

## Homework 11

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- 1) I would try the lower bound which is  $4^3 = 64$ , and the higher bound which is  $5^3 = 125$ .

Since 82 is in between 125 and 64, the floor of cube root(82) would be 4 since 4 is the lower bound

- 2) Yes, you can. If we root the inequality by  $r$ , then the inequality will be  $\text{root} \leq (n)^{1/r} < \text{root}+1$ . Because of this, the lower bound is root. Since the floor function returns the lower bound of the inequality, we can conclude the root =  $\text{floor}((n)^{1/r})$ .

- 3) Yes, if  $r$  is an even number, then  $g^r$  (which is  $n$ ) can be a positive number, while  $g$  can be negative. If  $r$  is negative, then  $g$  cannot be a negative number since  $n$  will become  $n$ , which violates the preconditions. There is no reason to try a guess that is greater than  $n$  because  $r$  can only be a positive integer, so root of  $n$  by  $r$  will always be less than  $n$ .

- 4) lowEnough could be  $-\text{root}$  and tooHigh could be  $\text{root}+1$ . Since there is a chance that  $r$  could be an even number and the root of  $n$  can be a negative, the lower bound has to be the negative of the the root. The high bound has to be the  $\text{root}+1$  since the both the positive and negative roots will be less than  $\text{root}+1$ .

- 5) I would first set the bounds at 0 and 47226 and guess 23613. Then if 23613 is less than the expression, which it is, I would set the bounds at 0 and 23613. I would do that again, but with the guess 11806. Set the bounds at 0 and 11806, and do that until 8 is the halfway point between the bounds.

```
private static int root(int n, int r) {  
    int lowerBound = 0;  
    int higherBound = n;  
    int guess = (lowerBound + higherBound) / 2;  
    while (guess != power(n, r))  
        if (guess < power(n, r)) {  
            lowerBound = guess;  
        }  
        else {  
            higherBound = guess;  
        }  
    guess = (lowerBound + higherBound) / 2;  
}
```

6)