

## Problem A. Required Length

**Time Limit** 2000 ms

### Problem Statement

Takahashi wants to set his password for a certain website to a string  $P$  consisting of lowercase English letters.

The password for that website must be a string of length at least  $L$ .

Determine whether  $P$  satisfies the length condition, that is, whether it is a string of length at least  $L$ .

### Constraints

- $P$  is a string consisting of lowercase English letters with length between 1 and 100, inclusive.
- $1 \leq L \leq 100$
- $L$  is an integer.

### Input

The input is given from Standard Input in the following format:

```
 $P$   
 $L$ 
```

### Output

If  $P$  satisfies the length condition, print **Yes**; otherwise, print **No**.

### Sample 1

| Input         | Output |
|---------------|--------|
| chokudai<br>5 | Yes    |

The length of `chokudai` is 8, which is at least 5, so it satisfies the length condition.  
Thus, print `Yes`.

### Sample 2

| Input   | Output |
|---------|--------|
| ac<br>3 | No     |

The length of `ac` is 2, which is less than 3, so it does not satisfy the length condition.  
Thus, print `No`.

### Sample 3

| Input        | Output |
|--------------|--------|
| atcoder<br>7 | Yes    |

The length of `atcoder` is 7, which is at least 7, so it satisfies the length condition.  
Thus, print `Yes`.

## Problem B. G1

**Time Limit** 2000 ms

### Problem Statement

In AtCoder Kingdom, there are  $N$  horse races being held.  
Horses aged  $A_i$  or younger can participate in the  $i$ -th race.  
Among the  $N$  races, how many races can a  $K$ -year-old horse participate in?

### Constraints

- All input values are integers.
- $1 \leq N \leq 100$
- $1 \leq A_i \leq 100$
- $1 \leq K \leq 100$

### Input

The input is given from Standard Input in the following format:

```
 $N$   
 $A_1 A_2 \dots A_N$   
 $K$ 
```

### Output

Output the answer as an integer.

### Sample 1

| Input               | Output |
|---------------------|--------|
| 5<br>3 1 4 1 5<br>4 | 2      |

- Horses aged 3 or younger can participate in the 1st race.
- Horses aged 1 or younger can participate in the 2nd race.

- Horses aged 4 or younger can participate in the 3rd race.
- Horses aged 1 or younger can participate in the 4th race.
- Horses aged 5 or younger can participate in the 5th race.

Among the 5 races, a 4-year-old horse can participate in the 3rd and 5th races, which is 2 races.

### Sample 2

| Input         | Output |
|---------------|--------|
| 1<br>1<br>100 | 0      |

There may be no races that a  $K$ -year-old horse can participate in.

### Sample 3

| Input  | Output |
|--|--------|
| 15<br>18 89 31 2 15 93 64 78 58 19 79 59 24 50<br>30<br>38 | 8      |

## Problem C. Reverse Proxy

**Time Limit** 2000 ms

### Problem Statement

There are  $N$  boxes numbered  $1, 2, \dots, N$ . Initially, all boxes are empty.

$Q$  balls will come in order.

Takahashi will put the balls into the boxes according to the sequence  $X = (X_1, X_2, \dots, X_Q)$ .

Specifically, he performs the following process for the  $i$ -th ball:

- If  $X_i \geq 1$ : Put this ball into box  $X_i$ .
- If  $X_i = 0$ : Put this ball into the box with the smallest number among those containing the fewest balls.

Find which box each ball was put into.

### Constraints

- All input values are integers.
- $1 \leq N \leq 100$
- $1 \leq Q \leq 100$
- $0 \leq X_i \leq N$

### Input

The input is given from Standard Input in the following format:

```
N Q
X1 X2 ... XQ
```

### Output

If the  $i$ -th ball was put into box  $B_i$ , output in the following format:

$$B_1 \ B_2 \ \dots \ B_Q$$

### Sample 1

| Input            | Output    |
|------------------|-----------|
| 4 5<br>2 0 3 0 0 | 2 1 3 4 1 |

There are 4 boxes, and 5 balls come.

- Initially, all boxes are empty.
  - The numbers of balls in box 1, 2, 3, 4 are 0, 0, 0, 0, respectively.
- Since  $X_1 = 2$ , put the 1st ball into box 2.
  - The numbers of balls in box 1, 2, 3, 4 are 0, 1, 0, 0, respectively.
- Since  $X_2 = 0$ , put the 2nd ball into box 1, which has the smallest number among those containing the fewest balls.
  - The numbers of balls in box 1, 2, 3, 4 are 1, 1, 0, 0, respectively.
- Since  $X_3 = 3$ , put the 3rd ball into box 3.
  - The numbers of balls in box 1, 2, 3, 4 are 1, 1, 1, 0, respectively.
- Since  $X_4 = 0$ , put the 4th ball into box 4, which has the smallest number among those containing the fewest balls.
  - The numbers of balls in box 1, 2, 3, 4 are 1, 1, 1, 1, respectively.
- Since  $X_5 = 0$ , put the 5th ball into box 1, which has the smallest number among those containing the fewest balls.
  - The numbers of balls in box 1, 2, 3, 4 are 2, 1, 1, 1, respectively.

The balls were put into boxes 2, 1, 3, 4, 1 in order. Thus, output **2 1 3 4 1**.

### Sample 2

| Input                | Output        |
|----------------------|---------------|
| 3 7<br>1 1 0 0 0 0 0 | 1 1 2 3 2 3 1 |

### Sample 3

| Input   | Output                                  |
|---|---|
| 6 20<br>4 6 0 3 4 2 6 5 2 3 0 3 2 5 0 3 5 0 2 0 | 4 6 1 3 4 2 6 5 2 3 1 3 2 5 1 3 5 4 2 6 |

## Problem D. Distance Table

**Time Limit** 2000 ms

### Problem Statement

There are  $N$  stations, station 1, station 2,  $\dots$ , station  $N$ , arranged in this order on a straight line.

Here, for  $1 \leq i \leq N - 1$ , the distance between stations  $i$  and  $(i + 1)$  is  $D_i$ .

For each pair of integers  $(i, j)$  satisfying  $1 \leq i < j \leq N$ , find the distance between stations  $i$  and  $j$ .

For the output format, refer to the Output section.

### Constraints

- $2 \leq N \leq 50$
- $1 \leq D_i \leq 100$
- All input values are integers.

### Input

The input is given from Standard Input in the following format:

```
N
D_1 D_2 ... D_{N-1}
```

### Output

Output  $N - 1$  lines.

On the  $i$ -th line ( $1 \leq i \leq N - 1$ ), output  $(N - i)$  integers, separated by spaces.

The  $j$ -th integer on the  $i$ -th line ( $1 \leq j \leq N - i$ ) should be the distance between stations  $i$  and  $(i + j)$ .

### Sample 1

| Input         | Output                             |
|---------------|------------------------------------|
| 5<br>5 10 2 3 | 5 15 17 20<br>10 12 15<br>2 5<br>3 |

The distances between stations are as follows:

- The distance between stations 1 and 2 is 5.
- The distance between stations 1 and 3 is  $5 + 10 = 15$ .
- The distance between stations 1 and 4 is  $5 + 10 + 2 = 17$ .
- The distance between stations 1 and 5 is  $5 + 10 + 2 + 3 = 20$ .
- The distance between stations 2 and 3 is 10.
- The distance between stations 2 and 4 is  $10 + 2 = 12$ .
- The distance between stations 2 and 5 is  $10 + 2 + 3 = 15$ .
- The distance between stations 3 and 4 is 2.
- The distance between stations 3 and 5 is  $2 + 3 = 5$ .
- The distance between stations 4 and 5 is 3.

Thus, output as shown above.

## Sample 2

| Input    | Output |
|----------|--------|
| 2<br>100 | 100    |



## Problem E. Black Intervals

**Time Limit** 3000 ms

### Problem Statement

There are  $N$  squares arranged in a row from left to right. Initially, all squares are painted white.

Process  $Q$  queries in order. The  $i$ -th query gives an integer  $A_i$  between 1 and  $N$ , inclusive, and performs the following operation:

Flip the color of the  $A_i$ -th square from the left. Specifically, if the  $A_i$ -th square from the left is painted white, paint it black; if it is painted black, paint it white. Then, find the number of intervals of consecutively painted black squares.

Here, an interval of consecutively painted black squares is a pair of integers  $(l, r)$  ( $1 \leq l \leq r \leq N$ ) that satisfy all of the following:

- The  $l$ -th,  $(l + 1)$ -th,  $\dots$ ,  $r$ -th squares from the left are all painted black.
- Either  $l = 1$ , or the  $(l - 1)$ -th square from the left is painted white.
- Either  $r = N$ , or the  $(r + 1)$ -th square from the left is painted white.

### Constraints

- $1 \leq N, Q \leq 5 \times 10^5$
- $1 \leq A_i \leq N$
- All input values are integers.

### Input

The input is given from Standard Input in the following format:

```
N Q
A1 A2 ... A_Q
```

### Output

Output  $Q$  lines. On the  $i$ -th line ( $1 \leq i \leq Q$ ), output the answer to the  $i$ -th query.

### Sample 1

| Input                | Output                          |
|----------------------|---------------------------------|
| 5 7<br>2 3 3 5 1 5 2 | 1<br>1<br>1<br>2<br>2<br>1<br>1 |

Below, the  $i$ -th square from the left is referred to as square  $i$ .

After each query, the state is as follows:

- After the 1st query, only square 2 is painted black. There is 1 interval of consecutively painted black squares:  $(l, r) = (2, 2)$ .
- After the 2nd query, squares 2, 3 are painted black. There is 1 interval of consecutively painted black squares:  $(l, r) = (2, 3)$ .
- After the 3rd query, only square 2 is painted black. There is 1 interval of consecutively painted black squares:  $(l, r) = (2, 2)$ .
- After the 4th query, squares 2, 5 are painted black. There are 2 intervals of consecutively painted black squares:  $(l, r) = (2, 2), (5, 5)$ .
- After the 5th query, squares 1, 2, 5 are painted black. There are 2 intervals of consecutively painted black squares:  $(l, r) = (1, 2), (5, 5)$ .
- After the 6th query, only squares 1, 2 are painted black. There is 1 interval of consecutively painted black squares:  $(l, r) = (1, 2)$ .
- After the 7th query, only square 1 is painted black. There is 1 interval of consecutively painted black squares:  $(l, r) = (1, 1)$ .

Thus, output 1, 1, 1, 2, 2, 1, 1 separated by newlines.

### Sample 2

| Input      | Output |
|------------|--------|
| 1 2<br>1 1 | 1<br>0 |

After the 2nd query, all squares are painted white, so output 0 on the 2nd line.

**Sample 3**

| Input        | Output      |
|--------------|-------------|
| 3 3<br>1 3 2 | 1<br>2<br>1 |

## Problem F. Conflict 2

**Time Limit** 2000 ms

### Problem Statement

There is one server and  $N$  PCs. The server and each PC each hold one string, and initially all strings are empty.

$Q$  queries are given. Each query is in one of the following formats:

- **1**  $p$  : Replace the string of PC  $p$  with the string of the server.
- **2**  $p$   $s$  : Append string  $s$  to the end of the string of PC  $p$ .
- **3**  $p$  : Replace the string of the server with the string of PC  $p$ .

Find the final string of the server after processing all queries in the given order.

### Constraints

- $N, Q$  are integers
- $1 \leq N, Q \leq 2 \times 10^5$
- For every query,  $p$  is an integer and  $1 \leq p \leq N$ .
- For every query of type 2,  $s$  is a string of length at least 1 consisting of lowercase English letters.
- The sum of the lengths of  $s$  over all queries of type 2 is at most  $10^6$ .

### Input

The input is given from Standard Input in the following format:

```
N Q
query1
query2
⋮
queryQ
```

Here, query <sub>$i$</sub>  represents the  $i$ -th query and is given in one of the following formats:

```
1 p
```

2 p s

3 p

## Output

Output the answer.

### Sample 1

| Input   | Output  |
|---|---------|
| 2 6<br>2 1 at<br>3 1<br>2 2 on<br>1 2<br>2 2 coder<br>3 2 | atcoder |

- Initially, the strings of the server and PCs 1, 2 are all empty.
- 1st query: Append **at** to the end of the string of PC 1. At this time, the strings of the server, PC 1, 2 are empty, **at**, empty, respectively.
- 2nd query: Replace the string of the server with the string of PC 1. At this time, the strings of the server, PC 1, 2 are **at**, **at**, empty, respectively.
- 3rd query: Append **on** to the end of the string of PC 2. At this time, the strings of the server, PC 1, 2 are **at**, **at**, **on**, respectively.
- 4th query: Replace the string of PC 2 with the string of the server. At this time, the strings of the server, PC 1, 2 are **at**, **at**, **at**, respectively.
- 5th query: Append **coder** to the end of the string of PC 2. At this time, the strings of the server, PC 1, 2 are **at**, **at**, **atcoder**, respectively.
- 6th query: Replace the string of the server with the string of PC 2. At this time, the strings of the server, PC 1, 2 are **atcoder**, **at**, **atcoder**, respectively.

Thus, the final string of the server is **atcoder**.

### Sample 2

| Input                                   | Output |
|---|--------|
| 100000 3<br>1 100<br>2 300 abc<br>3 200 |        |

The final string of the server is empty.

### Sample 3

| Input   | Output               |
|---|----------------------|
| 10 10<br>2 7 ladx<br>2 7 zz<br>2 7 kfm<br>3 7<br>1 5<br>2 5 irur<br>3 5<br>1 6<br>2 6 ptilun<br>3 6 | ladxfzzkfmirurptilun |

## Problem G. E [max]

**Time Limit** 3000 ms

### Problem Statement

There are  $N$  six-sided dice. The dice are numbered from 1 to  $N$ , and the numbers written on the faces of die  $i$  are  $A_{i,1}, A_{i,2}, \dots, A_{i,6}$ .

Now, all  $N$  dice will be rolled simultaneously. Find the expected value, modulo 998244353, of the maximum value among the numbers written on the face that comes up on each die.

For any die, the face that comes up when the die is rolled is chosen independently and uniformly at random.

► Finding the expected value modulo 998244353

### Constraints

- $1 \leq N \leq 10^5$
- $1 \leq A_{i,j} \leq 10^9$
- All input values are integers.

### Input

The input is given from Standard Input in the following format:

```
N
A1,1 A1,2 ... A1,6
A2,1 A2,2 ... A2,6
⋮
AN,1 AN,2 ... AN,6
```

### Output

Output the answer.

### Sample 1

| Input                           | Output    |
|---------------------------------|-----------|
| 2<br>1 1 4 4 4 4<br>1 1 1 3 3 3 | 332748121 |

Let  $x_i$  be the number written on the face that comes up on die  $i$ .

- Case  $x_1 = 1, x_2 = 1$ : Occurs with probability  $\frac{2}{6} \times \frac{3}{6} = \frac{1}{6}$ , and the maximum value among the numbers written on the faces that come up is 1.
- Case  $x_1 = 1, x_2 = 3$ : Occurs with probability  $\frac{2}{6} \times \frac{3}{6} = \frac{1}{6}$ , and the maximum value among the numbers written on the faces that come up is 3.
- Case  $x_1 = 4, x_2 = 1$ : Occurs with probability  $\frac{4}{6} \times \frac{3}{6} = \frac{1}{3}$ , and the maximum value among the numbers written on the faces that come up is 4.
- Case  $x_1 = 4, x_2 = 3$ : Occurs with probability  $\frac{4}{6} \times \frac{3}{6} = \frac{1}{3}$ , and the maximum value among the numbers written on the faces that come up is 4.

Thus, the expected value to be found is  $\frac{1}{6} \times 1 + \frac{1}{6} \times 3 + \frac{1}{3} \times 4 + \frac{1}{3} \times 4 = \frac{10}{3} \equiv 332748121 \pmod{998244353}$ .

### Sample 2

| Input                           | Output |
|---------------------------------|--------|
| 2<br>1 1 1 1 1 1<br>2 2 2 2 2 2 | 2      |

The numbers written on the faces that come up on dice 1, 2 are always 1, 2, respectively, and their maximum value is always 2.

### Sample 3

| Input  | Output    |
|--|-----------|
| 8<br>55 76 80 21 34 28<br>82 84 2 32 56 17<br>11 57 37 28 39 18<br>47 2 97 25 75 29<br>72 45 22 75 26 81<br>6 79 16 68 68 40<br>31 80 68 57 18 55<br>49 10 63 91 93 40 | 213725517 |



## Problem H. Contraction

**Time Limit** 4000 ms

### Problem Statement

You are given an undirected graph  $G_0$  with  $N$  vertices and  $M$  edges. The vertices and edges of  $G_0$  are numbered as vertices  $1, 2, \dots, N$  and edges  $1, 2, \dots, M$ , respectively, and edge  $i$  ( $1 \leq i \leq M$ ) connects vertices  $U_i$  and  $V_i$ .

Takahashi has a graph  $G$  and  $N$  pieces numbered as pieces  $1, 2, \dots, N$ .

Initially,  $G = G_0$ , and piece  $i$  ( $1 \leq i \leq N$ ) is placed on vertex  $i$  of  $G$ .

He will now perform  $Q$  operations in order. The  $i$ -th operation ( $1 \leq i \leq Q$ ) gives an integer  $X_i$  between 1 and  $M$ , inclusive, and performs the following operation:

In  $G$ , if pieces  $U_{X_i}$  and  $V_{X_i}$  are placed on different vertices and there exists an edge  $e$  (on  $G$ ) between them, create a graph  $G'$  by contracting that edge. In this case, if self-loops are created, remove them, and if multi-edges exist, replace them with simple edges.

Then, all pieces that were placed on the two vertices connected by edge  $e$  in  $G$  are placed on the newly generated vertex by the contraction of  $e$  in  $G'$ . Pieces that were placed on other vertices in  $G$  are placed on the corresponding vertices in  $G'$ . Finally, set this resulting  $G'$  as the new  $G$ .

If pieces  $U_{X_i}$  and  $V_{X_i}$  are placed on the same vertex, or if the vertices they are placed on are not connected by an edge, do nothing.

For each of the operations  $i = 1, 2, \dots, Q$ , output the number of edges in  $G$  after the  $i$ -th operation.

► Edge Contraction

### Constraints

- $2 \leq N \leq 3 \times 10^5$
- $1 \leq M \leq 3 \times 10^5$
- $1 \leq U_i < V_i \leq N$
- $(U_i, V_i) \neq (U_j, V_j)$  if  $i \neq j$ .
- $1 \leq Q \leq 3 \times 10^5$

- $1 \leq X_i \leq M$
- All input values are integers.

Input

The input is given from Standard Input in the following format:

```
N M
U1 V1
U2 V2
⋮
UM VM
Q
X1 X2 ... XQ
```

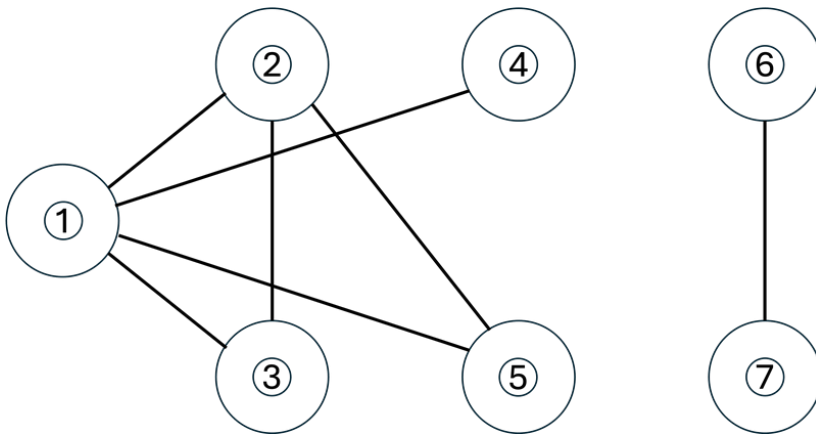
Output

Output  $Q$  lines. On the  $i$ -th line ( $1 \leq i \leq Q$ ), output the number of edges in  $G$  after the  $i$ -th operation.

Sample 1

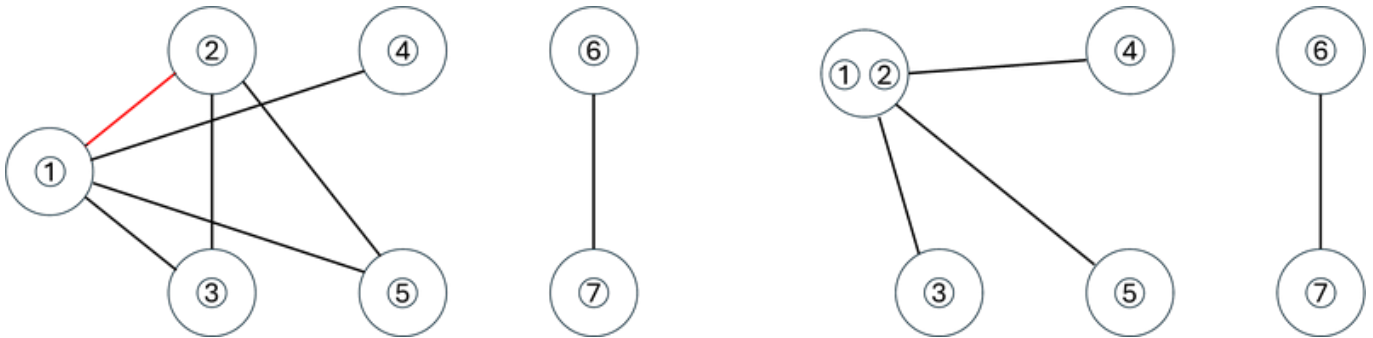
| Input     | Output |
|-----------|--------|
| 7 7       | 4      |
| 1 2       | 3      |
| 1 3       | 3      |
| 2 3       | 3      |
| 1 4       | 2      |
| 1 5       |        |
| 2 5       |        |
| 6 7       |        |
| 5         |        |
| 1 2 3 1 5 |        |

Initially,  $G$  is as shown in the figure below. The circled numbers represent pieces with those numbers.



In the 1st operation, we contract the edge between the vertices where pieces 1 and 2 are placed (left figure below).

After the operation,  $G$  becomes as shown in the right figure below, and in particular, the number of edges is 4. Note that self-loops have been removed and multi-edges have been replaced with simple edges.



In the 2nd operation, we contract the edge between the vertices where pieces 1 and 3 are placed.

After the operation,  $G$  becomes as shown in the left figure below, and the number of edges becomes 3.

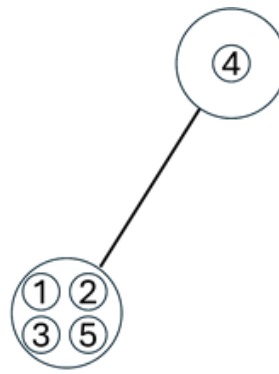
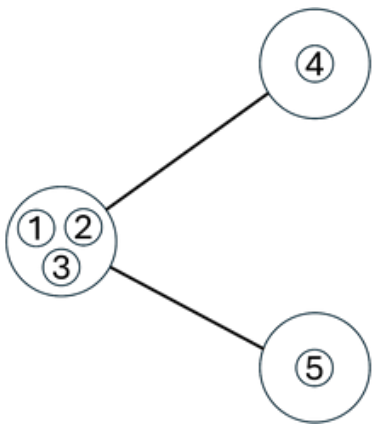
In the 3rd operation, since pieces 2 and 3 are placed on the same vertex,  $G$  remains unchanged, and the number of edges remains 3.

In the 4th operation as well, since pieces 1 and 2 are placed on the same vertex,  $G$  remains unchanged, and the number of edges remains 3.

In the 5th operation, we contract the edge between the vertices where pieces 1 and 5 are placed.

After the operation,  $G$  becomes as shown in the right figure below, and the number of edges becomes 2.

Thus, output 4, 3, 3, 3, 2 in this order, separated by newlines.



# Problem I. Count Cycles

**Time Limit** 6000 ms

## Problem Statement

There is an undirected graph  $G$  with  $N$  vertices and  $M$  edges.  $G$  does not contain self-loops, but may contain multi-edges. Vertices are numbered from 1 to  $N$ , and edges are numbered from 1 to  $M$ , with edge  $i$  connecting vertices  $U_i, V_i$ .

Find the number, modulo 998244353, of cycles contained in  $G$ .

More formally, find the number, modulo 998244353, of subsets  $\{e_1, e_2, \dots, e_k\} \subseteq \{1, 2, \dots, M\}$  ( $k \geq 2$ ) of the given edge set that satisfy the following condition.

- There exists a permutation  $(e'_1, e'_2, \dots, e'_k)$  of  $(e_1, e_2, \dots, e_k)$  and a vertex sequence  $(v_1, v_2, \dots, v_k)$  such that all of the following hold:
  - $v_1, v_2, \dots, v_k$  are pairwise distinct;
  - For all  $j$  ( $1 \leq j \leq k$ ), edge  $e'_j$  connects vertices  $v_j, v_{(j \bmod k)+1}$ .

## Constraints

- $2 \leq N \leq 20$
- $2 \leq M \leq 2 \times 10^5$
- $1 \leq U_i < V_i \leq N$
- All input values are integers.

## Input

The input is given from Standard Input in the following format:

```
N M
U1 V1
U2 V2
⋮
UM VM
```

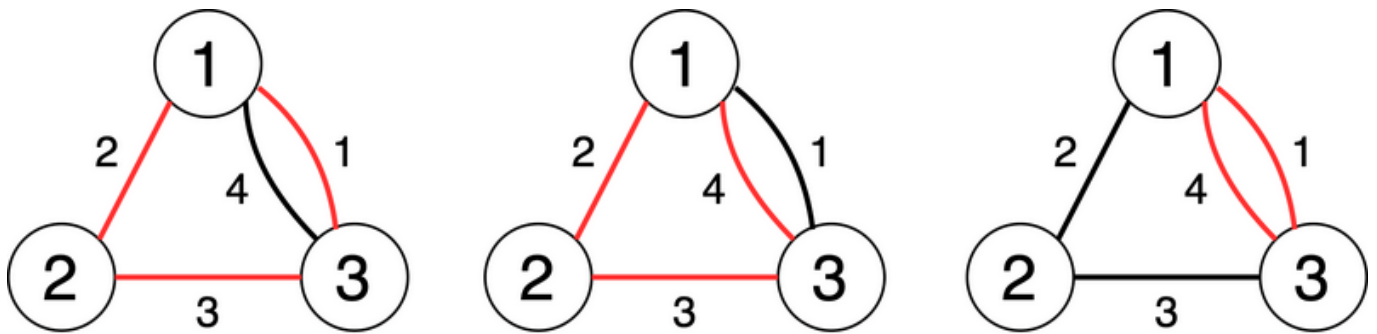
## Output

Output the answer.

### Sample 1

| Input                           | Output |
|---------------------------------|--------|
| 3 4<br>1 3<br>1 2<br>2 3<br>1 3 | 3      |

As shown in the figure below, there are a total of 3 cycles. The numbers inside the circles and the numbers next to the lines represent vertex numbers and edge numbers, respectively. Red lines represent edges included in cycles, and black lines represent the other edges.



From left to right, these correspond to choosing edge sets  $\{1, 2, 3\}$ ,  $\{2, 3, 4\}$ ,  $\{1, 4\}$ , respectively.

### Sample 2

| Input             | Output |
|-------------------|--------|
| 4 2<br>1 4<br>2 3 | 0      |

### Sample 3

| Input   | Output |
|---|--------|
| 5 15<br>1 5<br>3 4<br>2 3<br>2 4<br>3 5<br>4 5<br>2 5<br>2 3<br>1 3<br>4 5<br>2 5<br>4 5<br>1 2<br>3 4<br>1 5 | 166    |