



ARJUNA NEET BATCH



LAWS OF MOTION

LECTURE - 05

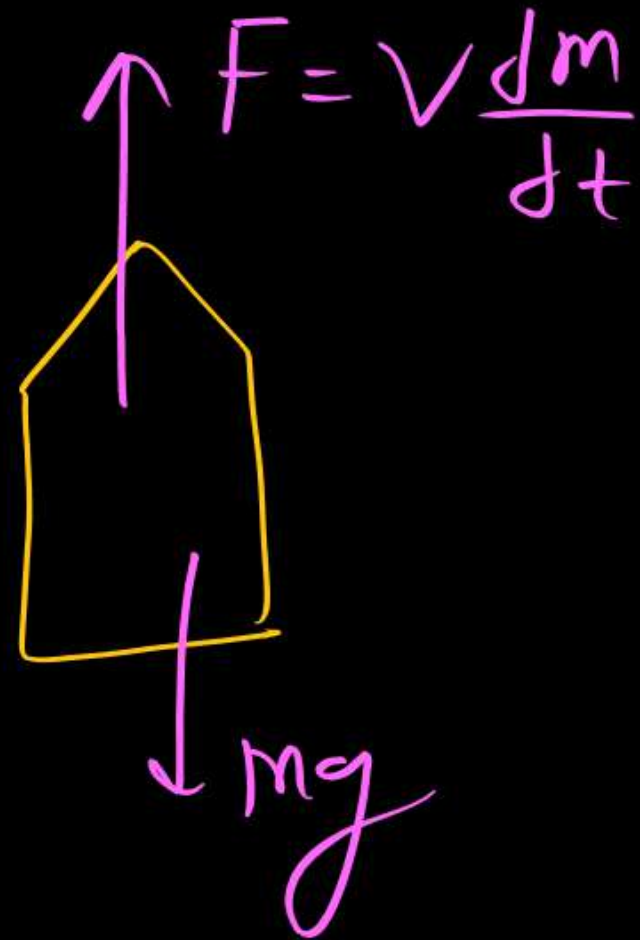
Today's Goal

⊗ question on Rocket Prob^m. ✓

⊗ Connected body motion ✓

⊗ Ph.D in Pulley block system
α

A 800 kg rocket is fired from earth so that exhaust speed is 1200 m/s. Then calculate mass of fuel burning per second, to provide initial thrust to overcome its weight. ($g = 10 \text{ m/s}^2$)



$$\frac{dm}{dt} = ??$$

$$mg = v \frac{dm}{dt}$$

$$800 \times 10 = 1200 \frac{dm}{dt}$$

$$\frac{80}{12} = \left(\frac{dm}{dt} \right)$$



$$\vec{F}_{\text{thrust}} = u \frac{dm}{dt}$$



Rocket (variable mass system)

$g \downarrow$

$$a_0 = \frac{F}{m_{\text{av}_0}} = \left(\frac{u \frac{dm}{dt}}{m_0} \right) - g$$

initial accn at time $(t=0)$

at time 't'

$$a_t = \frac{\left(u \frac{dm}{dt} \right)}{m_0 - \frac{dm}{dt} t} - g$$

A cracker rocket is ejecting gases at a rate of 0.05 kg/s with a velocity 400 m/s . The accelerating force on the rocket is:

- (a) 20 dyns — (b) 20 N
 (c) 200 N (d) Zero

$$\frac{dm}{dt} = 0.05 \text{ kg/s}$$

$$u = 400 \text{ m/s}$$

$$F = u \frac{dm}{dt} =$$



A rocket of mass 5700 kg ejected mass at a constant rate of 15 kg/s with constant speed of 12 km/s. The acceleration of the rocket 1 minute after the blast is ($g = 10 \text{ m/s}^2$)

(a) 34.9 m/s^2

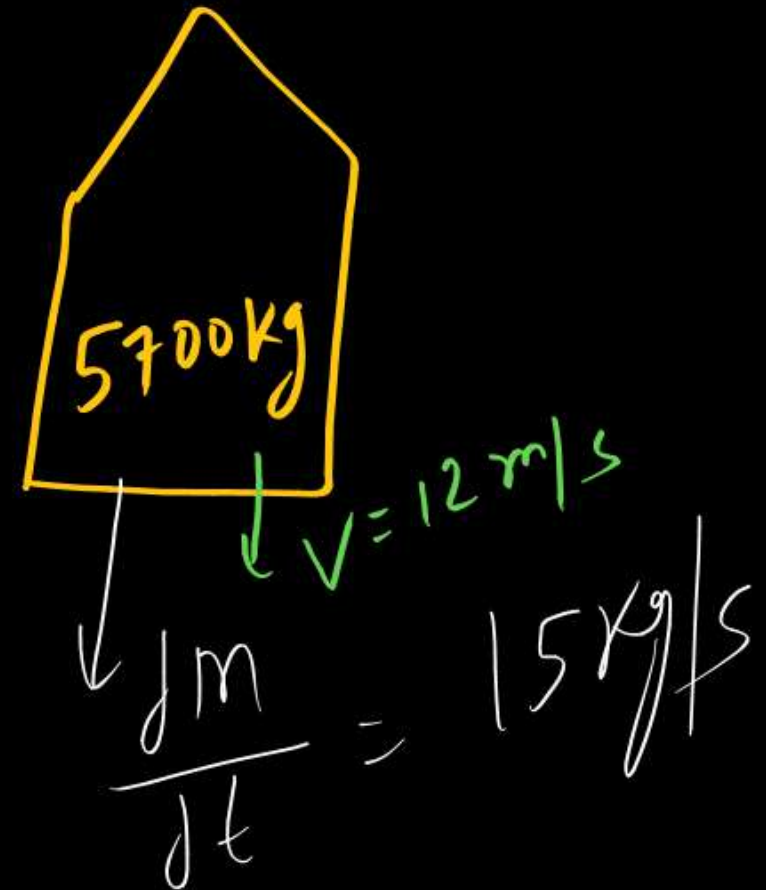
(b) 27.5 m/s^2

(c) 3.50 m/s^2

(d) 13.5 m/s^2

$$a = \frac{u \frac{dm}{dt}}{m_0 - \frac{dm}{dt} \times t} - g$$

$$= \left[\frac{12 \times 10^3 \times 15}{5700 - 15 \times 60} \right] - 10$$



If the force on a rocket, that releases the exhaust gases with a velocity of 300 m/s is 210 N, then the rate of combustion of the fuel is:

(a) 0.07 kg/s

(b) 1.4 kg/s

☒ (c) 0.7 kg/s

(d) 10.7 kg/s

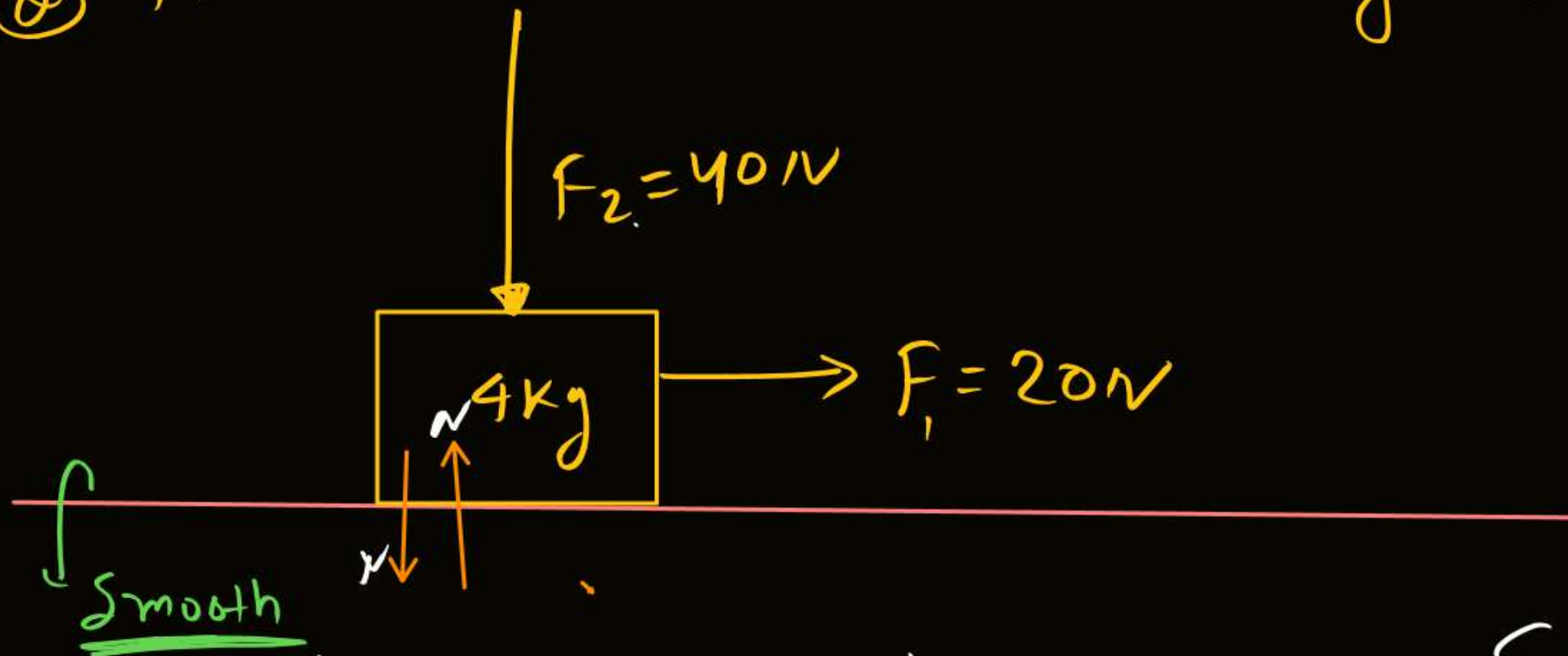
$$F = u \frac{dm}{dt}$$

$$210 = 300 \frac{dm}{dt}$$

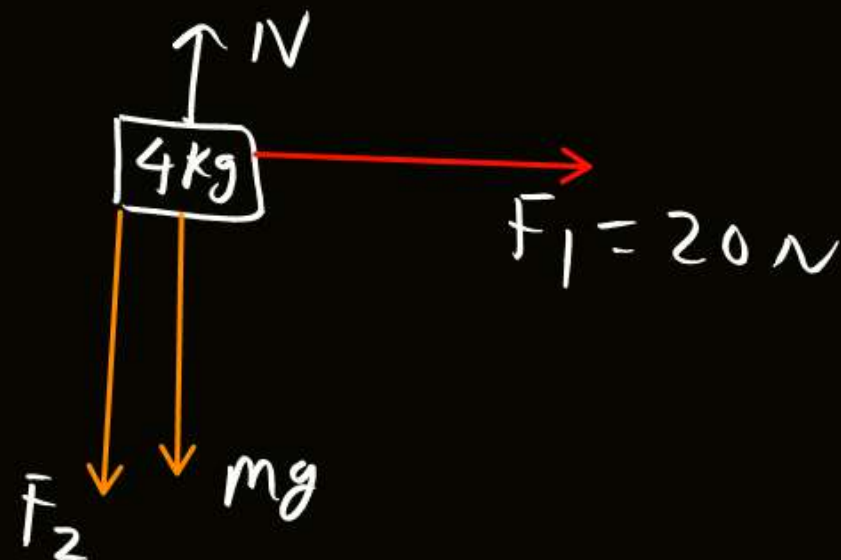


question on Dynamics [Newton 2nd Law]

① find accⁿ of block of mass 4kg ??



F.B.D of block



$$\vec{F} = \frac{d\vec{P}}{dt}$$

$$m = \text{const}^n$$

$$\boxed{\vec{F} = m\vec{a}}$$

$$\sum F_y = 0 \quad \boxed{a_y = 0}$$

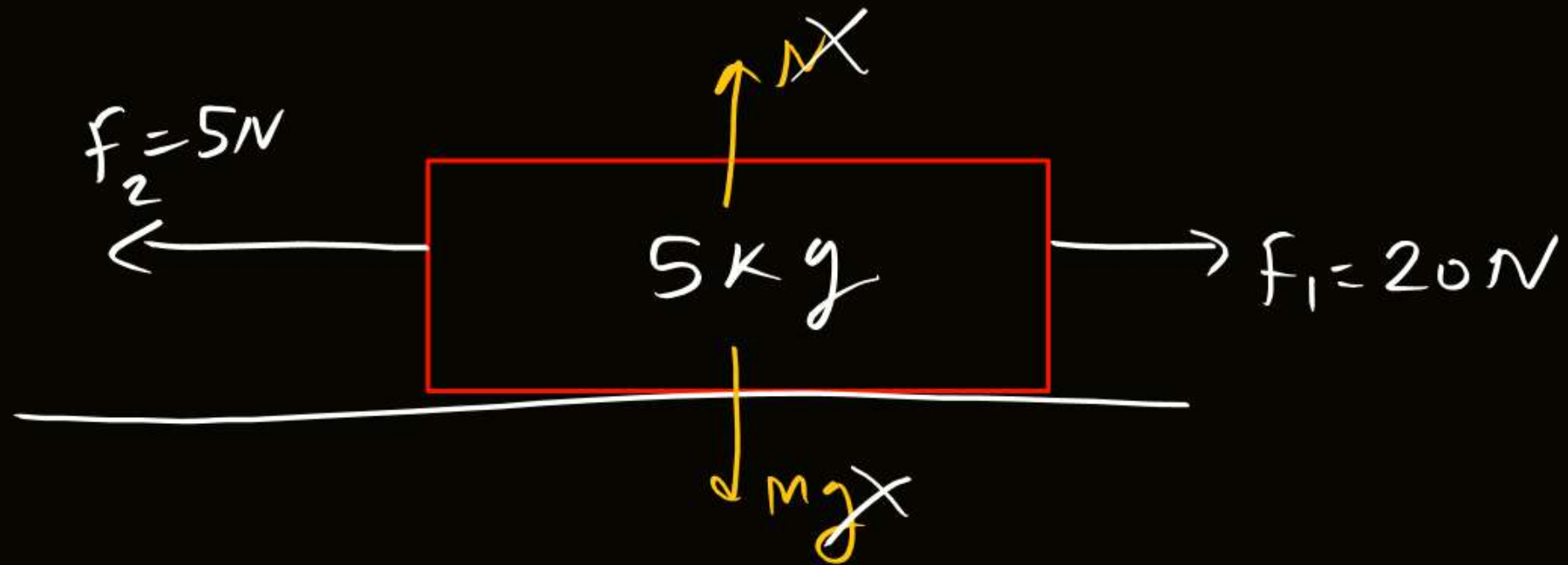
$$N = F_2 + mg = [40 + 40] = 80\text{N}$$

$$\# \sum F_x = ma_x$$

$$20 = 4 \times a_x$$

$$\boxed{a_x = 5\text{m/s}^2}$$

find accⁿ of 5kg??



$$\Sigma F_x = m \Sigma a_x$$

$$15 = 5 a_x$$

$$\boxed{a = 3 \text{ m/s}^2}$$

find accⁿ of 5kg



$$\Sigma F_x = m a_x$$

$$30 = 5 a_x$$

$$\boxed{a_x = 6 \text{ m/s}^2}$$

Figure shows a uniform rod of length 30 cm having a mass 3.0 kg. The rod is pulled by constant forces of 20 N and 32 N as shown. Find the force exerted by 20 cm part of the rod on the 10 cm part (all surfaces are smooth) is:

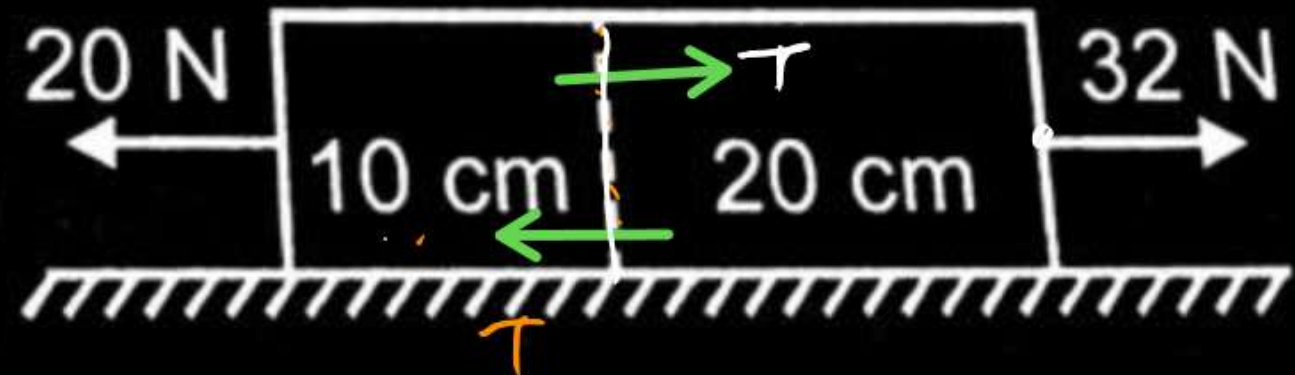
- ~~(a) 36 N~~
- ~~(b) 12 N~~
- ~~(c) 64 N~~
- ~~(d) 24 N~~

F.B.D of (2kg) \rightarrow 32

$$32 - T = ma$$

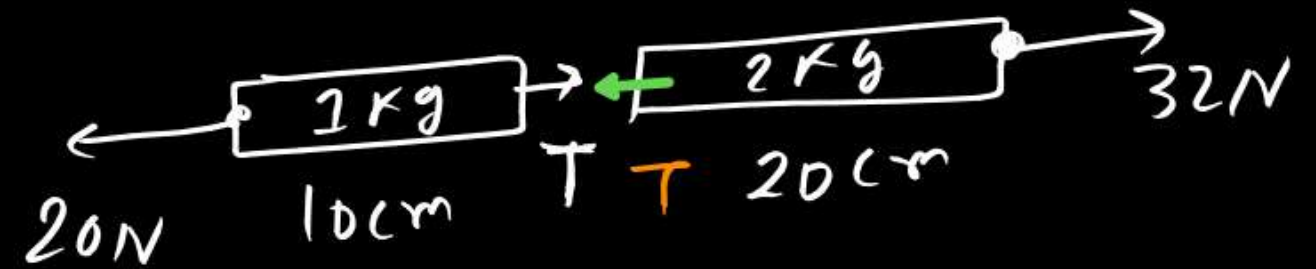
$$32 - T = 2 \times 4$$

$$T = 32 - 8 = 24 \text{ N}$$



$$a = \frac{F_{\text{net pulling force}}}{\text{net mass}} = \frac{12}{3}$$

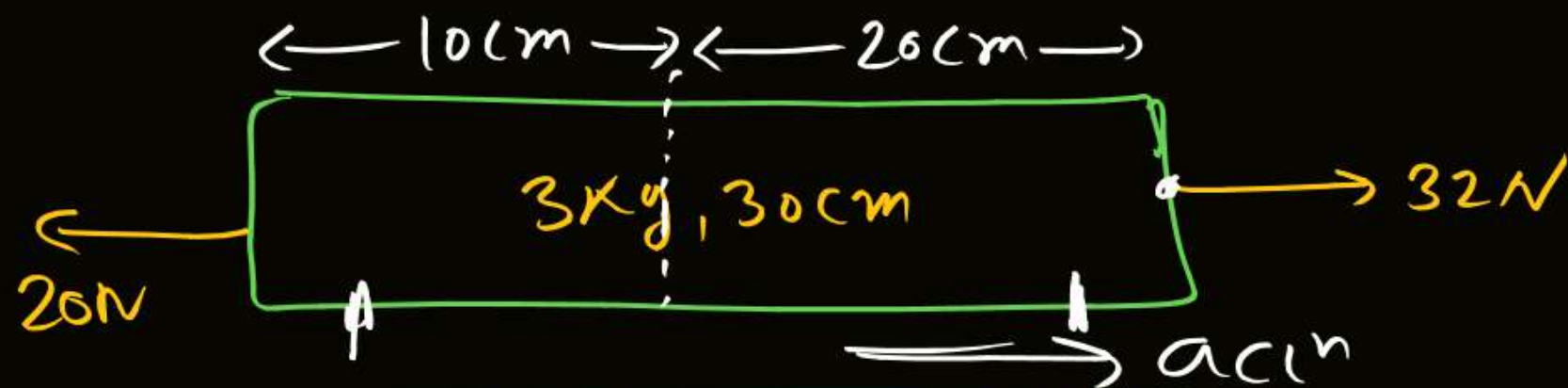
$$a = 4 \text{ m/s}^2$$



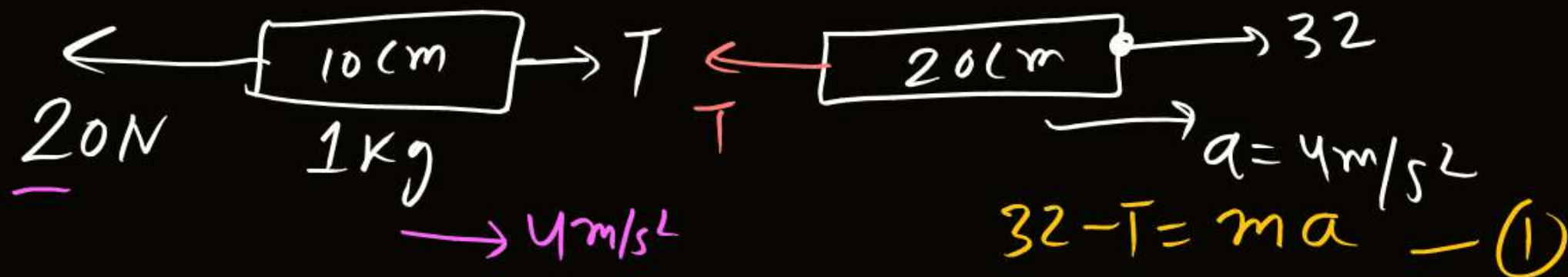
$$T - 20 = ma$$

$$T = 20 + 1 \times 4 = 24 \text{ N}$$

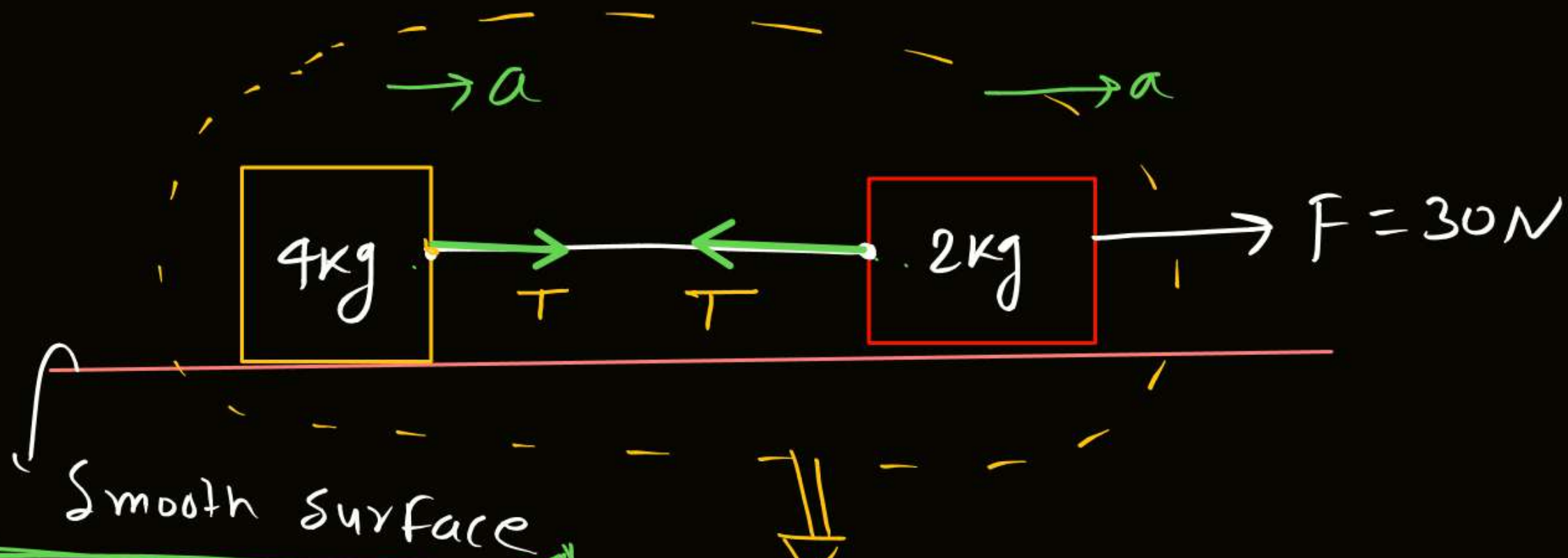




$$\# \quad a = \frac{F_{\text{net}}}{m} = \frac{12}{3} = 4 \text{ m/s}^2$$



① Find accⁿ of 4kg and 2kg • and Tension in string which is b/w 2kg & 4kg.



Free Body Diagrams (F.B.D.) for the blocks:

For 4kg: $T = ma$ — (1)

For 2kg: $30 - T = 2a$ — (2)

Adding (1) and (2):

$$30 = 6a$$

$$a = 30/6 = 5\text{ m/s}^2$$

Combined system F.B.D.:

For 6kg: $F = 30\text{N}$

$$a = \frac{F}{m} = \frac{30}{6} = 5\text{ m/s}^2$$

F.B.D. of 4kg:

For 4kg: T

$$F = ma$$

$$T = 4 \times 5 = 20\text{N}$$

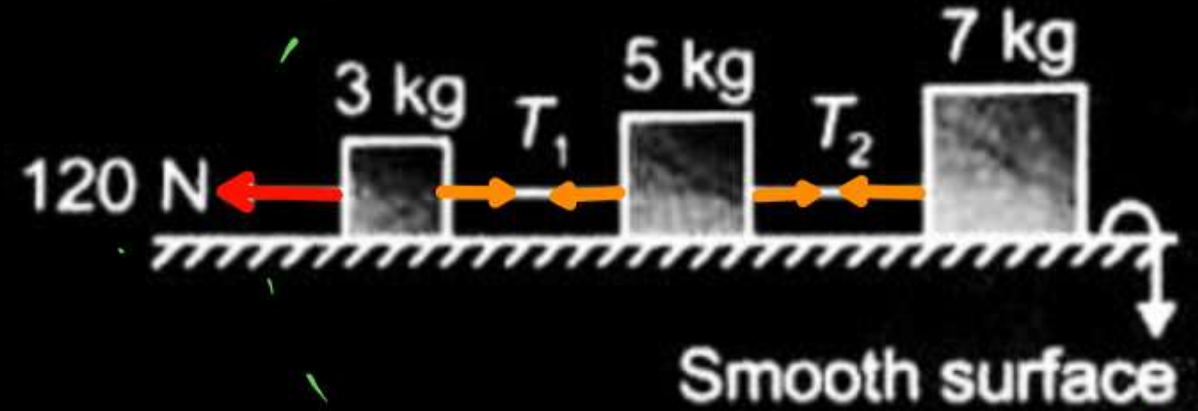
T_1 and T_2 in the given figure are

~~(a) 28 N, 48 N~~

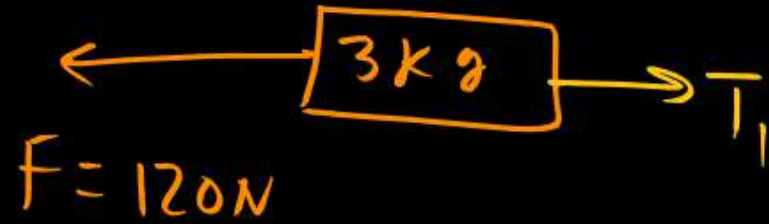
~~(c) 96 N, 56 N~~

~~(b) 48 N, 28 N~~

~~(d) 56 N, 96 N~~



++ F.B.D of 3kg



a

$$120 - T_1 = 3 \times a$$

$$120 - T_1 = 3 \times 8$$

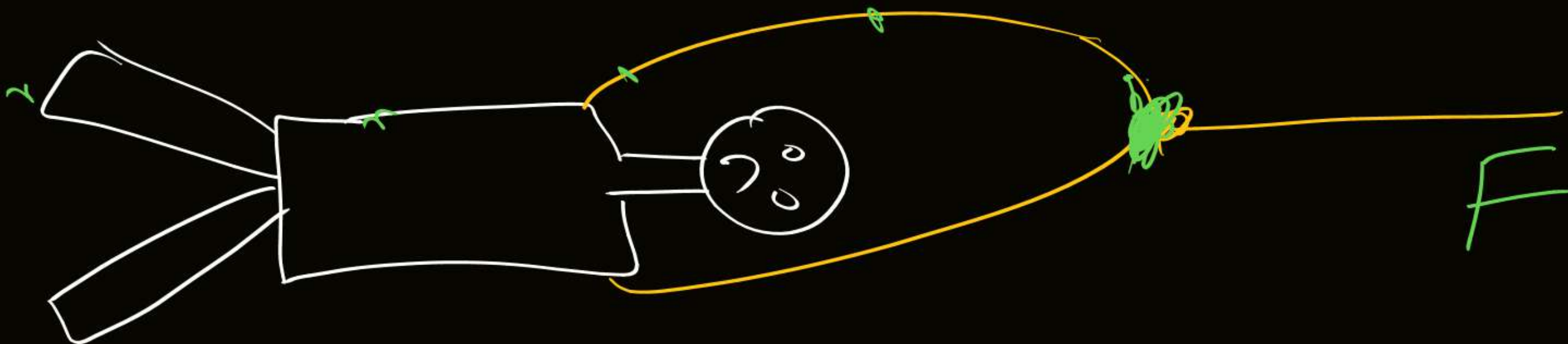
$$T_1 = 120 - 24 = 96N$$

$F = 120N$



$$a = \frac{F}{m} = \frac{120}{15} = 8m/s^2$$





Arrangement of two block system is as shown. The net force acting on 1 kg and 2 kg blocks are (assuming the surface to be frictionless) respectively

~~(a) 4 N, 8 N~~

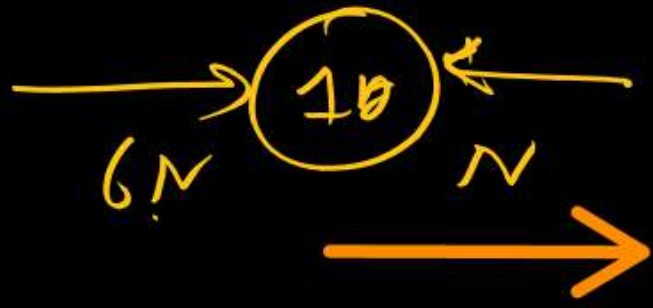
~~(c) 2 N, 4 N~~

~~(b) 1 N, 2 N~~

~~(d) 3 N, 6 N~~

NEET

F.B.D of 1kg

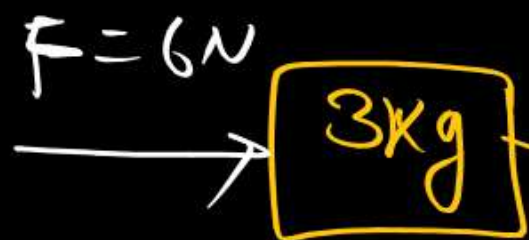
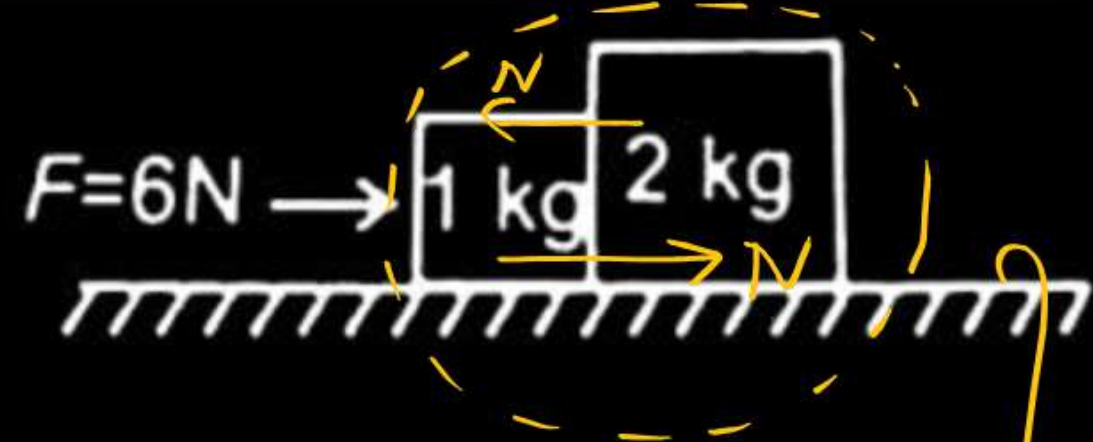


$$6 - N = ma$$

$$6 - N = 1 \times 2$$

$$6 - 2 = N$$

$$N = 4 \text{ N}$$



$$a = \frac{F}{m} = \frac{6}{3} = 2 \text{ m/s}^2$$

u=0
smooth



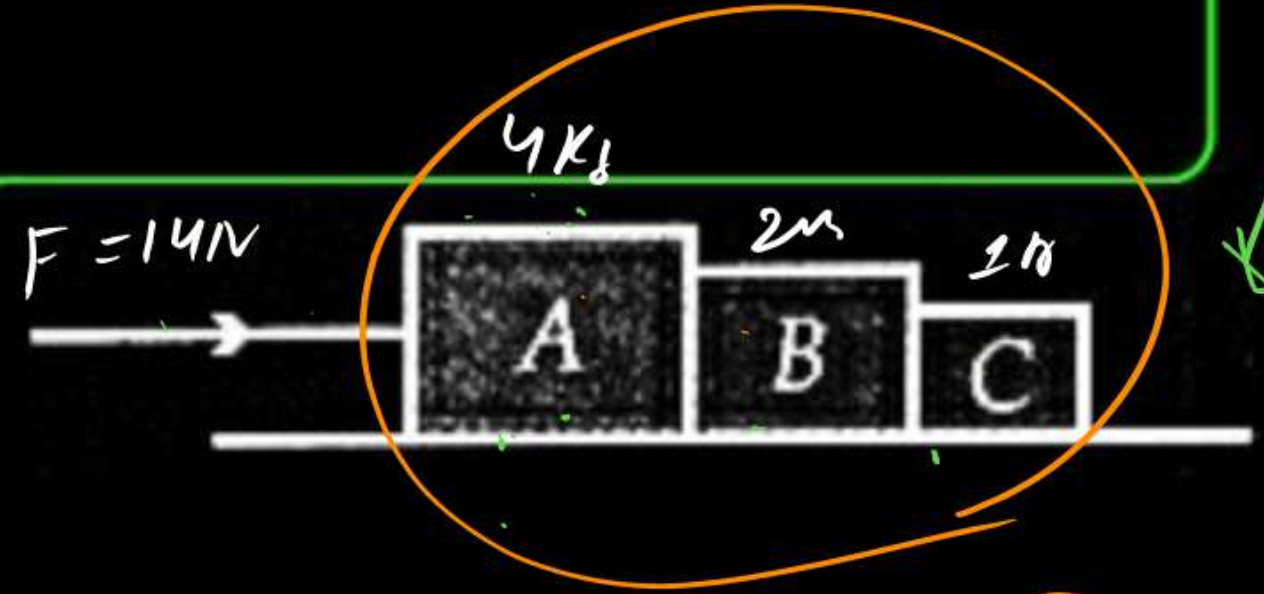
Three blocks A, B and C of masses 4 kg, 2 kg and 1 kg respectively, are in contact on a frictionless surface, as shown. If a force of 14 N is applied on the 4 kg block, then the contact force between A and B is **[AIPMT-2015]**

(a) 18 N

(b) 2 N

~~(c) 6 N~~

(d) 8 N



$$a = \frac{F}{m} = \frac{14}{7} = 2 \text{ m/s}^2$$

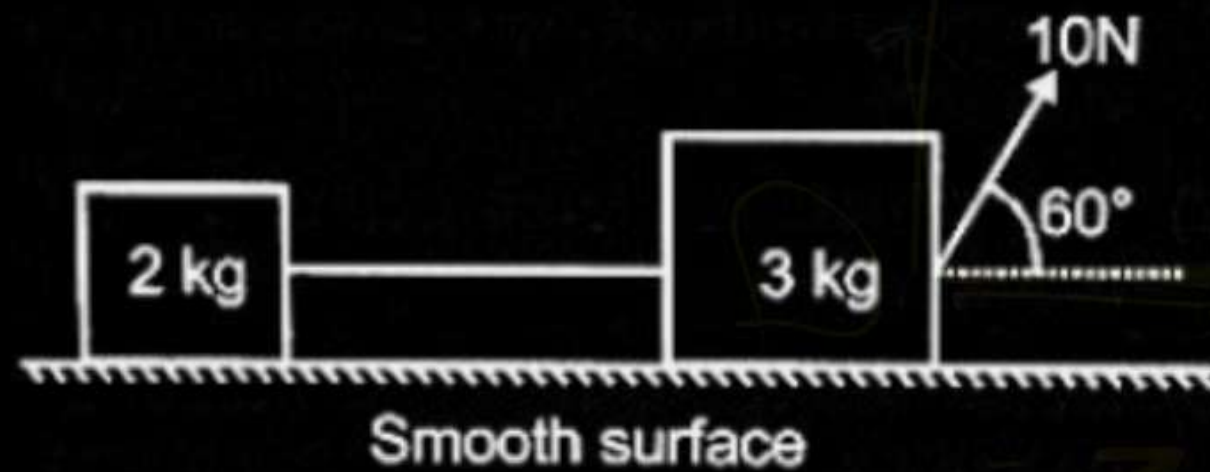
$$14 - 8 = 6 \text{ N}$$

~~mR^*~~



Figure shows two blocks connected by a light inextensible string as shown in figure. A force of 10 N is applied on the bigger block at 60° with horizontal, then the tension in the string connecting the two masses is

- (a) 5 N (b) 2 N
(c) 1 N (d) 3 N



Two blocks are in contact on a frictionless table. One has mass m and the other $2m$. A force F is applied on $2m$ as shown in the figure. Now the same force F is applied from the right on m . In the two cases respectively, the ratio of force of contact between the two blocks will be :

(a) same

~~(b) 1 : 2~~

(c) 2 : 1

(d) 1 : 3

Case-1

$$a = \frac{F}{3m}$$

F.B.D of (m)

$$(m) \rightarrow N_1$$

$$N_1 = \cancel{m} \frac{F}{3\cancel{m}} = \left(\frac{F}{3} \right)$$

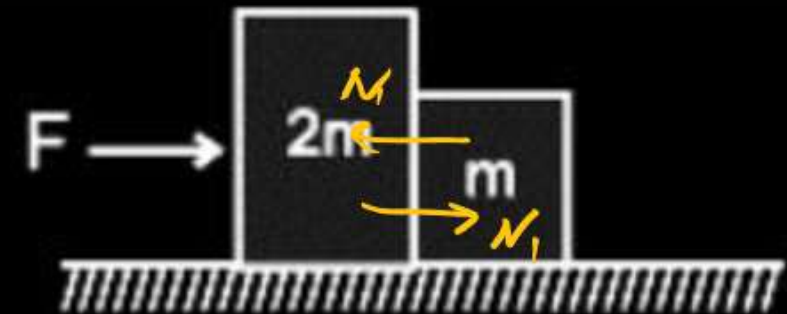
Case-2

$$a = \frac{F}{3m}$$

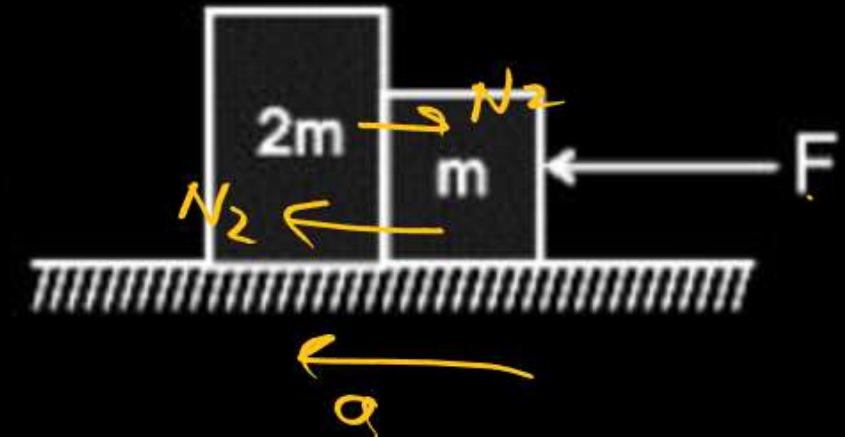
F.B.D of $(2m)$

$$N_2 = 2m \left(\frac{F}{3m} \right) = \frac{2F}{3}$$

Case-1



Case-2



What will be the tension T_1 and T_2 in the given figure?



$$a = 6 \text{ m/s}^2$$

$$T_1 = 36 \text{ N}$$

$$T_2 = 60 \text{ N}$$

Y.W



Find force applied on base of lift by 20 kg block.



F.B.D of 20kg



$$a = 2 \text{ m/s}^2 \quad F = ma$$
$$N - mg = ma$$

$$N = mg + ma$$
$$= 20[10 + 2] = \underline{\underline{240 \text{ N}}}$$



Tension in the rope at the rigid support is ($g = 10 \text{ m/s}^2$)

(a) 760 N

(b) 1360 N

☒ (c) 1580 N

(d) 1620 N

F.B.D of (A)



$$a = 2 \text{ m/s}^2$$

$$T_A - mg = ma \quad \text{--- (1)}$$

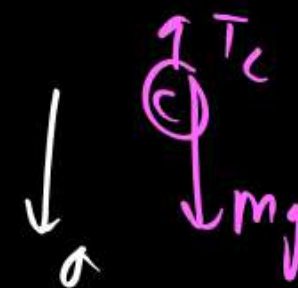
$$T_A = m(g + a) = 60[10 + 2] = 720 \text{ N}$$

F.B.D



$$T_B = mg = 50 \times 10 = 500 \text{ N}$$

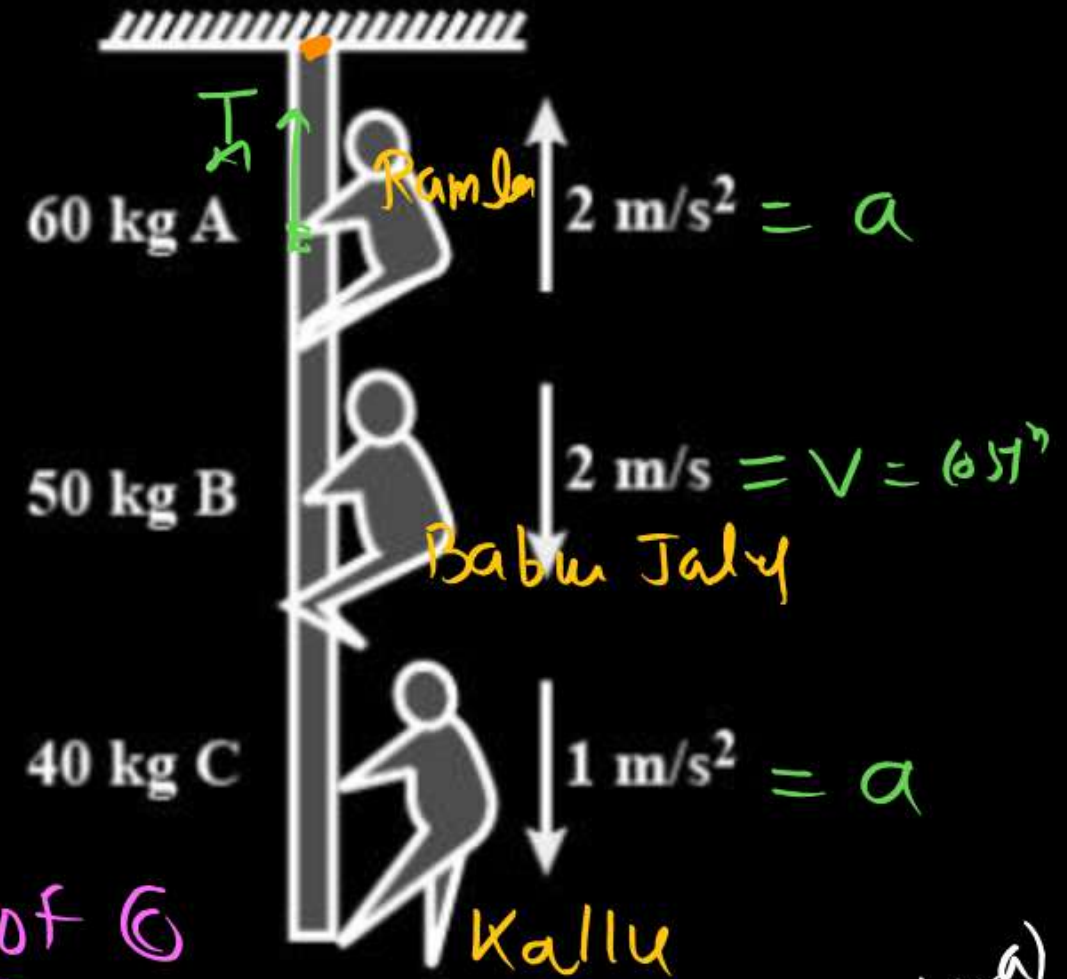
F.B.D of (C)



$$mg - T_C = ma$$

$$T_C = mg - ma = m(g - a)$$

$$= 40 \times 9 = 360 \text{ N}$$



If ($M_2 > M_1$) then find acceleration of M_1 and M_2 and Tension in string.



Schools

for (m_2)

$$m_2 g - T = m_2 a \quad \text{--- (1)}$$

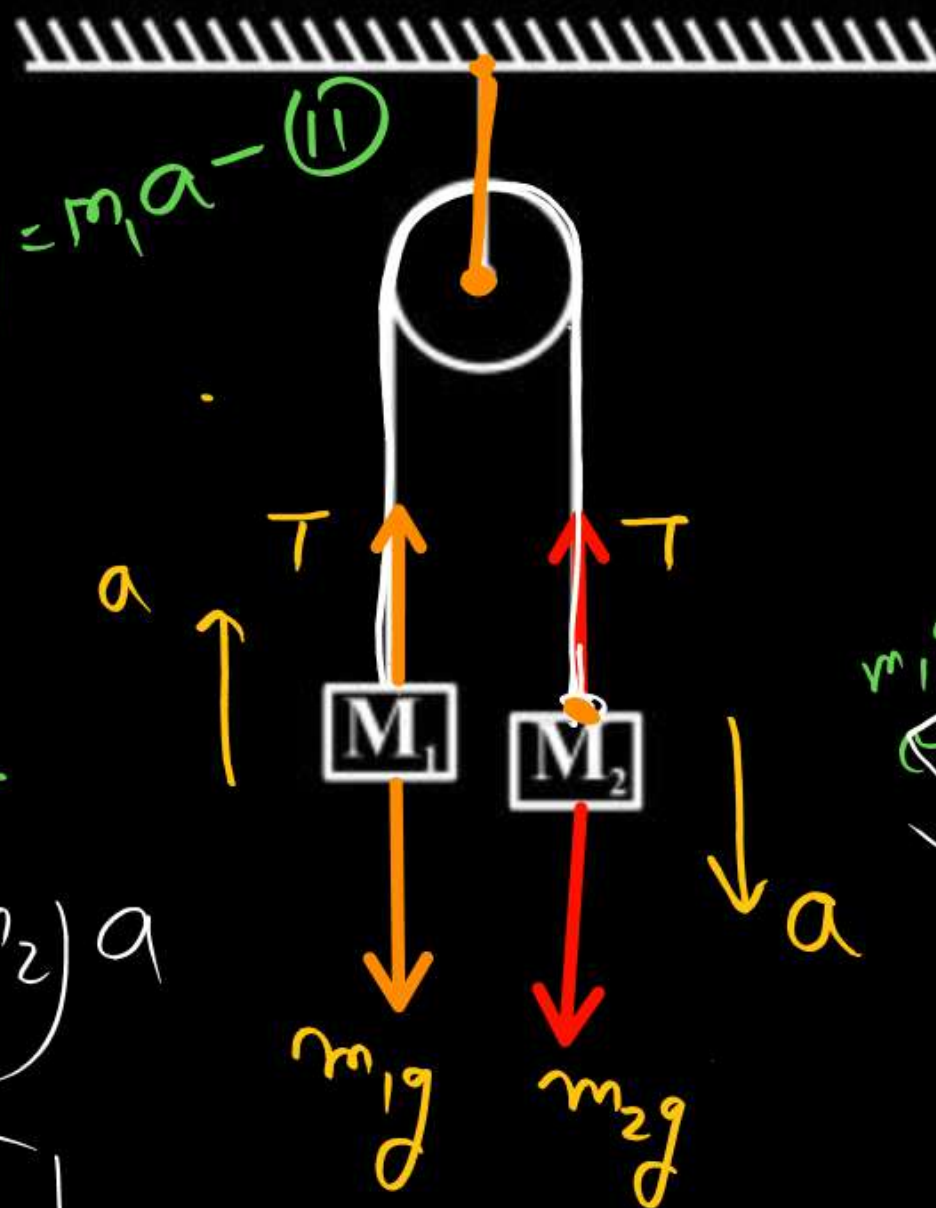
$$T - m_1 g = m_1 a \quad \text{--- (2)}$$

$$m_2 g - m_1 g = (m_1 + m_2) a$$

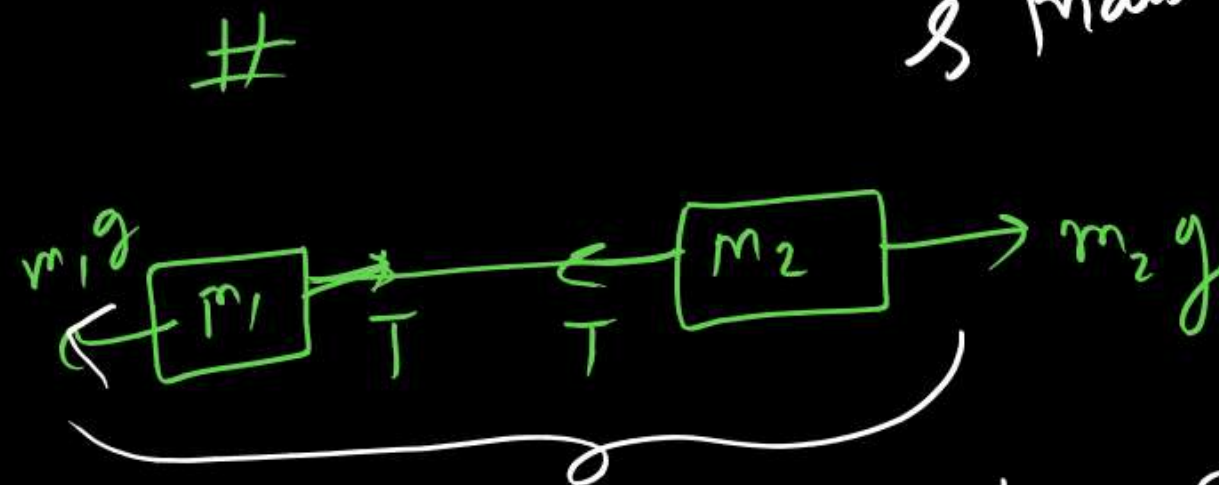
$$a = \left(\frac{m_2 - m_1}{m_1 + m_2} \right) g = g \cos \theta$$

for (m_1)

$$T - m_1 g = m_1 a \quad \text{--- (2)}$$



String & pulley are ideal
frictionless
& massless



$$a = \frac{\text{net unbalance force}}{\text{net mass}}$$

$$a = \frac{m_2 g - m_1 g}{m_1 + m_2}$$



~~fix~~ $a = \left(\frac{m_2 - m_1}{m_2 + m_1} \right) g$

m_R^*
 gf $m_1 = m_2$
 $a = 0$ ✓

~~fix~~ $a = \left(\frac{m_2 + m_1}{m_2 - m_1} \right) g = \frac{1}{0} = \infty$

~~fix~~ $a = \frac{2m_1 m_2}{m_1 + m_2} g$ (dimⁿ wrong)

using eq ①

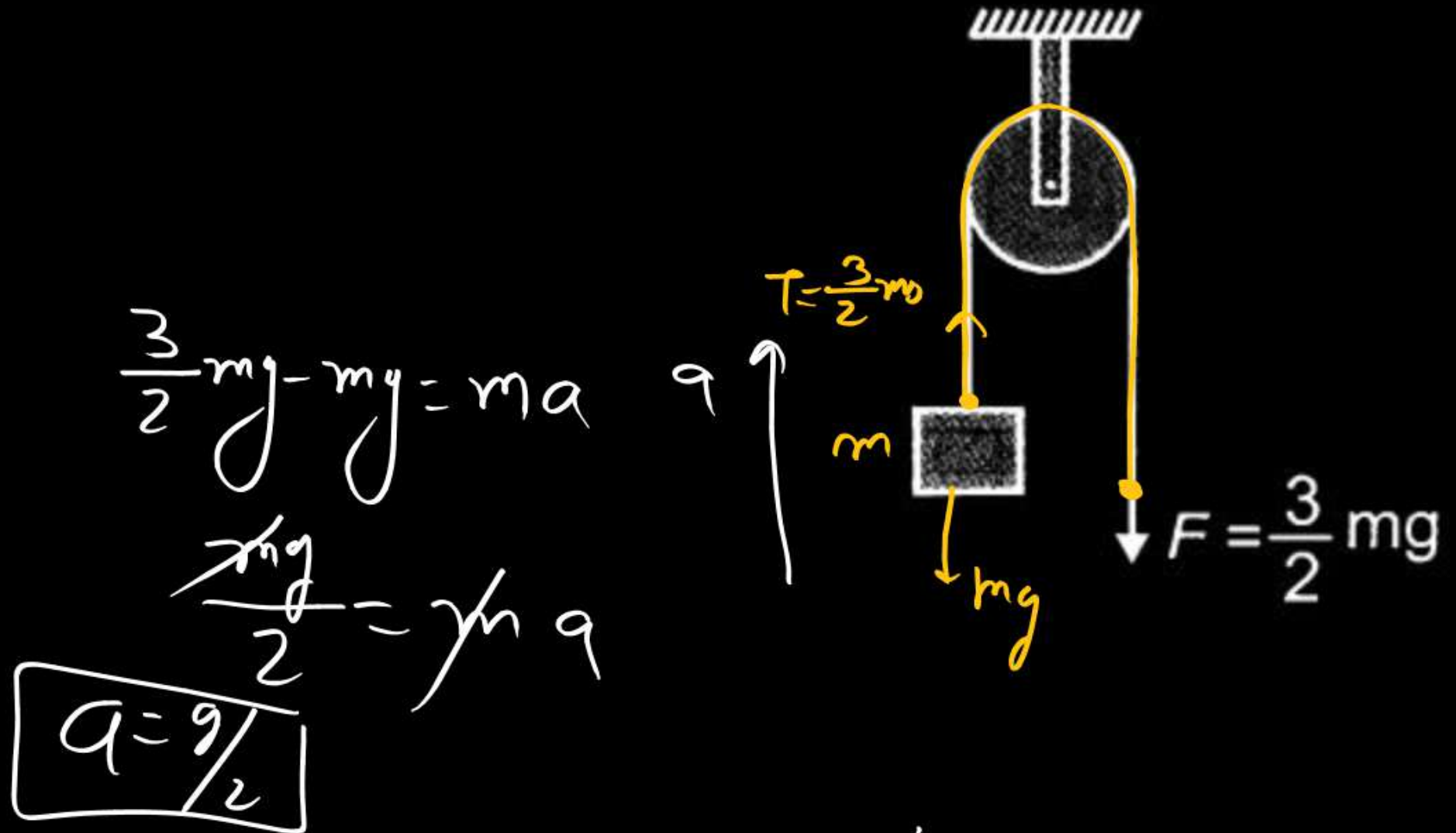
$m_2 g - T = m_1 a$

Put the value of a .

$T = \frac{2m_1 m_2}{m_1 + m_2} g$ #

In the arrangement shown, the mass m will ascend with an acceleration (Pulley and rope are massless)

- (a) Zero (b) $\frac{g}{2}$
(c) g (d) $2g$



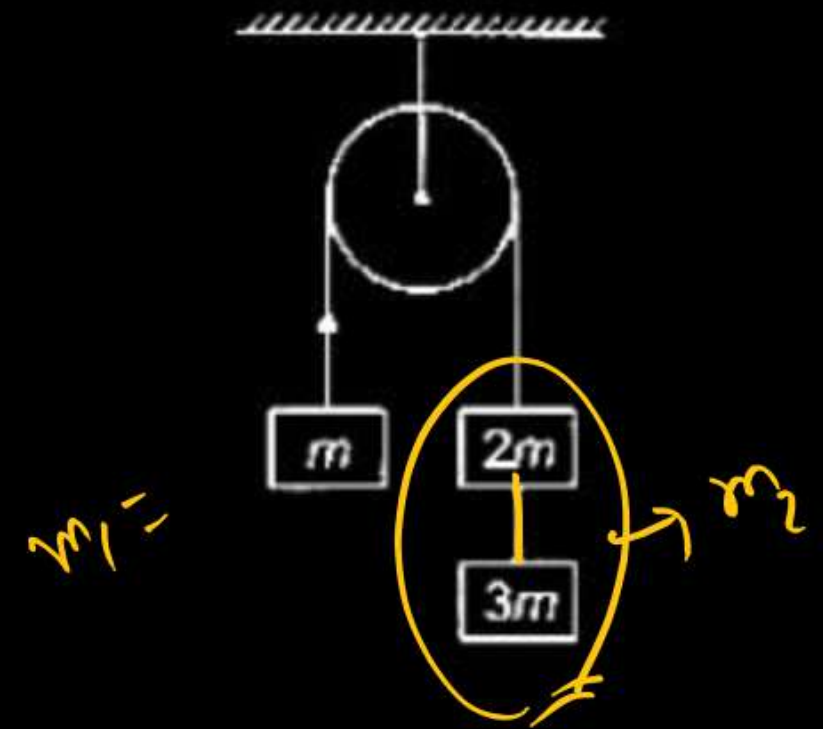
In the figure given below, with what acceleration does the block of mass m will move? (Pulley and strings are massless and frictionless)

(a) $\frac{g}{3}$

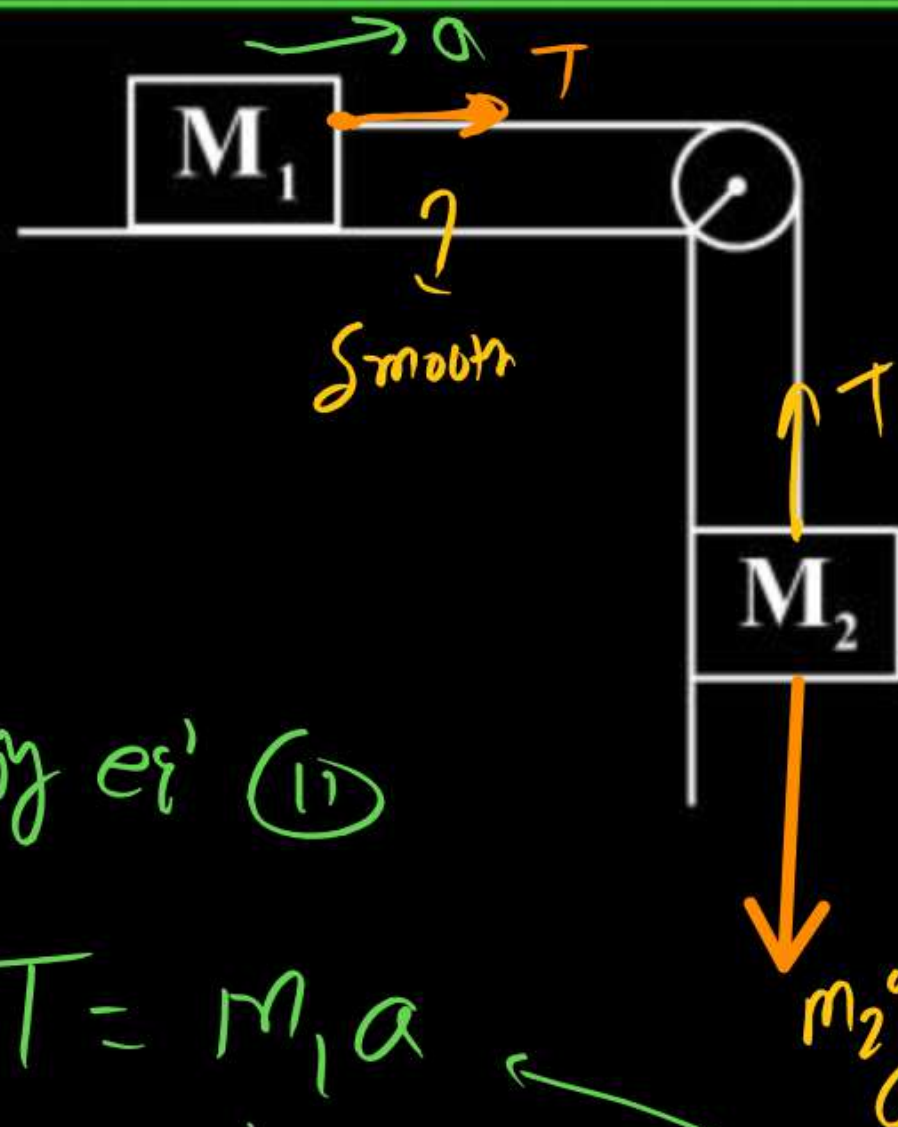
(b) $\frac{2g}{5}$

(c) $\frac{2g}{3}$

(d) $\frac{g}{2}$



Find acceleration of Block M_1 and M_2 and tension in string.



Using eqⁿ (i)

$$T = m_1 a$$

$$T = \frac{m_1 m_2}{m_1 + m_2} g$$

$$m_2 g - T = m_2 a \quad \text{--- (ii)}$$

$$T = m_1 a \quad \text{--- (i)}$$

$$m_2 g = (m_1 + m_2) a$$

$$a = \frac{m_2 g}{m_1 + m_2}$$





THANK YOU 😊

