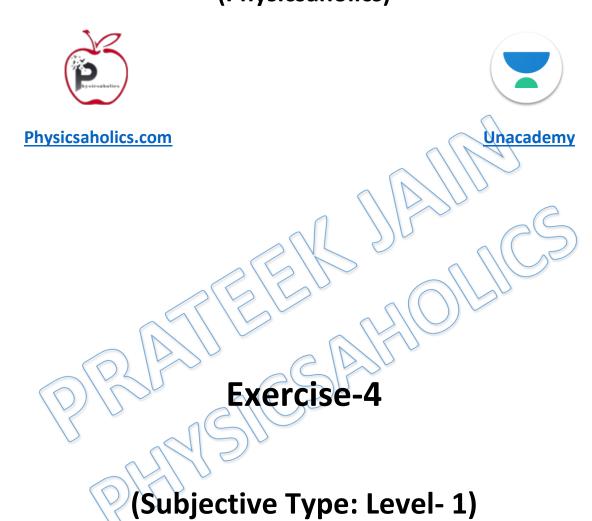




#### **Exercise**

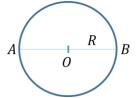
Kinematics- 1D (Physicsaholics)



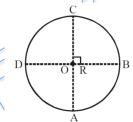




- **Q 1.** The position of a particle along the x-axis is given in centimeters by  $x=9.75+1.50t^3$ , where t is in seconds. Consider the time interval t=2s to t=3s and calculate
  - (a) the average velocity
  - (b) instantaneous velocity at t = 2s;
  - (c) the instantaneous velocity when t = 2.5s;
  - (d) the instantaneous velocity when the particle is mid way between its position at t = 2s and t = 3s.
- **Q 2.** What will be the distance and displacement while moving in a circle from A to B (along circular path) and then B to A (along circular path) as shown in adjoining figure?



Q 3. A particles starts from point A with constant speed v on a circle of radius R. Find magnitude of average velocity during its journey from :-

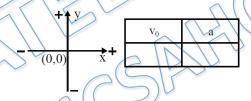


- (a) A to B (anticlockwise)
- (b) A to C (anticlockwise)
- (c) A to D (anticlockwise)
- Q 4. A ball is thrown vertically up with a certain velocity from the top of a tower of height 40 m. At 4.5 m above the top of the tower its speed is exactly half of that it will have at 4.5 m below the top of the tower. Find the maximum height reached by the ball above the ground?
- **Q 5.** A car accelerates with uniform rate from rest on a straight road. The distance travelled in the last second of a three second interval from the start is 15 m then find the distance travelled in first second in m.
- **Q 6.** A body travelling in straight line a travels 2 m in the first two seconds and 2.2m in the next four seconds with constant retardation. What will be its velocity at the end of the seventh second from the start?
- **Q 7.** A particle moving in one-dimension with constant acceleration of 10 m/s² is observed to cover a distance of 100 m during a 4s interval. How far will the particle move in the next 4s?

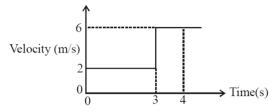




- **Q 8.** The window of the fourth floor of a building is 5 m high. A man looking out of the window sees an object moving up and down the height of window for 2 sec. Find the height that the object reaches from the top end of the window.
- **Q 9.** A car moving on a straight road with a speed 20m/s. At t = 0, the driver of the car applies the brakes after watching an obstacle 150m ahead. After application of brakes the car retards with 2m/s<sup>2</sup>. Find the position of the car from the obstacle at t = 15s.
- **Q 10.** A driver travelling at speed 36 kmh<sup>-1</sup> sees the light turn red at the intersection. If his reaction time is 0.6s, and then the car can deaccelerate at 4ms<sup>-2</sup>. Find the stopping distance of the car.
- **Q 11.** A particle starts from rest at t = 0 and x = 0 to move with a constant acceleration = +2 m/s<sup>2</sup>, for 20 seconds. After that, it moves with -4 m/s<sup>2</sup> for the next 20 seconds. Finally, it moves with positive acceleration for 10 seconds until its velocity becomes zero.
  - (a) What is the value of the acceleration in the last phase of motion?
  - (b) What is the final x-coordinate of the particle?
  - (c) Find the total distance covered by the particle during the whole motion.
- Q 12. A particle is moving along x-axis. Initially it is located 5 m left of origin and it is moving away from the origin and slowing down. In this coordinate system, what are the signs of the initial velocity and acceleration.



- Q 13. Speed of train is increasing linearly with time. The train passes a hut with speed 2 m/s and acquires a speed of 12 m/s after 10 s. What is the speed of the train in m/s, 5 s after passing the hut?
- Q 14. In the following graph variation with time (t), in velocity (v) of a particle moving rectilinearly is shown. What is average velocity in m/s of the particle in time interval from 0 s to 4 s?



**Q 15.** From the top of a tower, a ball is thrown vertically upwards. When the ball reaches h below the tower, its speed is double of what it was at height h above the tower. Find the greatest height attained by the ball from the tower.





- **Q 16.** A body is dropped from a height of 300 m. Exactly at the same instant another body is projected from the ground level vertically up with a velocity of 150 ms<sup>-1</sup>. Find when they will meet.
- **Q 17.** A particle goes from A to B with a speed of 40km/h and B to C with a speed of 60km/h. If AB = 6BC, the average speed in km/h between A and C is.
- **Q 18.** A body moving with uniform acceleration has a velocity of -11 cm/s when its x coordinate is 3.00 cm. If its x coordinate 2 s later is -5 cm, what is the magnitude in cm/s<sup>2</sup> of its acceleration?
- **Q 19.** A balloon rises from rest on the ground with constant acceleration  $\frac{g}{3}$ . A stone is dropped when the balloon has rises to a height 60 metre. The time taken by the stone to reach the ground is.
- Q 20. The momentum of a particle moving in straight line is given by  $p = \ln t + \frac{1}{t}$  (in kg m/s) find the time t > 0 at which the net force acting on particle is 0 and it's momentum at that time. [Hind:  $F = \frac{dp}{dt}$ ]
- **Q 21.** A wheel rotates so that the angle of rotation is proportional to the square of time. The first revolution was performed by the wheel for 8 sec. Find the angular velocity  $\omega$ , 32 sec after the wheel started. [Hint: Consider  $\theta = kt^2$ , find k]
- Q 22. Two particle A and B are moving in same direction on same straight line. A is ahead of B by 20m. A has constant speed 5 m/sec and B has initial speed 30 m/sec and retardation of 10 m/sec<sup>2</sup>. Then if x (in m) is total distance travelled by B as it meets A for second time. Then value of x will be
- Q 23. The charge flowing through a conductor beginning with time t = 0 is given by the formula  $q = 2 t^2 + 3t + 1$  (coulombs). Find the current  $i = \frac{dq}{dt}$  at the end of the 5<sup>th</sup> second.
- **Q 24.** A point moves in a straight line so that its distance from the start in time t is equal to

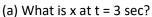
$$s = \frac{1}{4}t^4 - 4t^3 + 16t^2.$$

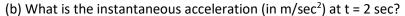
- (a) At what times was the point at its starting position?
- (b) At what times is its velocity equal to zero?
- **Q 25.** A body whose mass is 3 kg performs rectilinear motion according to the formula  $s = 1 + t + t^2$ , where s is measured in centimetres & t in seconds. Determine the kinetic energy  $\frac{1}{2} mv^2$  of the body in 5sec after its start.





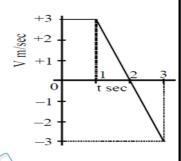
- **Q 26.** A driver applies brakes to the vehicle on seeing traffic signal 400 m ahead. At the time of applying the brakes vehicle was moving with 15 ms<sup>-1</sup> and then starts retarding with 0.3 ms<sup>-2</sup>. The distance of vehicle after 1 min from the traffic light?
- **Q 27.** A particle moves along a straight line, x. At time t = 0, its position is at x = 0. The velocity, V, of the object changes as a function of time t, as indicated in the figure; t is in seconds, V in m/sec and x in meters.





(c) What is the average velocity (in m/sec) between 
$$t = 0$$
 and  $t = 3$  sec?

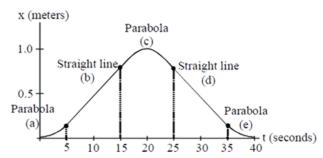
(d) What is the average speed (in 
$$m/sec$$
) between  $t = 1$  and  $t = 3$  sec?



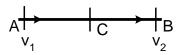
- **Q 28.** A force of 40N is responsible for the motion of a body governed by the equation  $s = 2t + 2t^2$  where s is in meters and t in sec. What is the momentum of the body at t = 2 sec? [Hint: Find acc. then m = F/a & p = mv]
- **Q 29.** A rocket is fired vertically upwards with initial velocity 40 m/s at the ground level. Its engines then fired and it is accelerated at 2 m/s<sup>2</sup> until it reaches an altitude of 1000 m. At that point the engines shut off and the rocket goes into free-fall. If the velocity (in m/s) just before it collides with the ground is 40a. Then fill the value of a. Disregard air resistance (g = 10m/s<sup>2</sup>).
- **Q 30.** The angle rotated by a disc is given by  $\theta = \frac{2}{3}t^3 \frac{25}{2}t^2 + 77t + 5$ , where  $\theta$  is in rad and t in seconds.
  - (a) Find the times at which the angular velocity of the disc is zero.
  - (b) Its angular acceleration at these times.
- **Q 31.** The velocity of the particle is given as  $v = 3t^3 + -\frac{1}{t^2}$ . Calculate the net force acting on the body at time t = 2 sec, if the mass of the body is 5 kg.
- **Q 32.** A stone is dropped from the top of a tall cliff, and 1s later a second stone is thrown vertically downward with a velocity of 20 ms<sup>-1</sup>. How far below the top of the cliff will the second stone overtake the first?
- **Q 33.** The acceleration of a particle starting from rest vary with respect to time is given by a = (2t 6), where t is in seconds. Find the time (in seconds) at which velocity of particle in negative direction is maximum.
- **Q 34.** The figure below is a displacement vs time plot for the motion of an object, answer questions (i) & (ii) with the letter of appropriate section of the graph.







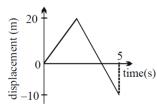
- (i) Which section represents motion in the forward direction with positive acceleration?
- (ii) Which section represents uniform motion backwards (-x direction)?
- **Q 35.** Acceleration of a particle is defined as  $a = (75V^2 30V + 3)(m/s^2)$ . If the constant speed achieved by the particle is given by  $V_C$ , then find the value of  $10V_C$ .
- **Q 36.** A particle moving with uniform acceleration from A to B along a straight line has velocities  $v_1$  and  $v_2$  at A and B respectively. If C is the mid point between A and B then determine the velocity of the particle at C.



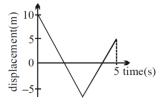
- **Q 37.** The angle  $\theta$  through which a pulley turns with time t is specified by the function  $\theta = t^2 + 3t 5$ . Find the angular velocity  $\omega = \frac{d\theta}{dt}$  at t = 5 sec.
- **Q 38.** Position vector of a particle is given by  $\hat{r} = 3t^3\hat{i} + 4t\hat{j} + t^2\hat{k}$ . Find avg. acceleration of particle from t = 1 to t = 2sec.
- **Q 39.** A particle moves along the x-axis according to  $x = 4t t^2$ . Find the distance travelled from t = 0s to t = 3s.
- **Q 40.** The motion of a particle in a straight line is defined by the relation  $x = t^4 12t^2 40$  where x is in meters and t is in sec. Determine the position x, velocity v and acceleration a of the particle at t = 2sec.
- **Q 41.** The position x of a particle w.r.t. time t along x-axis is given by  $x = 9t^2 t^3$  where x is in metre and t in second. Find
  - (a) Maximum speed along +x direction
  - (b) Position of turning point
  - (c) Displacement in first ten seconds
  - (d) Distance travelled in first ten seconds
- **Q 42.** (a) The diagram shows the displacement-time graph for a particle moving in a straight line. Find the average velocity for the interval from t = 0 to t = 5.



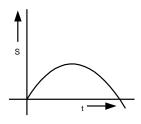




(b) The diagram shows the displacement-time graph for a particle moving in a straight line. Find the average speed for the interval from t=0 to t=5.

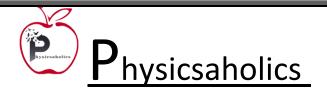


**Q 43.** The graph of displacement v/s time is



Draw its corresponding velocity-time graph.







#### **Answer Key**

Ans. 1 (a) 28.5 cm/s (b) 18.0 cm/s (c) 28.1 cm/s (d) 30.4 cm/s

Ans. 2

Physical quantity and direction	Half cycle A→B or B→A	
Distance	πR	
Displacement	2R	
Direction of	1. $A \rightarrow B$ , when particle	
	moves from A to B.	
displacement	2. B A, when particle	
	moves from B to A.	

Ans. 3 (a) 
$$2\sqrt{2} \frac{v}{\pi}$$
, (b)  $\frac{2v}{\pi}$  (c)  $\frac{2\sqrt{2}v}{3\pi}$ 

Ans. 4 47.5 m

Ans.5 3

Ans. 6 0.1m/s

Ans. 7 260

Ans. 8 Zero

Ans. 9 50 m

Ans. 10 18.5m





Ans. 11 (a) 4 m/s<sup>2</sup>, (b) 200, (c) 1000 m

$\mathbf{v}_0$	a
_	+

Because particle is slowing down so velocity & acceleration are in opposite direction.

- Ans. 13 7
- Ans. 143
- Ans. 15 5h/3
- Ans. 16 2 sec. after body is dropped
- Ans. 17 42km/hr
- Ans. 187
- Ans. 196
- Ans. 20 1 kg m/sec.
- Ans. 21  $2\pi$  rad/sec.
- Ans. 22 50
- Ans. 23 23 amp
- Ans. 24 (a) 0, 8 sec (b) 0, 4, 8 sec
- Ans. 25  $1.815 \times 10^5$  ergs.
- Ans. 26 25 m
- Ans. 27 (a) 3 m; (b)  $-3 \text{ m/s}^2$ ; (c) 1m/s; (d) 3/2 m/s
- Ans. 28 100 kgm/s
- Ans. 29 4
- Ans. 30 (a) 7,  $\frac{11}{2}$  (b) 3, -3





Ans. 31 186.25 N

Ans. 32 
$$\frac{45}{4}$$
 m

Ans. 33 3

Ans. 34 (i) section (a) as slope =  $v = \frac{dx}{dt}$  is positive and increasing.

(ii) section (d) as slope = v = 
$$\frac{dx}{dt}$$
 is negative and constant.

Ans. 35 2

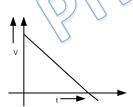
Ans. 36 V=
$$\sqrt{\frac{V_1^2 + V_2^2}{2}}$$

Ans. 37 13 rad/s

Ans. 38 
$$\left(27\hat{i}+2\hat{k}\right)$$
 m/s²

Ans. 39 5m

Ans. 42 Ans. (a) 
$$-2 \text{ ms}^{-1}$$
 (b) 5 m/s



Ans. 43