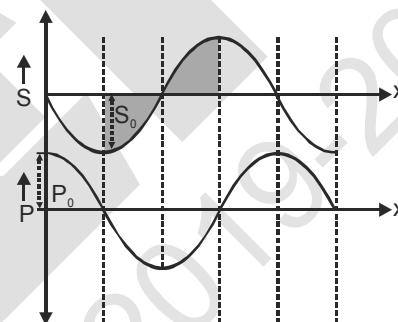
• When we consider the interference of sound as pressure wave then there is no change in phase when reflected from a "rigid boundary" but have a phase change of  $\pi$  when reflected from free end.

This is in contrast to reflection of displacement wave which have a phase change of  $\pi$  from a "rigid-end" and no change in phase from "free-end".

• A sound sensor-eg. ear, mike or listener, observer detects change in pressure. So in this case we prefer pressure wave.

• If detector is displacement sensor, we will prefer displacement wave.

• In stationary wave at the place of displacement node, pressure antinode will form and vice versa.



## 3.2 Speed of longitudinal (Sound) waves

**Newton Formula :**  $v_{\text{medium}} = \sqrt{\frac{E}{\rho}}$  (Use for every medium)

where  $E$  = Elasticity coefficient of medium &  $\rho$  = Density of medium

• **For solid medium :**  $v_{\text{solid}} = \sqrt{\frac{Y}{\rho}}$  where  $E = Y$  = Young's modulus of elasticity

• **For liquid medium :**  $v_{\text{liquid}} = \sqrt{\frac{B}{\rho}}$  where  $E = B$ , where  $B$  = volume elasticity coefficient of liquid

• **For gas medium :**

The formula for velocity of sound in air was first obtained by Newton. He assumed that when sound propagates through air temperature remains constant (i.e. the process is isothermal).



$$\text{so } E_{\text{TT}} = P \therefore v_{\text{air}} = \sqrt{(P/\rho)}$$

$$\text{At NTP for air } P = 1.01 \times 10^5 \text{ N/m}^2 \text{ and } \rho = 1.3 \text{ kg/m}^3 \text{ so } v_{\text{air}} = \sqrt{\frac{1.01 \times 10^5}{1.3}} = 279 \text{ m/s}$$

However, the experimental value of sound in air is 332 m/s which is much higher than that given by Newton's formula.

### • Laplace Correction

In order to remove the discrepancy between theoretical and experimental values of velocity of sound, Laplace modified Newton's formula assuming that propagation of sound in air is adiabatic process, i.e.

$$E_{\text{AD}} = \gamma P \text{ so that } v = \sqrt{\frac{\gamma P}{\rho}} \text{ i.e. } v = \sqrt{1.41} \times 279 = 331.3 \text{ m/s [as } \gamma_{\text{air}} = 1.41]$$

Which is in good agreement with the experimental value (332 m/s). This establishes that sound propagates adiabatically through gases.

The velocity of sound in air at NTP is 332 m/s which is much lesser than that of light and radio-waves ( $= 3 \times 10^8 \text{ m/s}$ ). This implies that –

- If we set our watch by the sound of a distant siren it will be slow.
- If we record the time in a race by hearing sound from starting point it will be lesser than actual.
- In a cloud-lightening, though light and sound are produced simultaneously but as  $c > v$ , light precedes thunder.

In case of gases –

$$v_s = \sqrt{\frac{\gamma P}{\rho}} = \sqrt{\frac{\gamma PV}{\text{mass}}} \left[ \text{as } \rho = \frac{\text{mass}}{\text{volume}} = \frac{M}{V} \right] \text{ or } v_s = \sqrt{\frac{\gamma \mu RT}{M}} \left[ \text{as } PV = \mu RT \right] \text{ or } v_s = \sqrt{\frac{\gamma RT}{M_w}}$$

$$\left[ \text{as } \mu = \frac{\text{mass}}{M_w} = \frac{M}{M_w} \text{ where } M_w = \text{Molecular weight} \right]$$

$$\text{And from kinetic-theory of gases } v_{\text{rms}} = \sqrt{(3RT/M_w)} \text{ So } \frac{v_s}{v_{\text{rms}}} = \sqrt{\frac{\gamma}{3}}$$

## 3.3 Effect of Various Quantities

### (a) Effect of temperature

$$\text{For a gas } \gamma \text{ \& } M_w \text{ is constant } v \propto \sqrt{T} \Rightarrow \frac{v_2}{v_1} = \sqrt{\frac{T_2}{T_1}} \Rightarrow \frac{v_t}{v_0} = \sqrt{\frac{t+273}{273}} \Rightarrow v_t = v_0 \left[ 1 + \frac{t}{273} \right]^{\frac{1}{2}}$$

By applying Binomial theorem.

$$\text{(i) For any gas medium } v_t = v_0 \left[ 1 + \frac{t}{546} \right] \quad \text{(ii) For air : } v_t = v_0 + 0.61t \text{ m/sec. (} v_0 = 332 \text{ m/sec.)}$$

### (b) Effect of Relative Humidity

With increase in humidity, density decreases so from  $v = \sqrt{\gamma(P/\rho)}$  we conclude that with rise in humidity velocity of sound increases. This is why sound travels faster in humid air (rainy season) than in dry air (summer) at same temperature. Due to this in rainy season the sound of factories siren and whistle of train can be heard more than summer.

(c) **Effect of Pressure**

$$\text{As velocity of sound } v = \sqrt{\frac{E}{\rho}} = \sqrt{\frac{\gamma P}{\rho}} = \sqrt{\frac{\gamma RT}{M_w}}$$

So pressure has no effect on velocity of sound in a gas as long as temperature remain constant. This is why while going up in the atmosphere, though both pressure and density decrease, velocity of sound remains constant as long as temperature remains constant. Further more it has also been established that all other factors such as amplitude, frequency, phase, loudness pitch, quality etc. has apparently no effect on velocity of sound.

Velocity of sound in air is measured by resonance tube or Hebb's method while in gases by Quinke's tube. Kundt's tube is used to determine velocity of sound in any medium solid, liquid or gas.

(d) **Effect of Motion of Air**

If air is blowing then the speed of sound changes. If the actual speed of sound is  $v$  and the speed of air is  $w$ , then the speed of sound in the direction in which air is blowing will be  $(v + w)$ , and in the opposite direction it will be  $(v - w)$ .

(e) **Effect of Frequency**

There is no effect of frequency on the speed of sound. Sound waves of different frequencies travel with the same speed in air although their wavelength in air are different. If the speed of sound were dependent on the frequency, then we could not have enjoyed orchestra.

### 3.4 Characteristics of Sound

Sound is characterised by the following three parameters :

**Loudness :-** The quality of sound on the basis of which, sound is said to be high or low. It depends on :

- (1) Shape & size of the source
- (2) Intensity of sound

⇒ According to **Weber - Fechner** the loudness of a sound of intensity  $I$  is given by:  $L \propto \log_{10} I$

Which is called Weber-Fechner law [unit of  $L$  is 'phon' It also measured in decibel]

$$\text{So } \Delta L = L_2 - L_1 = 10 \log_{10} \frac{I_2}{I_1}$$

For zero decibel Loudness, Intensity is called threshold of hearing.

In decibel the loudness of a sound of intensity  $I$  is given by  $L = 10 \log_{10} (I/I_0)$

Where  $I_0$  represents the threshold of hearing at 0 dB loudness level.

The loudness of a roaring lion is more than the sound produced by a mosquito.

**Range :**

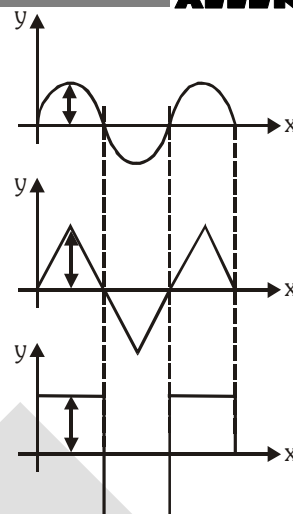
	Intensity	Loudness level
Threshold of hearing	$\approx 10^{-12}$	$\approx 0$ dB
Whispering	$10^{-11}$	10 dB
Normal Talk	$10^{-6}$	60 dB
Shout	$10^{-5}$	70 dB
non tolerable	1	above 120 dB

**Pitch :** It is the sensation received by the ear due to frequency and is the characteristic which distinguishes a shrill (or sharp) sound from a grave (or flat) sound. As pitch depends on frequency, higher the frequency higher will be the pitch and shriller will be the sound. For example

- (1) The buzzing of a bee or humming of a mosquito has high pitch but low loudness while the roar of a lion has large loudness but low pitch.
- (2) Due to more harmonics usually the pitch of female voice is higher than male.

**Quality (or timbre) :** It is the sensation received by the ear due to 'waveform'.

Two sounds of same intensity and frequency as shown in figure will produce different sensation on the ear if their waveforms are different. Now as waveform depends on overtones present, quality of sound depends on number of overtones, i.e., harmonics present and their relative intensities.



### GOLDEN KEY POINTS

- The density of a solid is much larger than that of a gas but the elasticity is larger by a greater factor. Hence longitudinal waves in a solid travel much faster than that in a gas.
- In a liquid the speed lies in between the two i.e.  $v_{\text{solid}} > v_{\text{liquid}} > v_{\text{gas}}$
- Speed of longitudinal waves in a solid rod :  $v = \sqrt{\frac{Y}{\rho}}$
- Speed of longitudinal waves in a liquid  $v = \sqrt{\frac{B}{\rho}}$  Where B is the bulk modulus of elasticity.
- The velocity of mechanical waves or sound waves in gases is given by :

$$v = \sqrt{\frac{\gamma P}{\rho}} \text{ where } P = \text{Pressure} \quad \rho = \text{Density}$$

$\gamma$  = ratio of specific heats of the gas at constant pressure and constant volume. This is known as Laplace's formula.

### Illustrations

#### Illustration 12.

Determine the change in volume of 6 liters of alcohol if the pressure is decreased from 200 cm of Hg to 75 cm. [velocity of sound in alcohol is 1280 m/s, density of alcohol = 0.81 gm/cc, density of Hg = 13.6 gm/cc and  $g = 9.81 \text{ m/s}^2$ ]

#### Solution

For propagation of sound in liquid  $v = \sqrt{\frac{B}{\rho}}$  i.e.,  $B = v^2 \rho$

But by definition  $B = -V \frac{\Delta P}{\Delta V}$

$$\text{So } -V \frac{\Delta P}{\Delta V} = v^2 \rho, \text{ i.e. } \Delta V = \frac{V(-\Delta P)}{\rho v^2}$$

Here  $\Delta P = H_2 \rho g - H_1 \rho g = (75 - 200) \times 13.6 \times 981 = -1.667 \times 10^6 \text{ dynes/cm}^2$

So  $\Delta V = \frac{(6 \times 10^3)(1.667 \times 10^6)}{0.81 \times (1.280 \times 10^5)^2} = 0.75 \text{ cc}$

### Illustration 13.

- (a) Speed of sound in air is 332 m/s at NTP. What will be the speed of sound in hydrogen at NTP if the density of hydrogen at NTP is (1/16) that of air.
- (b) Calculate the ratio of the speed of sound in neon to that in water vapour at any temperature. [Molecular weight of neon =  $2.02 \times 10^{-2} \text{ kg/mol}$  and for water vapours =  $1.8 \times 10^{-2} \text{ kg/mol}$ ]

### Solution

The velocity of sound in air is given by  $v = \sqrt{\frac{E}{\rho}} = \sqrt{\frac{\gamma P}{\rho}} = \sqrt{\frac{\gamma RT}{M_w}}$

(a) In terms of density and pressure  $\frac{v_H}{v_{\text{air}}} = \sqrt{\frac{P_H}{\rho_H} \times \frac{\rho_{\text{air}}}{P_{\text{air}}}} = \sqrt{\frac{\rho_{\text{air}}}{\rho_H}}$  [as  $P_{\text{air}} = P_H$ ]

$\Rightarrow v_H = v_{\text{air}} \times \sqrt{\frac{\rho_{\text{air}}}{\rho_H}} = 332 \times \sqrt{\frac{16}{1}} = 1328 \text{ m/s}$

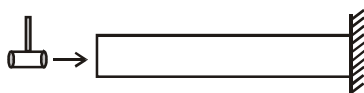
(b) In terms of temperature and molecular weight  $\frac{v_{\text{Ne}}}{v_W} = \sqrt{\frac{\gamma_{\text{Ne}}}{\gamma_W} \times \frac{M_W}{M_{\text{Ne}}}}$  [as  $T_{\text{Ne}} = T_W$ ]

Now as neon is mono atomic ( $\gamma = 5/3$ ) while water vapours poly atomic ( $\gamma = 4/3$ ) so

$\frac{v_{\text{Ne}}}{v_W} = \sqrt{\frac{(5/3) \times 1.8 \times 10^{-2}}{(4/3) \times 2.02 \times 10^{-2}}} = \sqrt{\frac{5}{4} \times \frac{1.8}{2.02}} = 1.055$

### BEGINNER'S BOX-3

1. A 1000 m long rod of density  $10.0 \times 10^4 \text{ kg/m}^3$  and having young's modulus  $Y = 10^{11} \text{ Pa}$ , is clamped at one end. It is hammered at the other free end as shown in the figure. The longitudinal pulse goes to right end, gets reflected and again returns to the left end. How much time (in sec) the pulse will take to go back to initial point?



2. If the bulk modulus of water is 4000 MPa, what is the speed of sound in water?
3. The minimum intensity of audibility of sound is  $10^{-12} \text{ watt/m}^2$ . If the intensity of sound is  $10^{-9} \text{ watt/m}^2$ , then calculate the intensity level of this sound in decibels.
4. Sound can be heard at great distances after rainfall. Explain.

5. A sound wave is propagating in given gaseous medium then plot graph between

- (a)  $v_{\text{gas}}$  &  $T$
- (b)  $v_{\text{gas}}$  &  $P$
- (c)  $v_{\text{gas}}$  &  $\sqrt{T}$

[ $v_{\text{gas}}$  = Speed of sound,  $P$  = Pressure,  $T$  = Temperature] Also write down proper units on axis.

6. Why are temple bells made of large size?

7. Explain why sound travels faster in warm air than in cool air?

8. Explosion on other planets are not heard on earth. Explain why?

9. Calculate velocity of sound in mixture of 1 mole He and 1 mole  $O_2$  at  $127^\circ\text{C}$ .

10. Use the formula  $v = \sqrt{\frac{\gamma P}{\rho}}$  to explain why the speed of sound in air

(a) is independent of pressure.

(b) increases with temperature.

(c) increases with humidity.

## 4. PRINCIPLE OF SUPERPOSITION OF WAVES

### 4.1 Superposition of Waves

Two or more waves can traverse the same medium without affecting the motion of one another. If several waves propagate in a medium simultaneously, then the resultant displacement of any particle of the medium at any instant is equal to the vector sum of the displacements produced by individual wave. The phenomenon of intermixing of two or more waves to produce a new wave is called Superposition of waves. Therefore according to superposition principle.

The resultant displacement of a particle at any point of the medium, at any instant of time is the vector sum of the displacements caused to the particle by the individual waves.

If  $\vec{y}_1, \vec{y}_2, \vec{y}_3, \dots$  are the displacement of particle at a particular time due to individual waves, then the resultant displacement is given by  $\vec{y} = \vec{y}_1 + \vec{y}_2 + \vec{y}_3 + \dots$

Principle of superposition holds for all types of waves, i.e., mechanical as well as electromagnetic waves. But this principle is not applicable to the waves of very large amplitude.

Due to superposition of waves the following phenomenon can be seen

1. **Interference** : Superposition of two waves having equal frequency and nearly equal amplitude.
2. **Beats** : Superposition of two waves of nearly equal frequency in same direction.
3. **Stationary waves** : Superposition of equal waves from opposite direction.
4. **Lissajous' figure** : Superposition of perpendicular waves.

### 4.2 Interference

When two coherent waves of same frequency propagate in same direction and superimpose on one another then the intensity of resultant wave becomes maximum at some points and at some points it becomes minimum. This phenomena of intensity variation w.r.t. position is known as interference.

#### Coherent Waves :

Two waves are said to be coherent if their phase difference does not depend on time.

(a) **Mathematical Analysis**

First wave  $\Rightarrow Y_1 = a_1 \sin(\omega t + \phi_1)$

Second wave  $\Rightarrow Y_2 = a_2 \sin(\omega t + \phi_2)$

$\Delta\phi$  = phase difference =  $\phi_1 - \phi_2$

For Ist  $I_1 \propto a_1^2$

For IInd  $I_2 \propto a_2^2$

From superposition

Resultant wave =  $y = y_1 + y_2$ ,  $y = A \sin(\omega t + \theta)$

$I \rightarrow I_1 \propto a_1^2 \Rightarrow I_1 = K a_1^2$

$I_2 \propto a_2^2 \Rightarrow I_2 = K a_2^2$

$I \propto A^2 \Rightarrow I = K A^2$

$$A^2 = a_1^2 + a_2^2 + 2a_1a_2 \cos \Delta\phi \Rightarrow I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \Delta\phi$$

(b) **Types of Interference**

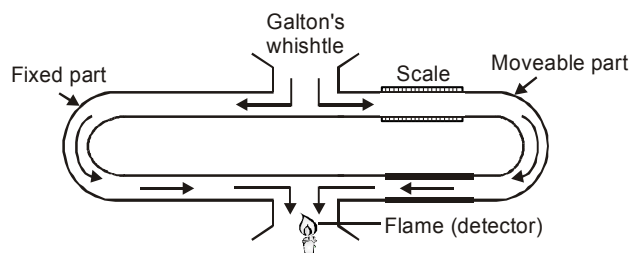
$$A^2 = a_1^2 + a_2^2 + 2a_1a_2 \cos \Delta\phi, \quad I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \Delta\phi$$

<b>Constructive Interference :</b> Same Phase [Maxima]	<b>Destructive Interference :</b> Opposite Phase [Minima]
$\Rightarrow$ If $\cos \Delta\phi = +1 \Rightarrow$ then $I_{\max}$ & $A_{\max}$ therefore phase difference $\Delta\phi = 0, 2\pi, 4\pi, 6\pi, \dots, 2N\pi$ $(N = 0, 1, 2, \dots)$ and Path difference $\Delta\lambda = 0, \lambda, 2\lambda, 3\lambda, \dots, N\lambda$ $(N = 0, 1, 2, \dots)$ So $A_{\max} = a_1 + a_2$ and $I_{\max} = I_1 + I_2 + 2\sqrt{I_1 I_2}$ or $I_{\max} = (\sqrt{I_1} + \sqrt{I_2})^2$ and obviously $I_{\max} > I_1 + I_2$ or $I_{\max} \propto (a_1 + a_2)^2$	$\Rightarrow$ If $\cos \Delta\phi = -1 \Rightarrow$ then $I_{\min}$ & $A_{\min}$ therefore phase difference $\Delta\phi = \pi, 3\pi, 5\pi, 7\pi, \dots, (2N+1)\pi$ $(N = 0, 1, 2, \dots)$ and path difference $\Delta\lambda = \lambda/2, 3\lambda/2, 5\lambda/2, \dots, (2N+1)\lambda/2$ $(N = 0, 1, 2, \dots)$ Put the value of $\Delta\phi$ in the formula $A_{\min} = a_1 - a_2$ and $I_{\min} = I_1 + I_2 - 2\sqrt{I_1 I_2}$ or $I_{\min} = (\sqrt{I_1} - \sqrt{I_2})^2$ obviously $I_{\min} < I_1 + I_2$ , $I_{\min} \propto (a_1 - a_2)^2$

If path difference is zero then maxima is obtained, if path difference is  $\lambda/2$  then minima and if path difference is  $\lambda$  then maxima. If path difference is  $3\lambda/2$  then minima. So the distance between to consecutive maximum or to consecutive minima is  $\lambda$ .

(c) **Quincke's Tube :-**

- It gives practical proof of interference of sound.
- Quincke's tube is practical method for finding the speed of sound in gaseous medium.
- As we slide movable part of tube by  $\ell$  unit, path difference will become  $2\ell$  so  $\Delta x = 2\ell$ .

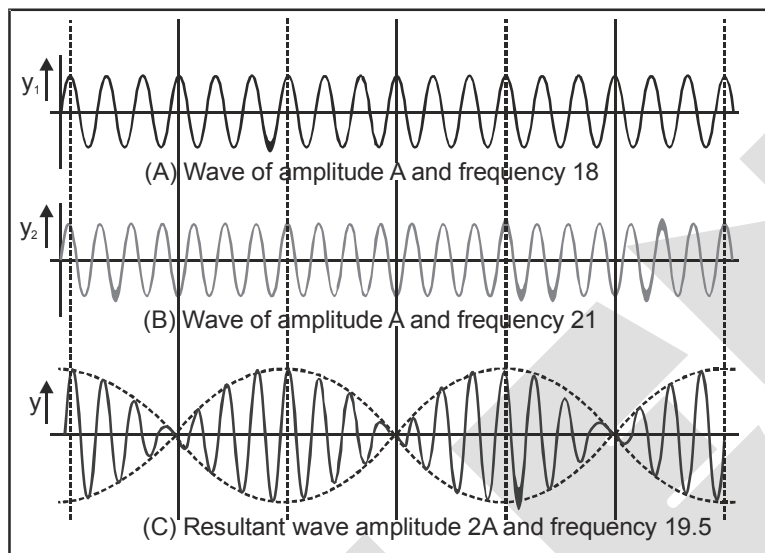


- If vibration in flame becomes **maximum** to **minimum** or **minimum** to **maximum** then  $\Delta x = \frac{\lambda}{2} = 2\ell$
- If vibration in flame becomes **minimum** to **minimum** or **maximum** to **maximum** then  $\Delta x = \lambda = 2\ell$

- (4) Quincke tube is used as a sound filter.  
 (5) Galton's whistle produces ultrasonic waves.

### 4.3 Beats

When two sound waves of nearly equal (but not exactly equal) frequencies travel in same direction, at a given point due to their superposition, intensity alternatively increases and decreases periodically. This periodic waxing and waning of sound at a given position is called beats.



1. **Condition:** Two waves of approximately equal frequency propagate in same direction

Time	$n_1 = 12 \text{ Hz}$	$n_2 = 10 \text{ Hz}$	Diff. of vibration	phase diff.	Intensity	Remarks
0 sec.	0	0	0	0	Max.	
$\frac{1}{4}$ sec.	3	2.5	0.5	$\pi$	Min.	
$\frac{1}{2}$ sec.	6	5	1	$2\pi$	Max.	Ist Beat
$\frac{3}{4}$ sec.	9	7.5	1.5	$3\pi$	Min.	
1 sec.	12	10	2	$4\pi$	Max.	IInd Beat
Beat frequency (b) = $n_1 - n_2$ ( $\sim$ = positive difference)						

2. **Mathematical analysis :**

$$\text{I} \longrightarrow y_1 = a \sin \omega_1 t = a \sin 2\pi n_1 t$$

$$\text{II} \longrightarrow y_2 = a \sin \omega_2 t = a \sin 2\pi n_2 t$$

For superposition

$$y = y_1 + y_2 = a \{ \sin 2\pi n_1 t + \sin 2\pi n_2 t \} = a \left\{ 2 \sin 2\pi \frac{(n_1 + n_2)t}{2} \cos 2\pi \frac{(n_1 - n_2)t}{2} \right\}$$

$$y = \left[ 2a \cos 2\pi \frac{(n_1 - n_2)t}{2} \right] \sin 2\pi \frac{(n_1 + n_2)t}{2}$$

$$y = A \sin 2\pi n' t \quad \text{Resultant wave} = y = A \sin 2\pi n' t \quad \text{Amplitude } A = 2a \cos 2\pi \frac{(n_1 - n_2)t}{2}$$

$$\text{Frequency of resultant wave} \Rightarrow n' = (n_1 + n_2)/2$$



**GOLDEN KEY POINTS**

- Superposition phenomena is applicable for all types of waves.
- For the resultant wave in interference phenomenon frequency, wavelength & velocity is identical to initial or superposing waves but, its amplitude and initial phase is changed.
- Superposition phenomena applicable for all vector quantities.

$$\frac{I_{\max}}{I_{\min}} = \left( \frac{\sqrt{I_1} + \sqrt{I_2}}{\sqrt{I_1} - \sqrt{I_2}} \right)^2 = \frac{(a_1 + a_2)^2}{(a_1 - a_2)^2} \text{ and } \frac{I_1}{I_2} = \left( \frac{a_1}{a_2} \right)^2$$

- Average intensity of interference pattern

$$I_{\text{av}} \text{ or } \langle I \rangle = \frac{I_{\max} + I_{\min}}{2} \quad \text{or} \quad I_{\text{av}} = I_1 + I_2$$

$I_{\text{av}}$  = Sum of intensities of individual waves

- **Degree of Interference pattern (f)** = f represents contrast effect (clarity of interference pattern)

$$f = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}} \times 100\%$$

- Conditions for perfect interference

$$\text{If } a_1 = a_2 = a \text{ and } I_1 = I_2 = I \quad I_{\max} = 4I \quad I_{\min} = 0$$

$$\frac{I_{\max}}{I_{\text{av}}} = \frac{2}{1} \Rightarrow I_{\text{av}} = 2I \quad f_{\max} = 1 \text{ (unity)} = 100\%$$

- Above formulae and Results also apply to interference of light.
- Frequency of resultant wave =  $\frac{(n_1 + n_2)}{2}$ , beats frequency or freq of intensity variation =  $n_1 \sim n_2$   
Frequency of amplitude variation =  $\frac{n_1 \sim n_2}{2}$
- When source of higher frequency execute one vibration more than source of lower frequency, one beat is formed.  
 $2\pi \equiv T$  (one oscillation difference)
- No. of Beats formed per sec is known as Beat frequency and time taken to complete one beat is known as beat time period.

- **Interference :-** Permanent intensity pattern and it is the function of position [ $I = f(x)$ .]

**Beats :-** Temporary intensity pattern and it is the function of time [ $I = f(t)$ ]

- Periodic vibration in the intensity (or amplitude) of sound due to superposition of two sound waves of slightly different frequencies are called beats.
- To hear beats, the number of beats per second should not be more than ten beats per sec. ( $n_1 \sim n_2 < 10$ )
- Filing the prongs of tuning fork raises the frequency and loading decreases the frequency.
- **Vibration of tuning fork :** when tuning fork is sounded by striking its one end on rubber pad, then the ends of prongs vibrate in and out while the stem vibrates up and down or vibration of the prongs are transverse and that of the stem is longitudinal. Generally tuning fork produces fundamental tone.



**Illustration 19.**

Three simple harmonic waves, identical in frequency  $n$  and amplitude  $A$  moving in the same direction are superimposed in air in such a way, that the first, second and the third wave have the phase angles  $\phi, \phi + \frac{\pi}{2}$  and  $(\phi + \pi)$  respectively at a given point  $P$  in the superposition.

Then as the waves progress, the superposition will result in

- (1) a periodic, non-simple harmonic wave of amplitude  $3A$
- (2) a stationary simple harmonic wave of amplitude  $3A$
- (3) a simple harmonic progressive wave of amplitude  $A$
- (4) the velocity of the superposed resultant wave will be the same as the velocity of each wave

**Solution**

**Ans. (3,4)**

Since the first wave and the third wave moving in the same direction have the phase angles  $\phi$  and  $(\phi + \pi)$ , they superpose with opposite phase at every point of the vibrating medium and thus cancel out each other, in displacement, velocity and acceleration. They, in effect, destroy each other out. Hence we are left with only the second wave which progresses as a simple harmonic wave of amplitude  $A$ . The velocity of this wave is the same

**Illustration 20.**

Two vibrating tuning forks produce progressive waves given by  $y_1 = 4 \sin(500\pi t)$  and  $y_2 = 2 \sin(506\pi t)$ . These tuning forks are held near the ear of a person. The person will hear  $\alpha$  beats/s with intensity ratio between maxima and minima equal to  $\beta$ . Find the value of  $\beta - \alpha$ .

**Solution**

**Ans. 6**

$$y_1 = 4 \sin(500\pi t) \quad y_2 = 2 \sin(506\pi t)$$

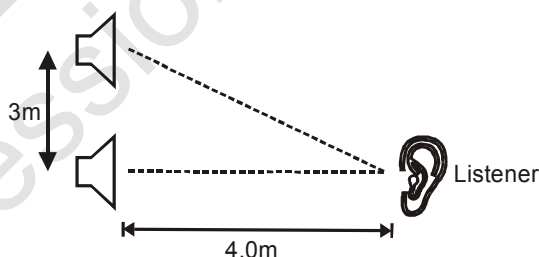
$$\text{Number of beats} = 253 - 250 = 3 \text{ beat/sec} \Rightarrow \alpha = 3 \text{ beats/sec}$$

$$\text{As } I_1 \propto (16) \text{ and } I_2 \propto 4 \Rightarrow \frac{I_{\max}}{I_{\min}} = \frac{(\sqrt{I_1} + \sqrt{I_2})^2}{(\sqrt{I_1} - \sqrt{I_2})^2} \Rightarrow \left(\frac{4+2}{4-2}\right)^2 = \left(\frac{6}{2}\right)^2 = 9 \Rightarrow \beta = 9$$

$$\text{So } \beta - \alpha = 9 - 3 = 6$$

**Illustration 21.**

Two loudspeakers as shown in fig. below separated by a distance 3 m, are in phase. Assume that the amplitudes of the sound from the speakers is approximately same at the position of a listener, Who is at a distance 4.0 m in front of one of the speakers. For what frequencies does the listener hear minimum signal? Given that the speed of sound in air is  $330 \text{ ms}^{-1}$ .



**Solution**

$$\text{The distance of the listener from the second speaker} = \sqrt{(3)^2 + (4)^2} = \sqrt{25} = 5 \text{ m}$$

$$\text{path difference} = (5 - 4.0) \text{ m} = 1 \text{ m}$$

$$\text{For fully destructive interference } 1 \text{ m} = (2m + 1)\lambda/2$$

$$\text{Hence } \lambda = 2/(2m + 1) \text{ m}$$

The corresponding frequencies are given by

$$n = [330 \times (2m + 1)]/2 \text{ s}^{-1}, \text{ for } m = 0, 1, 2, 3, 4, \dots$$

$$= 165 (2m + 1) \text{ s}^{-1}, \text{ for } m = 0, 1, 2, 3, 4, \dots$$

Therefore the frequencies for which the listener would hear a minimum intensity 165 Hz, 495 Hz, 825 Hz, .....

**Illustration 22.**

Two plane harmonic sound waves are expressed by the following equations

$$y_1(x,t) = A \sin (0.5 \pi x - 100 \pi t)$$

$$y_2(x,t) = A \sin (0.48 \pi x - 96 \pi t)$$

(All parameters are in MKS system)

- How many times does an observer hear maximum intensity in 1 second ?
- What is the speed of the sound ?
- What is the amplitude of  $y_1 + y_2$  at  $x = 0$  and  $t = 0.25$  s ?

**Solution**

$$(a) \text{ Beat frequency } = f_1 - f_2 = \frac{1}{2\pi} [100\pi - 96\pi] = 2$$

Therefore observer heard maximum intensity twice in one second.

$$(b) \text{ Speed of the sound wave } = \frac{\omega_1}{k_1} = \frac{100\pi}{0.5\pi} = 200 \text{ ms}^{-1}$$

$$(c) \text{ At } x = 0 \quad \& \quad t = 0.25 \text{ s} \quad y_1 = 0 \quad \& \quad y_2 = 0 \quad \text{so} \quad y_1 + y_2 = 0$$

**Illustration 23.**

Three tuning forks of frequencies 200, 203 and 207 Hz are sounded together. Find out the beat frequency.

**Solution**

$$\frac{1}{3} \quad \frac{2}{3} \quad \left(\frac{3}{3}\right)$$

$$\frac{1}{4} \quad \frac{2}{4} \quad \frac{3}{4} \quad \left(\frac{4}{4}\right)$$

$$\frac{1}{7} \quad \frac{2}{7} \quad \frac{3}{7} \quad \frac{4}{7} \quad \frac{5}{7} \quad \frac{6}{7} \quad \left(\frac{7}{7}\right)$$

**Ans.12**

Eliminate common time instants. Total Maxima in one second  $3 + 3 + 6 = 12$

**BEGINNER'S BOX-4**

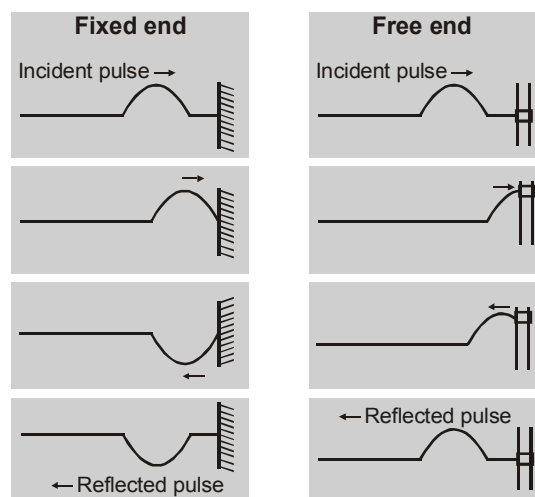
- Two waves having same frequency and same amplitude are superimposed at a point. Find the phase difference between two waves if resultant amplitude is :
  - $2a$
  - $\sqrt{2}a$
  - $a$
  - Zero
- During interference phenomenon of two wave it is observed that maximum amplitude to minimum amplitude ratio is  $9 : 7$ . Find the intensity ratio of waves.
- During interference phenomenon of two wave it is observed that amplitude ratio of waves is  $5 : 4$ . Find the maximum to minimum intensity ratio of resulting wave.

4. Two sound waves emitted by one sound source is approaching at a point through two path. When path difference is 36 cm or 60 cm, then points are silence point if speed of sound in air 330 m/sec then find the frequency of sound source.
5. In a Quincke's tube there are two positions where sound becomes minimum, the sliding distance between them is 16.6 cm. Find the freq. of sound source. (Sound velocity in air = 332 m/sec.)
6. A tuning fork having frequency 300 Hz produce, four beats per sec with x. If we file arm of unknown and again vibrate, number of beats decreases. Determine x.
7. 81 TF are arranged in the increasing order of their frequency and each TF produce 4 beats per sec. with its near by TF. If the frequency of last TF is octave of frequency of first TF then find the frequency of last TF.
8. Two sound waves  $y_1 = 3 \sin 400\pi t$  ;  $y_2 = 4 \sin 402\pi t$ 
  - (a) Find frequency of resultant wave
  - (b) Beat frequency
  - (c) Intensity ratio of waves
9. A Standard tuning fork contains frequency  $n_0$ , another TF  $n_A$  have 20% more compared to  $n_0$ ,  $n_B$  30% more compared to  $n_0$ ,  $n_A$  &  $n_B$  have beat relation of 6 beat/sec. Then determine  $n_0$ ,  $n_A$ ,  $n_B$
10. Two tuning fork having frequency 320 Hz & 324 Hz produce beat phenomena. Determine –
  - (a) Beat time period
  - (b) Minimum time interval in which maximum intensity become minimum.
  - (c) Number of beat per three seconds.
11. Two audio speakers are kept some distance apart and are driven by the same amplifier system. A person is sitting at a place 6.0 m from one of the speakers and 6.4 m from the other. If the sound signal is continuously varied from 500 Hz to 5000 Hz, what are the frequencies for which there is a destructive interference at the place of the listener ? Speed of sound in air = 320 m/s.
12. 51 tuning fork are arranged in a series in such a way that each fork produce five beats/sec with neighbouring tuning fork. If frequency of last is six time of first then determine frequency of first, 11<sup>th</sup>, 17<sup>th</sup>, 27<sup>th</sup>, 33<sup>th</sup> and last tuning fork.

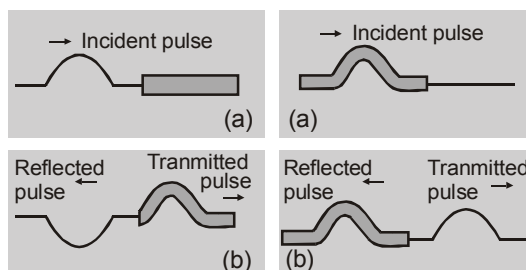
## 5. REFLECTION OF WAVES, STATIONARY WAVES, STANDING WAVES IN STRINGS AND ORGAN PIPE

### 5.1 Reflection and transmission of waves

Whenever a travelling wave reaches a boundary, part or all of the wave will be reflected. For example, consider a pulse travelling on a string fixed at one end (figure). When the pulse reaches the fixed wall, it will be reflected. Since the support attaching the string to the wall is assumed to be rigid, it does not transmit any part of the disturbance to the wall. Note that the reflected pulse is inverted. This can be explained by Newton's third law, the support must exert an equal and opposite (downward) reaction force on the string. This downward force causes the pulse to invert upon reflection.



Now consider another case where the pulse arrives at the end of a string that is free to move vertically. The tension at the free end is maintained by tying the string to a ring of negligible mass that to slide vertically on a smooth post. Again, the pulse will be reflected, but this time its displacement is not inverted. As the pulse reaches the post, it exerts a force on the free end, causing the ring to accelerate upward.



In the process, the ring "overshoots" the height of the incoming pulse and is then returned to its original position by the downward component of the tension.

Finally, we may have a situation in which the boundary is intermediate between these two extreme cases, that is, one in which the boundary is neither rigid nor free. In this case, part of the incident energy is transmitted and part is reflected. For instance, suppose a light string is attached to a heavier string as shown in figure. When a pulse travelling on the light reaches the junction, part of it is reflected and inverted, and part of it is transmitted to the heavier string. As one would expect, the reflected pulse has a smaller amplitude than the incident pulse, since part of the incident energy is transferred to the pulse in the heavier string. The inversion in the reflected wave is similar to the behavior of a pulse meeting a rigid boundary, when it is totally reflected.

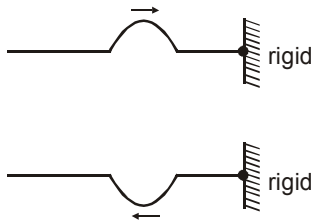
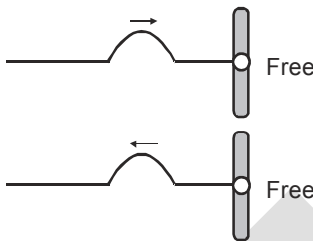
When a pulse travelling on a heavy string strikes the boundary of a lighter string, as shown in figure, again part is reflected and part is transmitted. However, in this case the reflected pulse is not inverted. In either case, the relative height of the reflected and transmitted pulses depend on the relative densities of the two string.

Thus, the speed of a wave on a string increases as the density of the string decreases. That is, a pulse travels more slowly on a heavy string than on a light string, if both are under the same tension. The following general rules apply to reflected waves :

- (1) When a wave pulse travels from medium A to medium B and  $v_A > v_B$  (B is denser than A), the pulse will be inverted upon reflection.
- (2) When a wave pulse travels from medium A to medium B and  $v_A < v_B$  (A is denser than B), it will not be inverted upon reflection.

## 5.2 Stationary Waves

- (1) When two identical progressive waves (transverse or longitudinal) propagating in opposite direction superimpose in a bounded medium (having boundaries) the resultant wave is called **stationary wave or standing wave**.
- (2) Stationary wave pattern may be obtained only and only in limited region.
- (3) We can obtain two same type of progressive waves, only & only by method of reflection.
- (4) According to the nature of reflected surface, reflection are of two types –

(a) Rigid End	(b) Free End
<p>In such type of reflection incident and reflected waves have phase difference of <math>\pi</math> and direction of propagation are opposite.</p>  <p>incident wave <math>y_1 = a \sin (\omega t - kx)</math>  reflected wave <math>y_2 = a \sin (\omega t + kx + \pi)</math>  or <math>y_2 = -a \sin (\omega t + kx)</math>  <math>y = y_1 + y_2</math>  <math>y = a \{ \sin (\omega t - kx) - \sin (\omega t + kx) \}</math>  after solving  <math>y = -2a \sin kx \cos \omega t</math>  <math>y = -A \cos \omega t</math> where <math>A = 2a \sin kx</math>  at <math>x = 0</math> <math>A = 0</math></p>	<p>In such type of reflection incident and reflected waves are in phase and direction of propagation are opposite.</p>  <p>incident wave <math>y_1 = a \sin (\omega t - kx)</math>  reflected wave <math>y_2 = a \sin (\omega t + kx)</math>  From superposition of wave  <math>y = y_1 + y_2</math>  <math>y = a \{ \sin (\omega t - kx) + \sin (\omega t + kx) \}</math>  after solving  <math>y = 2a \cos kx \sin \omega t</math>  <math>y = A \sin \omega t</math> where <math>A = 2a \cos kx</math>  so <math>x = 0</math> and <math>A = 2a</math></p>

### Special properties of stationary wave pattern

- **Zero wave velocity** : No transfer of energy between two points, particle velocity is non zero but wave velocity is zero.
- Position of antinodes & nodes in this pattern remains fix.
- The particles between two consecutive nodes vibrate in same phase while medium particles nearby of any node on both sides always vibrate in opposite phase.
- All medium particles doing simple harmonic vibrations have identical time period but different vibration Amplitude and because of this their maximum velocity at mean position is different
- All medium particles pass through their mean position simultaneously but with different maximum velocity.
- All medium particles pass their mean position in their one complete vibration two times hence stationary wave pattern is obtained as straight line twice in its one complete cycle.
- In this pattern, at antinode position, displacement and velocity is maximum, but wave strain is minimum.

Strain = slope of stationary wave pattern  $\left( \frac{dy}{dx} \right)$

At node position displacement and velocity is minimum but wave strain is maximum.

- Amplitude of incident wave > Amplitude of reflected wave

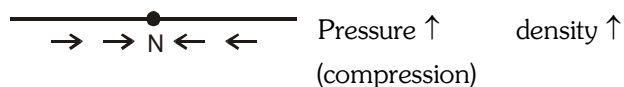
For node  $a_1 - a_2 \Rightarrow$  minima

For antinode  $a_1 + a_2 \Rightarrow$  maxima

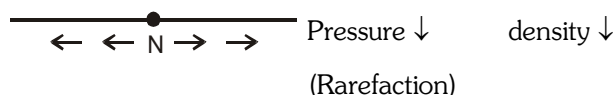
- For any wave each and every reflecting surface have some absorptive power and due to this the energy, intensity & amplitude of reflected wave is always less compared to that of incident wave. Two waves differ in their amplitude having same frequency and wavelength and propagate in reverse or opposite direction always give stationary wave pattern by their superposition.



- According to nature of superposing waves stationary waves are of two types –  
 Transverse stationary waves → Musical instruments based on wire (sonometer).  
 Longitudinal stationary waves → Musical instruments based on air (resonance tube).
- Only applied to longitudinal stationary wave



If medium particles move in this way



at antinode → Pressure & density constant so variations min.

at node → Pressure & density variations maximum.

$$E_{\text{gas}} = \frac{\text{change in pressure}}{\text{volumetric strain}} = \frac{dP}{\left(\frac{dy}{dx}\right)} = \text{const.} \quad \text{then } dP \propto \text{strain} \left(\frac{dy}{dx}\right)$$

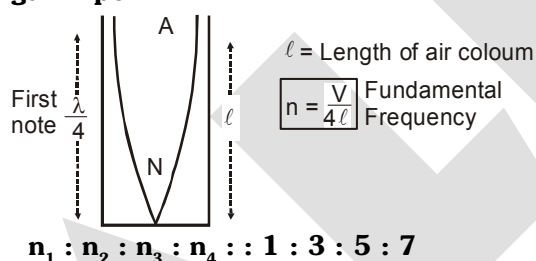
So strain is maximum at node positions and minimum at antinode positions.

### Types of Stationary Waves

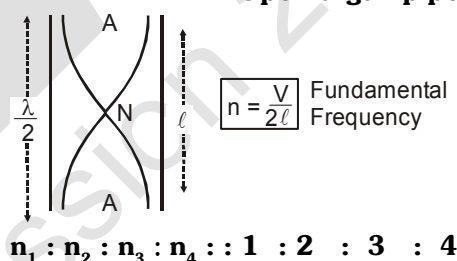
Longitudinal Stationary waves  
[Organ pipe (Ex. Resonance Tube)]

Transverse Stationary waves  
[Vibration in stretched string (Ex. Sonometer)]

#### Closed Organ Pipe



#### Open organ pipe

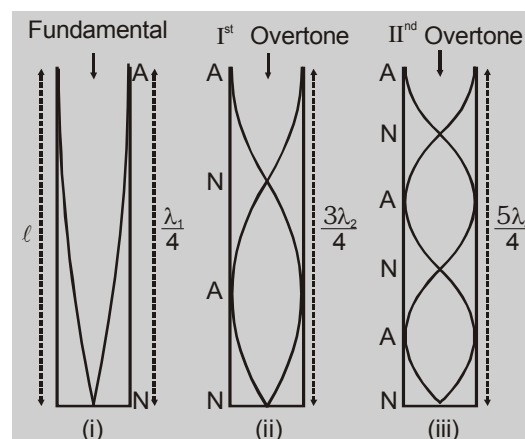


### 5.3 Vibration of Air Columns

When two longitudinal waves of same frequency and amplitude travel in a medium in opposite directions then by superposition, standing waves are produced. These waves are produced in air columns in cylindrical tube of uniform diameter. These sound producing tubes are called organ pipes.

#### Vibration of air column in closed organ pipe :

The tube which is closed at one end and open at the other end is called closed organ pipe. On blowing air at the open end, a wave travels towards closed end from where it is reflected towards open end. As the wave reaches open end, it is reflected again. So two longitudinal waves travel in opposite directions to superpose and produce stationary waves. At the closed end there is a node since particles does not have freedom to vibrate whereas at open end there is an antinode because particles have greatest freedom to vibrate.



Hence on blowing air at the open end, the column vibrates forming antinode at free end and node at closed end. If  $\ell$  is length of pipe and  $\lambda$  be the wavelength and  $v$  be the velocity of sound in organ pipe then

$$\text{Case (i) } \ell = \frac{\lambda_1}{4} \Rightarrow \lambda_1 = 4\ell \Rightarrow n_1 = \frac{v}{\lambda_1} = \frac{v}{4\ell} \quad \text{Fundamental frequency.}$$

$$\text{Case (ii) } \ell = \frac{3\lambda_2}{4} \Rightarrow \lambda_2 = \frac{4\ell}{3} \Rightarrow n_2 = \frac{v}{\lambda_2} = \frac{3v}{4\ell} = 3n_1 \quad \text{First overtone frequency.}$$

$$\text{Case (iii) } \ell = \frac{5\lambda_3}{4} \Rightarrow \lambda_3 = \frac{4\ell}{5} \Rightarrow n_3 = \frac{v}{\lambda_3} = \frac{5v}{4\ell} = 5n_1 \quad \text{Second overtone frequency.}$$

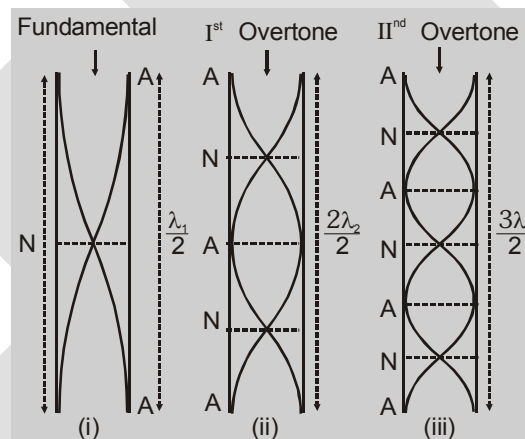
When closed organ pipe vibrate in  $m^{\text{th}}$  overtone then

$$\ell = (2m+1)\frac{\lambda}{4} \quad \text{so} \quad \lambda = \frac{4\ell}{(2m+1)} \Rightarrow n = (2m+1)\frac{v}{4\ell}$$

Hence frequency of overtones is given by  $n_1 : n_2 : n_3 : \dots = 1 : 3 : 5 \dots$

### Vibration of air columns in open organ pipe :

The tube which is open at both ends is called an open organ pipe. On blowing air at the open end, a wave travel towards the other end from which waves travel in opposite direction to superpose and produce stationary wave. Now the pipe is open at both ends by which an antinode is formed at open end. Hence on blowing air at the open end antinodes are formed at each end and nodes in the middle. If  $\ell$  is length of the pipe and  $\lambda$  be the wavelength and  $v$  is velocity of sound in organ pipe.



$$\text{Case (i) } \ell = \frac{\lambda_1}{2} \Rightarrow \lambda_1 = 2\ell \Rightarrow n_1 = \frac{v}{\lambda_1} = \frac{v}{2\ell} \quad \text{Fundamental frequency.}$$

$$\text{Case (ii) } \ell = \frac{2\lambda_2}{2} \Rightarrow \lambda_2 = \frac{2\ell}{2} \Rightarrow n_2 = \frac{v}{\lambda_2} = \frac{2v}{2\ell} = 2n_1 \quad \text{First overtone frequency.}$$

$$\text{Case (iii) } \ell = \frac{3\lambda_3}{2} \Rightarrow \lambda_3 = \frac{2\ell}{3} \Rightarrow n_3 = \frac{v}{\lambda_3} = \frac{3v}{2\ell} = 3n_1 \quad \text{Second overtone frequency.}$$

Hence frequency of overtones are given by the relation

$$n_1 : n_2 : n_3 : \dots = 1 : 2 : 3 \dots$$

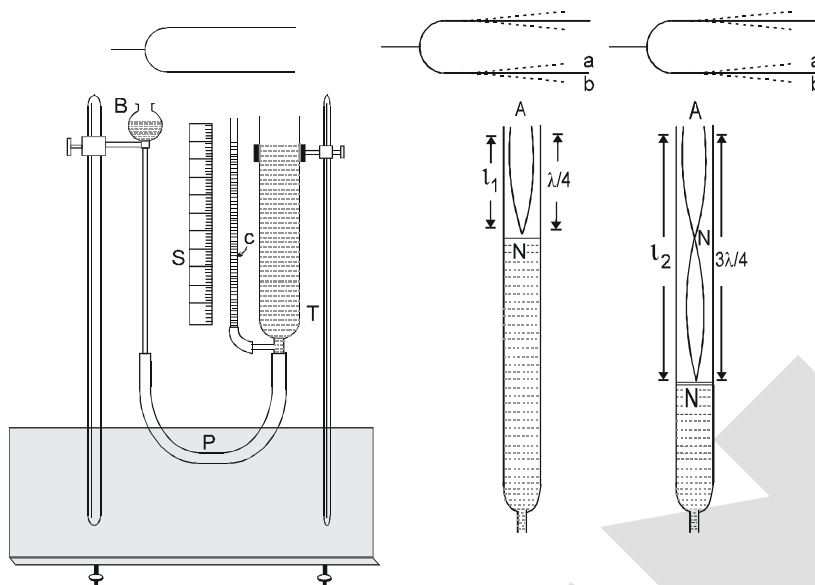
When open organ pipe vibrate in  $m^{\text{th}}$  overtone then

$$\ell = (m+1)\frac{\lambda}{2} \quad \text{so} \quad \lambda = \frac{2\ell}{(m+1)} \Rightarrow n = (m+1)\frac{v}{2\ell}$$

If an open pipe and a closed pipe have same length  $n_{\text{open}} = 2 n_{\text{closed}}$

## 5.4 Resonance Tube

**Construction :** The resonance tube is a tube T (figure) made of brass or glass, about 1 meter long and 5 cm in diameter and fixed on a vertical stand. Its lower end is connected to a water reservoir B by means of a flexible rubber tube. The rubber tube carries a pinch-cock P. The level of water in T can be raised or lowered by water adjusting the height of the reservoir B and controlling the flow of water from B to T or from T to B by means of the pinch-cock P. Thus the length of the air-column in T can be changed. The position of the water level in T can be read by means of a side tube C and a scale S.



### Determination of the speed of sound in air by resonance tube

First of all the water reservoir B is raised until the water level in the tube T rises almost to the top of the tube. Then the pinch-cock P is tightened and the reservoir B is lowered. The water level in T stays at the top. Now a tuning fork is sounded and held over the mouth of tube. The pinch-cock P is opened slowly so that the water level in T falls and the length of the air-column increases. At a particular length of air-column in T, a loud sound is heard. This is the first state of resonance. In this position the following phenomenon takes place inside the tube.

- (i) For first resonance  $\ell_1 = \lambda/4$   
 (ii) For second resonance  $\ell_2 = 3\lambda/4 \Rightarrow \ell_2 - \ell_1 = \lambda/2 \Rightarrow \lambda = 2(\ell_2 - \ell_1)$

If the frequency of the fork be  $n$  and the temperature of the air-column be  $t^\circ\text{C}$ , then the speed of sound at  $t^\circ\text{C}$  is given by

$$v_t = n\lambda = 2n(\ell_2 - \ell_1)$$

The speed of sound wave at  $0^\circ\text{C}$

$$v_0 = (v_t - 0.61 t) \text{ m/s.}$$

**End Correction :** In the resonance tube, the antinode is not formed exactly at the open end but slightly outside at a distance  $x$ . Hence the length of the air-column in the first and second states of resonance are  $(\ell_1 + x)$  and  $(\ell_2 + x)$  then

- (i) For first resonance  $\ell_1 + x = \lambda/4$  .....(i)  
 (ii) For second resonance  $\ell_2 + x = 3\lambda/4$  .....(ii)

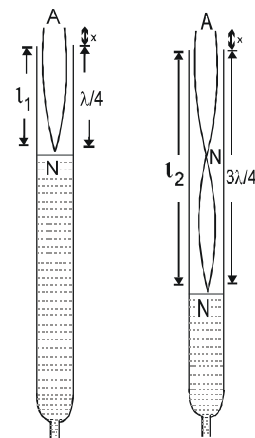
Subtract Equation (ii) from Equation (i)

$$\ell_2 - \ell_1 = \lambda/2$$

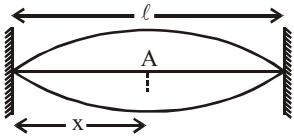
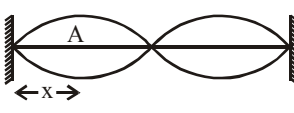
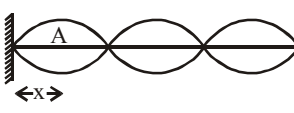
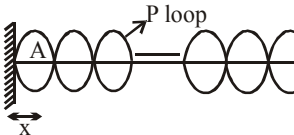
$$\lambda = 2(\ell_2 - \ell_1)$$

Put the value of  $\lambda$  in Equation (i)  $\ell_1 + x = \frac{2(\ell_2 - \ell_1)}{4}$

$$\Rightarrow \ell_1 + x = \frac{\ell_2 - \ell_1}{2} \Rightarrow x = \frac{\ell_2 - 3\ell_1}{2}$$



# 5.5 Transverse Stationary wave

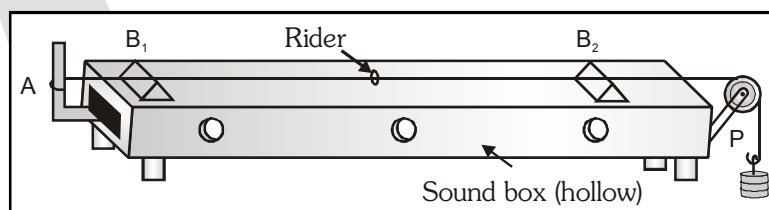
Sonometer wire	Plucking distance is x	Overtone	Harmonic	Node	Antinode
	$x = \frac{l}{2 \times 1}, \quad l = \frac{\lambda_1}{2}$ $\Rightarrow \lambda_1 = 2l, \quad n_1 = \frac{v}{2l}$	0	1	2	1
	$x = \frac{l}{2 \times 2}, \quad l = \frac{2\lambda_2}{2}$ $\Rightarrow \lambda_2 = \frac{2l}{2}, \quad n_2 = \frac{2v}{2l}$	1	2	3	2
	$x = \frac{l}{2 \times 3}, \quad l = 3\left(\frac{\lambda_3}{2}\right)$ $\Rightarrow \lambda_3 = \frac{2l}{3}, \quad n_3 = \frac{3v}{2l}$	2	3	4	3
	$x = \frac{l}{2 \times P}, \quad l = P\left(\frac{\lambda_p}{2}\right)$ $\Rightarrow \lambda_p = \frac{2l}{P}, \quad n_p = \frac{PV}{2l}$	P-1	P	P + 1	P

## Sonometer practical -

- If a vibrating Tuning fork is pressed against a sonometer wire then forced vibrations are produced in table of hollow box & these vibrations are transferred to air column filled in hollow box which results into increase in vibration amplitude of sound & intensity of sound increases. Air filled hollow box is called sound box.
- During contact with table some energy is transferred to table so TF can not do vibrations for longer duration.
- At resonance maximum energy is transferred to table so TF can do vibrations not for longer duration.
- At resonance maximum energy is transferred from TF to vibrating wire and sound intensity is maximum.

## Frequency corresponding to 'P' loop

$$n = \frac{P}{2l} \sqrt{\frac{T}{\pi r^2 d}} = \frac{P}{2l} \sqrt{\frac{T}{Ad}} = \frac{P}{2l} \sqrt{\frac{T}{m}} = \frac{P}{2} \sqrt{\frac{T}{Ml}} \quad \text{where } m = \frac{M}{l}$$



$$n \propto \frac{1}{l}; n \propto \sqrt{T}; n \propto \frac{1}{r}$$

$$n \propto \frac{1}{\sqrt{A}} \text{ \& } n \propto \frac{1}{\sqrt{d}}$$

at resonance vibration in rider will be maximum

## 5.6 Comparison of progressive and stationary waves

	Progressive waves	Stationary waves
1.	These waves travel in a medium with definite velocity.	These waves do not travel and remain confined between two boundaries in the medium.
2.	These waves transmit energy in the medium.	These waves do not transmit energy in the medium.
3.	The phase of vibration varies continuously from particle to particle.	The phase of all the particles in between two nodes is always same. But particles on adjacent side of a node differ in phase by $180^\circ$
4.	No particle of medium is permanently at rest.	Particles at nodes are permanently at rest.
5.	All particles of the medium vibrate and amplitude of vibration is same.	The amplitude of vibration changes from particle to particle. The amplitude is zero at nodes and maximum at antinodes.
6.	All the particles do not attain the maximum displacement position simultaneously.	All the particles attain the maximum displacement position simultaneously.

## GOLDEN KEY POINTS

Wave property	Reflection	Transmission (Refraction)
$v$	does not change	changes
$n, T, \omega$	do not change	do not change
$\lambda, k$	do not change	change
$A, I$	change	change
Phase difference ( $\Delta\phi$ )	$\Delta\phi = 0$ , from a rarer medium $\Delta\phi = \pi$ , from a denser medium	does not change

- A pulse undergoes a phase change of  $\pi$  on reflection from a rigid boundary.
- A pulse does not suffer any phase change on reflection from a free boundary.
- The transmitted wave is never inverted.
- A rod clamped at one end or a string fixed at one end is similar to vibration of closed end organ pipe.
- A rod clamped in the middle is similar to the vibration of open end organ pipe.
- If an open pipe is half submerged in water, it becomes a closed organ pipe of length half that of open pipe i.e. frequency remains same.
- Due to finite motion of air molecules in organ pipes reflection takes place not exactly at open end but little what above it so in an organ pipe antinode is not formed exactly at free-end but above it at a distance  $e = 0.6r$  (called end correction or Rayleigh's correction) with  $r$  being the radius of pipe. So for closed organ pipe  $L \rightarrow L + 0.6r$  while for open  $L \rightarrow L + 2 \times 0.6r$  (as both ends are open)

$$\text{so that } f_c = \frac{v}{4(L + 0.6r)} \quad \text{while } f_o = \frac{v}{2(L + 1.2r)}$$

This is why for a given  $v$  and  $L$  narrower the pipe higher will the frequency or pitch and shriller will be the sound.

- For an organ pipe (closed or open) if  $v = \text{constant}$ .  $f \propto (1/L)$   
So with decrease in length of vibrating air column wavelength decrease ( $\lambda \propto L$ ), frequency or pitch will increase and vice-versa. This is why the pitch increases gradually as an empty vessel fills slowly.
- For an organ pipe if  $f = \text{constant}$ .  $v \propto \lambda$  or  $v \propto L$ ,  $f = \frac{v}{\lambda} = \text{constant}$  i.e. the frequency of an organ pipe will remain unchanged if the ratio of speed of sound in to its wave length remains constant.
- As for a given length of organ pipe  $\ell = \text{constant}$   $f \propto v$  So

(a) With rise in temperature as velocity will increase ( $v \propto \sqrt{T}$ ), the pitch will increase.

(Change in length with temperature is not considered unless stated)

(b) With change in gas in the pipe as  $v$  will change and so  $f$  will change ( $v \propto \sqrt{\gamma / M_w}$ )

(c) With increase in moisture as  $v$  will increase and so the pitch will also increase.

- The equation of stationary wave is -

(a) When the wave is reflected from a free boundary  $y = 2a \cos \frac{2\pi x}{\lambda} \sin \frac{2\pi t}{T}$

(b) When the wave is reflected from a rigid boundary  $y = -2a \sin \frac{2\pi x}{\lambda} \cos \frac{2\pi t}{T}$

- Nodes are the points on a stationary wave, where the amplitude of oscillating particle is always minimum.
- Antinodes are the points on a stationary wave, where the amplitude of oscillating particle is maximum.
- Only odd harmonics are produced in a closed organ pipe. Moreover, first overtone is the third harmonic, second overtone is the fifth harmonic and so on.
- Both of the odd and even harmonic are produced in open organ pipe. Moreover, here first overtone is the second harmonic, second overtone is the third harmonic and so on.
- If the weight which produces tension in wire is immersed in any liquid, the frequency of vibrating wire decreases.
- If a wire fixed between two ends heat up from its one end, its frequency will increase because of thermal tension produced in it.

$T = Y A \alpha \Delta \theta$  where  $Y = \text{Young's module}$ ,  $\alpha = \text{coeff. of linear expansion}$ ,  $A = \text{cross-section area}$

$\Delta \theta = \text{change in temp.}$

- **Echo (Based on reflection) :**

Multiple reflection of sound is called an echo. If the distance of reflector from the source is  $d$  then,

$$2d = vt$$

Hence,  $v = \text{speed of sound}$  and  $t = \text{the time of echo}$ .  $\therefore d = \frac{vt}{2}$

Since, the effect of ordinary sound remains on our ear for  $1/10$  second, therefore, if the sound returns to the starting point before  $\frac{1}{10}$  second, then it will not be distinguished from the original sound and no echo will be heard. Therefore, the minimum distance of the reflector is,

$$d_{\min} = \frac{v \times t}{2} = \left( \frac{330}{2} \right) \left( \frac{1}{10} \right) = 16.5 \text{m}$$

### • Musical Interval

The ratio between the frequencies of two notes is called the musical interval. Following are the names of some musical intervals.

(i) Unison  $\frac{n_2}{n_1} = 1$

(ii) Octave  $\frac{n_2}{n_1} = 2$

## Illustrations

### Illustration 24.

Two tuning forks A and B produce 8 beats/s when sounded together. A gas column 37.5 cm long in a pipe closed at one end resonate to its fundamental mode with fork A whereas a column of length 38.5 cm of the same gas in a similar pipe is required for a similar resonance with fork B. Calculate the frequency of these two tuning forks. [AIPMT 2006]

### Solution

$$\left. \begin{array}{l} \text{For tuning fork 'A'} \quad \frac{\lambda_1}{4} = 37.5 \quad \text{so } n_1 = \frac{v}{\lambda_1} = \frac{v}{4 \times 37.5} \\ \text{For tuning fork 'B'} \quad \frac{\lambda_2}{4} = 38.5 \quad \therefore n_2 = \frac{v}{\lambda_2} = \frac{v}{4 \times 38.5} \end{array} \right\}$$

$$\therefore n_1 - n_2 = 8 \Rightarrow \frac{v}{4 \times 37.5} - \frac{v}{4 \times 38.5} = 8 \quad \therefore v = (8 \times 4 \times 37.5 \times 38.5)$$

$$n_1 = \frac{8 \times 4 \times 37.5 \times 38.5}{4 \times 37.5} = 308 \text{ Hz} \quad \text{and} \quad n_2 = 308 - 8 = 300 \text{ Hz}$$

### Illustration 25.

A transverse wave, travelling along the positive x-axis, given by  $y = A \sin(kx - \omega t)$  is superposed with another wave travelling along the negative x-axis given by  $y = -A \sin(kx + \omega t)$ . The point  $x=0$  is

- (1) a node (2) an antinode  
(3) neither a node nor an antinode (4) a node or antinode depending on t.

### Solution

Ans. (2)

$$\text{At } x=0, y_1 = A \sin(-\omega t) \text{ and } y_2 = -A \sin \omega t; y_1 + y_2 = -2A \sin \omega t \text{ (antinode)}$$

### Illustration 26.

A standing wave is created on a string of length 120 m and it is vibrating in 6th harmonic. Maximum possible amplitude of any particle is 10 cm and maximum possible velocity will be 10 cm/s. Choose the correct statement.

- (1) Angular wave number of two waves will be  $\frac{\pi}{20}$ .  
(2) Time period of any particle's SHM will be  $4\pi$  sec.  
(3) Any particle will have same kinetic energy as potential energy.  
(4) Amplitude of interfering waves are 10 cm each.

### Solution

Ans. (1)

$$6\left(\frac{\lambda}{2}\right) = 120 \Rightarrow \lambda = 40 \Rightarrow k = \frac{\pi}{20} \Rightarrow A\omega = v_{\max} \Rightarrow \omega = 1 \Rightarrow T = 2\pi$$



Illustration 27.

Column I represents the standing waves in air columns and string. Column II represents frequency of the note. Match the column-I with column-II. [ $v$  = velocity of the sound in the medium]

Column-I	Column-II
(A) Second harmonic for the tube open at both ends	(P) $\frac{v}{4\ell}$
(B) Fundamental frequency for the tube closed at one end	(Q) $\frac{v}{2\ell}$
(C) First overtone for the tube closed at one end	(R) $\frac{3v}{4\ell}$
(D) Fundamental frequency for the string fixed at both ends	(S) $\frac{v}{\ell}$
	(T) $\frac{5v}{4\ell}$

Solution

Ans. (A) S (B) P (C) R (D) Q

For (A) : For open organ pipe 2nd harmonic =  $2 \left( \frac{v}{2\ell} \right)$

For (B) : For closed organ pipe fundamental frequency =  $\frac{v}{4\ell}$

For (C) : For closed organ pipe, first overtone frequency =  $\frac{3v}{4\ell}$

For (D) : For string fixed at both ends, fundamental frequency =  $\frac{v}{2\ell}$

Illustration 28.

If an OOP of fundamental frequency 1400 Hz dipped 30% in water then calculate produced frequency.

Solution

$$\frac{v}{2L} = 1400 \text{ Hz} \Rightarrow \frac{v}{L} = 2800 \text{ Hz}$$

$$n' = \frac{v}{4L'} = \frac{v}{4[0.7L]} = \frac{v}{2.8L} = \frac{2800}{2.8} = 1000 \text{ Hz}$$

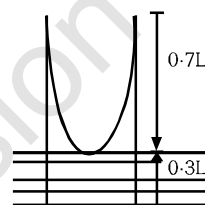


Illustration 29.

Two identical wires under the same tension have a fundamental frequency of 500 Hz. What fractional increase in the tension of one wire will give 5 beats per second ? [AIPMT 2007]

Solution

Let  $n_1$  be the frequency of the wire having tension  $T + \Delta T$  and  $n_2$  be the frequency of the wire having tension

$$T, \text{ then } \frac{n_1}{n_2} = \sqrt{\frac{T + \Delta T}{T}} = \frac{500 + 5}{500} = \frac{505}{500}$$

$$\Rightarrow \frac{T + \Delta T}{T} = \left( 1 + \frac{5}{500} \right)^2 \approx 1 + \frac{2}{100} \approx 1.02 \Rightarrow \frac{\Delta T}{T} = 0.02$$

OR

$$\text{For stretched wire frequency } n \propto \sqrt{T} \Rightarrow \frac{\Delta n}{n} = \frac{1}{2} \frac{\Delta T}{T}$$

$$\Rightarrow \frac{\Delta T}{T} = 2 \left( \frac{\Delta n}{n} \right) = 2 \left( \frac{5}{500} \right) = 0.02$$

**Illustration 30.**

A string with a mass density of  $4 \times 10^{-3} \text{ kg/m}$  is under tension of 360 N and is fixed at both ends. One of its resonance frequencies is 375 Hz. The next higher resonance frequency is 450 Hz. Find the mass of the string.

[AIPMT 2007]

**Solution**

$$n_1 = 375 = \frac{p}{2\ell} \sqrt{\frac{T}{m}} \text{ and } n_2 = 450 = \frac{p+1}{2\ell} \sqrt{\frac{T}{m}} \text{ where } p \text{ is number of loops}$$

$$\Rightarrow \frac{450}{375} = \frac{p+1}{p} \Rightarrow p = 5$$

$$\text{so } \ell = \frac{p}{2 \times n_1} \sqrt{\frac{T}{m}} = \frac{5}{2 \times 375} \sqrt{\frac{360}{4 \times 10^{-3}}} = 2\text{m} \Rightarrow \text{Mass of wire} = (m)(\ell) = (4 \times 10^{-3})(2) = 8 \times 10^{-3} \text{ kg}$$

**OR**

$$\text{Difference between two consecutive resonating frequency } n_2 - n_1 = \frac{1}{2\ell} \sqrt{\frac{T}{m}}$$

$$\Rightarrow 450 - 375 = \frac{1}{2\ell} \sqrt{\frac{360}{4 \times 10^{-3}}} \Rightarrow \ell = \frac{1}{2 \times 75} \sqrt{\frac{360}{4 \times 10^{-3}}} = \frac{1}{150} \times \frac{6 \times 10^2}{2} = 2 \text{ m}$$

$$\Rightarrow \text{Mass of wire} = (m)(\ell) = (4 \times 10^{-3})(2) = 8 \times 10^{-3} \text{ kg}$$

**Illustration 31.**

A steel wire of length 1 m and mass 0.1 kg and having a uniform cross-sectional area of  $10^{-6} \text{ m}^2$  is rigidly fixed at both ends. The temperature of the wire is lowered by  $20^\circ\text{C}$ . If the wire is vibrating in fundamental mode, find the frequency (in Hz). ( $Y_{\text{steel}} = 2 \times 10^{11} \text{ N/m}^2$ ,  $\alpha_{\text{steel}} = 1.21 \times 10^{-5}/^\circ\text{C}$ )

(1) 11

(2) 20

(3) 15

(4) 10

**Solution****Ans. (1)**

$$\Delta \ell = \alpha \ell \Delta \theta \Rightarrow Y = \frac{T/A}{\Delta \ell / \ell} \Rightarrow T = YA \frac{\Delta \ell}{\ell} \Rightarrow T = \alpha YA \Delta \theta = 48.4 \text{ N}; \quad v = \sqrt{\frac{T}{\mu}} = \sqrt{\frac{48.4}{\left(\frac{0.1}{1}\right)}} = 22 \text{ m/s}$$

$$\therefore \text{for fundamental note } \ell = \frac{\lambda}{2} \Rightarrow \lambda = 2\text{m} \Rightarrow f = \frac{v}{\lambda} = \frac{22}{2} = 11 \text{ Hz}$$

**Illustration 32.**

A piezo electric quartz plate of thickness 0.005 m is vibrating in resonant conditions. Calculate its fundamental frequency if for quartz  $Y = 8 \times 10^{10} \text{ N/m}^2$  and  $\rho = 2.65 \times 10^3 \text{ kg/m}^3$

**Solution**

$$\text{We know that for longitudinal waves in solids } v = \sqrt{\frac{Y}{\rho}}, \quad \text{So } v = \sqrt{\frac{8 \times 10^{10}}{2.65 \times 10^3}} = 5.5 \times 10^3 \text{ m/s}$$

$$\text{Further more for fundamental mode of plate } \Rightarrow (\lambda/2) = L \quad \text{So } \lambda = 2 \times 5 \times 10^{-3} = 10^{-2} \text{ m}$$

$$\text{But as } v = f\lambda, \quad \text{i.e., } f = (v/\lambda) \quad \text{so } f = [5.5 \times 10^3 / 10^{-2}] = 5.5 \times 10^5 \text{ Hz} = 550 \text{ kHz}$$

**Illustration 33.**

If a 'COP' is cut into two equal parts then determine frequency of both part. if initially it was 'n'.

$$\text{Solution } n = \frac{V}{4\ell}$$

$$n_1' = \frac{V}{2\left(\frac{\ell}{2}\right)} = \frac{V}{\ell} = 4\left(\frac{V}{4\ell}\right) = 4n;$$

$$n_2 = \frac{V}{4\left(\frac{\ell}{2}\right)} = \frac{V}{2\ell} = 2\left(\frac{V}{4\ell}\right) = 2n$$

**Illustration 34.**

For given C.O.P. (closed organ pipe) if 9<sup>th</sup> O.T. (over tone) has frequency 1900 Hz. then fundamental frequency of same length O.O.P. is ?

**Solution**

$$19n = 1900 ; \quad n = 100$$

$$OOP = 2n = 200 \text{ Hz}$$

For same length OOP have double freq. than COP.

**Illustration 35.**

Two C.O.P. having length 20 cm & 20.5 cm produce 5 beat/sec determine the freq of both C.O.P.

**Solution**

$$\frac{n}{n+5} = \frac{20}{20.5} ; \quad n = 200 \quad \text{For } 20.5 \text{ cm}$$

$$n + 5 = 205 \quad \text{For } 20 \text{ cm}$$

**Illustration 36.**

An organ pipe closed at one end vibrating in its first overtone and another pipe, open at both ends vibrating in its third overtone are in resonance with a given tuning fork. The ratio of their lengths are given by

**Solution**

$$\text{First Over tone of COP} = 3 \frac{V}{4\ell_c} \quad \text{and} \quad \text{Third Over tone of OOP} = \frac{4V}{2\ell_o}$$

$$\text{according to question both are equal} \quad \therefore \quad 3 \frac{V}{4\ell_c} = \frac{4V}{2\ell_o} \Rightarrow \frac{\ell_c}{\ell_o} = \frac{3}{8}$$

**Illustration 37.**

A stretched wire of length 114 cm is divide into three segment whose fundamental frequencies are in the ratio 4 : 3 : 1, the length of the segments must be in the ratio

**Solution**

$$n_1 : n_2 : n_3 = 4 : 3 : 1 \quad \left[ \because n \propto \frac{1}{\ell} \right] \Rightarrow \ell_1 : \ell_2 : \ell_3 = \frac{1}{4} : \frac{1}{3} : 1 = 3 : 4 : 12$$

**Illustration 38.**

A source emits ultrasonic sound of frequency 200 kHz. This sound falls on the water surface. Calculate the wavelength.

(a) in the reflected sound (b) in the transmitted sound

velocity of sound in air = 340 ms<sup>-1</sup>, velocity of sound in water = 1480 ms<sup>-1</sup>)

**Solution**

$$\text{Wave length } \lambda = \frac{\text{Velocity}}{\text{Frequency}}$$

$$(a) \quad \text{Reflected sound travels in air so} \quad \lambda = \frac{340}{200 \times 10^3} = 1.7 \times 10^{-3} \text{ m}$$

$$(b) \quad \text{Transmitted sound travels in water so} \quad \lambda = \frac{1480}{200 \times 10^3} = 7.4 \times 10^{-3} \text{ m}$$

## BEGINNER'S BOX-5

- The equation of progressive wave is  $y = 0.09 \sin 8\pi [t - (x/20)]$  after reflection of this wave from rigid end the amplitude of reflected wave becomes  $2/3$  of initial then (i) Find the equation of reflected wave (ii) Find the displacement of that particle which is situated at  $x = 0$ , in reflected wave.
- A string vibrates according to the equation  $y = 5 \sin \left( \frac{\pi x}{3} \right) \cos (40\pi t)$  where  $x$  and  $y$  are in centimeters and  $t$  is in seconds.
  - What is the equation of incident and reflected wave ?
  - What is the distance between the adjacent nodes ?
  - What is the velocity of the particle of the string at the position  $x = 1.5$  cm when  $t = \frac{9}{8}$  sec ?
- The transverse displacement of a string is given by
 
$$y(x, t) = 0.06 \sin \left( \frac{2\pi}{3} x \right) \cos (120\pi t)$$
 where  $x$  and  $y$  are in m and  $t$  in s. The length of the string is 1.5m and its mass is  $3.0 \times 10^{-2}$  kg. Answer the following :
  - Does the function represent a travelling wave or a stationary wave ?
  - What are the wavelength, frequency, and speed of each wave ?
  - Determine the tension in the string.
- For a plane progressive wave :  $y = 0.02 \sin 2\pi (330t - x)$ 
  - If this wave is reflected from rigid end and amplitude becomes 60% of initial then equation of wave will be ?
  - If this wave is reflected from free end and amplitude becomes 75% of initial then equation of wave will be ?
- A progressive wave the equation is  $y = 0.08 \sin 2\pi (200t - x)$  it is reflected from rigid end and amplitude becomes half then equation of reflected wave and if it is reflected from free end then equation of reflected wave is .
- An organ pipe produces a sound of frequency 400 Hz. If it is blown a little harder then it produces a sound of frequency 800 Hz. It is an open pipe or a closed pipe ?
- If a stretched string which is fixed at both ends has  $m$  nodes, then calculate its length.
- A 20 cm long pipe is closed at one end. Which harmonic mode of the pipe is resonantly excited by 425 Hz source ? Will the same source be in resonance with the pipe if both ends are open ? (Speed of sound in air = 340 m/s)
- If frequency of third overtone of closed organ pipe is equal to frequency of sixth overtone of an open organ pipe, then determine their length ratio  $\frac{\ell_c}{\ell_o}$ .
- A sonometer wire emits a fundamental note of frequency 150 Hz. Calculate the frequency of the note emitted when the tension is changed in the ratio of 9 : 16 and length in the ratio of 1 : 2.
- Third overtone of a closed organ pipe is in unison with fourth harmonic of an open organ pipe. find the ratio of lengths of the pipes.
- Two successive resonant frequencies in an open organ pipe are 1944 and 2592 Hz. If the speed of sound in air  $324 \text{ ms}^{-1}$ , then find the length of tube.

13. Given below are some functions of  $x$  and  $t$  to represent the displacement (transverse or longitudinal) of an elastic wave. State which of these represent (i) a travelling wave, (ii) a stationary wave or (iii) none at all :
- (a)  $y = \cos(3x) \sin(10t)$  (b)  $y = 2\sqrt{x - vt}$   
 (c)  $y = 3 \sin(5x - 0.5t) + 4 \cos(5x - 0.5t)$  (d)  $y = \cos x \sin t + \cos 2x \sin 2t$
14. If OOP have 10 antinodes and fundamental freq. 300 Hz. then freq at 10<sup>th</sup> Antinode.
15. The sum of frequencies of COP's first overtone and OOP's second overtone is 180 find fundamental frequencies of COP and OOP. (length is same)
16. A tuning fork produce four beats per second with two OOP's having length 30 & 31 cm find the freq. of T.F.
17. A tuning fork is found to give 20 beats in 12 seconds when sounded in conjunction with a stretched string vibrating under a tension of 14.4 or 10 kgf. Calculate the frequency of the fork.
18. Two tuning fork  $n_1, n_2$  produce two beats per sec.  $n_1$  resonant with 15 cm COP and  $n_2$  resonant with 30.5 cm OOP. Find the freq. of  $n_1$  &  $n_2$ .
19. A tube 1 m long is closed at one end. A stretched wire is placed near the open end. The wire is 0.3m long and has a mass of 0.01kg. It is held fixed at both ends and vibrates in its fundamental mode. It sets the air column in the tube into vibration at its fundamental frequency by resonance. Find –
- (a) the frequency of oscillation of the air column.  
 (b) the tension in the wire, If speed of sound in air is 330 m/s.
20. In resonance tube experiment if  $V = 300$  m/s,  $n = 500$  Hz.,  $L = 125$  cm
- (i) Find out maximum order of resonance that can be established ?  
 (ii) Maximum number of resonance ?  
 (iii) Maximum & minimum water level kept at resonance condition ?
21. If we increase the tension of streached wire by 5 kg. wt. then fundamental freq increase with ratio of 2 : 3 find the initial tension.
22. **Fill in the blanks for COP and OOP.**
- (i) In COP if the freq of 7<sup>th</sup> overtone is 600 Hz then fundamental frequency of COP is.....  
 (ii) In COP if the frequency of 3<sup>rd</sup> overtone is 1400 Hz then fundamental frequency of same length OOP is.....  
 (iii) In OOP if the frequency of 7<sup>th</sup> overtone is 800 Hz then fundamental frequency of OOP is.....  
 (iv) In COP if the frequency of 7<sup>th</sup> overtone is 600 Hz then frequency of 3<sup>rd</sup> overtone is.....  
 (v) In OOP if the frequency of 7<sup>th</sup> overtone is 1600 Hz then frequency of 3<sup>rd</sup> overtone is.....  
 (vi) In OOP if the frequency of 7<sup>th</sup> overtone is 1600 Hz then fundamental frequency of same length COP is.....  
 (vii) In OOP if the frequency of 7<sup>th</sup> overtone is 800 Hz then frequency of OOP corresponding to first overtone is.....  
 (viii) Length of OOP is 44 cm speed of sound 340 m/s fundamental frequency is 340 Hz then value of end correction is.....  
 (ix) Length of OOP is 38 cm speed of sound 340 m/s fundamental frequency is 340 Hz then value of radius of pipe is.....

**23. Fill in the blanks for Sonometer.**

- (i) In sonometer if tension of wire and length of wire becomes double and mass per unit length of wire remain constant then fundamental frequency of wire will becomes.....
- (ii) In sonometer if tension of wire and length becomes double and mass of wire remain constant then fundamental frequency of wire will becomes.....
- (iii) In sonometer if tension of wire and length becomes double and mass per unit length remain constant then wave velocity will becomes.....
- (iv) In a stretched wire calculate speed of wave if tension in wire is 40 N and mass for unit length is  $4 \times 10^{-3}$  kg/m. ....
- (v) In a stretched wire calculate speed of wave in wire if tension in wire is 80 N and mass is  $4 \times 10^{-3}$  kg. and length of wire is 2 m. ....
- (vi) In sonometer, if tensions and length both becomes four times, taking mass per unit length constant then, for vibration of same frequency Tuning fork, Number of loop will becomes.....

**24. Fill in the blanks for Resonance tube.**

- (i) In resonance tube first resonating length is 25 cm then its second resonating length will be (if  $e = 0$ ) .....
- (ii) In resonance tube first resonating length is 25 cm then its second resonating length will be (if  $e \neq 0$ ) .....
- (iii) Length of resonance tube is 140 cm. How many resonance are possible for wave have wave length 40 cm. ....
- (iv) Length of resonance tube is 150 cm. How many resonance are possible for wave having frequency 400 Hz and speed of sound 320 m/s. ....
- (v) Length of resonance tube is 150 cm. Maximum level of liquid , in resonance condition for wave having wavelength 80 cm. is.....
- (vi) Length of resonance tube is 150 cm Minimum level of liquid , in resonance condition for wave having wavelength 80 cm. is.....
- (vii) In resonance tube first resonating length is 17 cm, second resonating length is 55 cm then wavelength of wave is.....
- (viii) In resonance tube first resonating length is 17 cm, second resonating length is 55 cm then radius of tube is.....

**6. DOPPLER EFFECT IN SOUND WAVES AND LIGHT WAVES****6.1 Acoustic Doppler Effect (Doppler Effect for Sound Waves)**

The apparent change in frequency or pitch due to relative motion of source and observer along the line of sight is called Doppler Effect.

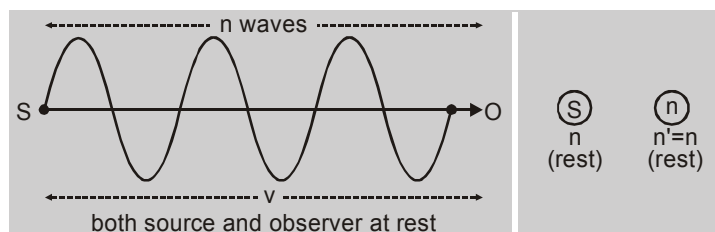
While deriving these expressions, we make the following assumptions :

- (i) The velocity of the source, the observer and the medium are along the line joining the positions of the source and the observer.
- (ii) The velocity of the source and the observer is less than velocity of sound.

Doppler effect takes place both in sound and light. In sound it depends on whether the source or observer or both are in motion while in light it depends on whether the distance between source and observer is increasing or decreasing.

$n \rightarrow$ actual frequency	$n' \rightarrow$ observed frequency (apparent frequency)
$\lambda \rightarrow$ actual wave length	$\lambda' \rightarrow$ observed (apparent) wave length
$v \rightarrow$ velocity of sound	$v_s \rightarrow$ velocity of source
$v_o \rightarrow$ velocity of observer	$v_w \rightarrow$ wind velocity

**Case I : Source in motion, observer at rest, medium at rest :**

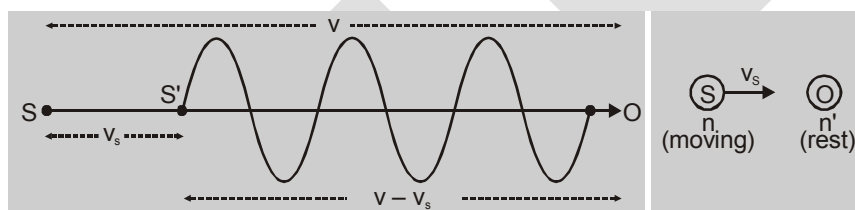


Suppose the source S and observer O are separated by distance  $v$ . Where  $v$  is the velocity of sound. Let  $n$  be the frequency of sound emitted by the source. Then  $n$  waves will be emitted by the source in one second. These  $n$  waves will be accommodated in distance  $v$ .

So, wave length  $\lambda = \frac{\text{total distance}}{\text{total number of waves}} = \frac{v}{n}$

**(1) Source moving towards stationary observer :**

Let the source start moving towards the observer with velocity  $v_s$ . After one second, the  $n$  waves will be crowded in distance  $(v - v_s)$ . Now the observer shall feel that he is listening to sound of wavelength  $\lambda'$  and frequency  $n'$



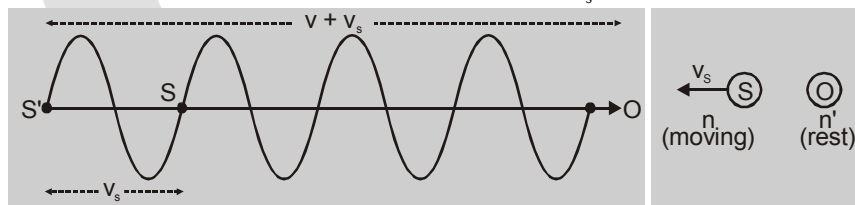
Now apparent wavelength  $\lambda' = \frac{\text{total distance}}{\text{total number of waves}} = \frac{v - v_s}{n}$

and changed frequency,  $n' = \frac{v}{\lambda'} = \frac{v}{\left(\frac{v - v_s}{n}\right)} = n \left(\frac{v}{v - v_s}\right)$

So, as the source of sound approaches the observer the apparent frequency  $n'$  becomes greater than the true frequency  $n$ .

**(2) When source move away from stationary observer :-**

For this situation  $n$  waves will be crowded in distance  $v + v_s$ .



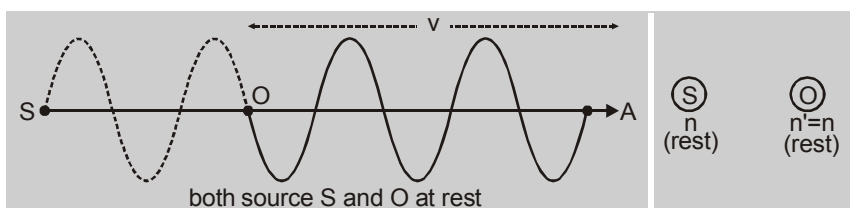
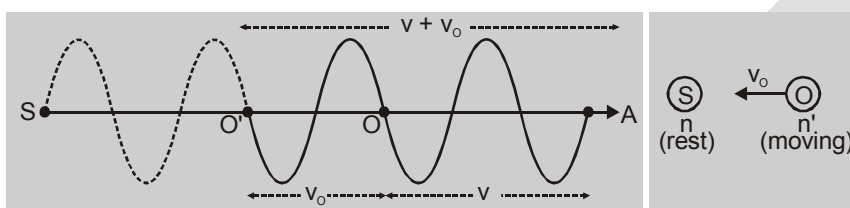
So, apparent wavelength  $\lambda' = \frac{v + v_s}{n}$

and apparent frequency,  $n' = \frac{v}{\lambda'} = \frac{v}{\left(\frac{v + v_s}{n}\right)} = n \left(\frac{v}{v + v_s}\right)$

So,  $n'$  becomes less than  $n$ . ( $n' < n$ )

**Case II :****Observer in motion, source at rest, medium at rest :-**

Let the source (S) and observer (O) are in rest at their respective places. Then  $n$  waves given by source 'S' would be crossing observer 'O' in one second and fill the space  $OA (=v)$

**(1) Observer move towards stationary source :-**

When observer 'O' moves towards 'S' with velocity  $v_o$ , it will cover  $v_o$  distance in one second. So the observer has received not only the  $n$  waves occupying  $OA$  but also received additional number of  $\Delta n$  waves occupying the distance  $OO' (=v_o)$ .

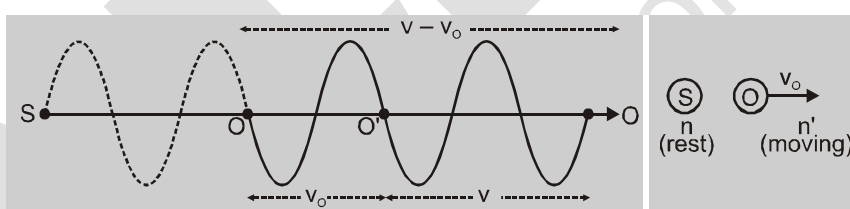
So, total waves received by observer in one second

i.e., apparent frequency  $(n') = \text{Actual waves } (n) + \text{Additional waves } (\Delta n)$

$$n' = \frac{v}{\lambda} + \frac{v_o}{\lambda} = \frac{v + v_o}{(v/n)} = n \left( \frac{v + v_o}{v} \right) \quad \left( \because \lambda = \frac{v}{n} \right) \quad (\text{so, } n' > n)$$

**(2) Observer move away from stationary source :-**

For this situation  $n$  waves will be crowded in distance  $v - v_o$ .



When observer move away from source with  $v_o$  velocity then he will get  $\Delta n$  waves less than real number of waves. So, total number of waves received by observer i.e.,

Apparent frequency  $(n') = \text{Actual waves } (n) - \text{reduction in number of waves } (\Delta n)$

$$n' = \frac{v}{\lambda} - \frac{v_o}{\lambda} = \frac{v - v_o}{\lambda} = \frac{v - v_o}{(v/n)} = \left( \frac{v - v_o}{v} \right) n \quad \left( \because \lambda = \frac{v}{n} \right) \quad (\text{so } n' < n)$$

**Case III :****Effect of motion of medium :-**

$$\text{General formula for doppler effect} = n' = n \left[ \frac{v \pm v_o}{v \mp v_s} \right] \quad \dots(i)$$



If medium (air) is also moving with  $v_m$  velocity in direction of source and observer. Then velocity of sound relative to observer will be  $v \pm v_m$  (-ve sign, if  $v_m$  is opposite to sound velocity). So,

$$n' = n \left( \frac{v \pm v_m \pm v_o}{v \pm v_m \mp v_s} \right) \text{ [On replacing } v \text{ by } v \pm v_m \text{ in equation (i)]}$$

**Note :-** When both 'S' and 'O' are in rest (i.e.  $v_s = v_o = 0$ ) then there is no effect on frequency due to motion of air.

### SPECIAL CASES

**Case-I** If medium moves in a direction opposite to the direction of propagation of sound, then

$$n' = \left( \frac{v - v_m \pm v_o}{v - v_m \pm v_s} \right) n$$

**Case-II** Source in motion towards the observer. Both medium and observer are at rest.

$$n' = \left( \frac{v}{v - v_s} \right) n; \text{ Clearly } n' > n$$

So, when a source of sound approaches a stationary observer, the apparent frequency is more than the actual frequency.

**Case-III** Source in motion away from the observer. Both medium and observer are at rest.

$$n' = \left( \frac{v}{v + v_s} \right) n; \text{ Clearly } n' < n$$

So, when a source of sound moves away from a stationary observer, the apparent frequency is less than actual frequency.

**Case-IV** Observer in motion towards the source. Both medium and source are at rest.

$$n' = \left( \frac{v + v_o}{v} \right) n; \text{ Clearly } n' > n$$

So, when observer is in motion towards the source, the apparent frequency is more than the actual frequency.

**Case-V** Observer in motion away from the source. Both medium and source are at rest.

$$n' = \left( \frac{v - v_o}{v} \right) n; \text{ Clearly } n' < n$$

So, when observer is in motion away from the source, the apparent frequency is less than the actual frequency.

**Case-VI** Both source and observer are moving away from each other. Medium at rest.

$$n' = \left( \frac{v - v_o}{v + v_s} \right) n; \text{ Clearly } n' < n$$

## 6.2 Doppler's effect in reflection of sound (echo)

When the sound is reflected from the reflector the observer receives two notes one directly from the source and other from the reflector. If the two frequencies are different then superposition of these waves result in beats and by the beat frequency we can calculate speed of the source.

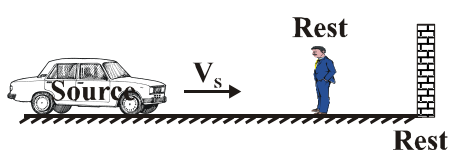
**Case-I**

- When source moves towards stationary target.

$n'_D$  = direct apparent frequency

$n'$  = apparent frequency at reflector

$n'_R$  = reflected apparent frequency

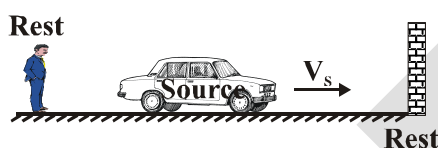


$$n'_D = \left( \frac{V}{V - V_s} \right) n$$

$$n' = \left( \frac{V}{V - V_s} \right) n$$

$$n'_R = n'$$

$$b = \Delta n = n'_R - n'_D = 0$$



$$n'_D = \left( \frac{V}{V + V_s} \right) n$$

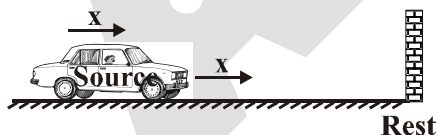
$$n' = \left( \frac{V}{V - V_s} \right) n$$

$$b = \Delta n = \left( \frac{V}{V - V_s} - \frac{V}{V + V_s} \right) n = \frac{2V_s V n}{V^2 - V_s^2} \approx \left( \frac{2V_s}{V} \right) n$$

**Note** Stationary target behave as an observer for incident sound and behave as a source for reflected sound.

**Case-II**

When source and observer both move towards stationary target.



$$n'_D = n,$$

$$n' = \left( \frac{V}{V - x} \right) n$$

$$n'_R = \left( \frac{V + x}{V} \right) n' = \left[ \frac{V + x}{V} \right] \left[ \frac{V}{V - x} \right] n$$

$$n'_R = \left( \frac{V + x}{V - x} \right) n$$

$$b = n'_R - n'_D = \left( \frac{V + x}{V - x} \right) n - n \Rightarrow b = \frac{2x}{V - x} n$$

### CONDITIONS WHEN DOPPLER'S EFFECT IS NOT OBSERVED FOR SOUND WAVES

1. When the source of sound and observer both are at rest then doppler effect is not observed.
2. When the source and observer both are moving with same velocity in same direction.
3. When the source and observer are moving mutually in perpendicular directions.
4. When the medium only is moving.
5. When the distance between the source and observer is constant.

### 6.3 Doppler effect in light :

Doppler effect holds also for EM waves. As speed of light is independent of relative motion between source and observer, the formulae are different from that of sound. Here when either source or observer (detector) or both are in motion, only two cases are possible (approach or recession)

Doppler's effect in light is symmetrical (unlike sound). It means the observer moving towards the source at a particular speed will produce the same frequency change as the source moving towards the observer at the same speed.

In case of approach 
$$n' = n \left( \frac{1 + \frac{v}{c}}{1 - \frac{v}{c}} \right)^{\frac{1}{2}} \quad \text{and} \quad \lambda' = \lambda \left( \frac{1 - \frac{v}{c}}{1 + \frac{v}{c}} \right)^{\frac{1}{2}}$$

In case of recession 
$$n' = n \left( \frac{1 - \frac{v}{c}}{1 + \frac{v}{c}} \right)^{\frac{1}{2}} \quad \text{and} \quad \lambda' = \lambda \left( \frac{1 + \frac{v}{c}}{1 - \frac{v}{c}} \right)^{\frac{1}{2}}$$

If  $v \ll c$  then in case of approach  $n' \approx n \left( 1 + \frac{v}{c} \right)$  in case of recession  $n' \approx n \left( 1 - \frac{v}{c} \right)$

So at low speeds doppler effect in light and sound is governed by the same formula.

### DOPPLER'S SHIFT :

When radiation coming from distant stars are analysed by radio telescopes and compared with their natural radiation wavelength focussed on mean wavelength on a visible spectrum, it is observed that coming radiation has a shift towards red or violet end.

**Red shift** 
$$\Delta\lambda = \lambda' - \lambda = \left( \frac{v}{c} \right) \lambda \quad \Rightarrow \quad \Delta\lambda = \frac{v}{c} \lambda$$

**Violet shift (or blue shift)** 
$$\Delta\lambda = \lambda' - \lambda = - \left( \frac{v}{c} \right) \lambda \quad \Rightarrow \quad \Delta\lambda = - \frac{v}{c} \lambda$$

In case of approach frequency increases while wavelength decreases i.e. shift  $\Delta\lambda$  is towards violet end of the spectrum while in case of recession frequency decreases and wavelength increases i.e. shift  $\Delta\lambda$  is towards red end.

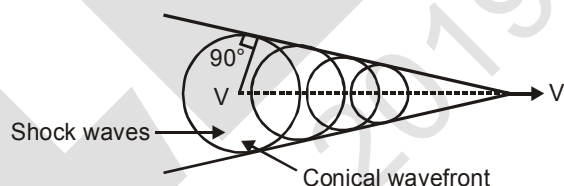
## GOLDEN KEY POINTS

SONAR System	RADAR System
To find out velocity and position of submarines	To find out velocity and position of planes
If $V_s$ = vel. of submarine w.r.t. SONAR system	If $V_R$ = vel. of fighter plane w.r.t. RADAR System
$V$ = Vel. of sound	$\nu_0$ = Material frequency of Radio wave transmitted from RADAR
$n_0$ = Original frequency	$\Delta \nu$ = Change in frequency in light
$\Delta n$ = change in frequency then	
$\Delta n = \frac{2V_s}{V} (n_0)$	$\Delta \nu = \frac{2V_R}{C} (\nu_0)$

- Shock waves :** - A body moving with a supersonic velocity leaves behind itself a conical disturbance region. Disturbance of this kind is called a shock wave. These have a large amount of energy which can damage the buildings.

$$\sin \theta = \frac{V}{V_s} = \frac{1}{\text{Mach number}}$$

$2\theta$  = cone angle.



- Mach number** =  $\frac{\text{speed of any vehicle or body}}{\text{speed of sound}}$ , for super sonic sound mach No.  $> 1$

Generally mach number remain less than one.

## Illustrations

## Illustration 39.

Two tuning forks A and B lying on opposite sides of observer 'O' and of natural frequency 85 Hz move with velocity 10 m/s relative to stationary observer O. Fork A moves away from the observer while the fork B moves towards him. A wind with a speed 10 m/s is blowing in the direction of motion of fork A. Find the beat frequency measured by the observer in Hz. [Take speed of sound in air as 340 m/s]

(1) 5

(2) 6

(3) 7

(4) 8

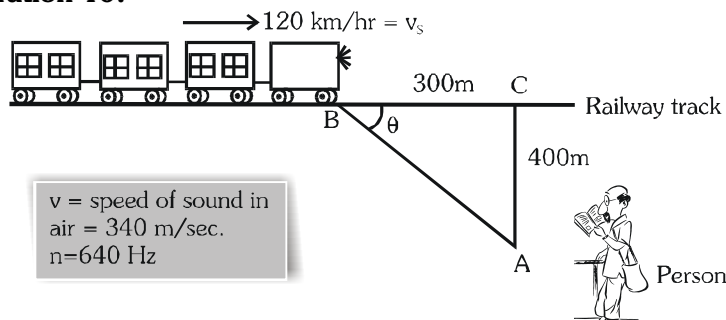
**Solution**

**Ans. (1)**

$$f_{\text{observer for source 'A'}} = f_0 \left[ \frac{v_{\text{sound}} - v_{\text{medium}}}{v_{\text{sound}} - v_{\text{medium}} + v_{\text{source}}} \right] = \frac{33}{34} f_0; f_{\text{observer for source 'B'}} = f_0 \left[ \frac{v_{\text{sound}} + v_{\text{medium}}}{v_{\text{sound}} + v_{\text{medium}} - v_{\text{source}}} \right] = \frac{35}{34} f_0$$

$$\therefore \text{Beat frequency} = f_1 - f_2 = \left( \frac{35 - 33}{34} \right) f_0 = 5$$

**Illustration 40.**



If engine of train produce horn at B point then find apparent frequency observed by observer at A point.

**Solution**

$$n' = \left( \frac{v}{v - v_s \cos \theta} \right) n ; \text{ Direction in AB velocity} = v_s \cos \theta = \left[ 120 \times \frac{5}{18} \right] \times \cos \theta = 120 \times \frac{5}{18} \times \frac{3}{5} = 20 \text{ m/sec.}$$

$$\Rightarrow n' = \left( \frac{340}{340 - 20} \right) \times 640 = 680 \text{ Hz.}$$

**Illustration 41.**

A train, standing in a station-yard, blows a whistle of frequency 400 Hz in still air. The wind starts blowing in the direction from the yard to the station with at a speed of  $10 \text{ ms}^{-1}$ . What are the frequency, wavelength, and speed of sound for an observer standing on the station's platform? Is the situation exactly identical to the case when the air is still and the observer runs towards the yard at a speed of  $10 \text{ ms}^{-1}$ ? The speed of sound in still air can be taken as  $340 \text{ ms}^{-1}$ .

**Solution**

Here source and observer both are at rest when wind starts blowing from source to observer then effecting velocity of sound,  $v_{\text{sound}} = v + v_m = 340 + 10 = 350 \text{ ms}^{-1}$

Since there is no relative motion between source and observer therefore frequency remains the same i.e. 400 Hz.

$$\text{Now wave length } \lambda = \frac{v_{\text{sound}}}{n} = \frac{350}{400} = 0.875 \text{ m}$$

The two situations are not exactly identical, because in second case medium is at rest, while observer in motion.

**Illustration 42.**

A SONAR system fixed in a submarine operates at a frequency 40.0 kHz. An enemy submarine moves towards the SONAR with a speed of  $360 \text{ km h}^{-1}$ . What is the frequency of sound reflected by the submarine? Take the speed of sound in water to be  $1450 \text{ ms}^{-1}$ .

**Solution**

As the sound is observed by enemy submarine.

Here observer (enemy submarine) is moving towards the source (SONAR)

$$\therefore \text{ Apparent frequency } n' = \left( \frac{v + v_0}{v - v_s} \right) n = \left( \frac{1450 + 100}{1450} \right) \times 40 \times 10^3 = \frac{1550}{1450} \times 40 \times 10^3 \text{ Hz}$$

After the sound is reflected, enemy submarine acts. as a source of frequency  $n'$ . This source moves with a speed of  $100 \text{ ms}^{-1}$  towards the observer (SONAR)

$\therefore$  Apparent frequency of sound reflected by the enemy submarine

$$n'' = \left( \frac{v - v_0}{v - v_s} \right) n' = \left( \frac{1450 - 0}{1450 - 100} \right) \times \left( \frac{1550}{1450} \times 40 \times 10^3 \right) = 45.93 \text{ kHz}$$

**Illustration 43.**

Two trains travelling in opposite directions at 126 km/hr each, cross each other while one of them is whistling. If the frequency of the note is 2.22 kHz find the apparent frequency as heard by an observer in the other train :

(a) Before the trains cross each other, (b) After the trains have crossed each other. ( $v_{\text{sound}} = 335 \text{ m/sec}$ )

**Solution**

Here  $v_1 = 126 \times \frac{5}{18} = 35 \text{ m/s}$

(i) In this situation  $\circ \longrightarrow v_1 \quad v_1 \longleftarrow \circ$

$$\text{Observed freq} \quad n' = \left( \frac{v + v_1}{v - v_1} \right) \times n = \left( \frac{335 + 35}{335 - 35} \right) \times 2220 = 2738 \text{ Hz}$$

(ii) In this situation  $v_1 \longleftarrow \circ \quad \circ \longrightarrow v_1$

$$\text{Observed freq} \quad n' = \left( \frac{v - v_1}{v + v_1} \right) \times n = \left( \frac{335 - 35}{335 + 35} \right) \times 2220 = 1800 \text{ Hz}$$

**Illustration 44.**

A star which is emitting radiation at a wavelength of  $5000 \text{ \AA}$ , is approaching the earth with a velocity of  $1.5 \times 10^3 \text{ m/s}$ . Calculate the change in wavelength of the radiation as received by the earth.

**Solution**

$$\Delta\lambda = \frac{v}{c} \lambda = \frac{1.5 \times 10^3}{3 \times 10^8} \times 5000 = 0.025 \text{ \AA}$$

**Illustration 45.**

A person going away from a factory on his scooter at a speed of 36 km/hr listens to the siren of the factory. If the actual frequency of the siren is 700 Hz and a wind is blowing along the direction of the scooter at 36 km/hr, find the observed frequency heard by the person. (Given speed of sound = 340 m/s)

**Solution**

$$\text{In this situation} \quad n' = \left( \frac{v + w - v_0}{v + w} \right) n$$

where  $w = v_0 = 36 \text{ km/hr} = 10 \text{ m/s}$

$$n' = \left( \frac{340 + 10 - 10}{340 + 10} \right) \times 700 = \frac{340}{350} \times 700 = 680 \text{ Hz}$$

**BEGINNER'S BOX-6**

- A bat is flitting about in a cave, navigating via ultrasonic bleeps. Assume that the sound emission frequency of the bat is 40 kHz. During one fast swoop directly toward a flat wall surface, the bat is moving at 0.03 times the speed of sound in air. What frequency does the bat hear reflected off the wall?
- A railway engine moving with a speed of 60 m/s passes a stationary listener. The real frequency of its whistle is 400 Hz. Calculate the apparent frequency heard by the listener.
  - When the engine is approaching the listener.
  - When the engine is moving away from the listener. (velocity of sound = 340 m/s)
- A stationary source emits sound of frequency 1200 Hz. If wind blows at the speed of  $0.1v$ , deduce
  - the change in the frequency for a stationary observer on the wind side of the source.
  - Report the calculations for the case when there is no wind but the observer moves at  $0.1v$  speed towards the source. (given : velocity of sound =  $v$ )
- A car has two horns having a difference in frequency of 180 Hz. The car is approaching a stationary observer with a speed of  $60 \text{ ms}^{-1}$ . Calculate the difference in frequencies of the notes as heard by the observer, if velocity of sound in air is  $330 \text{ ms}^{-1}$ .
- When both source and observer approach each other with a speed equal to the half the speed of sound, then determine the percentage change in frequency of sound as detected by the listener.

# ANSWERS

## BEGINNER'S BOX-1

1. 10 cm. 2. 8.707 s

## BEGINNER'S BOX-2

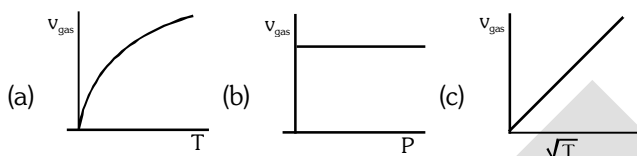
1. 200 cm/s 2.  $\frac{1}{100}$  s, 20 m/s 3. No, None  
4. 0.02 s 5. 220 N 6. 0.5 s  
7. (a) 2.21 m/sec; (b) 1 sec.

## BEGINNER'S BOX-3

1. 2 s 2. 2000 ms<sup>-1</sup> 3. 30dB  
4. After rain fall, the humidity of air increases.  
This lowers the density of air hence there is

increase in velocity of sound  $\left( \because v \propto \frac{1}{\sqrt{\rho}} \right)$

5. We know  $v_{\text{gas}} = \sqrt{\frac{\gamma RT}{M_w}}$



6. Due to this loudness of sound increases.  
7. Velocity of sound wave in air  $v_{\text{air}} = \sqrt{\frac{\gamma RT}{M_w}} \Rightarrow v_{\text{air}} \propto \sqrt{T}$   
so sound travels faster in warm air than in cool air.  
8. Sound wave require material medium for their propagation.  
9.  $\sqrt{27 \cdot 7} \times 100$  m/s  
10. (a) Independent of pressure.  
(b) Increases as  $\sqrt{T}$  (c) Increase

## BEGINNER'S BOX-4

1. 0°, 90°, 120°, 180° 2. 64 : 1 3. 81 : 1  
4. 1375 Hz 5. 1000 Hz 6. 296 Hz  
7. 640 Hz  
8. (a) 200.5, (b) 1, (c) nearly 9/16 9. 60, 72, 78  
10. (a)  $\frac{1}{4}$  s, (b)  $\frac{1}{8}$  s, (c) 12 beats  
11. 1200 Hz, 2000 Hz, 2800 Hz, 3600 Hz, 4400 Hz  
12.  $n_1 = 50$  Hz  $n_{11} = 100$  Hz  
 $n_{17} = 130$  Hz  $n_{27} = 180$  Hz  $n_{33} = 210$  Hz  
 $n_{51} = 300$  Hz

## BEGINNER'S BOX-5

1. (i)  $y = -0.06 \sin 8\pi [t + (x/20)]$ , (ii)  $y = -0.06 \sin 8\pi t$

2. (a)  $y_L = -2.5 \sin \left( 40\pi t - \frac{\pi}{3} x \right)$ ,  $y_R = +2.5 \sin \left( 40\pi t + \frac{\pi}{3} x \right)$

- (b) 3 cm (c) 0

3. (a) The function represents a stationary wave.  
(b) 3m, 60 Hz, 180 ms<sup>-1</sup> (c) 648 N

4. (i)  $y = -0.012 \sin 2\pi (330 t + x)$

(ii)  $y = 0.015 \sin 2\pi (330 t + x)$

5.  $\pm 0.04 \sin 2\pi (200 t + x)$ ; + = free, - = rigid

6. Open organ pipe 7.  $(m-1) \frac{\lambda}{2}$

8. For closed organ pipe  $f_0 = \frac{v}{4\ell} = \frac{340}{4 \times 20 \times 10^{-2}}$   
 $= 425$  Hz  $\Rightarrow$  first harmonic

If pipe is open, its fundamental frequency  $= \frac{v}{2\ell}$   
 $= 850$  Hz so it will not resonant with the given source

9.  $\frac{1}{2}$  10. 100 Hz 11.  $\frac{7}{8}$  12. 0.25m

13. (a) Stationary wave.  
(b) Unacceptable function for any travelling wave.  
(c) Travelling harmonic wave.  
(d) Superposition of two stationary waves.

14. 2700 15. 20, 40 16. 244

17.  $\frac{55}{3}$  Hz. 18. 122, 120

19. (a) 82.5 Hz; (b) 81.675 N

20. (1) forth order; (2) 4; (3) 110 cm, 20 cm

21. 4 kg wt.

22. (i) 40 Hz (ii) 400 Hz (iii) 100 Hz (iv) 280 Hz  
(v) 800 Hz (vi) 100 Hz (vii) 200 Hz  
(viii) 3 cm (ix) 10 cm

23. (i)  $\frac{1}{\sqrt{2}}$  times (ii) No change  
(iii)  $\sqrt{2}$  times (iv) 100 m/s (v) 200 m/s  
(vi) 2 times

24. (i) 75 cm (ii) Slightly more than 75 cm  
(iii) 7 (iv) 4 (v) 130 cm (vi) 10 cm  
(vii) 76 cm (viii) 3.33 cm

## BEGINNER'S BOX-6

1. 42.47 kHz  
2. (a) 485.7 Hz; (b) 340 Hz  
3. (a) no change in frequency; (b) 1320 Hz  
4. 220 Hz 5. 200%

## EXERCISE-I (Conceptual Questions)

## Build Up Your Understanding

## WAVE AND ITS CHARACTERISTICS

- Water waves are of the nature :
  - (1) Transverse
  - (2) Longitudinal
  - (3) Sometimes longitudinal and some times transverse and longitudinal both
  - (4) Neither transverse nor longitudinal
- Sound wave are not polarized because :
  - (1) Their speed is less
  - (2) A medium is needed for their propagation
  - (3) These are longitudinal
  - (4) Their speed depends on temperature
- A thunder tap is heard 5.5 second after the lightening flash. The distance of the flash is (velocity of sound in air is 330 m/sec.) :-
  - (1) 3560 m
  - (2) 300 m
  - (3) 1780 m
  - (4) 1815 m
- Transverse waves can propagate
  - (1) only in solids
  - (2) both in solids and gases
  - (3) neither in solids nor in gases
  - (4) only in gases
- Transverse elastic waves can be propagate in
  - (1) Both solid & gas
  - (2) In solid but not gas
  - (3) Neither solid nor gas
  - (4) None
- A wave of frequency 500 Hz travels between X and Y and travel a distance of 600 m in 2 sec. between X and Y. How many wavelength are there in distance XY :
  - (1) 1000
  - (2) 300
  - (3) 180
  - (4) 2000
- If at a place the speed of a sound wave of frequency 300 Hz is V, the speed of another wave of frequency 150 Hz at the same place will be:
  - (1) V
  - (2) V/2
  - (3) 2V
  - (4) 4V
- The equation of a progressive wave for a wire is:
 
$$Y = 4 \sin \left[ \frac{\pi}{2} \left( 8t - \frac{x}{8} \right) \right]$$
 If x and y are measured in cm then velocity of wave is :
  - (1) 64 cm/s along - x direction
  - (2) 32 cm/s along - x direction
  - (3) 32 cm/s along + x direction
  - (4) 64 cm/s along + x direction
- The equation of progressive wave is
 
$$Y = 4 \sin \left\{ \pi \left( \frac{t}{5} - \frac{x}{9} \right) + \frac{\pi}{6} \right\}$$
 where x and y are in cm. Which of the following statement is true ?
  - (1)  $\lambda = 18$  cm
  - (2) amplitude = 0.04 cm
  - (3) velocity v = 50 cm/s
  - (4) frequency f = 20 Hz
- A plane progressive wave is represented by the equation  $y = 0.25 \cos (2\pi t - 2\pi x)$ . The equation of a wave is with double the amplitude and half frequency but travelling in the opposite direction will be.
  - (1)  $y = 0.5 \cos (\pi t - \pi x)$
  - (2)  $y = 0.5 \cos (2\pi t + 2\pi x)$
  - (3)  $y = 0.25 \cos (\pi t + 2\pi x)$
  - (4)  $y = 0.5 \cos (\pi t + \pi x)$
- A plane wave is described by the equation
 
$$y = 3 \cos \left( \frac{x}{4} - 10t - \frac{\pi}{2} \right)$$
 The maximum velocity of the particles of the medium due to this wave is
  - (1) 30
  - (2)  $\frac{3\pi}{2}$
  - (3) 3/4
  - (4) 40
- The equation  $y = 4 + 2 \sin (6t - 3x)$  represents a wave motion with
  - (1) amplitude 6 units
  - (2) amplitude 4 units
  - (3) wave speed 2 units
  - (4) wave speed 1/2 units



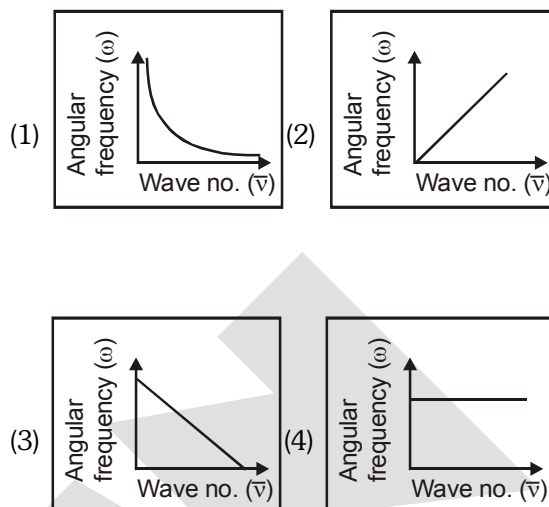
13. The equation of a progressive wave are

$$Y = \sin \left[ 200\pi \left( t - \frac{x}{330} \right) \right], \text{ where } x \text{ is in meter and}$$

$t$  is in second. The frequency and velocity of wave are

- (1) 100 Hz, 5 m/s
  - (2) 300 Hz, 100 m/s
  - (3) 100 Hz, 330 m/s
  - (4) 30 m/s, 5 Hz
14. Due to propagation of longitudinal wave in a medium, the following quantities also propagate in the same direction :
- (1) Energy, Momentum and Mass
  - (2) Energy
  - (3) Energy and Mass
  - (4) Energy and Linear Momentum
15. The waves in which the particles of the medium vibrate in a direction perpendicular to the direction of wave motion is known as :
- (1) transverse waves
  - (2) propagated waves
  - (3) longitudinal waves
  - (4) stationary waves
16. Two wave are represented by equation  
 $y_1 = a \sin \omega t$      $y_2 = a \cos \omega t$   
 the first wave –
- (1) leads the second by  $\pi$
  - (2) lags the second by  $\pi$
  - (3) leads the second by  $\frac{\pi}{2}$
  - (4) lags the second by  $\frac{\pi}{2}$
17. The distance between two consecutive crests in a wave train produced in string is 5 m. If two complete waves pass through any point per second, the velocity of wave is
- (1) 2.5 m/s
  - (2) 5 m/s
  - (3) 10 m/s
  - (4) 15 m/s

18. The graph between wave number ( $\bar{\nu}$ ) and angular frequency ( $\omega$ ) is :



19. The waves produced by a motorboat sailing on water are
- (1) Transverse
  - (2) Longitudinal
  - (3) Longitudinal and Transverse
  - (4) Stationary

### PROGRESSIVE WAVE ON STRING

20. In a string the speed of wave is 10 m/s and its frequency is 100 Hz . The value of the phase difference at a distance 2.5 cm will be :
- (1)  $\pi/2$
  - (2)  $\pi/8$
  - (3)  $3\pi/2$
  - (4)  $2\pi$
21. A uniform rope of mass 0.1 kg and length 2.5 m hangs from ceiling. The speed of transverse wave in the rope at upper end and at a point 0.5 m distance from lower end will be :
- (1) 5 m/s, 2.24 m/s
  - (2) 10 m/s, 3.23 m/s
  - (3) 7.5 m/s, 1.2 m/s
  - (4) 2.25 m/s, 5 m/s
22. The equation of a wave on a string of linear density  $0.04 \text{ kg m}^{-1}$  is given by
- $$y = 0.02(\text{m}) \sin \left[ 2\pi \left( \frac{t}{0.04(\text{s})} - \frac{x}{0.50(\text{m})} \right) \right].$$
- The tension in the string is :
- (1) 6.25 N
  - (2) 4.0 N
  - (3) 12.5 N
  - (4) 0.5 N

23. The mathematical forms for three sinusoidal travelling waves are given by

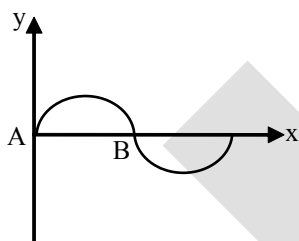
Wave 1 :  $y(x,t) = (2\text{cm}) \sin(3x-6t)$

Wave 2 :  $y(x,t) = (3\text{cm}) \sin(4x-12t)$

Wave 3 :  $y(x,t) = (4\text{cm}) \sin(5x-11t)$

where  $x$  is in meters and  $t$  is in seconds. Of these waves :

- (1) wave 1 has the greatest wave speed and the greatest maximum transverse string speed.
  - (2) wave 2 has the greatest wave speed and wave 1 has the greatest maximum transverse string speed.
  - (3) wave 3 has the greatest wave speed and the greatest maximum transverse string speed.
  - (4) wave 2 has the greatest wave speed and wave 3 has the greatest maximum transverse string speed.
24. The figure shows an instantaneous profile of a rope carrying a progressive wave moving from left to right, then



- (a) the phase at A is greater than the phase at B
  - (b) the phase at B is greater than the phase at A
  - (c) A is moving upwards
  - (d) B is moving upwards
- (1) a & c
  - (2) a & d
  - (3) b & c
  - (4) b & d
25. Linear density of a string is  $1.3 \times 10^{-4} \text{ kg/m}$  and wave equation is  $y = 0.021 \sin(x + 30t)$ . Find the tension in the string where  $x$  in meter,  $t$  in sec.
- (1)  $1.17 \times 10^{-2} \text{ N}$
  - (2)  $1.17 \times 10^{-1} \text{ N}$
  - (3)  $1.17 \times 10^{-3} \text{ N}$
  - (4) None

## SOUND WAVES AND ITS CHARACTERISTICS

26. The speed of sound in air at constant temperature
- (1) is proportional to the atmospheric pressure.
  - (2) is proportional to the square of atmospheric pressure.
  - (3) is proportional to the square root of atmospheric pressure
  - (4) does not depend on atmospheric pressure.
27. At the room temperature the velocity of sound in  $\text{O}_2$  gas is  $V$ . Then in mixture of  $\text{H}_2$  and  $\text{O}_2$  gas the speed of sound at same temprature:
- (1) will be less than  $V$ .
  - (2) will be more than  $V$
  - (3) will be equal to  $V$
  - (4) nothing can be said
28. The velocity of sound in a gas depends
- (1) only on its wave length
  - (2) on the density and the elasticity of gas
  - (3) on intensity of the sound
  - (4) on the amplitude and the frequency.
29. If at some point the amplitude of the sound becomes double and the frequency becomes one fourth then at that point the intensity of sound will be :-
- (1) Become double
  - (2) Be half
  - (3) Become one fourth
  - (4) Remain unchanged
30. A sound is produced in water and moves towards surface of water and some sound moves in air velocity of sound in water is  $1450 \text{ m/s}$  and that in air is  $330 \text{ m/s}$ . When sound moves from water to air then the effect on frequency  $f$  and wave length  $\lambda$  will be:
- (1)  $f$  and  $\lambda$  will remain same
  - (2)  $f$  will remain same but  $\lambda$  will increase
  - (3)  $f$  will remain same but  $\lambda$  will decrease
  - (4)  $f$  will increase and  $\lambda$  will decrease
31. When sound wave travels from air to water, which are of the following remain constant :
- (1) wavelength
  - (2) velocity
  - (3) frequency
  - (4) intensity

32. Newton's formula for the velocity of sound in gases is :

$$(1) v = \sqrt{\frac{2p}{\rho}} \quad (2) v = \sqrt{\frac{p}{\rho}}$$

$$(3) v = \sqrt{\frac{p}{\rho}} \quad (4) v = \frac{3}{2} \sqrt{\frac{p}{\rho}}$$

33. Intensity level of a sound of intensity  $I$  is 30 dB. The ratio  $I/I_0$  is

( $I_0$  is the threshold of hearing)

- (1) 1000 (2) 3000 (3) 300 (4) 30

34. If  $v_m$  is the velocity of sound in moist air and  $v_d$  is the velocity of sound in dry air then :

$$(1) v_m < v_d \quad (2) v_m > v_d$$

$$(3) v_d \gg v_m \quad (4) v_m = v_d$$

35. A sine wave has an amplitude  $A$  and wavelength  $\lambda$ . Let  $V$  be wave velocity and  $v$  be the maximum velocity of a particle in medium then.

$$(1) V = v \text{ if } A = \frac{\lambda}{2\pi}$$

$$(2) V \text{ can not be equal to } v$$

$$(3) V = v \text{ if } \lambda = \frac{3A}{2\pi}$$

$$(4) V = v \text{ if } A = 2\pi\lambda$$

36. A sings with a frequency ( $n$ ) and B sings with a frequency  $1/8$  that of A. If the energy remains the same and the amplitude of A is  $a$ , then amplitude of B will be :

- (1)  $2a$  (2)  $8a$  (3)  $4a$  (4)  $a$

37. The velocities of sound at the same pressure in two monoatomic gases of densities  $\rho_1$  and  $\rho_2$  are  $v_1$  and  $v_2$  respectively. If  $\frac{\rho_1}{\rho_2} = 4$ , then the value of  $\frac{v_1}{v_2}$  is :

- (1)  $\frac{1}{4}$  (2)  $\frac{1}{2}$  (3) 2 (4) 4

38. The time period of SHM of a particle is 12 s. The phase difference between the position at  $t = 3s$  and  $t = 4s$  will be :

- (1)  $\pi/4$  (2)  $3\pi/5$  (3)  $\pi/6$  (4)  $\pi/2$

39. Velocity of sound in medium is  $V$ . If the density of the medium is doubled, what will be the new velocity of sound ?

- (1)  $\sqrt{2}V$  (2)  $V$  (3)  $V/\sqrt{2}$  (4)  $2V$

### REFLECTION OF WAVES AND ECHO

40. A man standing on a cliff claps his hand and hears its echo after one second. If the sound is reflected from another mountain then the distance between the man & reflection points is  $V_{\text{sound}} = 340 \text{ m/sec}$ .

- (1) 680 m (2) 340 m  
(3) 170 m (4) 85 m

### PRINCIPLE OF SUPERPOSITION OF WAVES : INTERFERENCE, BEATS

41. At a particle two simple harmonic motion are acting along the same direction. These are  $y_1 = a_1 \sin \omega t$  and  $y_2 = a_2 \sin (\omega t + \phi)$ . The resultant motion is also a simple harmonic motion whose amplitude will be:

$$(1) a_1^2 + a_2^2 + 2a_1a_2 \cos \phi$$

$$(2) \sqrt{a_1^2 + a_2^2 + 2a_1a_2 \cos \phi}$$

$$(3) \sqrt{a_1^2 + a_2^2 - 2a_1a_2 \cos \phi}$$

$$(4) a_1^2 + a_2^2 - 2a_1a_2 \cos \phi$$

42. The energy in the superposition of waves :

- (1) Is lost  
(2) Increase  
(3) remain same, only redistribution occurs  
(4) None of the above

43. Waves from two sources superimpose on each other at a particular point. Amplitude and frequency of both the waves are equal. The ratio of intensities when both waves reach in the same phase and they reach with the phase difference of  $90^\circ$  will be

- (1) 1:1 (2)  $\sqrt{2}$ :1 (3) 2:1 (4) 4:1

44. Two waves whose intensity are same ( $I$ ) move towards a point P in same phase, then the resultant intensity at point P will be:

- (1)  $4I$  (2)  $2I$  (3)  $\sqrt{2}I$  (4) None

45. Ratio of amplitudes of two waves is 3:4. The ratio of maximum and minimum intensity obtained from them will be :

(1) 7:1 (2) 49:1  
(3) 1:25 (4) 5:1

46. Two coherent sources of intensities  $I_1$  and  $I_2$  produce an interference pattern, the maximum intensity in the interference pattern will be –

(1)  $I_1 + I_2$  (2)  $I_1^2 + I_2^2$   
(3)  $(I_1 + I_2)^2$  (4)  $(\sqrt{I_1} + \sqrt{I_2})^2$

47. Intensities ratio of two waves are 9:1 then the ratio of their maximum and minimum intensities will be:-

(1) 10 : 8 (2) 7 : 2  
(3) 4 : 1 (4) 2 : 1

48. When two tuning forks are sounded together  $x$  beats/sec are heard and frequency of A is  $n$ . Now when one prong of B is loaded with a little wax, the number of beats per second decreases. The frequency of fork B is :

(1)  $n + x$  (2)  $n - x$   
(3)  $n - x^2$  (4)  $n - 2x$

49. A source  $x$  of unknown frequency produces 8 beats with a source of 250 Hz and 12 beats with a source of 270 Hz. The frequency of source  $x$  is :

(1) 258 Hz (2) 242 Hz  
(3) 262 Hz (4) 282 Hz

50. Two waves of wave length 2 m and 2.02 m respectively moving with the same velocity and superimpose to produce 2 beats per sec. The velocity of the waves is:

(1) 400.0 m/s (2) 402 m/s  
(3) 404 m/s (4) 406 m/s

51. A tuning fork produces 4 beats/sec. with another tuning fork B of frequency 288 Hz. If fork is loaded with little wax no. of beats per sec decreases. The frequency of the fork A, before loading is

(1) 290 Hz (2) 288 Hz  
(3) 292 Hz (4) 284 Hz

52.

Column I		Column II	
A	Longitudinal waves	P	Particles of the medium vibrate perpendicular to the wave propagation.
B	Transverse waves	Q	Two progressive waves of slightly different frequencies superimpose in the same direction
C	Beats	R	Two progressive waves of same frequency superimpose in the opposite directions
D	Stationary waves	S	Particles of the medium vibrate along the wave propagation.

(1) A-Q, B-R, C-Q, D-P (2) A-S, B-P, C-Q, D-R  
(3) A-Q, B-S, C-P, D-R (4) A-P, B-Q, C-S, D-R

53. What is the path difference for destructive interference?

(1)  $n\lambda$  (2)  $n(\lambda + 1)$   
(3)  $\frac{(n+1)\lambda}{2}$  (4)  $\frac{(2n+1)\lambda}{2}$

54. When beats are produced by two progressive waves of the same amplitude and of nearly the same frequency, the ratio of maximum intensity to the intensity of one of the waves will be  $n$ . Where  $n$  is

(1) 3 (2) 1 (3) 4 (4) 2

55. The lengths of two closed organ pipes are 0.750 m and 0.770 m. If they are sounded together, 3 beats per second are produced. The velocity of sound will be :-

(1) 350.5 m/sec (2) 335.5 m/sec  
(3) 346.5 m/sec (4) None of these

56. Two waves having equation

$$x_1 = a \sin(\omega t + \phi_1) \quad x_2 = a \sin(\omega t + \phi_2)$$

If in the resultant wave the frequency and amplitude remains equals to amplitude of superimposing waves. Then phase diff. between them –

(1)  $\frac{\pi}{6}$  (2)  $\frac{2\pi}{3}$  (3)  $\frac{3\pi}{4}$  (4)  $\frac{\pi}{4}$

57. Two sources have frequency 256 Hz and 258 Hz, then time difference between two consecutive maxima is –

(1) 1 s (2) 0.5 s (3) 2 ms (4) None

58. Two vibrating tuning forks produce progressive waves given by  $Y_1 = 4 \sin 500\pi t$  and  $Y_2 = 2 \sin 506\pi t$ . Number of beats produced per minute is:

- (1) 3 (2) 360 (3) 180 (4) 60

59. Two plane progressive waves shows destructive interference at point P. Which of the following statement is true at point P :-

- (1) Crest of one wave is superimposed on crest of another wave  
(2) Trough of one wave is superimposed on crest of another wave  
(3) Intensity of resultant wave is equal to the intensity difference of two waves  
(4) Resultant amplitude is equal to the amplitude sum of two waves

### STATIONARY WAVES OR STANDING WAVES IN STRINGS & ORGAN PIPES

60. A uniform string of length L and mass M is fixed at both ends under tension T, Then it can vibrate with frequency given by the formula.

- (1)  $f = \frac{1}{2} \sqrt{\frac{T}{ML}}$  (2)  $f = \frac{1}{2L} \sqrt{\frac{T}{M}}$   
(3)  $f = \frac{1}{2} \sqrt{\frac{T}{M}}$  (4)  $f = \frac{1}{2} \sqrt{\frac{M}{LT}}$

61. The speed of transverse waves in a stretched string is 700 cm/s. If the string is 2 m long, the frequency with which it resonates in fundamental mode is:

- (1) (7/2) Hz (2) (7/4) Hz  
(3) (14) Hz (4) (2/7) Hz

62. With the increase of temperature, the frequency of the organ pipe-

- (1) increases  
(2) decreases  
(3) remains unchanged  
(4) can not say

63. An empty vessel is partially filled with water the frequency of vibration of air column in the vessel

- (1) decreases  
(2) increases  
(3) depends on the purity of water  
(4) remains the same

64. A string is rigidly fixed by two ends and its equation is given by  $y = \cos 2\pi t \sin 2\pi x$

Then minimum length of string is

- (1) 1m (2) 1/2m  
(3) 5m (4)  $2\pi$  m

65. A wave represented by the equation  $y = a \cos(\omega t - kx)$  is superposed by another wave to form a stationary wave such that the point  $x = 0$  is a node. The equation for other wave is -

- (1)  $y = a \sin(\omega t + kx)$  (2)  $y = -a \cos(\omega t - kx)$   
(3)  $y = -a \cos(\omega t + kx)$  (4)  $y = -a \sin(\omega t - kx)$

66. A stretched string is vibrating according to the equation  $y = 5 \sin\left(\frac{\pi x}{2}\right) \cos 4\pi t$ , where y and a are in cm and t is in sec. The distance between two consecutive nodes on the strings is :-

- (1) 2 cm (2) 4 cm  
(3) 8 cm (4) 16 cm

67. The end correction of resonance tube is 1 cm. If lowest resonant length is 15 cm then next resonant length will be :-

- (1) 36 cm (2) 45 cm  
(3) 46 cm (4) 47 cm

68. If the fundamental frequency for a COP is n, then the next three overtones will have ratio :-

- (1) 2 : 3 : 4 (2) 3 : 4 : 5  
(3) 3 : 7 : 11 (4) 3 : 5 : 7

69. A tube closed at one end and containing air produces, when excited, the fundamental note of frequency 512 Hz. If the tube is open at both ends, the fundamental frequency that can be excited is (in Hz)

- (1) 1024 (2) 512  
(3) 256 (4) 128

70. An air column in pipe, which is closed at one end will be in resonance with a vibrating tuning fork of frequency 264 Hz if the length of the column in cm is : [ $v = 330$  m/s]

- (1) 31.25 (2) 62.50  
(3) 110 (4) 125

- 71.** Velocity of sound in air is 320 m/s. A pipe closed at one end has a length of 1 m neglecting end corrections, the air column in the pipe can resonant for sound of frequency.
- (a) 80 Hz (b) 240 Hz  
(c) 500 Hz (d) 400 Hz  
(1) a (2) a,b  
(3) a,b,d (4) a,d
- 72.** The velocity of sound in air is 330 m/s. The fundamental frequency of an organ pipe open at both ends and of length 0.3 metre will be:
- (1) 200 Hz (2) 550 Hz  
(3) 300 Hz (4) 275 Hz
- 73.** A hollow metallic tube of length  $L$  and closed at one end produce resonance with a tuning fork of frequency  $n$ . The entire tube is then heated carefully so that at equilibrium temperature its length changes by  $\ell$ . If the change in velocity  $V$  of sound is  $v$ , the resonance will now be produced by tuning fork of frequency.
- (1)  $(V + v) / [4(L + \ell)]$  (2)  $(V + v) / [4(L - \ell)]$   
(3)  $(V - v) / [4(L + \ell)]$  (4)  $(V - v) / [4(L - \ell)]$
- 74.** A wave of frequency 100 Hz travels along a string towards its fixed end. When this wave travels back, after reflection, a node is formed at a distance of 10 cm from the fixed end. The speed of the wave (incident and reflected) is :
- (1) 5 m/s (2) 10 m/s  
(3) 20 m/s (4) 40 m/s
- 75.** Stationary wave is represented by  $Y = A \sin (100 t) \cos (0.01 x)$  where  $y$  and  $A$  are in mm,  $t$  in sec and  $x$  in m. The velocity of the wave:
- (1) 1 m/s (2)  $10^2$  m/s  
(3)  $10^4$  m/s (4) zero
- 76.** If the tension in a sonometer wire is increased by a factor of four then fundamental frequency of vibration changes by a factor of :
- (1) 4 (2)  $(1/4)$   
(3) 2 (4)  $(1/2)$
- 77.** A sonometer wire, with a suspended mass of  $M = 1$  kg., is in resonance with a given tuning fork. The apparatus is taken to moon where the acceleration due to gravity is  $1/6$  that of earth. To obtain resonance on the moon, the value of  $M$  should be
- (1) 1 kg. (2)  $\sqrt{6}$  kg  
(3) 6 kg (4) 36 kg
- 78.** Stationary waves are produced in 10m long stretched string. If the string vibrates in 5 segments and wave velocity is 20m/sec, then the frequency is-
- (1) 10 Hz (2) 5 Hz  
(3) 4 Hz (4) 2Hz
- 79.** A standing wave having 3 nodes and 2 antinodes is formed between  $1.21 \text{ \AA}$  distance then the wavelength is :-
- (1)  $1.21 \text{ \AA}$  (2)  $2.42 \text{ \AA}$   
(3)  $0.605 \text{ \AA}$  (4)  $4.84 \text{ \AA}$
- 80.** A string under a tension of 129.6 N produces 10 beats/sec when it is vibrated along with a tuning fork. When the tension is the string is increased to 160 N it sounds in unison with same tuning fork. Calculate fundamental freq. of tuning fork.
- (1) 100 Hz (2) 50 Hz  
(3) 150 Hz (4) 200 Hz
- 81.** If vibrations of a string are to be increased to a factor of two, then tension in the string must be made :
- (1) half (2) thrice  
(3) four times (4) eight times
- 82.** An air column having one end closed contains minimum resonance length 50 cm. If it is vibrated by same tuning fork then its next resonance length will be -
- (1) 250 cm (2) 200 cm  
(3) 150 cm (4) 100 cm
- 83.** Stationary waves are so called because in them -
- (1) The particles of the medium are not disturbed at all  
(2) The particles of the medium do not execute S.H. M.  
(3) There occur no flow of energy along the wave  
(4) The interference effect can't be observed

84. The maximum length of a closed pipe that would produce a just audible sound is ( $V_{\text{sound}} = 336 \text{ m/s}$ )  
 (1) 4.2 cm (2) 4.2 m  
 (3) 4.2 mm (4) 1.0 cm
85. In a sonometer wire, the tension is maintained by suspending a mass  $M$  from free end of wire. The fundamental frequency of the wire is  $N \text{ Hz}$ . If the suspended mass is completely immersed in water the fundamental frequency will  
 (1) increases (2) constant  
 (3) decrease (4) can't say
86. A second harmonic has to generated in a string of length  $\ell$  stretched between two rigid supports. The points where the string has to be plucked and touched are –  
 (1) Pluck at  $\frac{\ell}{2}$  touch at  $\frac{3\ell}{4}$   
 (2) Pluck at  $\frac{\ell}{2}$  touch at  $\frac{\ell}{4}$   
 (3) Pluck at  $\frac{\ell}{4}$  touch at  $\frac{3\ell}{4}$   
 (4) Pluck at  $\frac{\ell}{4}$  touch at  $\frac{\ell}{2}$
87. A wave is represented by the equation  $y = a \sin(kx - \omega t)$  is superimposed with another wave to form a stationary wave such that the point  $x = 0$  is a node. Then the equation of other wave is –  
 (1)  $y = a \cos(kx - \omega t)$  (2)  $y = a \cos(kx + \omega t)$   
 (3)  $y = -a \sin(kx + \omega t)$  (4)  $y = a \sin(kx + \omega t)$
88. If the air column in a pipe which is closed at one end, is in resonance with a vibrating tuning fork of frequency  $260 \text{ Hz}$ , then the length of the air column is :  
 (1) 35.7 cm (2) 31.7 cm  
 (3) 12.5 cm (4) 62.5 cm
89. If the tension and diameter of a sonometer wire of fundamental frequency ( $n$ ) is doubled and density is halved then its fundamental frequency will become :-  
 (1)  $\frac{n}{4}$  (2)  $\sqrt{2}n$   
 (3)  $n$  (4)  $\frac{n}{\sqrt{2}}$
90. The tension in a piano wire is  $10\text{N}$ . What should be the tension in the wire to produce a note of double the frequency ?  
 (1)  $10\text{N}$  (2)  $20\text{N}$   
 (3)  $40\text{N}$  (4)  $80\text{N}$
91. A sound wave of frequency  $330\text{Hz}$  is incident normally at reflected wall then minimum distance from wall at which partial vibrate very much :- ( $V_{\text{sound}} = 330 \text{ m/s}$ )  
 (1)  $0.25 \text{ m}$  (2)  $0.125 \text{ m}$   
 (3)  $1 \text{ m}$  (4)  $0.5 \text{ m}$
92. An open organ pipe of length  $33 \text{ cm}$ , vibrates with frequency  $1000 \text{ Hz}$ . If velocity of sound is  $330 \text{ m/s}$ , then its frequency is:-  
 (1) Fundamental frequency  
 (2) First overtone of pipe  
 (3) Second overtone  
 (4) Fourth overtone
93. Fundamental frequency of sonometer wire is  $n$ . If the length, tension and diameter of wire are tripled, the new fundamental frequency is :-  
 (1)  $n/\sqrt{3}$  (2)  $n/3$   
 (3)  $n\sqrt{3}$  (4)  $n/3\sqrt{3}$
94. A string in a musical instrument is  $50 \text{ cm}$  long and its fundamental frequency is  $800 \text{ Hz}$ . If a frequency of  $1000 \text{ Hz}$  is to be produced, then required length of string is :  
 (1)  $62.5 \text{ cm}$  (2)  $50 \text{ cm}$   
 (3)  $40 \text{ cm}$  (4)  $37.5$
95. Four wires of identical lengths, diameters and of the same material are stretched on a sonometer wire. The ratio of their tension is  $1 : 4 : 9 : 16$ . The ratio of their fundamental frequencies is  
 (1)  $1 : 2 : 3 : 4$  (2)  $16 : 9 : 4 : 1$   
 (3)  $1 : 4 : 9 : 16$  (4)  $4 : 3 : 2 : 1$
96. Given equation is related to  

$$y = \cos\left(\frac{2\pi}{\lambda}x\right) \cos(2\pi vt)$$
  
 (1) Transverse progressive  
 (2) Longitudinal progressive  
 (3) Longitudinal stationary wave  
 (4) Transverse stationary wave

97. If  $V$  is the speed of sound in air then the shortest length of the closed pipe which resonates to a frequency  $n$  :

(1)  $\frac{V}{2n}$       (2)  $\frac{V}{4n}$       (3)  $\frac{4n}{V}$       (4)  $\frac{2n}{V}$

98. A stretched string is 1 m long. Its mass per unit length is 0.5 g/m. It is stretched with a force of 20 N. It plucked at a distance of 25 cm from one end. The frequency of note emitted by it will be:

(1) 400 Hz                      (2) 300 Hz  
(3) 200 Hz                      (4) 100 Hz

99. What is the beat frequency produced when following two waves are sounded together ?

$$x_1 = 10 \sin (404\pi t - 5\pi x),$$

$$x_2 = 10 \sin (400\pi t - 5\pi x).$$

(1) 4              (2) 1              (3) 3              (4) 2

100. What is minimum length of a tube, open at both ends, that resonates with tuning fork of frequency 350 Hz ? (velocity of sound in air = 350 m/s)

(1) 50 cm    (2) 100 cm    (3) 75 cm    (4) 25 cm

101. An underwater sonar source operating at a frequency of 60 kHz directs its beam towards the surface. If velocity of sound in air is 330 m/s, wavelength and frequency of the waves in air are:-

(1) 5.5 mm, 60 kHz      (2) 3.30 m, 60kHz  
(3) 5.5 mm, 30 kHz      (4) 5.5 mm, 80 kHz

102. An organ pipe closed at one end has fundamental frequency of 1500 Hz. The maximum number of overtones generated by this pipe which a normal person can hear is

(1) 14              (2) 13              (3) 6              (4) 9

103. Length of the close organ pipe is 1 m. At which frequency resonance will not occur ( $v = 320$  m/sec.)

(1) 80 Hz    (2) 240 Hz    (3) 300 Hz    (4) 400 Hz

104. A 10 cm long organ pipe is open at one end and closed at other end. What is the maximum wavelength of wave produced by it :-

(1) 40cm    (2) 20cm    (3) 10cm    (4) 5cm

105. An open resonating tube has fundamental frequency of  $n$ . When half of its length is dipped into water, then its fundamental frequency will be:

(1)  $n$               (2)  $n/2$               (3)  $2n$               (4)  $3/2 n$ .

106. A pipe is closed from one end and open from another end then which statement is true ?

(1) Node is formed slightly above the open end.  
(2) Node is formed slightly below the open end.  
(3) Antinode is formed slightly above the open end.  
(4) Antinode formed slightly below the open end.

### DOPPLER EFFECT IN SOUND WAVES AND LIGHT WAVES

107. The apparent change in the pitch of sound due to relative motion between observer and the source is called:

(1) Doppler's effect              (2) Resonance of waves  
(3) interference              (4) none of the above

108. A siren blown in workshop emits waves of frequency 1000 Hz. A car driver approaches the workshop with velocity 90 km/hour then frequency of sound heard by driver will be in Hz. ( $V_{\text{sound}} = 330$  m/s)

(1) 926              (2) 1076              (3) 1176              (4) 1000

109. A star is continuously moving away from us than the wavelength coming from star on the earth :

(1) Will shift towards violet colour  
(2) Will shift towards red colour.  
(3) remain unchanged  
(4) Will shift sometimes towards violet and some other time it will shift towards red colour.

110. A source of frequency 200 Hz is moving towards an observer with a velocity equal to the sound velocity  $V$ . If observer also moves away from the source with same velocity then apparent frequency heard by observer will be :

(1) 50 Hz                      (2) 160 Hz  
(3) 150 Hz                      (4) 200 Hz

111. Doppler's effect in the form of frequency doesn't depend upon :

(1) Frequency produced by waves  
(2) Velocity of source  
(3) Velocity of observer.  
(4) Separation between source & observer.

112. The wavelength of the light received from a galaxy is 0.4% greater than the wave length on the earth then the velocity of galaxy relative to the earth will be:

(1)  $1.2 \times 10^7$  m/sec              (2)  $1.2 \times 10^6$  m/sec  
(3)  $1.2 \times 10^5$  m/sec              (4)  $1.2 \times 10^4$  m/sec



- 113.** The term "Red shift" referring to doppler's effect for light represent which of following property :  
 (1) decrease in frequency  
 (2) increase in frequency  
 (3) decrease in intensity  
 (4) Increase in intensity
- 114.** A source and an observer moves away from each other, with a velocity of 15 m/sec with respect to ground. If observer finds the frequency of sound coming from source as 1950 Hz. Then actual frequency of source will be  
 (velocity of sound = 340 m/sec.) :  
 (1) 1785 Hz (2) 1968 Hz  
 (3) 1950 Hz (4) 2130 Hz
- 115.** A source of sound of frequency  $n$  and a listener approach each other with a velocity equal to  $\frac{1}{20}$  of velocity of sound. The apparent frequency heard by the listener is :  
 (1)  $\left(\frac{21}{19}\right)n$  (2)  $\left(\frac{20}{21}\right)n$  (3)  $\left(\frac{21}{20}\right)n$  (4)  $\left(\frac{19}{20}\right)n$
- 116.** A source of sound of frequency 1000 Hz is moving with a uniform velocity 20 m/s. The ratio of apparent frequency heard by the observer before and after the source crosses him would be :  
 $[v = 340 \text{ m/s}]$   
 (1) 9 : 8 (2) 8 : 9 (3) 1 : 1 (4) 9 : 10
- 117.** Two sound sources (of same frequency) are placed at distance of 100 meter. An observer, when moving between both sources, hears 4 beats per second. The distance between sound source is now changed to 400 meter then the beats/second heard by observer will be:  
 (1) 2 (2) 4 (3) 8 (4) 16
- 118.** Doppler effect for sound depends upon the relative motion of source and listener and it also depends upon that which one of these is in motion. Whereas in doppler effect for light it only depends upon the relative motion of the source of light and observer. The reason for it is :  
 (1) Einstein's mass energy relation  
 (2) Einstein's theory of relativity  
 (3) Photo electric effect  
 (4) none of above
- 119.** A source of sound of frequency 500 Hz is moving towards an observer with velocity 30 m/s. The speed of sound is 330 m/s. The frequency heard by the observer will be :  
 (1) 550 Hz (2) 458.3 Hz  
 (3) 530 Hz (4) 545.5 Hz
- 120.** A bus is moving with a velocity of 5 m/s towards a huge wall. The driver sounds a horn of frequency 165 Hz. If the speed of sound in air is 335 m/s, No. of beats heard by a passenger on bus will be—  
 (1) 6 (2) 5 (3) 3 (4) 4
- 121.** A sound source is going away from an observer with the sound speed. The apparent frequency which the observer listen  
 (1) will be half  
 (2) will remains same  
 (3) will be double  
 (4) will not be observed
- 122.** The wavelength of a distant star is  $5700 \text{ \AA}$  and the spectral light has a shift of  $1.9 \text{ \AA}$  towards red end then the velocity of star relative to the earth will be:  
 (1)  $5 \times 10^5 \text{ m/sec}$  (2)  $2 \times 10^5 \text{ m/sec}$   
 (3)  $1.8 \times 10^5 \text{ m/sec}$  (4)  $1 \times 10^5 \text{ m/sec}$ .
- 123.** Two trains A and B are moving in the same direction with velocities 30 m/s and 10 m/s respectively. B is behind from A and A blows a horn of frequency 450 Hz. Then the apparent frequency heard by observer on train B is (speed of sound is 330 m/s):  
 (1) 425 Hz (2) 300 Hz  
 (3) 450 Hz (4) 350 Hz
- 124.** If a star emitting light of wavelength  $5000 \text{ \AA}$  is moving towards earth with a velocity of  $1.5 \times 10^6 \text{ m/s}$  then the shift in the wavelength due to Doppler's effect will be :  
 (1)  $2.5 \text{ \AA}$  (2)  $250 \text{ \AA}$   
 (3)  $25 \text{ \AA}$  (4) Zero
- 125.** Two stationary sources each emitting waves of wave length  $\lambda$ . An observer moves from one source to other with velocity  $u$ . Then number of beats heard by him :-  
 (1)  $\frac{2u}{\lambda}$  (2)  $\frac{u}{\lambda}$  (3)  $\sqrt{u\lambda}$  (4)  $\frac{u}{2\lambda}$

**126.** A vehicle, with a horn of frequency  $n$  is moving with a velocity of 30 m/s in a direction perpendicular to the straight line joining the observer and the vehicle. The observer perceives the sound to have a frequency  $n + n_1$ . Then : (Take velocity of sound in air 330 m/s) :

- (1)  $n_1 = 10n$  (2)  $n_1 = -n$   
 (3)  $n_1 = 0$  (4)  $n_1 = 2n$

**127.** Doppler effect for light differs from that for sound in regards that :

- (1) the relative frequency shift is smaller for light than for sound.  
 (2) the velocity addition valid for sound is not true for light waves.  
 (3) velocity of light is very large as compared to sound.  
 (4) light waves are electromagnetic waves but sound waves are mechanical.

**128.** If a source is moving away from a stationary observer with half of velocity of sound. The frequency observed will be :-

- (1) one-third (2) doubled  
 (3) halved (4) two-third

**129.** A siren emitting sound of frequency 800 Hz is going away, from a static listener, with a speed of 30 m/s. Frequency of sound to be heard by the listener is : (Velocity of sound = 330 m/s) :-

- (1) 286.5 Hz (2) 481.2 Hz  
 (3) 733.3 Hz (4) 644.8 Hz

**130.** As temperature increase, difference between apparent doppler frequency and actual frequency

- (1) Decreases  
 (2) Remains unchanged  
 (3) Increases  
 (4) Depending on frequency, increase or decrease.

**131.** An observer moves towards a stationary source of sound with a speed  $1/5$ th of the speed of sound. The wavelength and frequency of the source are  $\lambda$  and  $f$  respectively. The apparent frequency and wavelength recorded by the observer are respectively :-

- (1)  $1.2f, 1.2\lambda$  (2)  $1.2f, \lambda$   
 (3)  $f, 1.2\lambda$  (4)  $0.8f, 0.8\lambda$

**132.** Velocity of star is  $10^6$  m/s and frequency of emitted light is  $4.5 \times 10^{14}$  Hz. If star is moving away, then apparent frequency will be :

- (1) 4.5 Hz. (2)  $4.5 \times 10^{16}$  Hz.  
 (3)  $4.485 \times 10^{14}$  Hz. (4)  $4.5 \times 10^8$  Hz.

**EXERCISE-I (Conceptual Questions)****ANSWER KEY**

Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans.	3	3	4	2	2	1	1	4	1	4	1	3	3	4	1
Que.	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Ans.	4	3	2	3	1	1	1	4	2	2	4	2	2	3	3
Que.	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45
Ans.	3	2	1	2	1	2	2	3	3	3	2	3	3	1	2
Que.	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
Ans.	4	3	1	1	3	3	2	4	3	3	2	2	3	2	1
Que.	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75
Ans.	2	1	2	2	3	1	4	4	1	1	3	2	1	3	4
Que.	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90
Ans.	3	3	2	1	1	3	3	3	2	3	4	4	2	3	3
Que.	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105
Ans.	1	2	4	3	1	4	2	3	4	1	1	3	3	1	1
Que.	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120
Ans.	3	1	2	2	4	4	2	1	4	1	1	2	2	1	2
Que.	121	122	123	124	125	126	127	128	129	130	131	132			
Ans.	1	4	1	3	1	3	2	4	3	1	2	3			

**EXERCISE-II (Previous Year Questions)**

**AIPMT/NEET & AIIMS (2006-2018)**

**AIPMT 2006**

- Which one of the following statements is true:-  
 (1) Both light and sound waves in air are transverse  
 (2) The sound waves in air are longitudinal while the light waves are transverse  
 (3) Both light and sound waves in air are longitudinal  
 (4) Both light and sound waves can travel in vacuum

**AIIMS 2006**

- A boat at anchor is rocked by waves whose crests are 100m apart and velocity is 25m/sec. The boat bounces up once in every –  
 (1) 2500 s (2) 75 s (3) 4 s (4) 0.25 s
- For waves propagating in a medium, identify the property that is independent of the others:-  
 (1) Velocity  
 (2) Wavelength  
 (3) Frequency  
 (4) All these depend on each other
- When a guitar string is sounded with a 440 Hz tuning fork a beat frequency of 5 Hz is heard. If the experiment is repeated with a tuning fork of 437 Hz the beat frequency is 8 Hz. The string frequency (Hz) is –  
 (1) 445 (2) 435 (3) 429 (4) 448

**AIPMT 2009**

- The driver of a car travelling with speed 30 m/sec towards a hill, sounds a horn of frequency 600 Hz. If the velocity of sound in air is 330 m/s, the frequency of reflected sound as heard by driver is  
 (1) 500 Hz (2) 550 Hz  
 (3) 555.5 Hz (4) 720 Hz
- A wave in a string has an amplitude of 2cm. The wave travels in the +ve direction of x axis with a speed of 128 m/sec and it is noted that 5 complete waves fit in 4 m length of the string. The equation describing the wave is :-  
 (1)  $y = (0.02) \sin (7.85x - 1005t)$   
 (2)  $y = (0.02) \sin (7.85x + 1005t)$   
 (3)  $y = (0.02) \sin (15.7x - 2010t)$   
 (4)  $y = (0.02) \sin (15.7x + 2010t)$

**AIPMT (Pre) 2010**

- A transverse wave is represented by  $y = A \sin (\omega t - kx)$ . For what value of the wavelength is the wave velocity equal to the maximum particle velocity ?  
 (1) A (2)  $\frac{\pi A}{2}$   
 (3)  $\pi A$  (4)  $2\pi A$
- A tuning fork of frequency 512 Hz makes 4 beats per second with the vibrating string of a piano. The beat frequency decreases to 2 beats per seconds when the tension in the piano string is slightly increased. The frequency of the piano string before increasing the tension was :  
 (1) 508 Hz (2) 510 Hz  
 (3) 514 Hz (4) 516 Hz

**AIPMT (Pre) 2011**

- Two waves are represented by the equations  $y_1 = a \sin (\omega t + kx + 0.57)$  m and  $y_2 = a \cos (\omega t + kx)$  m where x is in meter and t in sec. The phase difference between them is :-  
 (1) 1.0 radian (2) 1.25 radian  
 (3) 1.57 radian (4) 0.57 radian
- Sound waves travel at 350 m/s through a warm air and at 3500 m/s through brass. The wavelength of a 700 Hz acoustic wave as it enters brass from warm air :  
 (1) decreases by a factor 10  
 (2) increases by a factor 20  
 (3) increases by a factor 10  
 (4) decreases by a factor 20

**AIPMT (Mains) 2011**

- Two identical piano wires, kept under the same tension T have a fundamental frequency of 600 Hz. The fractional increase in the tension of one of the wires which will lead to occurrence of 6 beats/s when both the wires oscillate together would be :-  
 (1) 0.01 (2) 0.02  
 (3) 0.03 (4) 0.04

## AIIMS 2011

12. What is your observation when two source are emitting sound with frequency 499 Hz & 501 Hz:
- (1) Frequency of 500 Hz is heard with change in intensity takes place twice.
  - (2) Frequency of 500 Hz is heard with change in intensity takes place Once.
  - (3) Frequency of 2Hz is heard with change in intensity takes place Once.
  - (4) Frequency of 2Hz is heard with change in intensity takes place twice.

## AIPMT (Pre) 2012

13. Two sources of sound placed close to each other, are emitting progressive waves given by  $y_1 = 4 \sin 600\pi t$  and  $y_2 = 5 \sin 608\pi t$ . An observer located near these two sources will hear :-
- (1) 8 beats per second with intensity ratio 81 : 1 between waxing and waning
  - (2) 4 beats per second with intensity ratio 81 : 1 between waxing and waning
  - (3) 4 beats per second with intensity ratio 25 : 16 between waxing and waning
  - (4) 8 beats per second with intensity ratio 25 : 16 between waxing and waning

## AIPMT (Mains) 2012

14. The equation of a simple harmonic wave is given by :

$$y = 3 \sin \frac{\pi}{2} (50 t - x),$$

where x and y are in metres and t is in seconds. The ratio of maximum particle velocity to the wave velocity is :-

- (1)  $3\pi$       (2)  $\frac{2}{3}\pi$       (3)  $2\pi$       (4)  $\frac{3}{2}\pi$

## AIIMS 2012

15. A particle moving about its equilibrium position with equation  $y = -ax - bt$ . Interpret the condition :-
- (1) It will always perform the SHM
  - (2) It can never perform the SHM
  - (3) It can perform SHM only when  $t \geq \frac{bx}{a}$
  - (4) It can perform SHM only when  $t \leq \frac{bx}{a}$

## NEET-UG 2013

16. A wave travelling in the +ve x-direction having displacement along y-direction as 1m, wavelength  $2\pi$  m and frequency of  $\frac{1}{\pi}$  Hz is represented by :
- (1)  $y = \sin (2\pi x + 2\pi t)$
  - (2)  $y = \sin (x - 2t)$
  - (3)  $y = \sin (2\pi x - 2\pi t)$
  - (4)  $y = \sin (10\pi x - 20\pi t)$
17. A source of unknown frequency gives 4 beats/s, when sounded with a source of known frequency 250 Hz. The second harmonic of the source of unknown frequency gives five beats per second, when sounded with a source of frequency 513 Hz. The unknown frequency is
- (1) 260 Hz
  - (2) 254 Hz
  - (3) 246 Hz
  - (4) 240 Hz
18. If we study the vibration of a pipe open at both ends, then the following statement is not true :
- (1) Pressure change will be maximum at both ends
  - (2) Open end will be antinode
  - (3) Odd harmonics of the fundamental frequency will be generated
  - (4) All harmonics of the fundamental frequency will be generated

## AIIMS 2013

19. In astronomy, increase in wavelength due to doppler effect is known as :-
- (1) Red shift
  - (2) Voilet shift
  - (3) UV shift
  - (4) IR shift

## AIPMT 2014

20. If  $n_1$ ,  $n_2$  and  $n_3$  are the fundamental frequencies of three segments into which a string is divided, then the original fundamental frequency n of the string is given by :-

$$(1) \frac{1}{n} = \frac{1}{n_1} + \frac{1}{n_2} + \frac{1}{n_3}$$

$$(2) \frac{1}{\sqrt{n}} = \frac{1}{\sqrt{n_1}} + \frac{1}{\sqrt{n_2}} + \frac{1}{\sqrt{n_3}}$$

$$(3) \sqrt{n} = \sqrt{n_1} + \sqrt{n_2} + \sqrt{n_3}$$

$$(4) n = n_1 + n_2 + n_3$$

21. The number of possible natural oscillations of air column in a pipe closed at one end of length 85 cm whose frequencies lie below 1250 Hz are: (velocity of sound = 340 ms<sup>-1</sup>)
- (1) 4 (2) 5  
(3) 7 (4) 6

AIIMS 2014

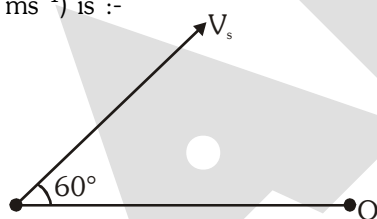
22. An astronomical object is moving with such a speed that red shift of 1nm is observed in wavelength of 600 nm of wave received from it, the speed of wave is :-
- (1)  $5 \times 10^5$  m/s (2)  $4 \times 10^5$  m/s  
(3)  $3 \times 10^5$  m/s (4)  $2 \times 10^5$  m/s

AIPMT 2015

23. The fundamental frequency of a closed organ pipe of length 20 cm is equal to the second overtone of an organ pipe open at both the ends. The length of organ pipe open at both the ends is :-
- (1) 100 cm (2) 120 cm  
(3) 140 cm (4) 80 cm

RE-AIPMT-2015

24. A source of sound S emitting waves of frequency 100 Hz and an observer O are located at some distance from each other. The source is moving with a speed of 19.4 ms<sup>-1</sup> at an angle of 60° with the source observer line as shown in the figure. The observer is at rest. The apparent frequency observed by the observer (velocity of sound in air 330 ms<sup>-1</sup>) is :-



- (1) 97 Hz (2) 100 Hz  
(3) 103 Hz (4) 106 Hz
25. A string is stretched between two fixed points separated by 75.0 cm. It is observed to have resonant frequencies of 420 Hz and 315 Hz. There are no other resonant frequencies between these two. The lowest resonant frequencies for this string is :-
- (1) 105 Hz (2) 155 Hz  
(3) 205 Hz (4) 10.5 Hz

AIIMS 2015

26. A uniform string of length 20 m & mass 1 kg is hung vertically. Find the speed of wave at the mid point of the string :-

- (1) 20 m/s (2) 30 m/s  
(3)  $10\sqrt{2}$  m/s (4) 10 m/s

27. A string of linear mass density 4 g/cm is vibrating according to equation :-

$$y = A \sin(120\pi t) \cos\left(\frac{2\pi}{5}x\right)$$

where x is in centimeters.

Find the tension in the string

- (1) 3.6 N (2) 36 N  
(3) 7.2 N (4) 72 N

NEET-I 2016

28. A siren emitting a sound of frequency 800 Hz moves away from an observer towards a cliff at a speed of 15ms<sup>-1</sup>. Then, the frequency of sound that the observer hears in the echo reflected from the cliff is :

(Take velocity of sound in air = 330 ms<sup>-1</sup>)

- (1) 765 Hz (2) 800 Hz  
(3) 838 Hz (4) 885 Hz

29. A uniform rope of length L and mass m<sub>1</sub> hangs vertically from a rigid support. A block of mass m<sub>2</sub> is attached to the free end of the rope. A transverse pulse of wavelength λ<sub>1</sub> is produced at the lower end of the rope. The wavelength of the pulse when it reaches the top of the rope is λ<sub>2</sub>. The ratio λ<sub>2</sub>/λ<sub>1</sub> is :

- (1)  $\sqrt{\frac{m_1}{m_2}}$  (2)  $\sqrt{\frac{m_1 + m_2}{m_2}}$   
(3)  $\sqrt{\frac{m_2}{m_1}}$  (4)  $\sqrt{\frac{m_1 + m_2}{m_1}}$

30. An air column, closed at one end and open at the other, resonates with a tuning fork when the smallest length of the column is 50 cm. The next larger length of the column resonating with the same tuning fork is :

- (1) 66.7 cm (2) 100 cm  
(3) 150 cm (4) 200 cm

## NEET-II 2016

31. The second overtone of an open organ pipe has the same frequency as the first overtone of a closed pipe  $L$  metre long. The length of the open pipe will be

(1)  $\frac{L}{2}$       (2)  $4L$       (3)  $L$       (4)  $2L$

32. Three sound waves of equal amplitudes have frequencies  $(n-1)$ ,  $n$ ,  $(n+1)$ . They superimpose to give beats. The number of beats produced per second will be :-

(1) 3                                      (2) 2  
(3) 1                                      (4) 4

## AIIMS 2016

33. Two waves  $E_1 = E_0 \sin \omega t$  and  $E_2 = E_0 \sin(\omega t + 60^\circ)$  superimpose each other then find out initial phase of resultant wave ?

(1)  $30^\circ$                                       (2)  $60^\circ$   
(3)  $120^\circ$                                       (4)  $0^\circ$

34. Fundamental frequency of open organ pipe is 250 Hz. Third harmonic of closed organ pipe is equal to second harmonic of open organ pipe. Find length of closed organ pipe.

( $v_{\text{air}} = 343 \text{ m/s}$ )

(1) 100.53 cm                                      (2) 75.53 cm  
(3) 45.32 cm                                      (4) 51.45 cm

35. Intensity of two waves are  $9I$  and  $I$  respectively. Find out resultant intensity if phase difference between them is  $\pi$ .

(1)  $3I$                                       (2)  $4I$   
(3)  $5I$                                       (4)  $6I$

36. An aeroplane of frequency  $f$  is moving towards a stationary observer. Frequency heard by observer is  $3f$  then find out ratio of speed of aeroplane and sound.

(1)  $\frac{1}{4}$       (2)  $\frac{2}{3}$       (3)  $\frac{1}{3}$       (4)  $\frac{3}{5}$

37. A stretched string with tension 20N and mass per unit length 5 gm/cm is vibrating with frequency 20Hz. Calculate minimum length of string ?

(1) 20 cm                                      (2) 30 cm  
(3) 5 cm                                      (4) 15.8 cm

## NEET(UG) 2017

38. The two nearest harmonics of a tube closed at one end and open at other end are 220 Hz and 260 Hz. What is the fundamental frequency of the system?

(1) 20 Hz                                      (2) 30 Hz  
(3) 40 Hz                                      (4) 10 Hz

39. Two cars moving in opposite directions approach each other with speed of 22 m/s and 16.5 m/s respectively. The driver of the first car blows a horn having a frequency 400 Hz. The frequency heard by the driver of the second car is [velocity of sound 340 m/s] :-

(1) 361 Hz                                      (2) 411 Hz  
(3) 448 Hz                                      (4) 350 Hz

## AIIMS 2017

40. Two sound waves having pressure

$$P_1 = 2 \times 10^4 \sin(2\pi \times 10^4 t) \text{ Pa and}$$

$$P_2 = 4 \times 10^4 \sin(3\pi \times 10^4 t + \pi/6) \text{ Pa}$$

superimpose with each other. Find the amplitude of resultant wave.

(1)  $4.47 \times 10^4 \text{ Pa}$   
(2) 4.47 Pa  
(3)  $5.67 \times 10^4 \text{ Pa}$   
(4) 5.67 Pa

## NEET(UG) 2018

41. A tuning fork is used to produce resonance in a glass tube. The length of the air column in this tube can be adjusted by a variable piston. At room temperature of  $27^\circ\text{C}$  two successive resonances are produced at 20 cm and 73 cm column length. If the frequency of the tuning fork is 320 Hz, the velocity of sound in air at  $27^\circ\text{C}$  is :-

(1) 330 m/s                                      (2) 339 m/s  
(3) 350 m/s                                      (4) 300 m/s

42. The fundamental frequency in an open organ pipe is equal to the third harmonic of a closed organ pipe. If the length of the closed organ pipe is 20 cm, the length of the open organ pipe is :-

(1) 13.2 cm                                      (2) 8 cm  
(3) 12.5 cm                                      (4) 16 cm

AIIMS 2018

43. A string of mass 100 gm is clamped between two rigid support. A wave of amplitude 2 mm is generated in string. If angular frequency of wave is 5000 rad/s then total energy of the wave in string is:-

- (1) 25 J      (2) 5 J      (3) 0.5 J      (4) 2.5 J

44. A string of mass 10 gram and length 1 m is stretched between two rigid supports. It vibrates with its fundamental node of 50 Hz. Tension in string is :-

- (1) 50 N                      (2) 100 N  
(3) 150 N                    (4) 10 N

45. Two waves of frequency 10 KHz and 10.2 KHz propagate and superimpose. Time after which wave envelope repeats is :-

- (1) 5 ms                      (2) 10 ms  
(3) 0.5 ms                    (4) 50 ms

EXERCISE-II (Previous Years Questions)

ANSWER KEY

Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans.	2	3	1	1	4	1	4	1	1	3	2	1	2	4	2
Que.	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Ans.	2	2	1	1	1	4	1	2	3	1	4	1	3	2	3
Que.	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45
Ans.	4	2	1	4	2	2	4	1	3	1	2	1	4	2	1



## EXERCISE-III (Analytical Questions)

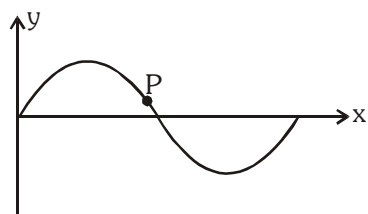
## Check Your Understanding

1. Transverse wave of same frequency are generated in two steel wires A and B. The diameter of A is twice of B and the tension in A is half that in B. The ratio of velocities of waves in A and B is –

(1)  $1:\sqrt{2}$  (2)  $1:2$

(3)  $3:2\sqrt{2}$  (4)  $1:2\sqrt{2}$

2. A transverse sinusoidal wave moves along a string in the positive x-direction at a speed of 10 cm/s. The wavelength of the wave is 0.5 m and its amplitude is 10 cm. At a particular time t, the snap shot of the wave is shown in figure. The velocity of P when its displacement is 5 cm is :



(1)  $\frac{\sqrt{3}\pi}{50} \hat{i}$  m/s (2)  $-\frac{\sqrt{3}\pi}{50} \hat{j}$  m/s

(3)  $\frac{\sqrt{3}\pi}{50} \hat{j}$  m/s (4)  $-\frac{\sqrt{3}\pi}{50} \hat{i}$  m/s

3. The power of sound from the speaker of a radio is 20 milliwatt. By turning the knob of the volume control the power of the sound is increased to 400 milliwatt. The power increase in decibels as compared to the original power is :

(1) 13 db (2) 10 db  
(3) 20 db (4) 800 db

4. Frequency of tuning fork A is 256 Hz. It produces four beats/sec with tuning fork B. When wax is applied at tuning fork B then 6 beats/sec are heard. Frequency of B is :

(1) 252 (2) 260 Hz  
(3) (1) & (2) both (4) 264

5. Frequency of tuning fork A is 256 Hz. It produces four beats/sec with tuning fork B. When wax is applied at tuning fork B then 6 beats/sec are heard. By reducing little amount of wax 4 beats/sec are heard. Frequency of B is :

(1) 250 Hz (2) 260 Hz  
(3) 252 Hz (4) 256 Hz

6. A set of 56 tuning forks are so arranged in series that each fork gives 4 beats per second with the previous one. The freq. of the last fork is 3 times that of first. The freq. of first fork is :

(1) 110 (2) 60 (3) 56 (4) 65

7. Two wires are fixed in a sonometer. Their tensions are in the ratio 8:1. The lengths are in the ratio 36:35. The diameters are in the ratio 4:1. Densities of the materials are in the ratio 1:2. If the higher frequency in the setting is 360 Hz, the beat frequency when the two wires sounded together is:

(1) 8 (2) 5 (3) 10 (4) 6

8. Sound source of frequency 170 Hz is placed near a wall. A man walking from the source towards the wall finds, that there is periodic rise and fall of sound intensity. If the speed of sound in air is 340 m/s, then the distance separating the two adjacent portions of minimum intensity is:

(1)  $(1/2)$  m (2)  $(3/2)$  m (3) 1 m (4) 2 m

9. An open pipe is suddenly closed with the result that the second overtone of the closed pipe is found to be higher in frequency by 100 Hz, than the first overtone of the original pipe. The fundamental frequency of open pipe will be :

(1) 100 Hz (2) 300 Hz (3) 150 Hz (4) 200 Hz

10. For a certain organ pipe three successive resonable frequencies are observed at 425, 595 and 765 Hz respectively. Taking the speed of sound in air to be 340 m/sec (i) whether the pipe is closed end or open end (ii) determine the length of pipe.

(1) closed end, 1 m (2) open end, 1 m  
(3) closed end, 2m (4) open end, 2 m

11. An under water swimmer sends a sound signal to the surface. It produces 5 beats/sec when compared with fundamental tone of a pipe of 20 cm length closed at one end. What is wavelength of sound in water.

(take  $V_{\text{water}} = 1500$  m/sec,  $V_{\text{air}} = 360$  m/sec)

(1) 3.3 m or 3.37 m (2) 4.4 m or 4.47 m  
(3) 2.5 m or 2.7 m (4) 1m or 1.7 m

12. A cylindrical tube ( $L = 120$  cm.) is resonant with a tuning fork of frequency 330 Hz. If it is filling by water then to get resonance minimum length of water column is ( $V_{\text{air}} = 330$  m/s)

(1) 45 cm. (2) 60 cm. (3) 25 cm. (4) 20 cm.



- 13.** A man standing between two cliffs hears the first echo of a sound after 2 sec and the second echo 3 sec after the initial sound. If the speed of sound be 330 m/s, the distance between the two cliffs should be:  
 (1) 1650 m (2) 990 m  
 (3) 825 m (4) 660 m
- 14.** A man standing between two cliffs claps his hands and starts hearing a series of echoes at intervals of 2 sec. Since the speed of sound in air is 340 m/sec. The distance between the cliffs must be:  
 (1) 340 m (2) 680 m  
 (3) 1020 m (4) 170 m
- 15.** A vibrator makes 150 cm of a string to vibrate in 6 loops in the longitudinal arrangement when it is stretched by 150 N. The entire length of the string is then weighed and is found to weigh 400 mg. Then  
 (1) frequency of the vibrator is 3 kHz  
 (2) frequency of the vibrator is 1.5 kHz  
 (3) distance between two nodes is 25 cm  
 (4) distance between two nodes is 33 cm
- 16.** The equation of a plane progressive wave is  $y = 0.02 \sin 8\pi \left[ t - \frac{x}{20} \right]$ . When it is reflected at a rarer medium (medium with higher velocity) at  $x = 0$ , its amplitude becomes 75% of its previous value. The equation of the reflected wave is  
 (1)  $y = 0.02 \sin 8\pi \left[ t - \frac{x}{20} \right]$   
 (2)  $y = 0.02 \sin 8\pi \left[ t + \frac{x}{20} \right]$   
 (3)  $y = +0.015 \sin 8\pi \left[ t + \frac{x}{20} \right]$   
 (4)  $y = -0.015 \sin 8\pi \left[ t + \frac{x}{20} \right]$
- 17.** A sonometer wire resonates with a given tuning fork forming standing waves with five antinodes between the two bridges when a mass of 9kg is suspended from the wire. When this mass is replaced by mass M, the wire resonates with the same tuning fork forming three antinodes for the same positions of the bridges. Then find the value of square root of M.  
 (1) 5 (2) 10 (3) 25 (4) None
- 18.** A wave  $y = 10 \sin (ax + bt)$  is reflected from a dense medium at an origin. If 81% of energy is reflected then the equation of reflected wave is:  
 (1)  $y = -8.1 \sin (ax - bt)$   
 (2)  $y = 8.1 \sin (ax + bt)$   
 (3)  $y = -9 \sin (bt - ax)$   
 (4)  $y = 10 \sin (ax - bt)$
- 19.** An observer moves towards a stationary source of sound with a velocity one tenth of the velocity of sound. The apparent increase in frequency is -  
 (1) zero (2) 5% (3) 10% (4) 0.1%
- 20.** A person observes a change of 2.5% in frequency of sound of horn of a car. If the car is approaching toward the person & sound velocity is 320 m/sec., then velocity of car in m/sec will be approximately.  
 (1) 8 (2) 800 (3) 7 (4) 6
- 21.** A railway engine moving with a speed of 60 m/sec passes in front of a stationary listener. The real frequency of whistle is 400 Hz. Calculate the apparent frequency heard by listener (a) when the engine is approaching the listener. (b) when the engine moving away from the listener ( $V = 340$  m/sec)  
 (1) 484 Hz, 340 Hz (2) 220 Hz, 180 Hz  
 (3) 320 Hz, 155 Hz (4) 400 Hz, 330 Hz
- 22.** A sound source is moving with speed 5 m/s towards a wall. If the velocity of sound is 330 m/s the stationary observer would hear beats is equal to (frequency of source = 240 Hz) -  
 (1) 0 (2) 0 or 8 (3) 8 (4) 0 or 4
- 23.** A person observes two trains one of them is coming with speed of 4m/sec and another is going with same speed. If two trains blowing a whistle with frequency 240 Hz. The beat frequency heard by stationary person will be (speed of sound in air = 320 m/sec.)  
 (1) zero (2) 3 (3) 6 (4) 12
- 24.** A car moving at a speed of 28 m/s blows a horn of frequency 500 Hz and overtakes a car moving in the same direction with a speed of 13 m/s. The apparent frequency heard by the observer of another car will be (after overtaking) :  
 (sound speed = 342 m/sec.)  
 (1) 480 Hz (2) 500 Hz  
 (3) 520 Hz (4) 580 Hz

25. Two source of sound  $s_1$  and  $s_2$  emitting sound of frequency 324 Hz and 320 Hz are situated at certain distance apart. An observer moves along the line joining the two sources. What should be the velocity of the observer if no beats are heard: (Velocity of sound is 344 m/s)  
 (1) 20 m/s (2) 10 m/s  
 (3) 5 m/s (4) 2.1 m/s
26. An astronaut approaches moon and sends a signal of frequency 5000 M Hz. The frequency of the reflected signal increases by 86 K Hz. The speed of the astronaut in Km/s will be  
 (1) 1.29 (2) 2.58 (3) 5.16 (4) 10.32
27. Length of a sonometer wire is either 95 cm or 100 cm, in both the cases a tuning fork produces 4 beats. Then the frequency of tuning fork is-  
 (1) 152 (2) 156 (3) 160 (4) 164
28. Two tuning forks having frequency 256 Hz (A) and 262 Hz (B). Tuning fork A produces some beats per second with unknown tuning fork, same unknown tuning fork produce double beats per second from B tuning fork then the frequency of unknown tuning fork is  
 (1) 262 (2) 260 (3) 250 (4) 300
29. A tuning fork gives 4 beats with 50 cm length of a sonometer wire. If the length of the wire is shortened by 1 cm then no. of beats still the same. The frequency of the fork is -  
 (1) 396 (2) 400 (3) 404 (4) 384
30. A body is walking away from a wall towards an observer at a speed of 1 m/s and blows a whistle whose frequency is 680 Hz. The number of beats heard by the observer per second is :-  
 (velocity of sound in air = 340 m/s)  
 (1) 4 (2) 8 (3) 2 (4) zero
31. In a resonance tube, the first resonance with a tuning fork occurs at 16 cm and second at 49 cm. If the velocity of sound is 330 m/s, the frequency of tuning fork is :-  
 (1) 500 (2) 300 (3) 330 (4) 165
32. A whistle revolves in a circle with angular speed  $\omega = 20$  rad/sec using a string of length 50 cm. If the frequency of sound from the whistle is 385 Hz, then what is the minimum frequency heard by an observer which is far away from the centre: ( $V_{\text{sound}} = 340$  m/s)  
 (1) 385 Hz (2) 374 Hz  
 (3) 394 Hz (4) 333 Hz
33. An earthquake generates both transverse (S) and longitudinal (P) sound waves in the earth. The speed of S waves is about 4.5 km/s and that of P waves is about 8.0 km/s. A seismograph records P and S waves from an earthquake. The first P wave arrives 4.0 min before the first S wave. The epicenter of the earthquake is located at a distance of about  
 (1) 25 km (2) 250 km  
 (3) 2500 km (4) 5000 km
34. A car is moving towards a high cliff. The car driver sounds a horn of frequency 'f'. The reflected sound heard by the driver has a frequency 2f. If 'v' be the velocity of sound then the velocity of the car, in the same velocity units, will be :  
 (1)  $\frac{v}{3}$  (2)  $\frac{v}{4}$   
 (3)  $\frac{v}{2}$  (4)  $\frac{v}{\sqrt{2}}$

## EXERCISE-III (Analytical Questions)

## ANSWER KEY

Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans.	4	3	1	3	2	1	3	3	4	1	1	1	3	3	2,3
Que.	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Ans.	3	1	3	3	1	1	2	3	1	4	2	2	3	1	1
Que.	31	32	33	34											
Ans.	1	2	3	1											

EXERCISE-IV (Assertion & Reason)

Target AIIMS

Directions for Assertion & Reason questions

These questions consist of two statements each, printed as Assertion and Reason. While answering these Questions you are required to choose any one of the following four responses.

- (A) If both Assertion & Reason are True & the Reason is a correct explanation of the Assertion.  
 (B) If both Assertion & Reason are True but Reason is not a correct explanation of the Assertion.  
 (C) If Assertion is True but the Reason is False.  
 (D) If both Assertion & Reason are false.

1. **Assertion** : In standing wave pattern particle of medium between two consecutive nodes vibrates in same phase but with different amplitude.

**Reason** : In stationary wave, the amplitude of vibration does not depends on the position of the particle.

- (1) A (2) B (3) C (4) D

2. **Assertion** : The velocity of sound in air decreases if the pressure of air decreases at constant temperature.

**Reason** : According to Laplace's formula as modified by Newton, velocity of sound in air is given

$$\text{by } V = \sqrt{\frac{\gamma P}{\rho}}.$$

- (1) A (2) B (3) C (4) D

3. **Assertion** : The wave function of a pulse is given

$$\text{by } y = \frac{3}{(2x + 3t)^2 + 4}, \text{ it propagates in (-ve)}$$

x-direction.

**Reason** : The given wave function is of the form  $y = f(kx + \omega t)$ , which represent a wave travelling in negative X-direction.

- (1) A (2) B (3) C (4) D

4. **Assertion** : Longitudinal waves are called pressure waves.

**Reason** : Propagation of longitudinal waves through a medium involves changes in pressure (density of medium particles), when compressions and rarefactions are formed.

- (1) A (2) B (3) C (4) D

5. **Assertion** : Mechanical transverse waves cannot be generated in gaseous medium.

**Reason** : Mechanical transverse waves can be produced only in such medium which have shearing property.

- (1) A (2) B (3) C (4) D

6. **Assertion** : If three sources of sound of equal intensities with frequency  $n$ ,  $n+1$  and  $n+2$  Hz are sounded simultaneously, the beat frequency heard is 2.

**Reason** : In beats at a given position, intensity varies periodically with time with periodicity  $T = 1/(n_1 - n_2)$  while in interference at a given time, intensity varies periodically with position with periodicity  $\lambda$ .

- (1) A (2) B (3) C (4) D

7. **Assertion** : In transverse wave particle velocity is perpendicular to the direction of wave velocity.

**Reason** : In wave motion energy is always transferred in the direction of wave propagation.

- (1) A (2) B (3) C (4) D

8. **Assertion** : In longitudinal wave propagation the distance between two consecutive compression is equal to wavelength of wave.

**Reason** : Standing wave does not get transferred.

- (1) A (2) B (3) C (4) D

9. **Assertion** : Sound wave travels faster in moist air.

**Reason** : The density of moist air is less than density of dry air.

- (1) A (2) B (3) C (4) D

10. **Assertion** : Standing wave does not transfer energy in the medium.

**Reason** : Every particle vibrates with its own energy and it does not share its energy with any other particle.

- (1) A (2) B (3) C (4) D

11. **Assertion** : When two vibrating tuning forks having frequencies 240 Hz and 300 Hz are held near each other, beats cannot be heard by us

**Reason** : This is because beats cannot be distinctly heard due to the property of persistence of hearing.

- (1) A (2) B (3) C (4) D

12. **Assertion** : Harmonics are the notes (a single sound of a certain pitch & wavelength) of frequencies which are integral multiple of the fundamental frequency.

**Reason** : Tones of frequencies higher than fundamental note are called overtones.

- (1) A (2) B (3) C (4) D

- 13. Assertion :** Due to end correction fundamental frequency of any pipe becomes less than frequency without end correction.  
**Reason :** Due to end correction effective length of pipe increases.  
 (1) A (2) B (3) C (4) D
- 14. Assertion :** In R.T.  $\ell_2 > 3\ell_1$ , ( $\ell_1, \ell_2$  first and second resonating length).  
**Reason :**  $e = \frac{\ell_2 - 3\ell_1}{2}$  ( $e$  = end correction) and 'e' remain always positive.  
 (1) A (2) B (3) C (4) D
- 15. Assertion :** For stationary wave general equation is  $2A \sin(Bt) \sin(Kx)$ .  
**Reason :** For progressive wave general equation is  $A \sin(Bt \pm Kx)$ .  
 (1) A (2) B (3) C (4) D
- 16. Assertion :** For same length but different gas COP fundamental frequency are different.  
**Reason :** Here frequency is proportional to velocity for same length given.  
 (1) A (2) B (3) C (4) D
- 17. Assertion :** For same length but different gas COP fundamental wavelength remain same.  
**Reason :** Here length is same.  
 (1) A (2) B (3) C (4) D
- 18. Assertion :** Sound waves can not propagate through vacuum but light waves can.  
**Reason :** Sound waves can not be polarised but light waves can be. [AIIMS 1998]  
 (1) A (2) B (3) C (4) D
- 19. Assertion :** Like sound, light can not propagate in vacuum. [AIIMS 2000]  
**Reason :** Sound is a square wave. It propagates in a medium by virtue of damping oscillation.  
 (1) A (2) B (3) C (4) D
- 20. Assertion :** The flash of lightening is seen before the sound of thunder is heard. [AIIMS 2002]  
**Reason :** Speed of sound is greater than speed of light.  
 (1) A (2) B (3) C (4) D
- 21. Assertion :** When a beetle moves along the sand within a few tens of centimeters of a sand scorpion the scorpion immediately turns towards the beetle and dashes towards it.  
**Reason :** When a beetle disturbs the sand, it sends pulses along the sand's surface. One set of pulses is longitudinal while the other set is transverse. [AIIMS 2003]  
 (1) A (2) B (3) C (4) D
- 22. Assertion :** Partially transverse waves are possible on a liquid surface.  
**Reason :** Surface tension provide some rigidity on a liquid surface.  
 (1) A (2) B (3) C (4) D
- 23. Assertion :** Description of sound as pressure wave is preferred over displacement wave.  
**Reason :** Sound sensors (ear or mike) detect pressure changes.  
 (1) A (2) B (3) C (4) D
- 24. Assertion :** In the case of a stationary wave, a person hear a loud sound at the nodes as compared to the antinodes.  
**Reason :** In a stationary wave all the particles of the medium vibrate in same phase.  
 (1) A (2) B (3) C (4) D
- 25. Assertion :** Waves generated in a metal piece can be transverse or longitudinal.  
**Reason :** Waves generated depend upon the method of creating waves in the metal.  
 (1) A (2) B (3) C (4) D
- 26. Assertion :** A balloon filled with  $\text{CO}_2$  gas acts as a converging lens for a sound wave.  
**Reason :** Sound waves travel faster in air than in  $\text{CO}_2$ .  
 (1) A (2) B (3) C (4) D
- 27. Assertion :** Node of pressure wave is formed at the open end of an organ pipe.  
**Reason :** Due to huge volume of the atmosphere outside the tube, deformation in its volume is negligible.  
 (1) A (2) B (3) C (4) D
- 28. Assertion :** When two vibrating tuning forks have  $f_1 = 300 \text{ Hz}$  and  $f_2 = 350 \text{ Hz}$  and held close to each other; beats cannot be heard.  
**Reason :** The principle of superposition is valid only when  $f_1 - f_2 < 10 \text{ Hz}$   
 (1) A (2) B (3) C (4) D
- 29. Assertion :** The fundamental frequency of an organ pipe increases as the temperature increases.  
**Reason :** As the temperature increases, the velocity of sound increases more rapidly than length of the pipe.  
 (1) A (2) B (3) C (4) D
- 30. Assertion :** Explosions on other planets are not heard on earth.  
**Reason :** To hear distinct beats, difference in frequencies of two sources should be less than 10.  
 (1) A (2) B (3) C (4) D

**31. Assertion :** Vacuum is densest for sound and rarest for light.

**Reason :** A medium is said to be denser, when velocity of waves through this medium is smaller.

- (1) A (2) B (3) C (4) D

**32. Assertion :-** Transverse waves can travel in all medium.

**Reason :-** All the gases have some bulk modulus.

- (1) A (2) B (3) C (4) D

**33. Assertion :-** When a wave is generated in an ideal string, in a non dispersive medium, energy does not change significantly.

**Reason :-** Velocity of the wave generated on the string depends upon the tension applied.

- (1) A (2) B (3) C (4) D

**34. Assertion :-** When a stone is dropped in water the amplitude of progressive wave decreases with distance.

**Reason :-** Amplitude of spherical wavefront is inversely proportional to radius.

- (1) A (2) B (3) C (4) D

**35. Assertion :-** Water waves in a lake can not be polarised. [AIIMS 2018]

**Reason :-** These waves are longitudinal in nature.

- (1) A (2) B (3) C (4) D

**36. Assertion :-** In a medium group velocity is greater than phase velocity. [AIIMS 2018]

**Reason :-**  $\frac{dv}{d\lambda}$  is +ve.

- (1) A (2) B (3) C (4) D

**37. Assertion :-** In a string wave, during reflection from fixed end, the reflected wave is inverted.

**Reason :-** The force on string by clamp is in downward direction while string is pulling the clamp in upward direction. [AIIMS 2018]

- (1) A (2) B (3) C (4) D

**38. Assertion :-** If a wave pulse propagating on a string is reflected from free end then it is not inverted.

**Reason :-** Transverse force is absent and medium is discontinuous at free end. [AIIMS 2018]

- (1) A (2) B (3) C (4) D

**39. Assertion :-** Sound wave propagation in form of compressions and rarefactions is an adiabatic process. [AIIMS 2018]

**Reason :-** Air is a bad conductor of heat.

- (1) A (2) B (3) C (4) D

EXERCISE-IV (Assertion & Reason)

ANSWER KEY

Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans.	3	4	1	1	1	2	2	2	1	1	1	2	1	1	2
Que.	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Ans.	1	1	2	4	3	1	1	1	3	1	1	1	3	1	2
Que.	31	32	33	34	35	36	37	38	39						
Ans.	1	4	2	2	1	4	1	1	2						