



ARJUNA NEET BATCH



KINEMATICS

LECTURE 11

MR*

NEET



Today's goal

- Motion under gravity
- Ground to ground
- Height to ground
- मोरसु (MR*)



Today's GOAL

MOTION UNDER GRAVITY



Object is projected with 40 m/s then find average speed and velocity in 6 sec.



$$Total = \frac{2u}{g} = \frac{2 \times 40}{10} = 8 \text{ sec}$$

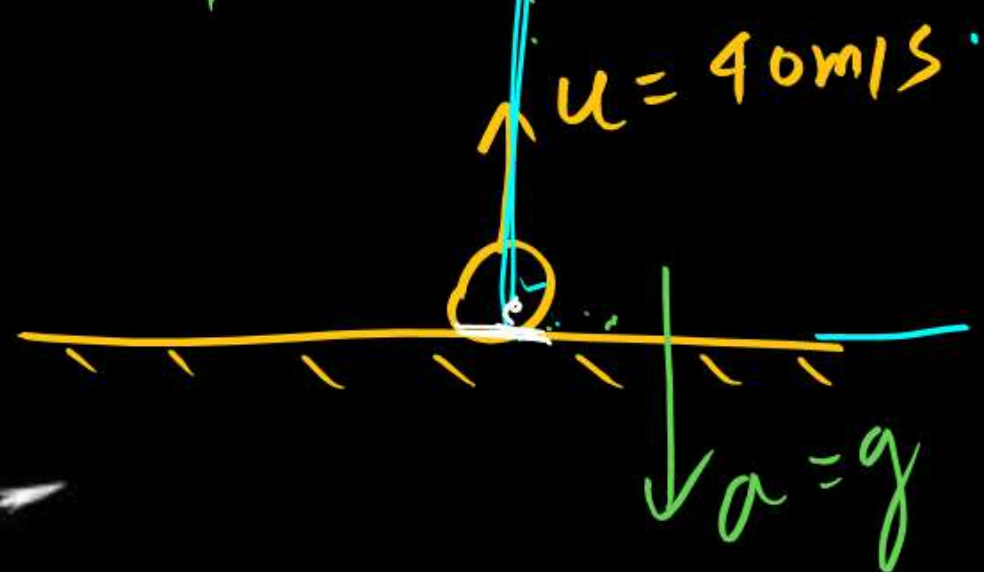
$v = 0$ ($t = 4 \text{ sec}$)

$$T_{up} = \frac{u}{g}$$

$$= \frac{40}{10} = 4 \text{ sec}$$

$$S = ut + \frac{1}{2}at^2$$

$$= \frac{1}{2}10(2)^2 = 20 \text{ m}$$



$$Avg \text{ speed} = \frac{(\text{total dist}^n)_{t=6 \text{ sec}}}{6} = \left(\frac{100}{6} \right)$$

$$Avg \text{ velocity} = \frac{60}{6} = 10 \text{ m/s}$$



$$S_{n^{th}} = u + \frac{a}{2}(2n-1)$$

$$\underline{S_{nsec}} = u(n) + \frac{1}{2}a(n)^2$$

$$t = nsec$$

#

in 4-sec

(dispⁿ in 8 sec)
(0 to 8 sec)
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12th

2nd

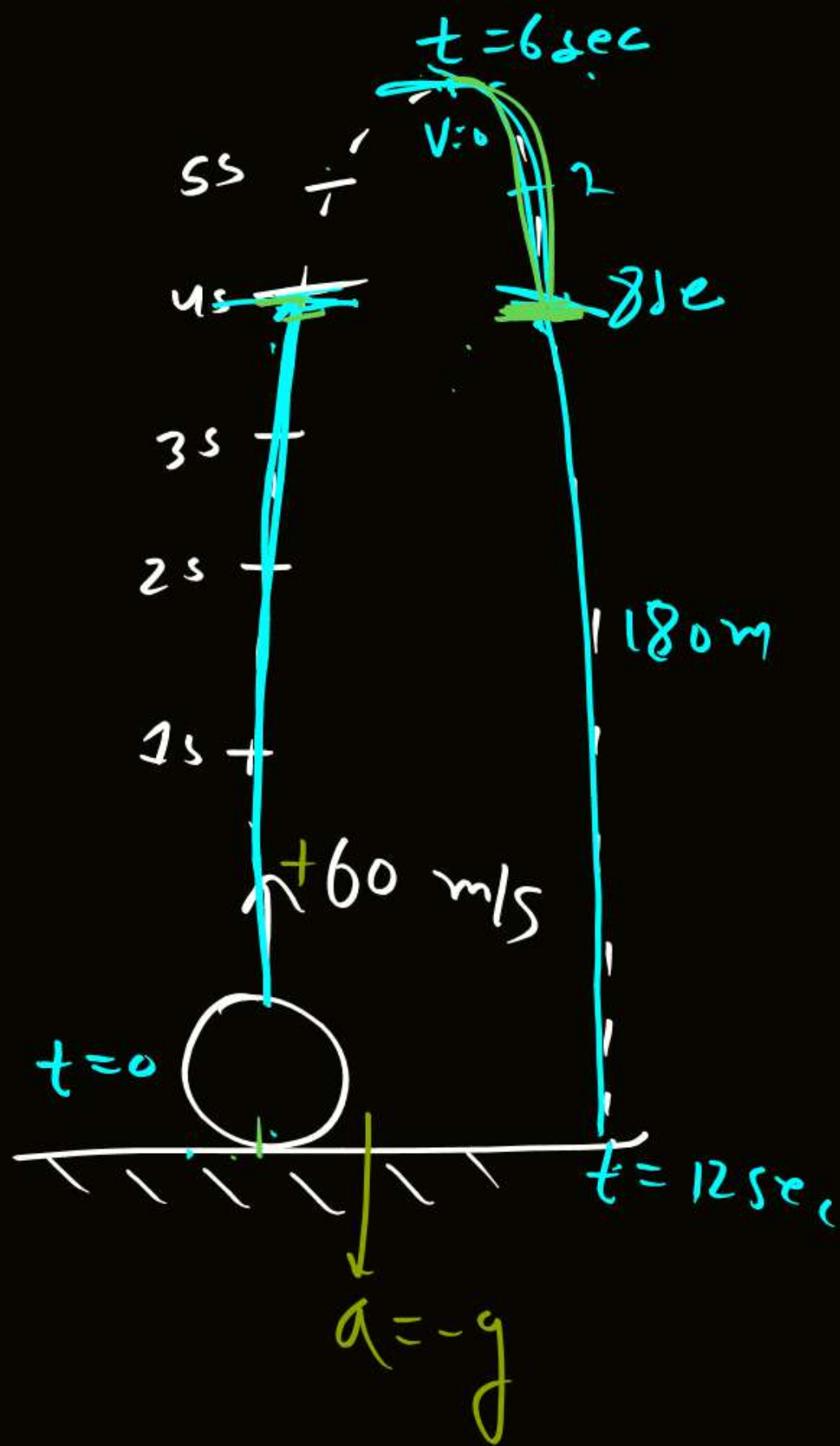
3rd 13th

8th

9th

t = 7th sec

342 वाली



$$(i) T_f = \frac{2u}{g} = \frac{2 \times 60}{10} = 12 \text{ sec} *$$

$$(ii) H_{\max} = \frac{u^2}{2g} = \frac{60 \times 60}{2 \times 10} = 180 \text{ m}$$

$$(iii) \text{disp}^m \text{ in 4-sec} =$$

$$(iv) \text{distance in 4-sec} = \boxed{160 \text{ m}}$$

$$(v) \text{disp}^m \text{ in 8-sec} \rightarrow \boxed{160 \text{ m}}$$

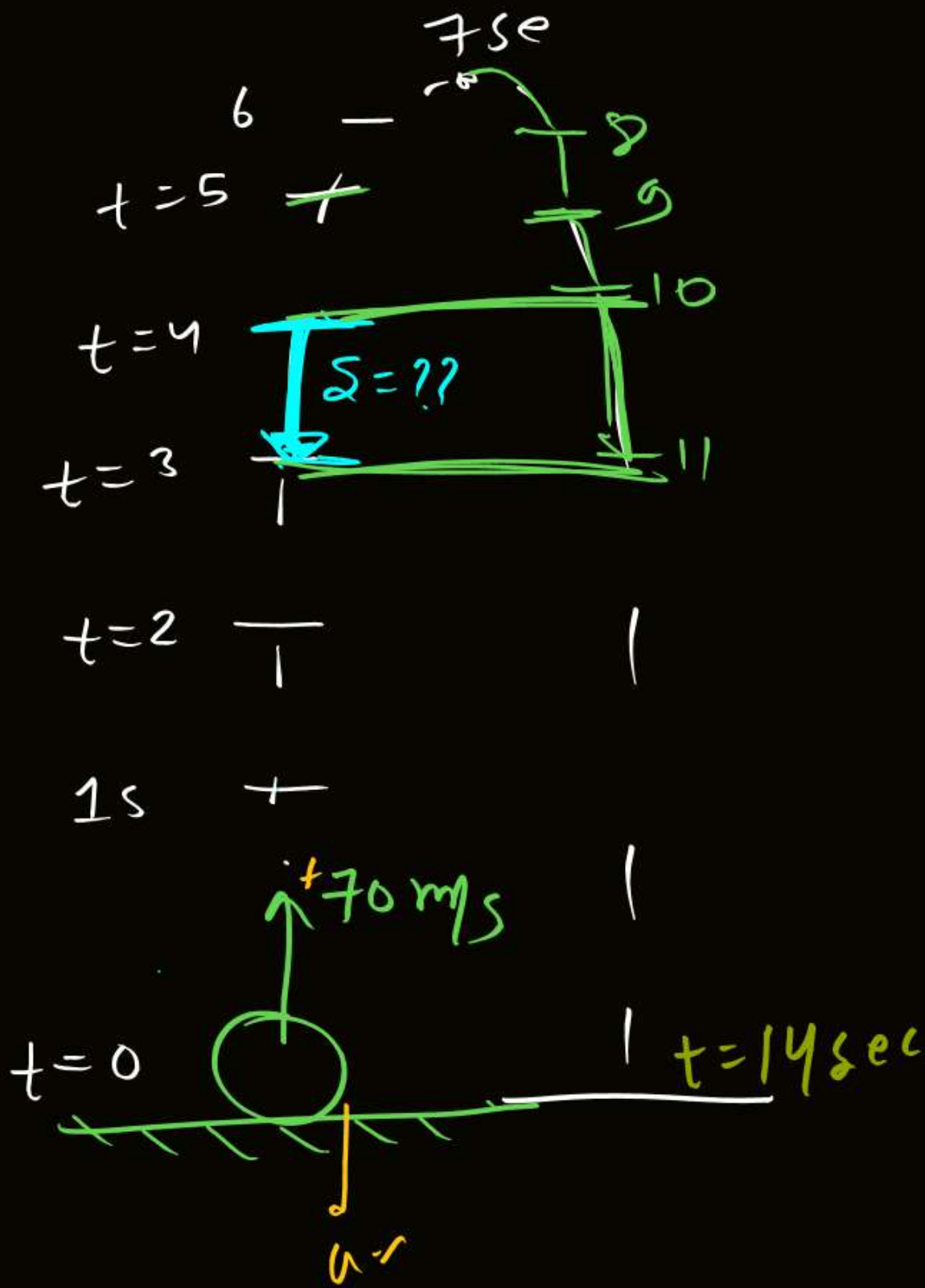
$$(vi) \text{dist}^n \text{ in 8-sec} = \underline{\underline{200 \text{ m}}}$$

$$* S = ut + \frac{1}{2} at^2$$

$$= 60 \times 4 - \frac{1}{2} \times 10 (4)^2$$

$$= 240 - 80 = \underline{\underline{160 \text{ m}}}$$

$$\boxed{S = ut + \frac{1}{2} at^2}$$



$$(i) \quad T_f = \frac{2u}{g} = \frac{2 \times 70}{10} = 14 \text{ sec}$$

$$(ii) \quad H_{\text{max}} = \frac{u^2}{2g} = \frac{70 \times 70}{2 \times 10} = \frac{4900}{2} = 2450 \text{ m}$$

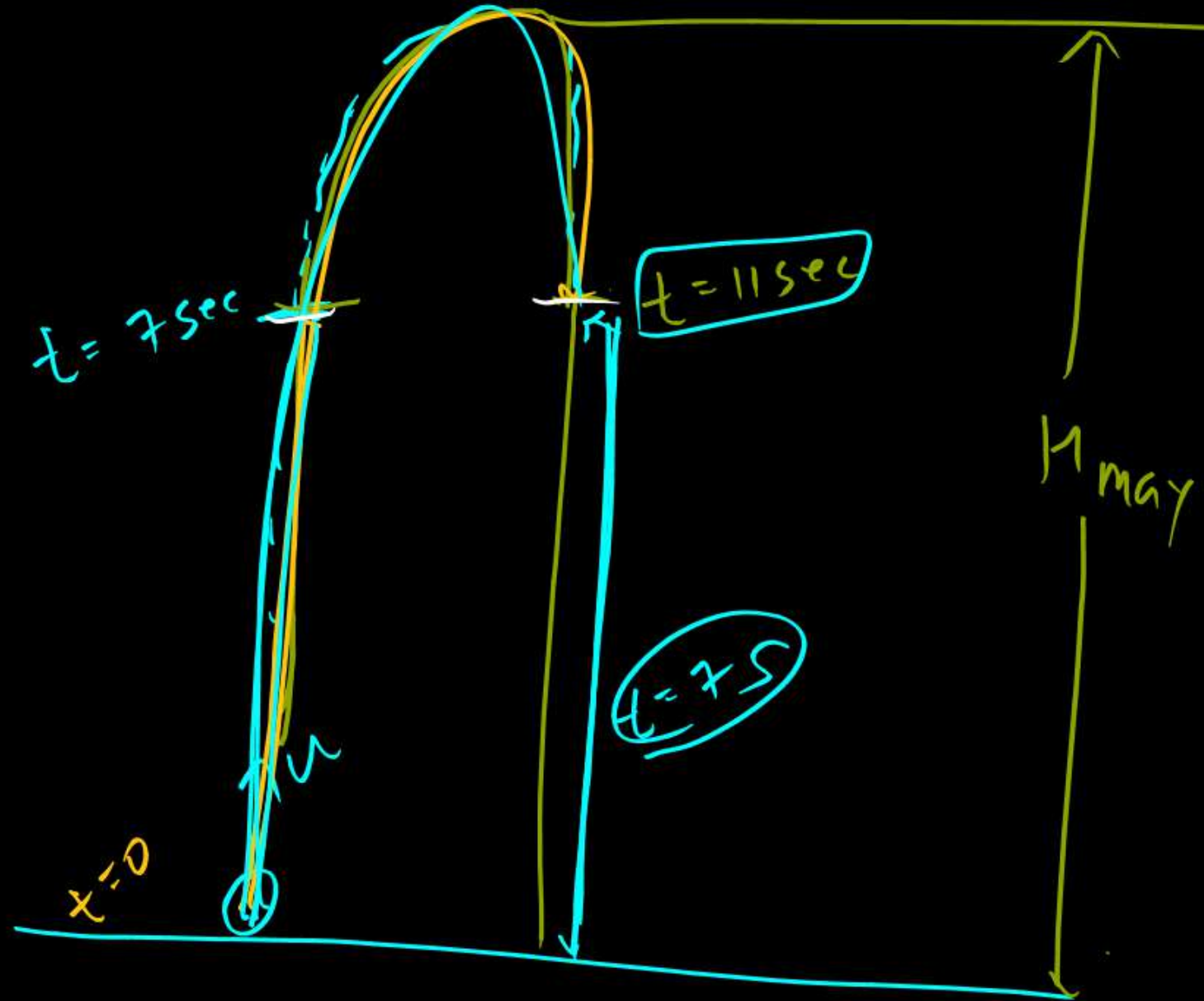
(iii) distance in 4th sec (3 sec से 4 sec)

$$S_{n^{\text{th}}} = u + \frac{a}{2}(2n-1)$$

$$= 70 - \frac{10}{2}(4 \times 2 - 1)$$

$$= 70 - 5 \times 7 = 70 - 35 = 35 \text{ m}$$

Object is projected up and it is at same height at $t = 7$ sec and $t = 11$ sec then find maximum height.



$$T_f = 11 \text{ sec} + 7 \text{ sec} \\ = 18 \text{ sec}$$

$$t_{up} = 9 \text{ sec} \\ u = 90 \text{ m/s} \\ H_n = \frac{90 \times 90}{2g} = \frac{810}{2} \\ = 405 \text{ m}$$



Object is projected up the distance travelled in 3rd sec and 8th sec then find that distance.

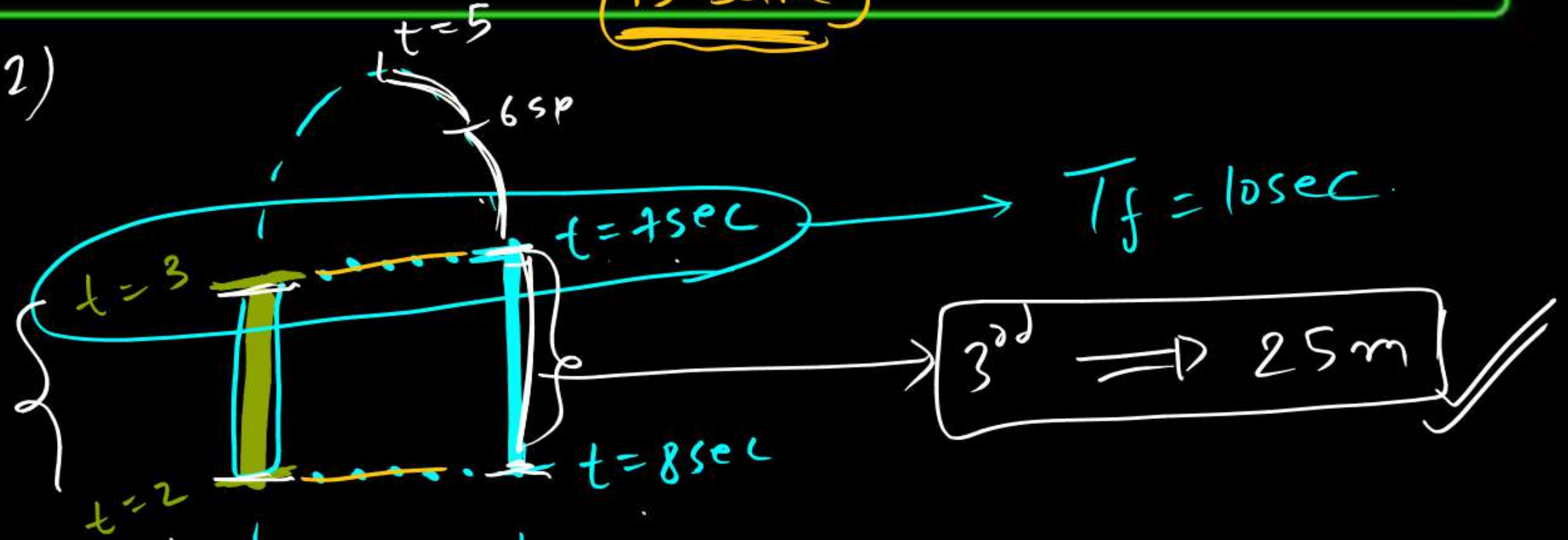
is same

$$S_{nth} = u + \frac{a}{2}(2n-2)$$

$$= 50 - \frac{10}{2}(3 \times 2 - 2)$$

$$= 50 - 25$$

$$= \underline{\underline{25m}}$$

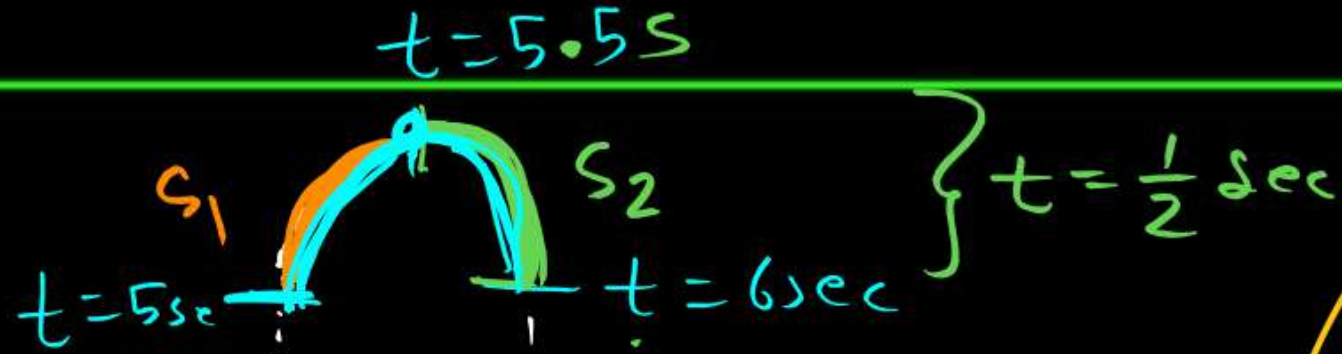


$$T_f = \frac{2u}{g}$$

$$T = 10 \text{ sec}$$



Object is projected up with, speed 55 m/s then find distance in 6th sec of journey.



distance = 2.5m

dis^m = 0m
In 6th sec

$$\begin{aligned}
 [S_2] &= u + \frac{1}{2} at^2 \\
 &= 0 + \frac{1}{2} 10 \times \left(\frac{1}{2}\right)^2 \\
 &= \frac{10}{8} = 1.25m
 \end{aligned}$$

$u = 55 \text{ m/s}$

$$T_f = 11 \text{ sec} \left(\frac{2u}{g} \right)$$

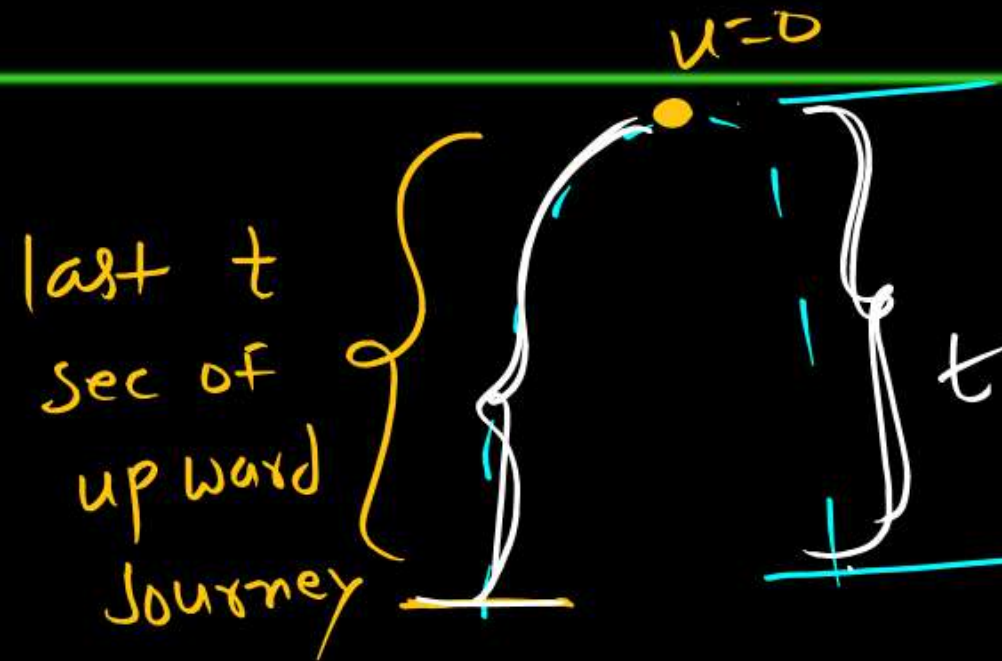
$$T_{up} = 5.5 \text{ sec}$$

time from
 $t = 5 \text{ sec}$ to $t = 6 \text{ sec}$

direction \rightarrow Change
 \rightarrow $\text{dist}^n \neq \text{dis}^m$



Object is projected with speed u then find distance in last ' t ' sec of upward journey.



distⁿ in 1st t sec of downward Journey = distance in last t - sec of upward Journey.

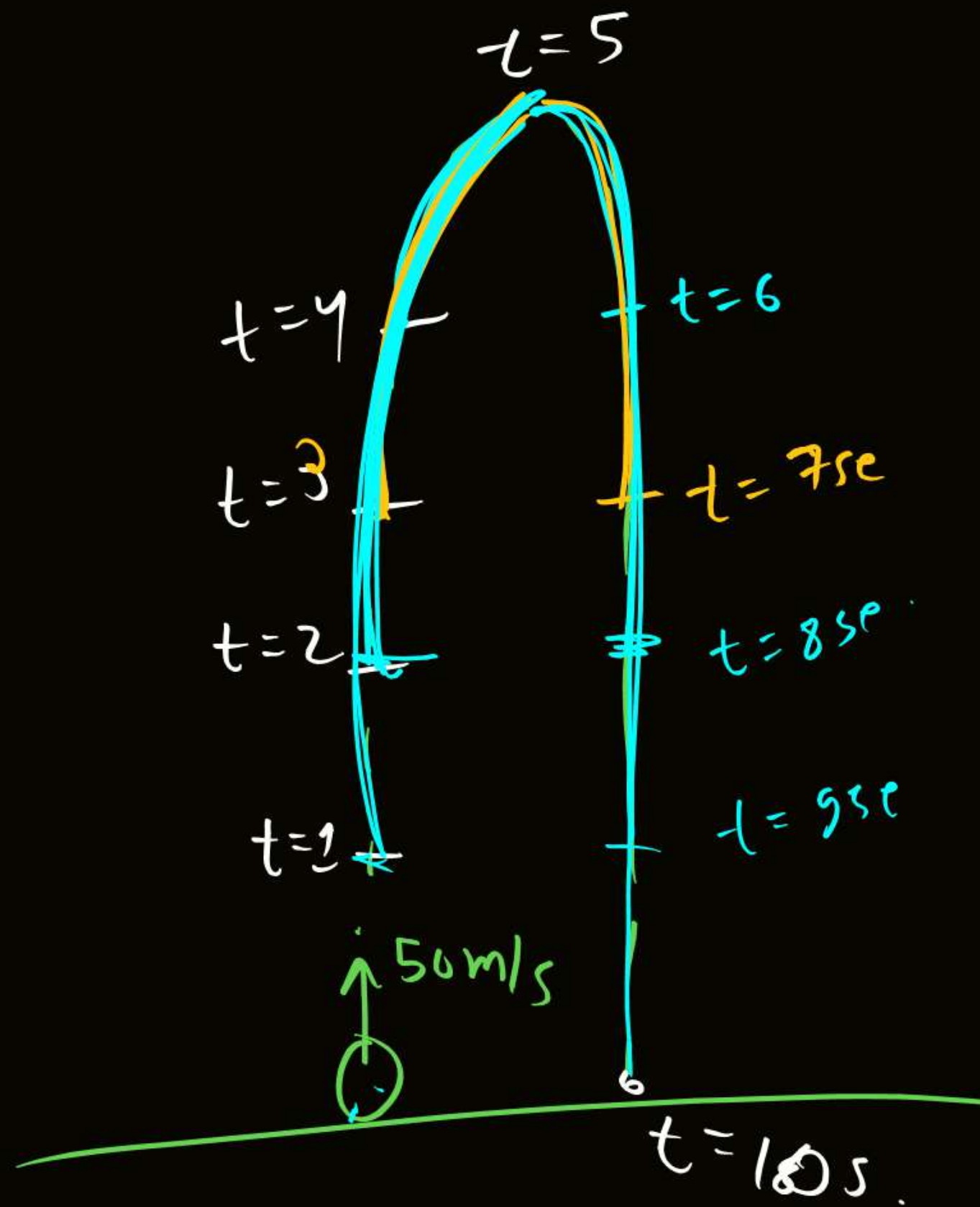
$$S_{n+1} = u + \frac{a}{2}(2n-1)$$

Not applic

1 sec se,

$$S_t = ut + \frac{1}{2}at^2 = \frac{1}{2}gt^2 = 5t^2 \text{ m}$$





Ball is projected with speed u and its speed is 10 m/s at half of the maximum height then find maximum height.

AI PMT

2 times

$$\frac{H_{\max}}{2} = \frac{(10)^2}{2g}$$

$$H_{\max} = 10 \text{ m}$$

$$\frac{H_{\max}}{2}$$

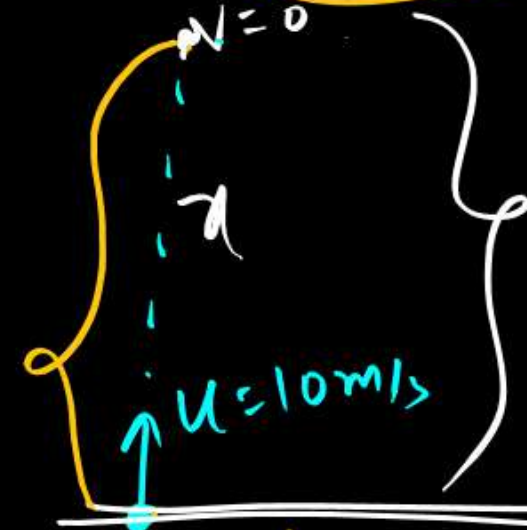
$$H_{\max} = ??$$

$$\frac{H_m}{2}$$

$$u$$

$$u=0$$

$$10 \text{ m/s}$$



$$v^2 - u^2 = 2as$$

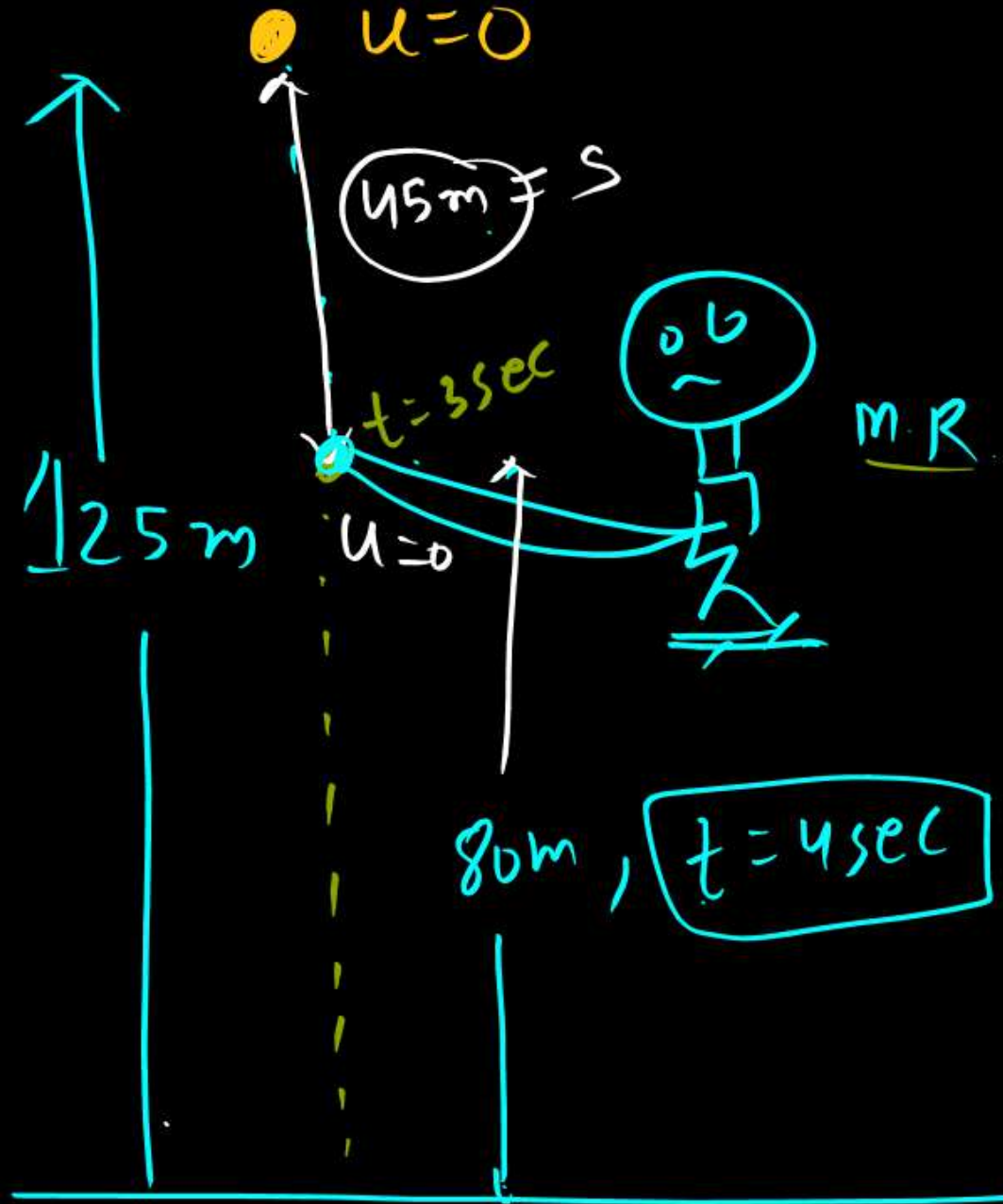
$$0 + (10)^2 = 2 \times 10 \times x$$

$$\frac{5 \text{ m}}{100} = \frac{x}{20}$$

$$H_{\max} = 2x = 10 \text{ m}$$



A ball is dropped from 125 m and after 3 sec it is stopped and released from rest instantaneously then find total time of flight.



$$T = 7\text{ sec}$$



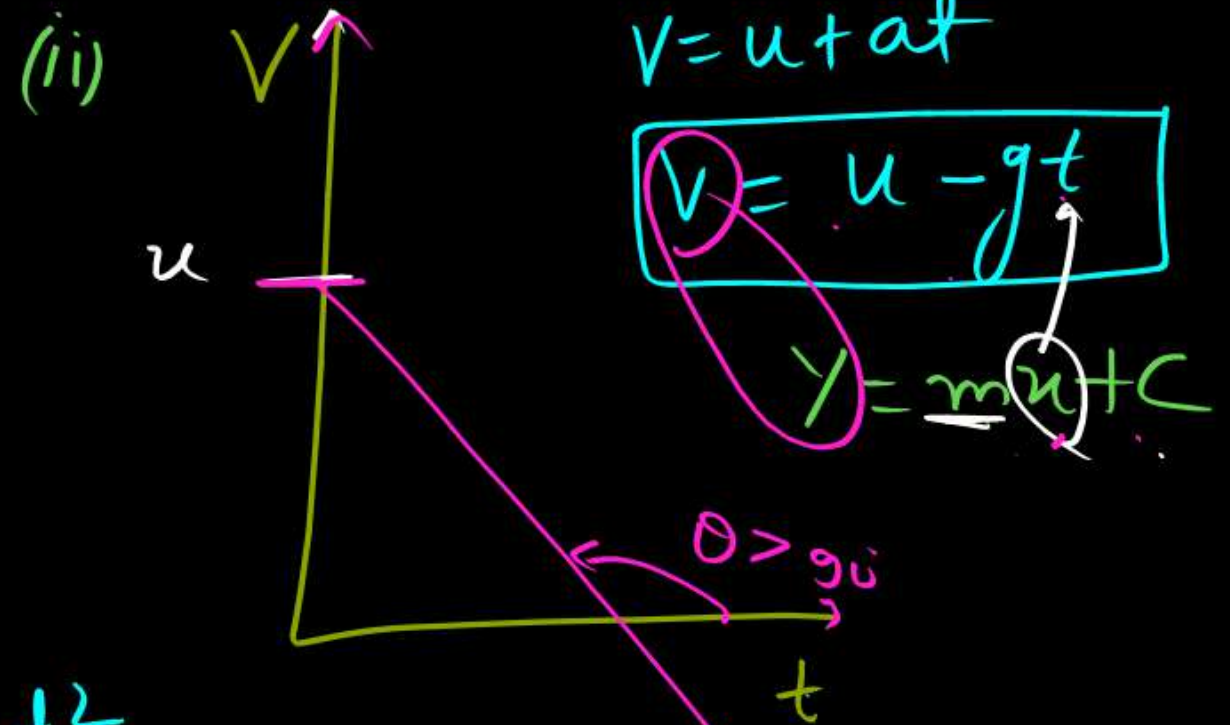
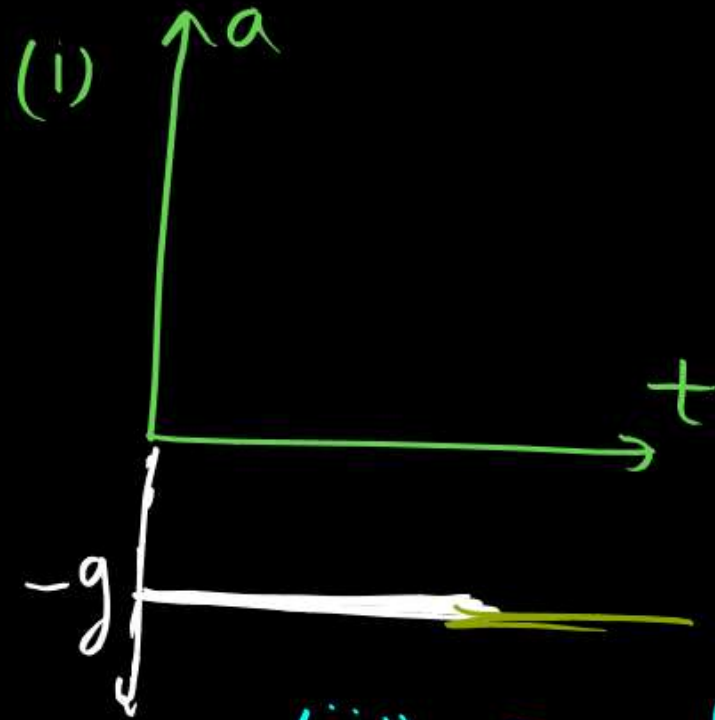
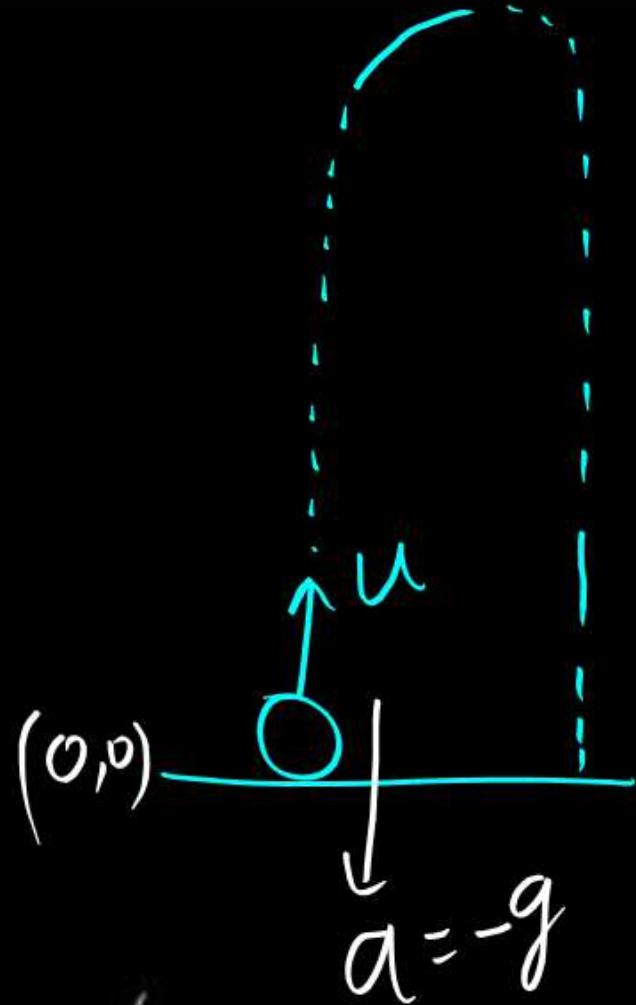
Ball is projected up with speed u then draw graph between

(i) a/t

(ii) v/t

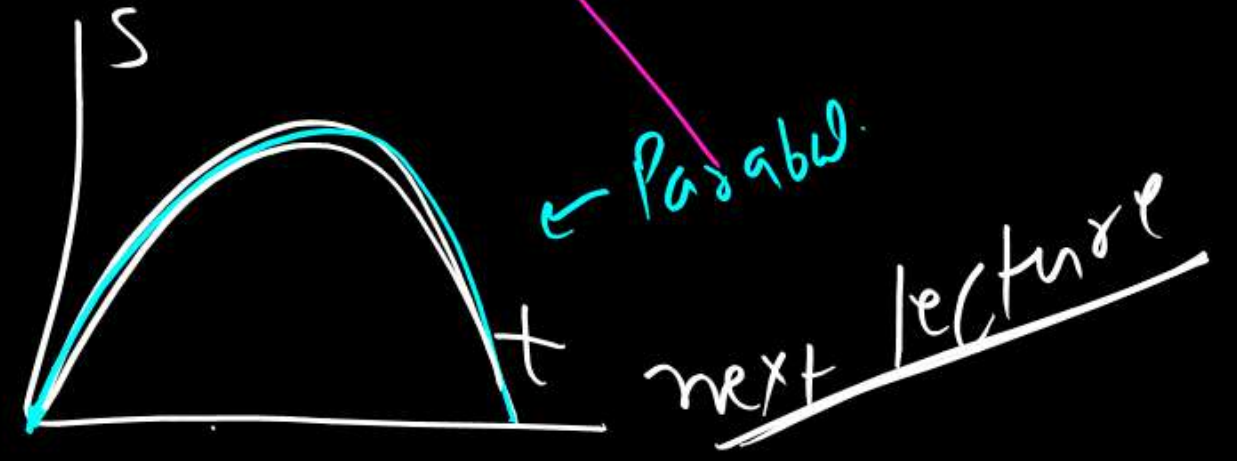
(iii) s/t

In next lecture of
g-rap.



(iii) $s = ut + \frac{1}{2}at^2$

$s = ut - \frac{1}{2}gt^2$



next lecture

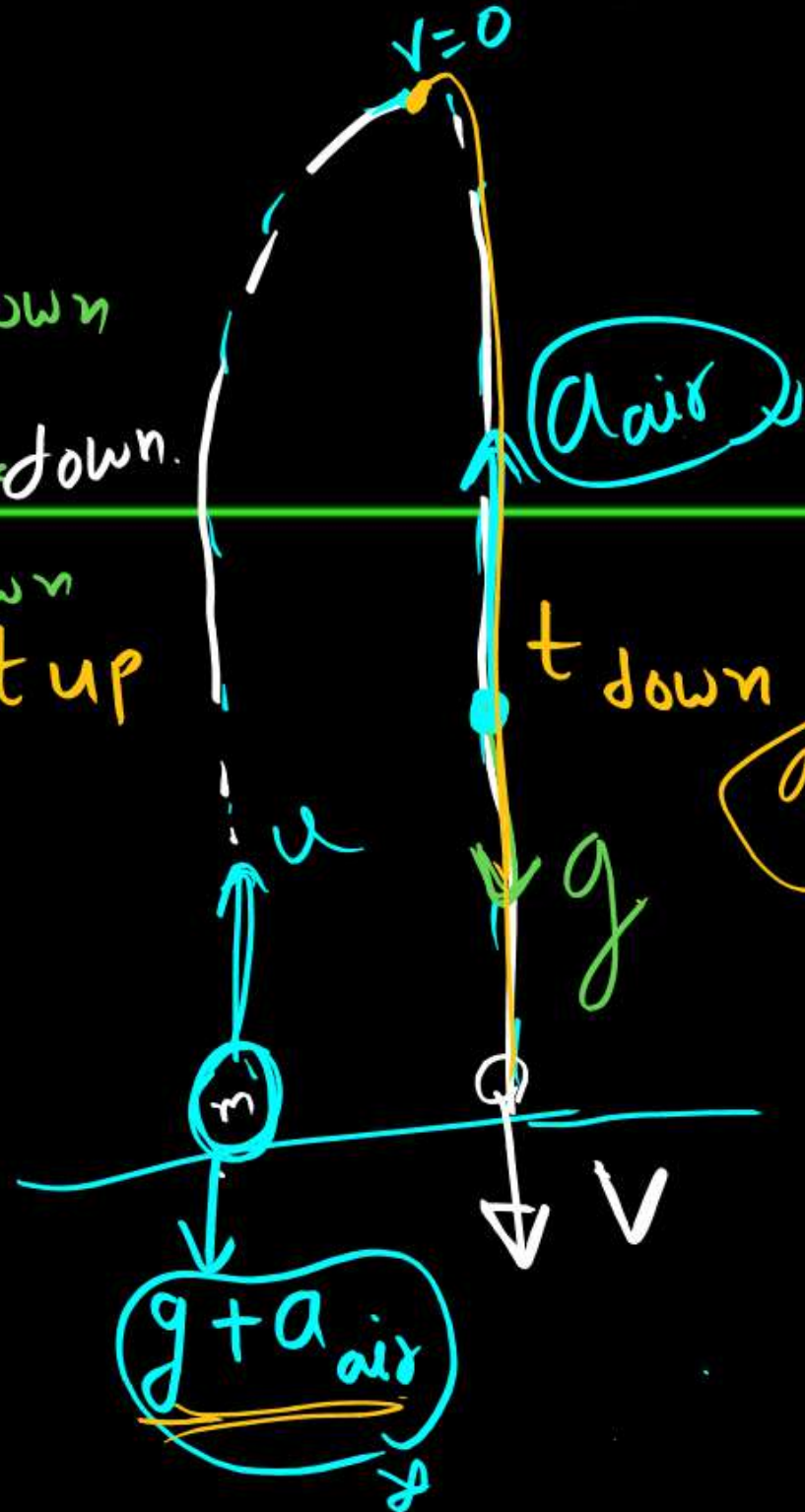


If air friction is not ignored then effect on time of flight and ^{on} speed of collision (constant air friction)

No air friction then
 $V = u$

(i) $t_{up} > t_{down}$
~~(ii)~~ $t_{up} < t_{down}$

(iii) $t_{up} = t_{down}$



$$a = g - a_{air}$$

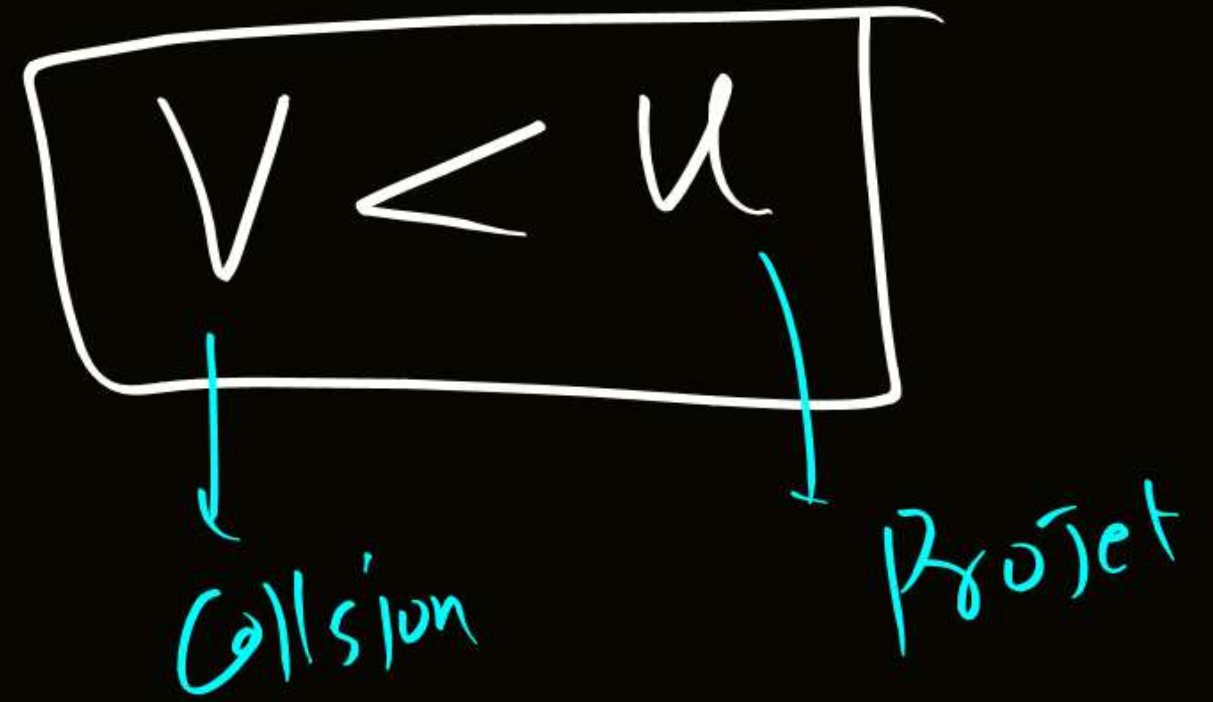
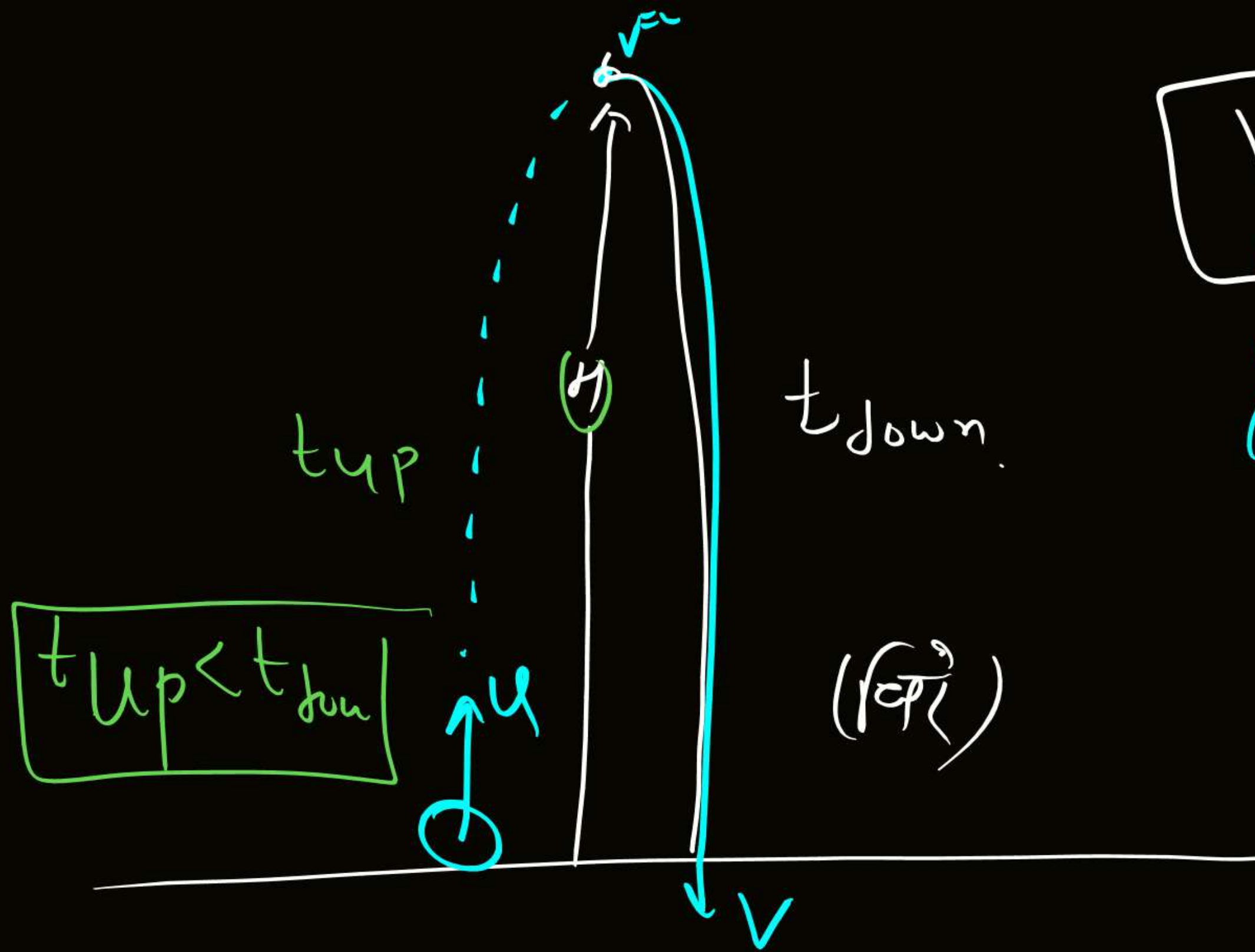
\rightarrow

$$V < u$$

* loss in energy due to friction

$$\frac{1}{2}mu^2 > \frac{1}{2}mv^2 \quad \boxed{u > v}_{\text{coll}}$$





friction
energy
loss

Ball is projected up and constant air resistance is acting on it 2 m/s^2 then
find $\frac{t_{\text{up}}}{t_{\text{down}}}$.

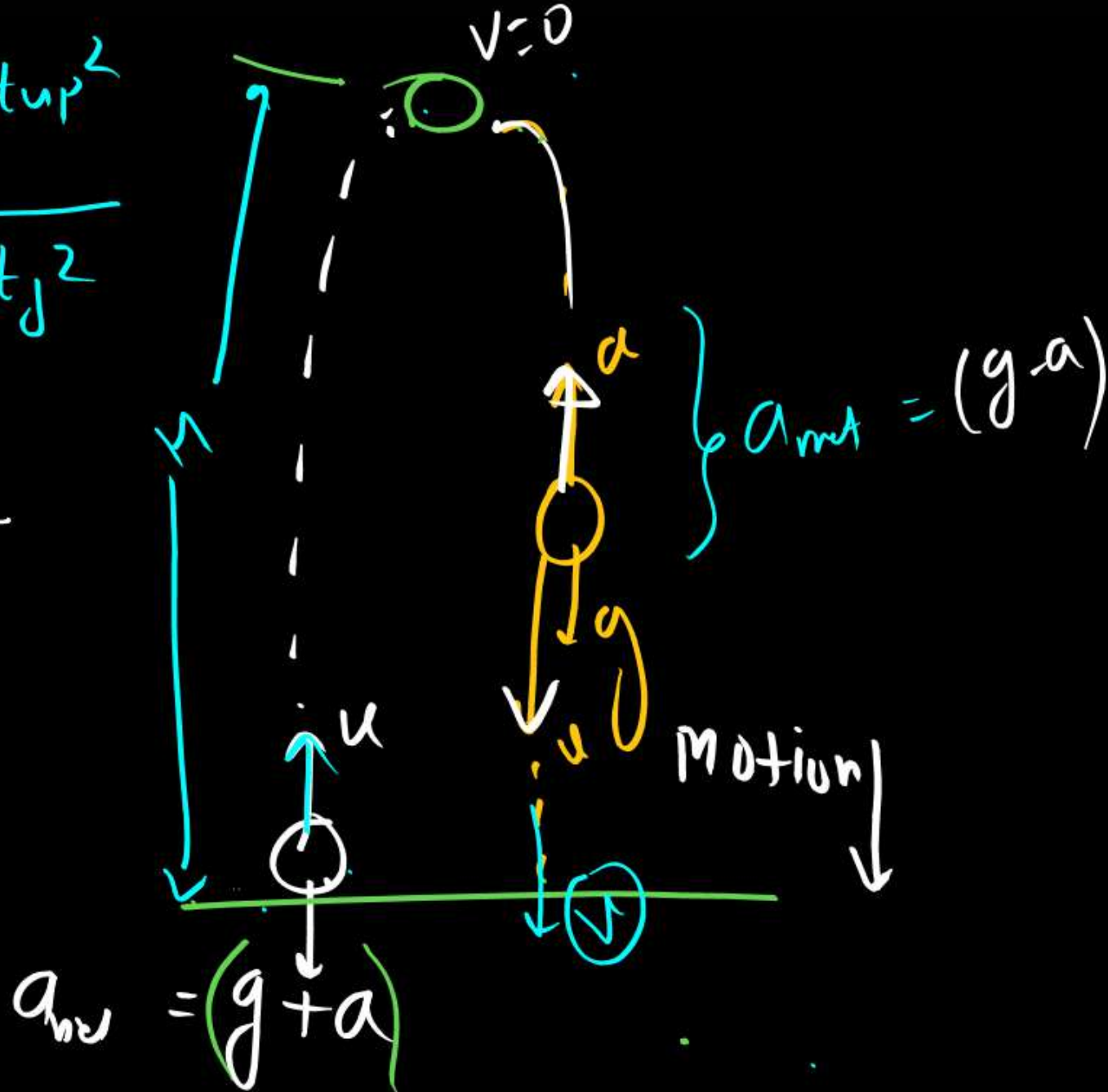
$$\textcircled{1} \quad \cancel{H = \frac{1}{2}(g+a)t_{\text{up}}^2}$$

$$\cancel{H = \frac{1}{2}(g-a)t_{\text{d}}^2}$$

$$\frac{t_{\text{up}}}{t_{\text{d}}} = \sqrt{\frac{g-a}{g+a}}$$

$$= \sqrt{\frac{8}{12}}$$

$$= \sqrt{\frac{2}{3}}$$



for upward journey

$$\textcircled{1} \quad H = \frac{1}{2}(g+a)t_{\text{up}}^2 \quad *$$

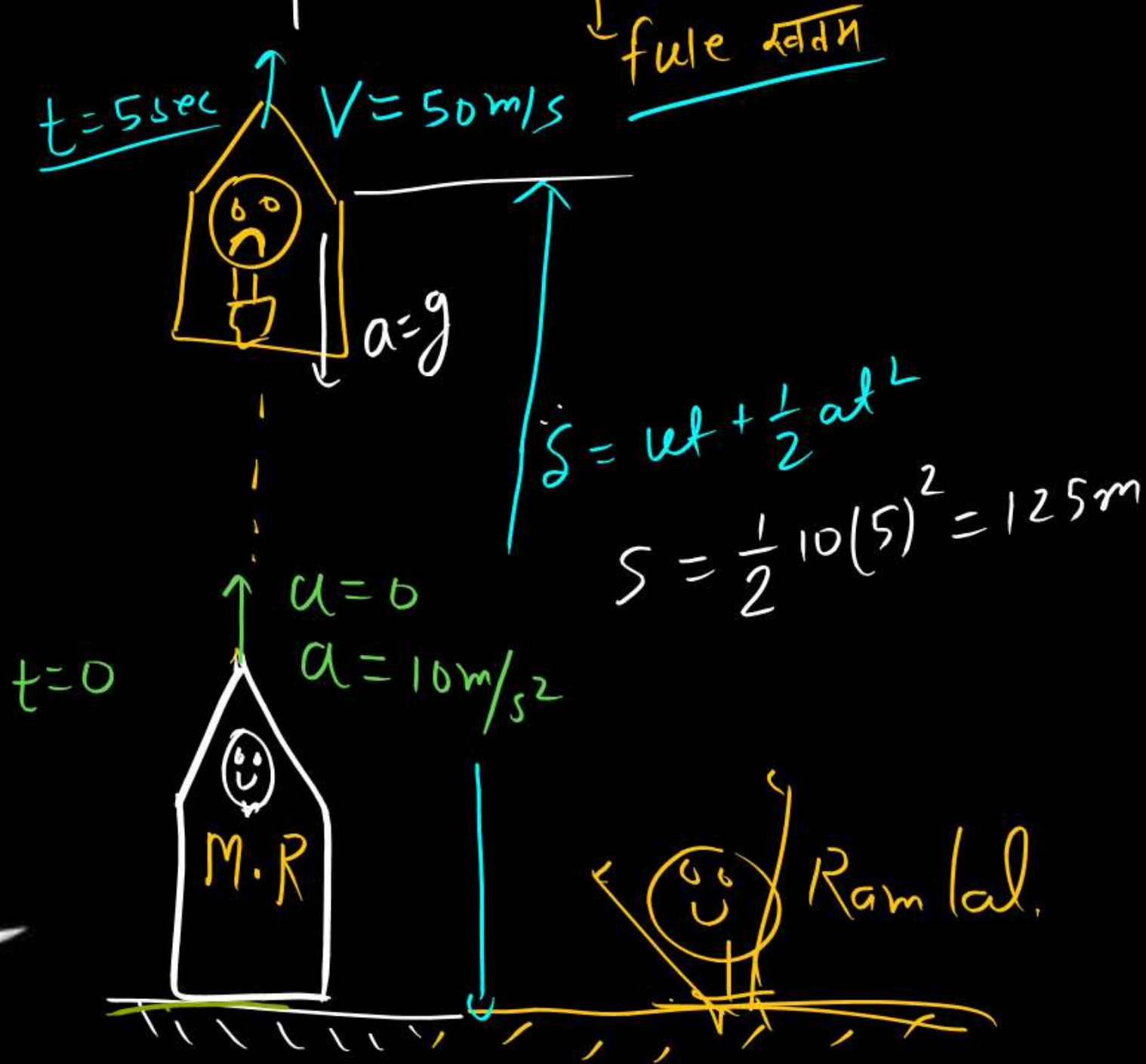
$$H = (u)t_{\text{up}} - \frac{1}{2}(g+a)t_{\text{up}}^2$$

for downward

$$\textcircled{II} \quad H = \frac{1}{2}(g-a)t_{\text{d}}^2$$

$$t_{\text{up}} = \frac{u}{g+a}$$

Rocket starts his motion in upward direction with acceleration 10 m/s^2 upward. After 5 sec engine off then find maximum height from ground.



$$(H_{\text{max}}) = \frac{u^2}{2g} = \frac{50 \times 50}{2 \times 10} = 125 \text{ m}$$

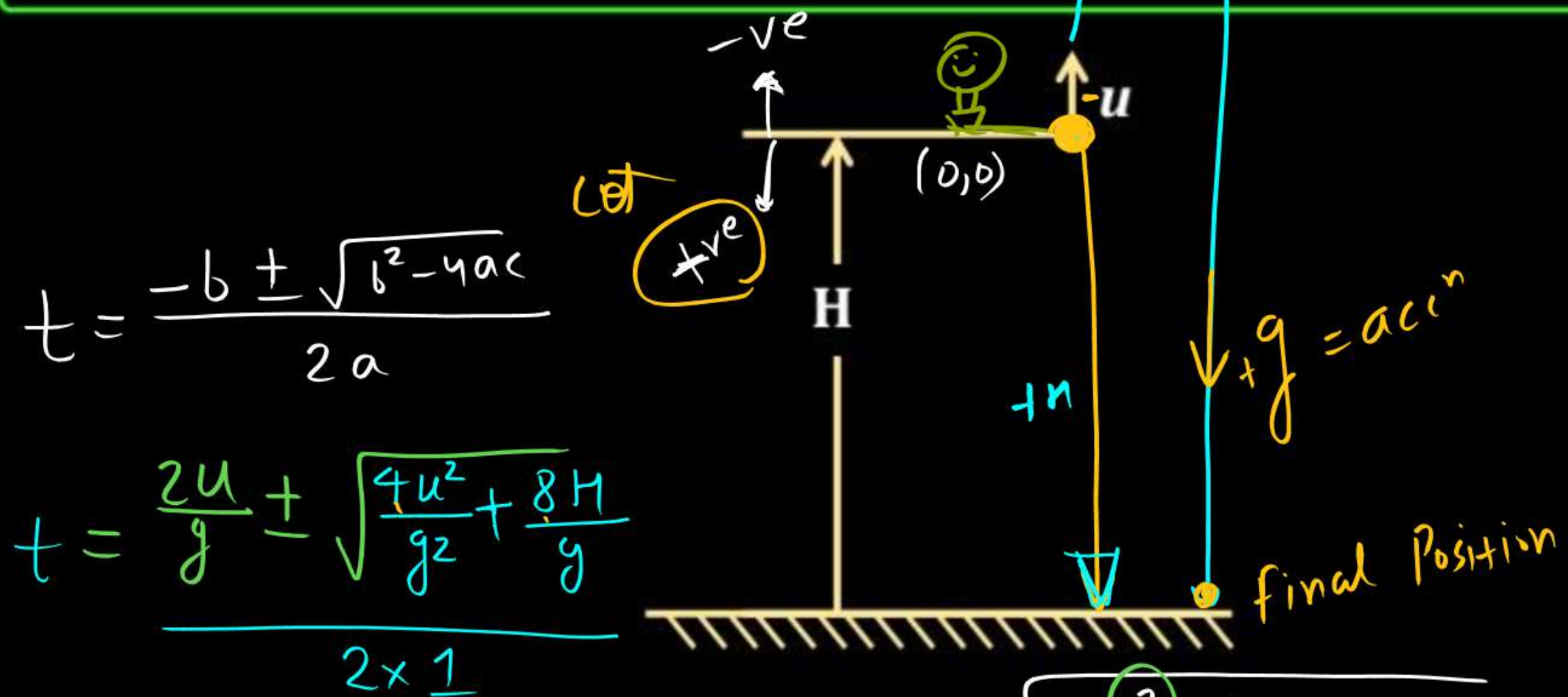
after 5-sec.

$$H_{\text{max from ground}} = 250 \text{ m}$$

Total time of Journey (time of flight) = 11.0



Motion under gravity from Height to ground.



$$t = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$t = \frac{2u}{g} \pm \sqrt{\frac{4u^2}{g^2} + \frac{8H}{g}}$$

2×1

$$t = \frac{2}{g} \left[\frac{u}{g} \pm \sqrt{\frac{u^2}{g^2} + \frac{2H}{g}} \right]$$

$$ax^2 + bx + c = 0$$

$$\text{disp}^m = +H$$

$$s = ut + \frac{1}{2}at^2$$

$$H = -ut + \frac{1}{2}gt^2 \quad \times \frac{2}{g}$$

$$t^2 - \frac{2u}{g}t - \frac{2H}{g} = 0$$



$$* t = \frac{u}{g} \pm \sqrt{\frac{u^2}{g^2} + \frac{2H}{g}}$$

जै

MR* ①

Dimⁿ

MR* ②

let $u=0$

drop

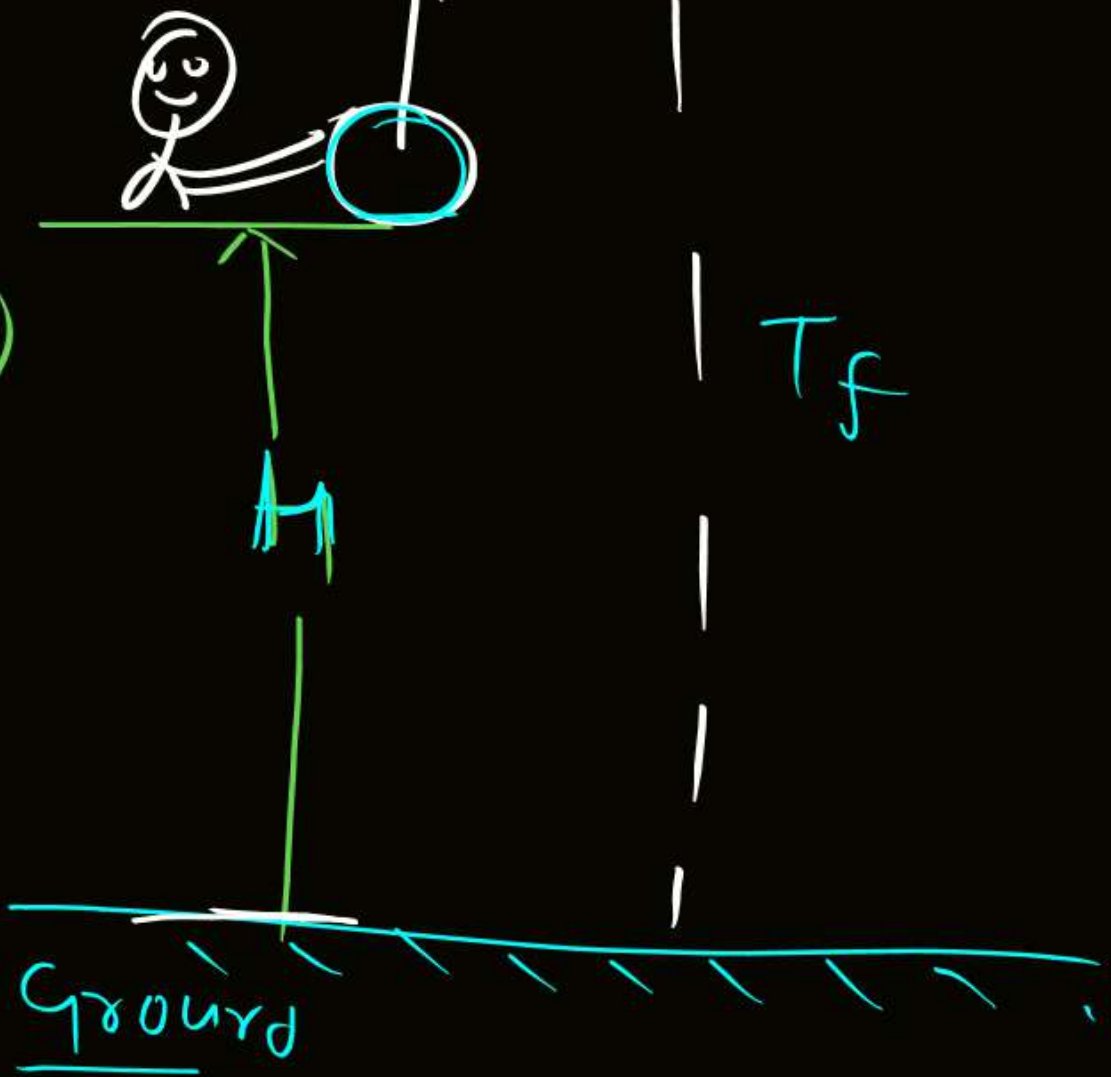
$$t = \sqrt{\frac{2H}{g}}$$

MR* ③

let $H=0$

Ground to Ground.

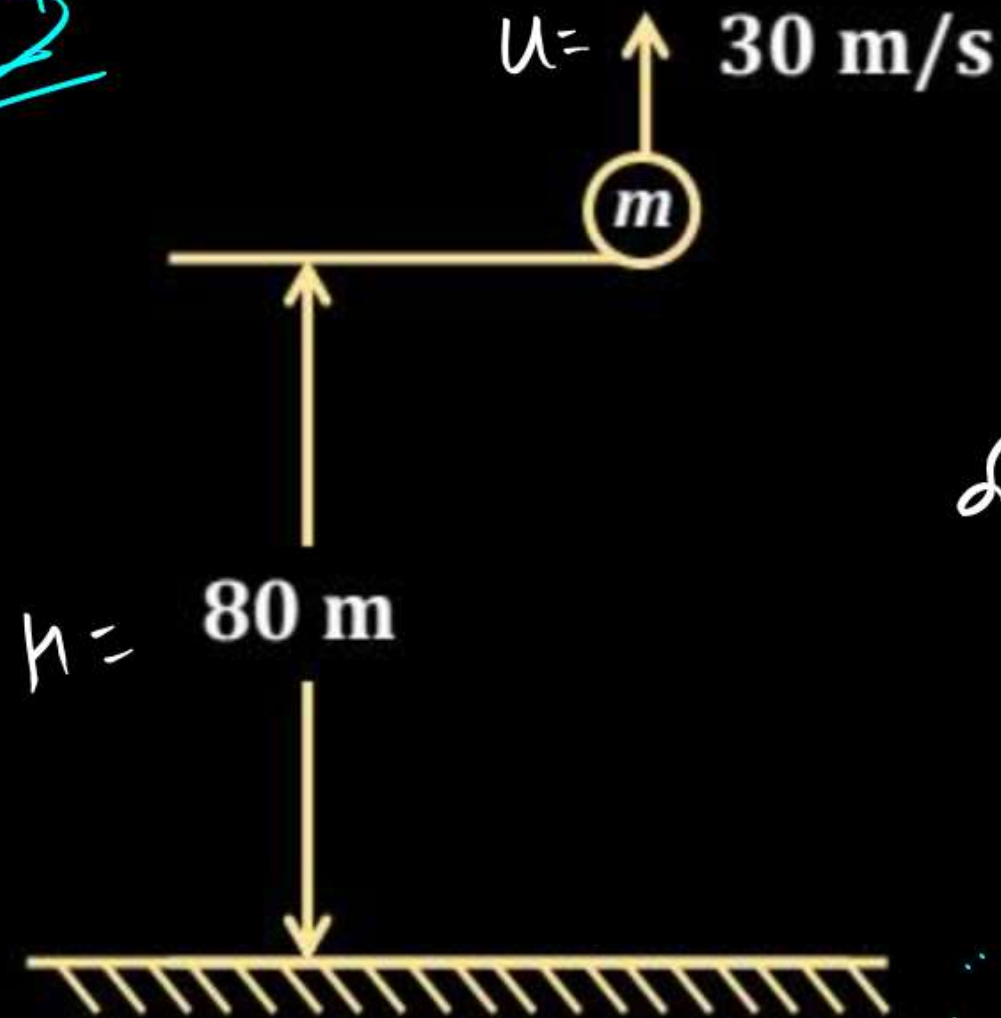
$$T = \frac{2u}{g}$$



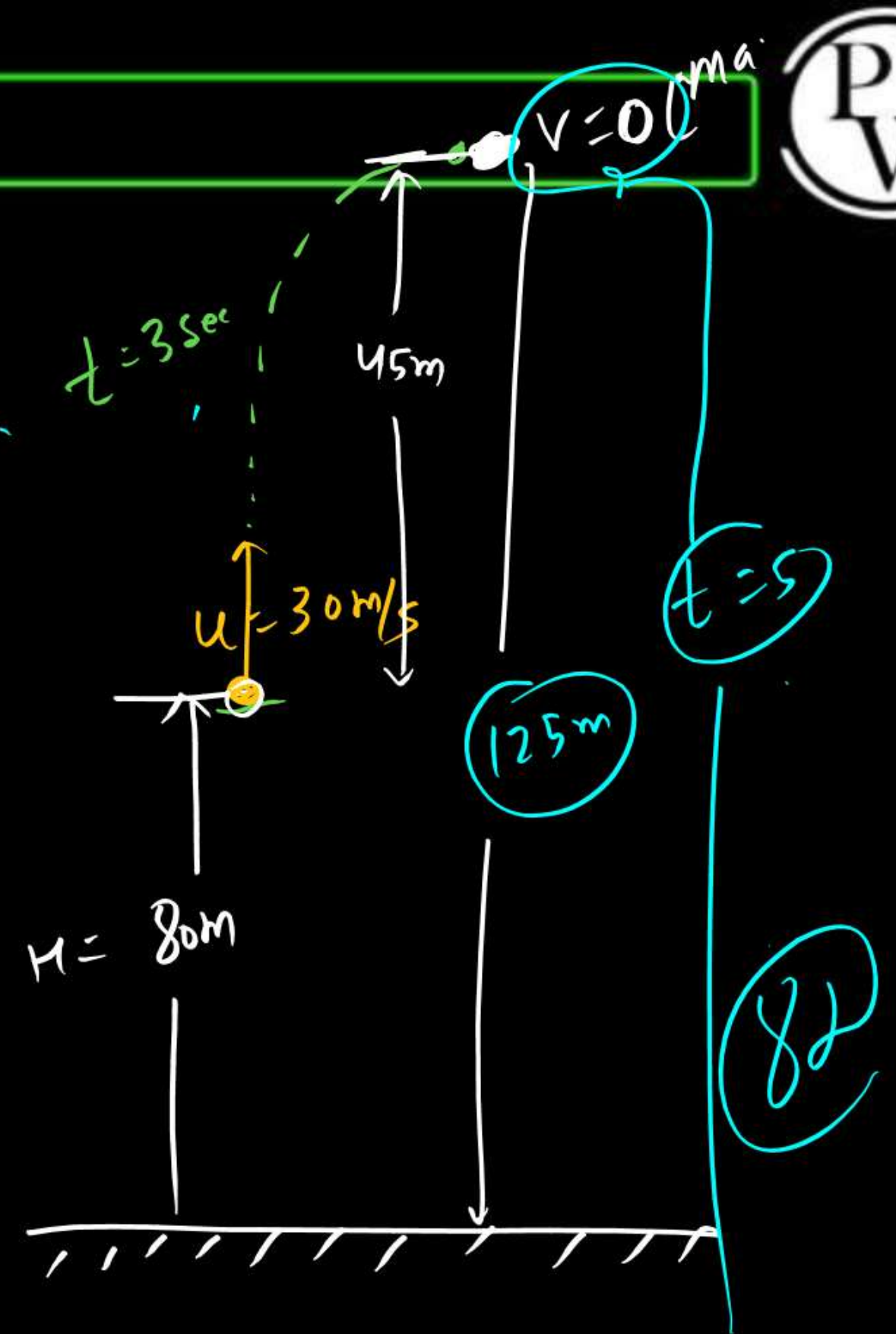
Find time of flight. =??



AIIMS



soln

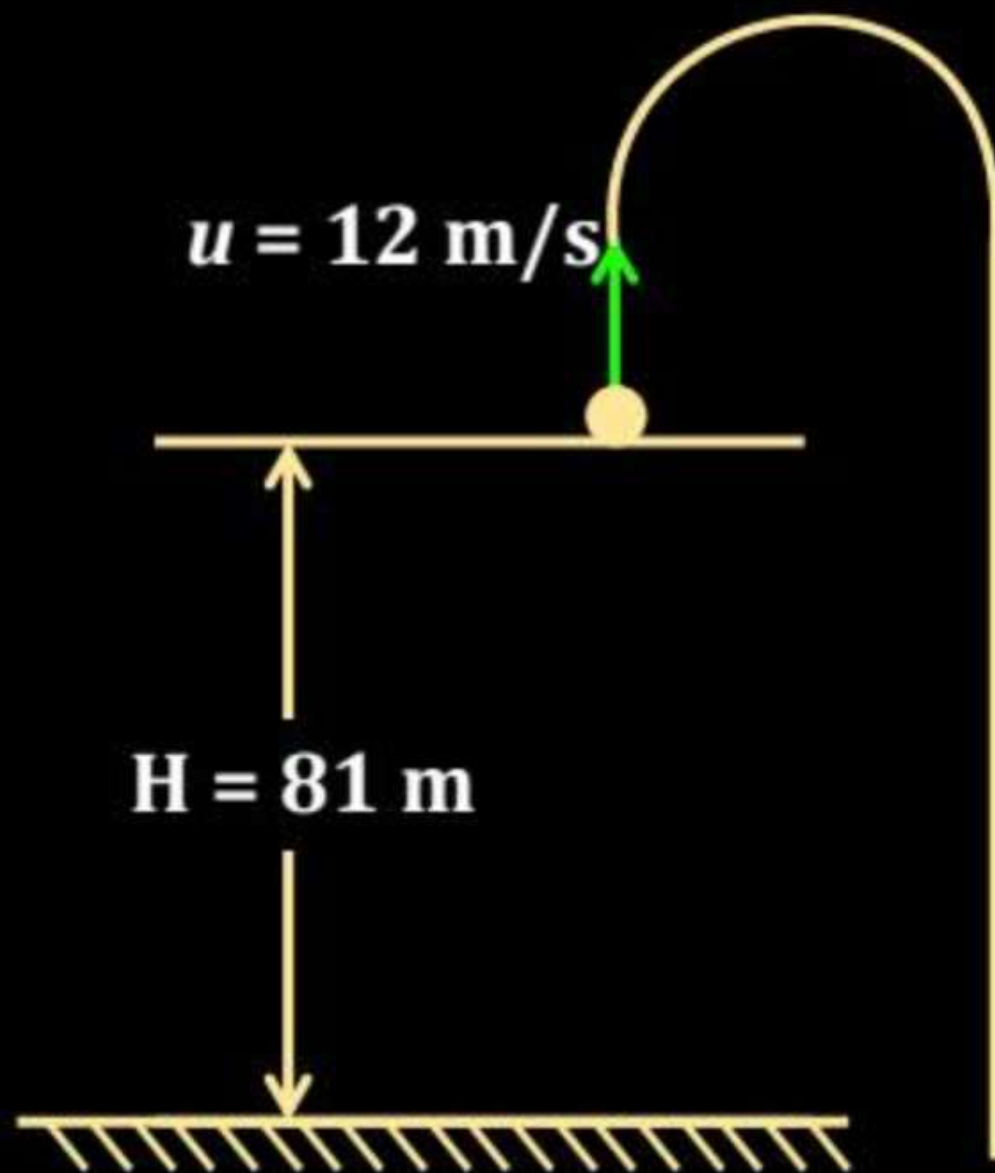


82



Find time of flight.

[AIIMS]



(i) 5.2 sec

(ii) 4 sec

(iii) 8 sec

(iv) 3.8 sec

N.W → No match



Ball is projected up with u from height H and collide with $3u$ at ground then find $H = ?$



17. W
use 3rd eqⁿ of
motion



Ball is projected with up with speed u from Height H then time of flight is 9 sec. with some speed u it is projected downward then time of flight is 4 sec. Then find time of flight when object is dropped from same height.

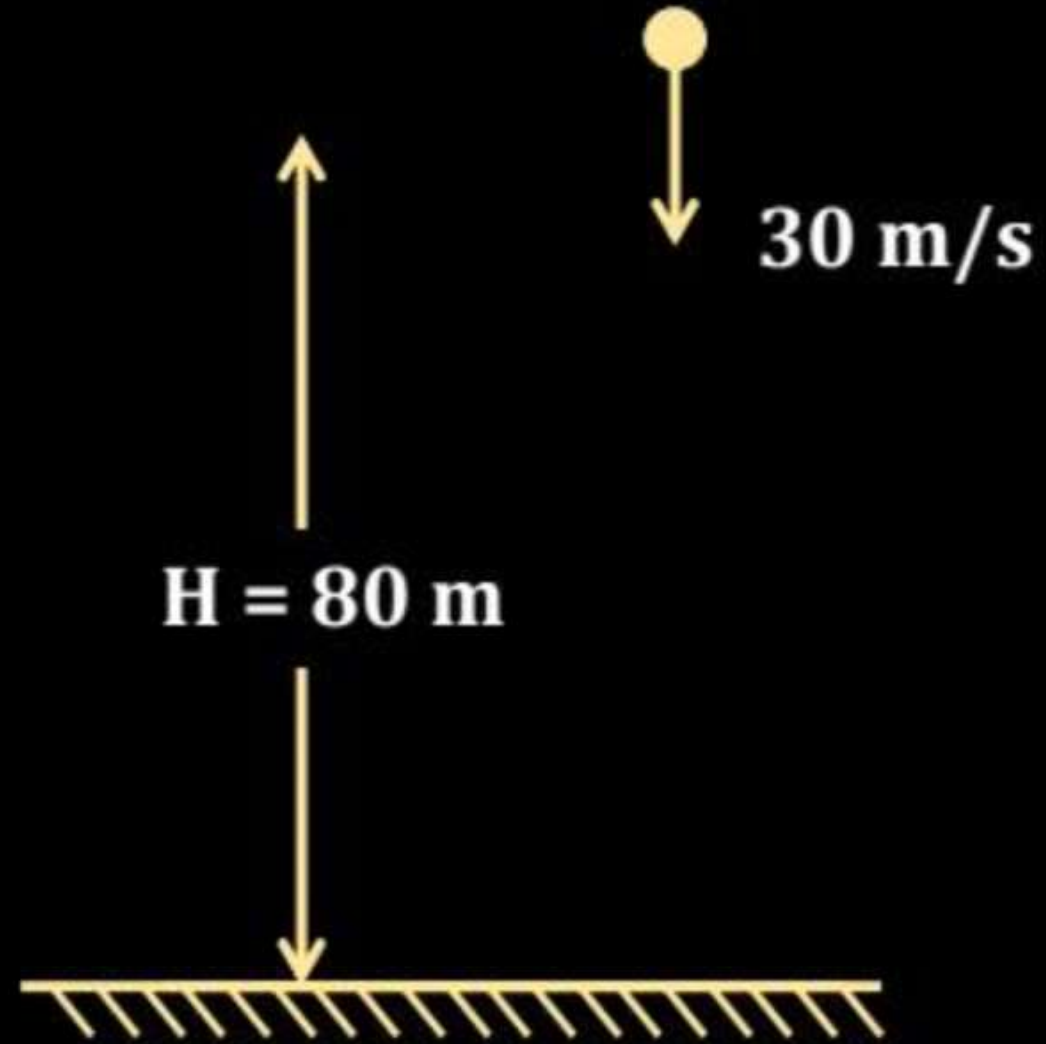
$$t = \sqrt{t_1 t_2}$$

H.W

Ans
 $t = 6 \text{ sec}$



Find time of flight.



H.W

*use 3rd eqⁿ of
motⁿ find v*

then

$$\frac{v-u}{a} = t$$





THANK YOU 😊

