
Computer Graphics

6 - Projection, Mesh 1

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Spring 2022

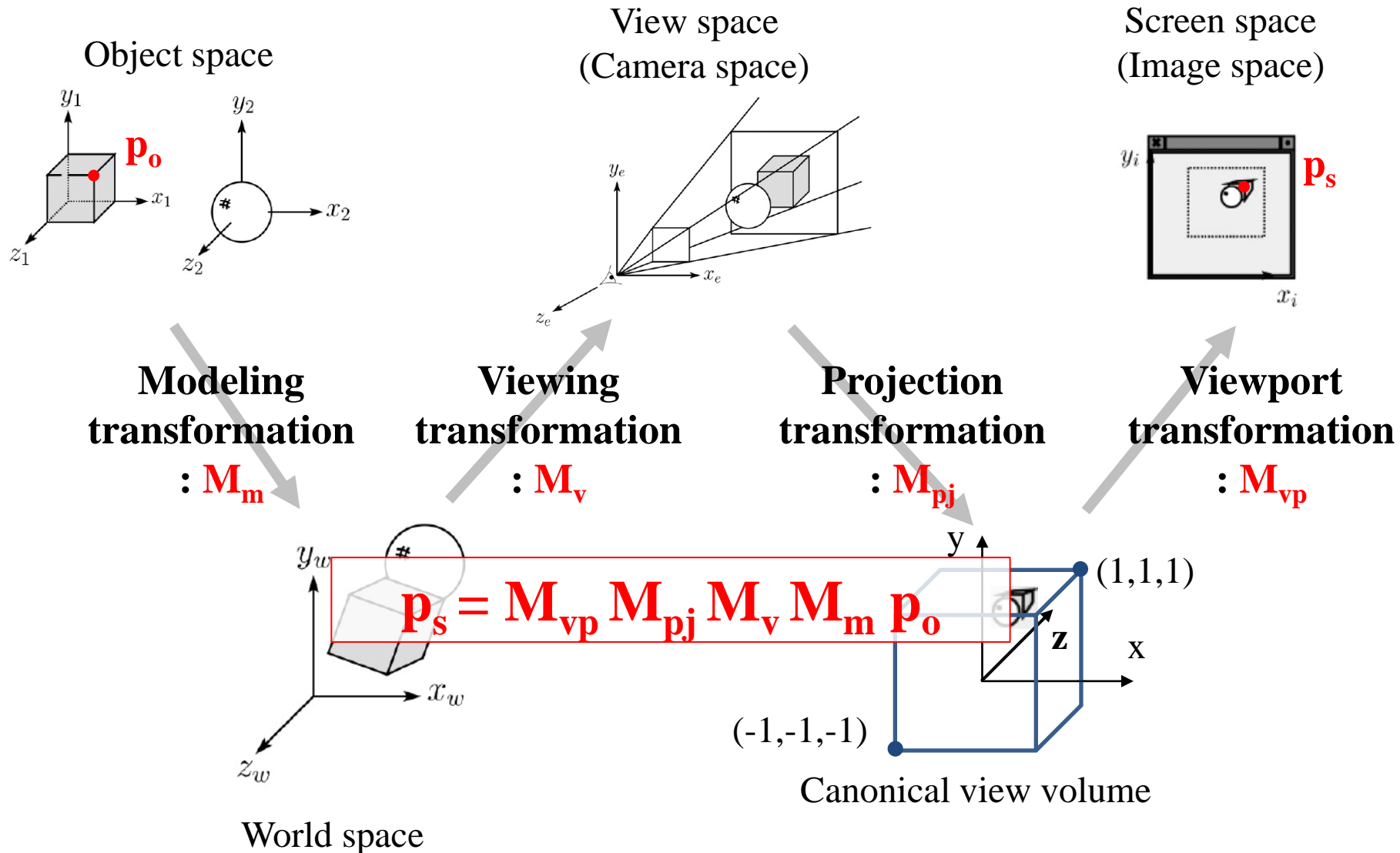
Midterm Exam Announcement

- Date & time: **Apr 27**, 09:30 - 10:30 am
- Place: IT.BT, 508
- Scope: Lecture 2 ~ 7
- **You cannot leave the room until the end of the exam** even if you finish the exam earlier.
- That means, **you cannot enter the room after 30 minutes** from the start of the exam (**do not be late, never too late!**).
- Please bring your student ID card to the exam.
- If you are unable to take the offline exam (stay abroad, corona confirmed, etc.), please contact the TA in advance.
 - Chaejun Sohn (손채준 조교), thscowns@gmail.com

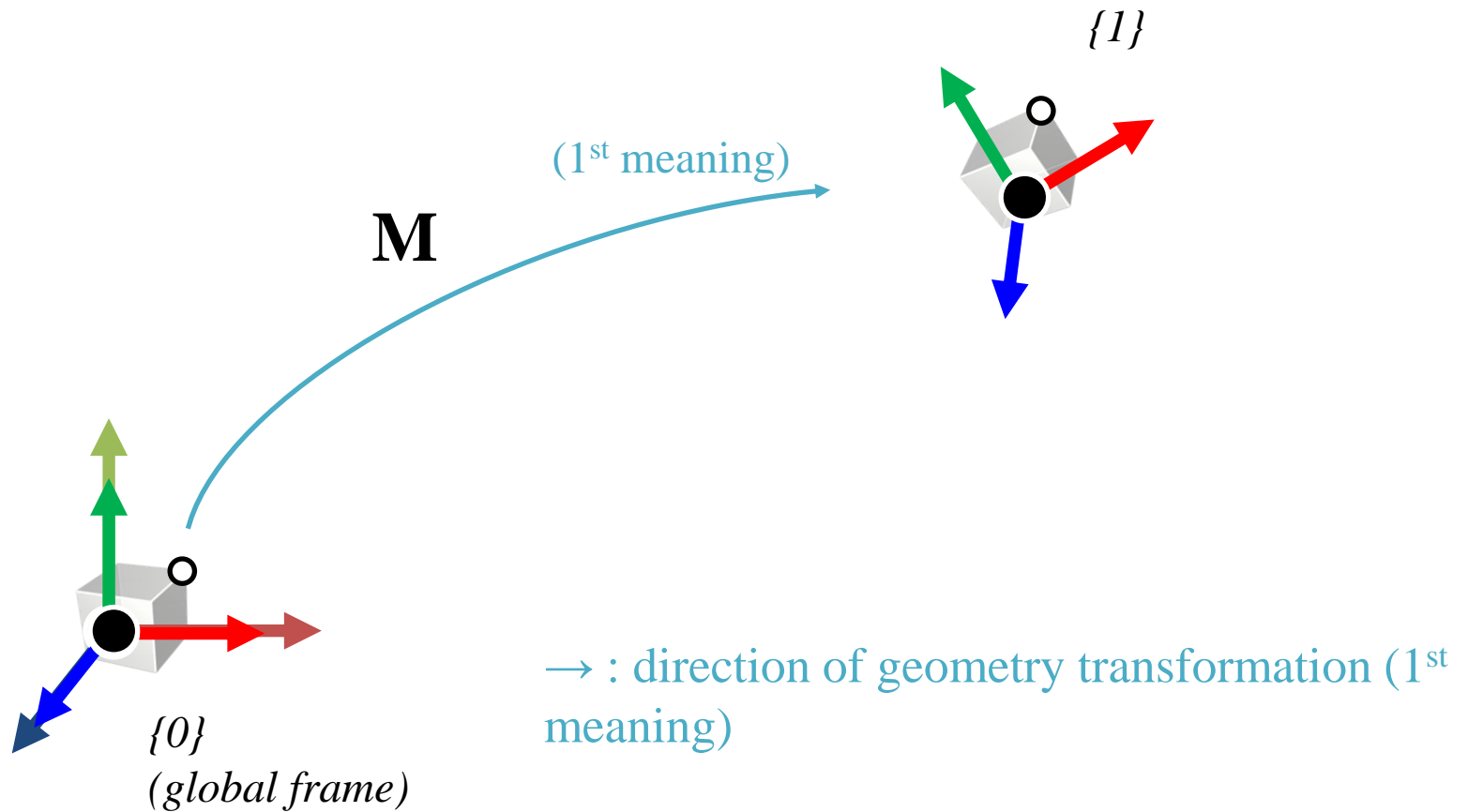
Questions from Last Lecture

- why the order of matrix is $MvpMpjMvMm$ which newer matrix locate left side?
- why vertex processing's multiple order is reversed?

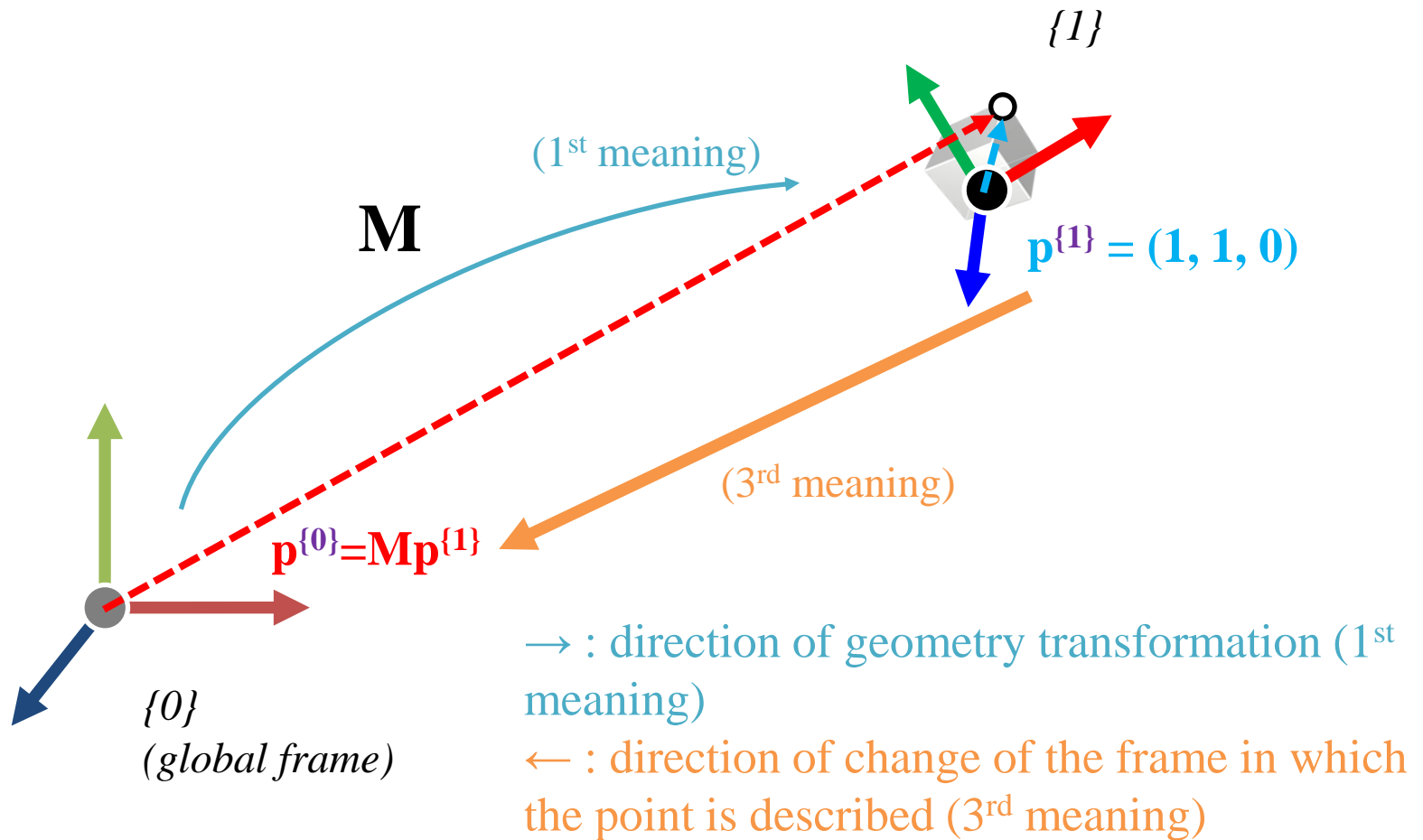
Vertex Processing (Transformation Pipeline)



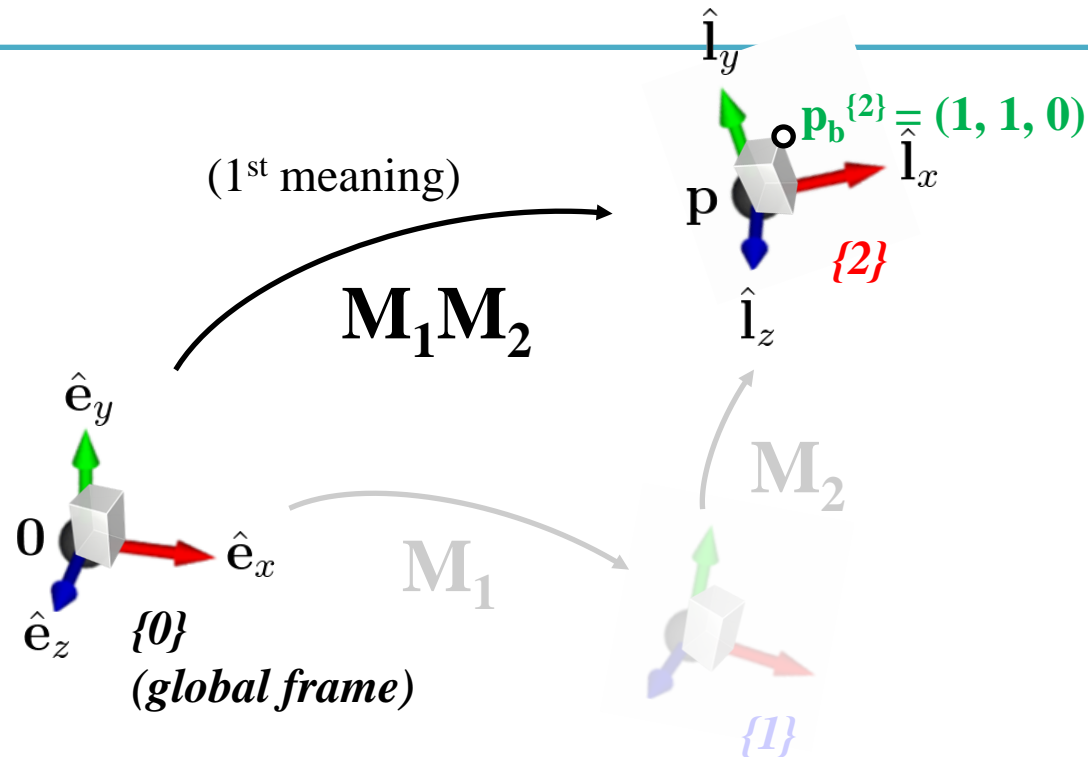
Directions of the "arrow"



Directions of the "arrow"

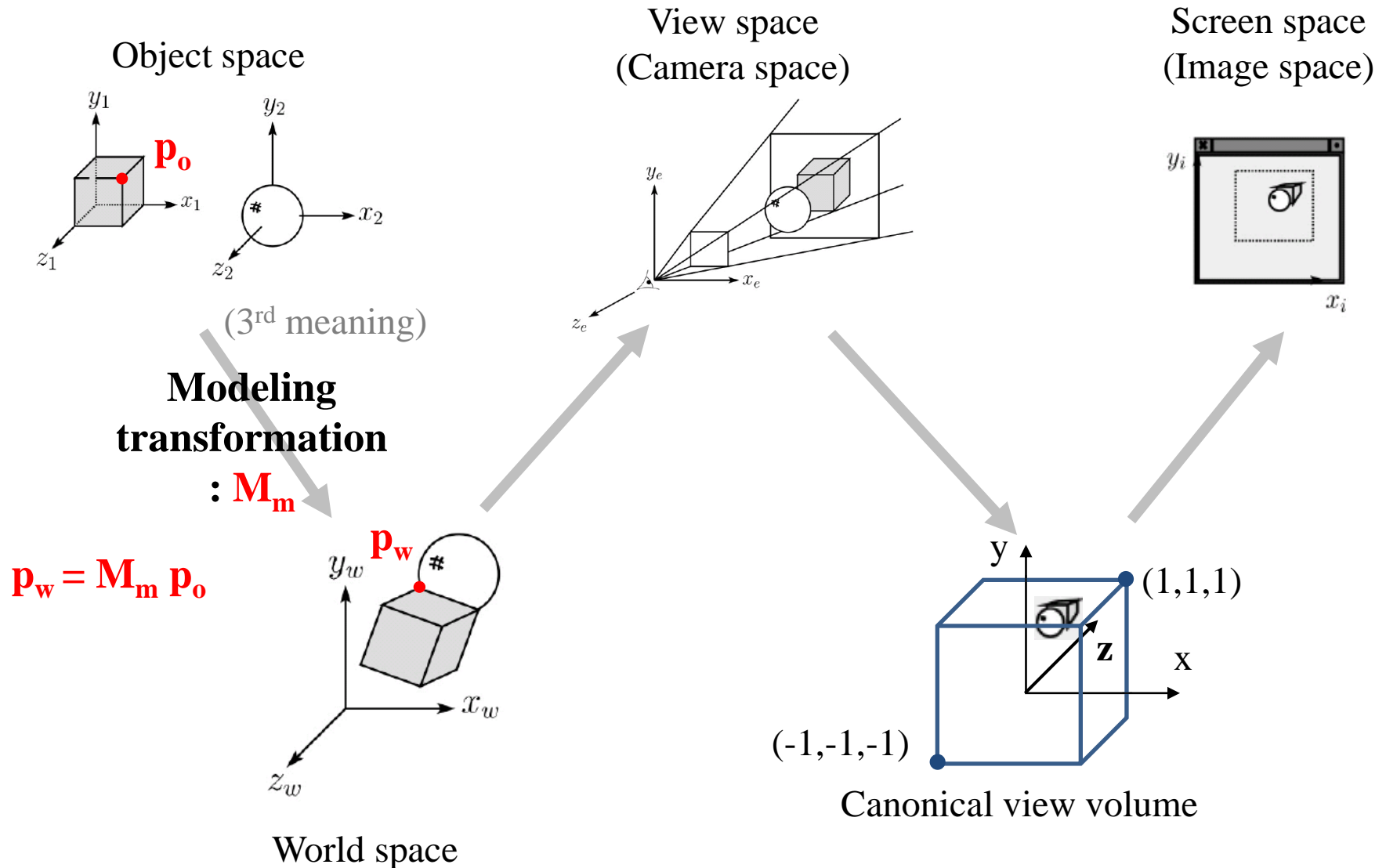


{0} to {2}

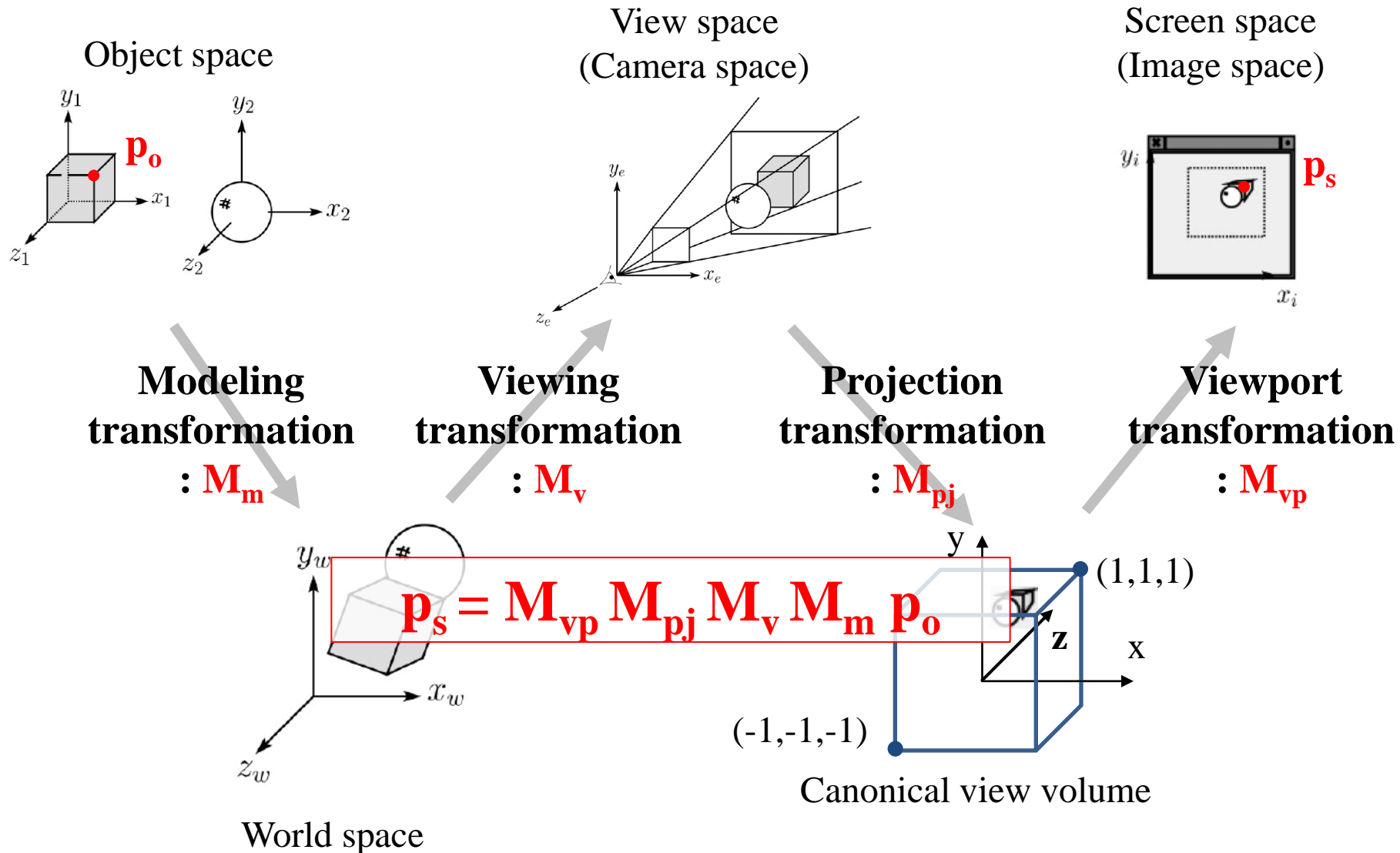


- 1) $M_1 M_2$ transforms a geometry (represented in {0}) w.r.t. {0}
- 2) $M_1 M_2$ defines an {2} w.r.t. {0}
- 3) $M_1 M_2$ transforms a point represented in {2} to the same point but represented in {0}
 - $p_b^{\{1\}} = M_2 p_b^{\{2\}}$, $p_b^{\{0\}} = M_1 p_b^{\{1\}} = M_1 M_2 p_b^{\{2\}}$

Modeling Transformation



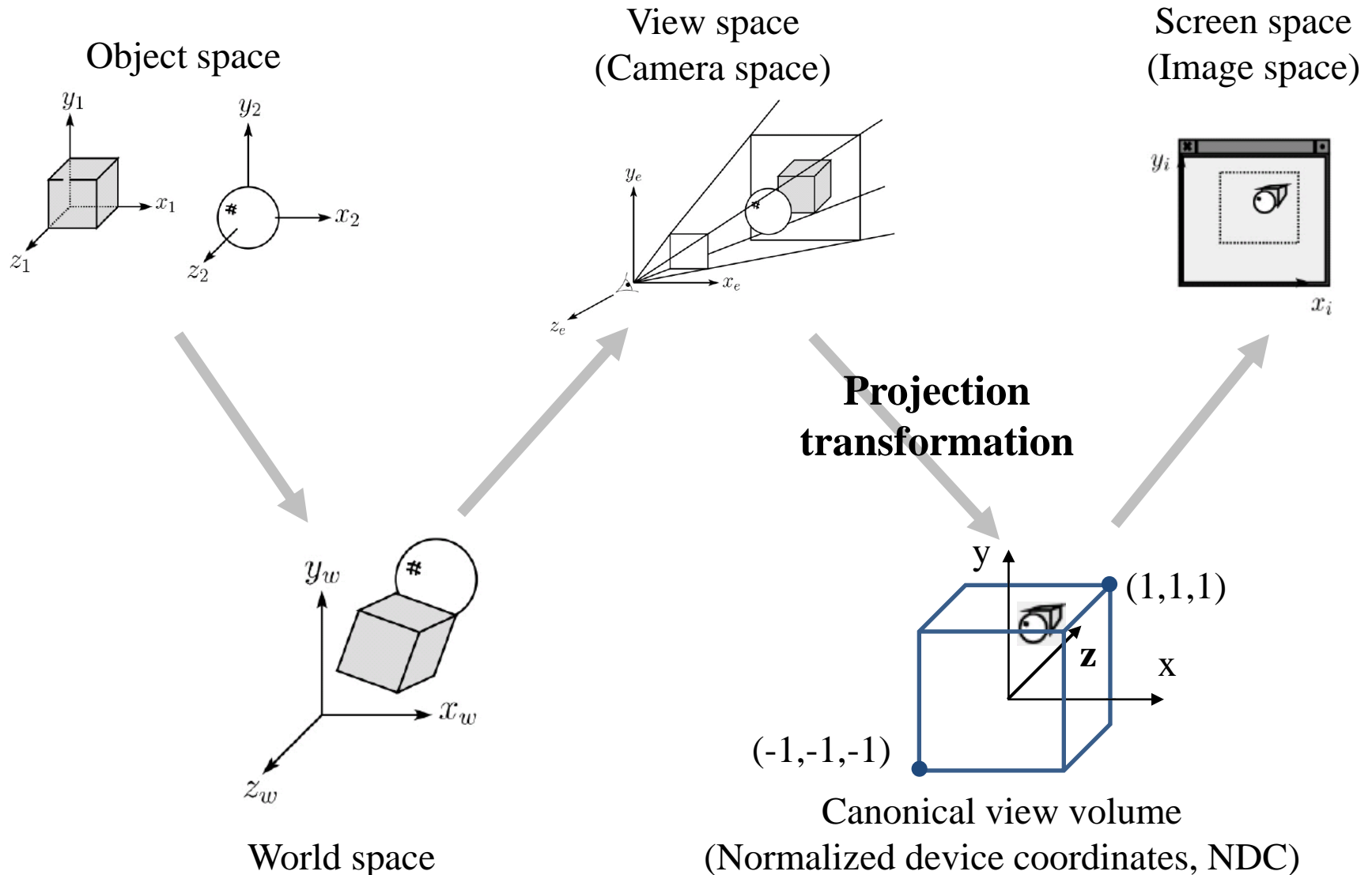
Vertex Processing (Transformation Pipeline)



Topics Covered

- Projection Transformation
 - Orthographic (Orthogonal) Projection
 - Perspective Projection
- Viewport Transformation
- Mesh
 - Polygon mesh & triangle mesh
 - Representations for triangle meshes - Seperate triangle
 - OpenGL vertex array

Projection Transformation

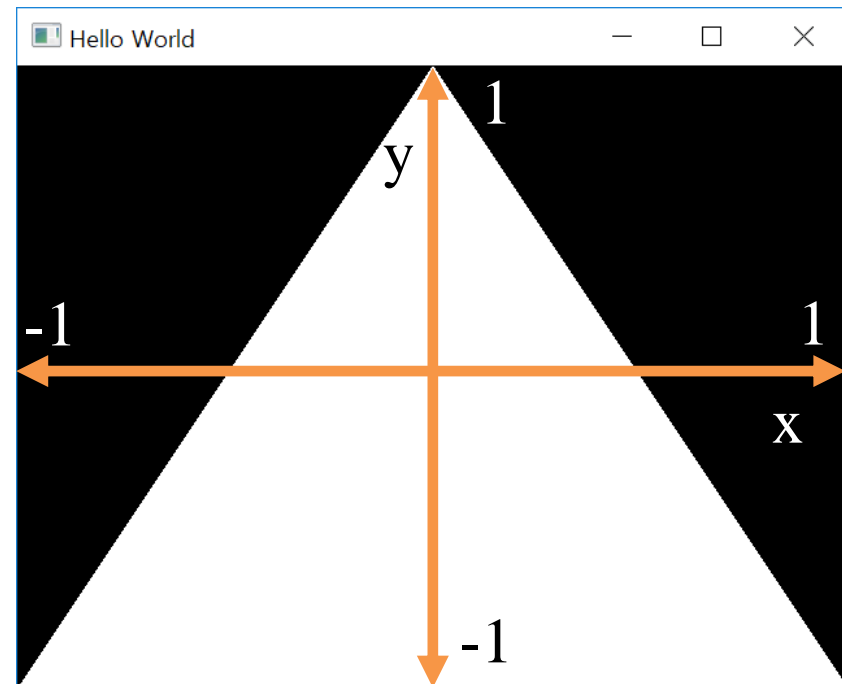


Recall that...

- 1. Placing objects
→ **Modeling transformation**
- 2. Placing the “camera”
→ **Viewing transformation (covered in the last class)**
- 3. Selecting a “lens”
→ **Projection transformation**
- 4. Displaying on a “cinema screen”
→ **Viewport transformation**

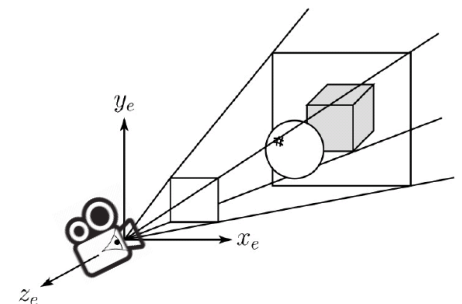
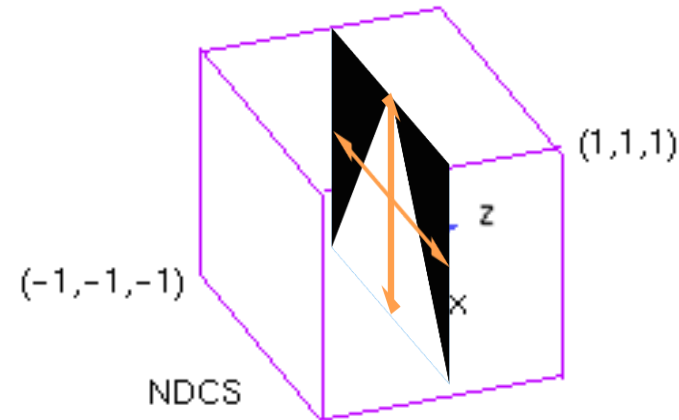
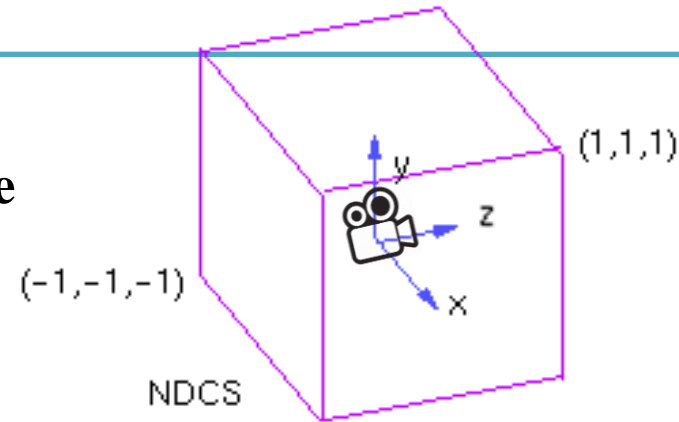
Review: Normalized Device Coordinates

- Remember that you could draw the triangle anywhere in a 2D square ranging from $[-1, -1]$ to $[1, 1]$.
- This coordinate system is called **normalized device coordinates (NDC)**.
- And the space expressed with NDC is called **canonical view volume**.



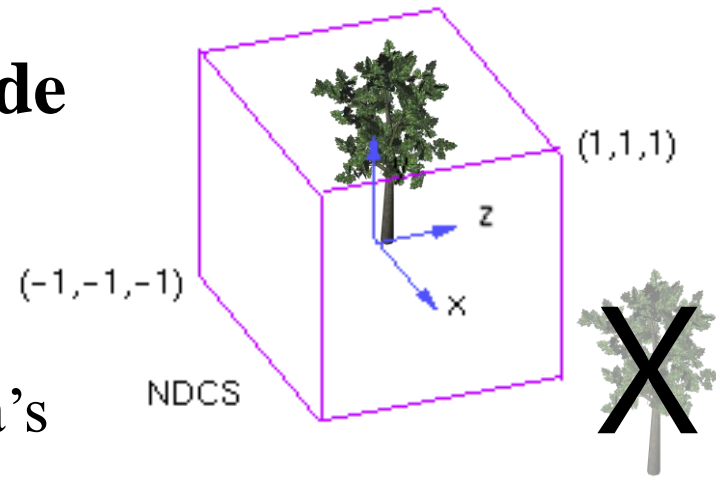
Canonical View “Volume”

- Actually, a canonical view volume is a **3D cube** ranging from $[-1,-1,-1]$ to $[1,1,1]$ in OpenGL.
 - Its coordinate system is NDC.
- Its **xy** plane is a 2D “viewport”.
- Note that NDC in OpenGL is a left-handed coordinate system.
 - Viewing direction in NDC : +z direction
- But OpenGL’s projection functions change the hand-ness – Thus view, world, model spaces use right-handed coordinate system.
 - Viewing direction in view space : -z direction



Canonical View Volume

- OpenGL only draws objects **inside** the canonical view volume
 - To draw objects only in the camera's view
 - Not to draw objects too near or too far from the camera



Do we always have to use the cube of size 2 as a view volume?

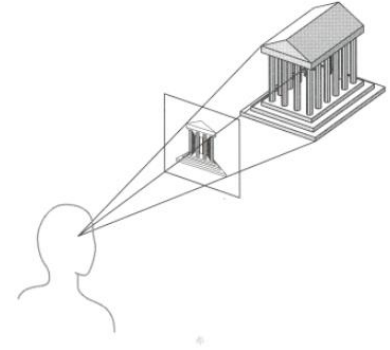
- No. You can set up a view volume of any size and draw objects in it.
 - Even you can use “frustums” as well as cuboids.
- Then everything in the visible volume is mapped (projected) into the canonical view volume.
- Then 3D points in the canonical view volume are projected onto its xy plane as 2D points.
- → **Projection transformation**

Projection in General

- General definition:
- Mapping points in a n -dim space to a m -dim space ($m < n$).

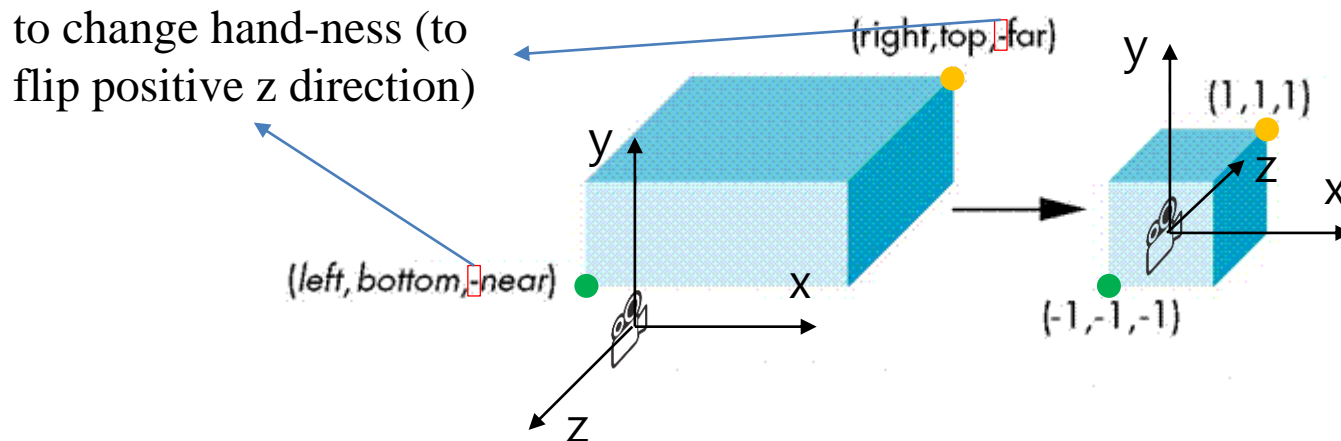
Projection in Computer Graphics

- Mapping 3D coordinates to 2D screen coordinates.
- Two stages:
 - Map an arbitrary view volume to a canonical view volume
 - ~~Map 3D points in the canonical view volume onto its xy plane : But we still need z values of points for *depth test*, so do not consider this second stage~~
- Two common projection methods:
 - Orthographic projection
 - Perspective projection



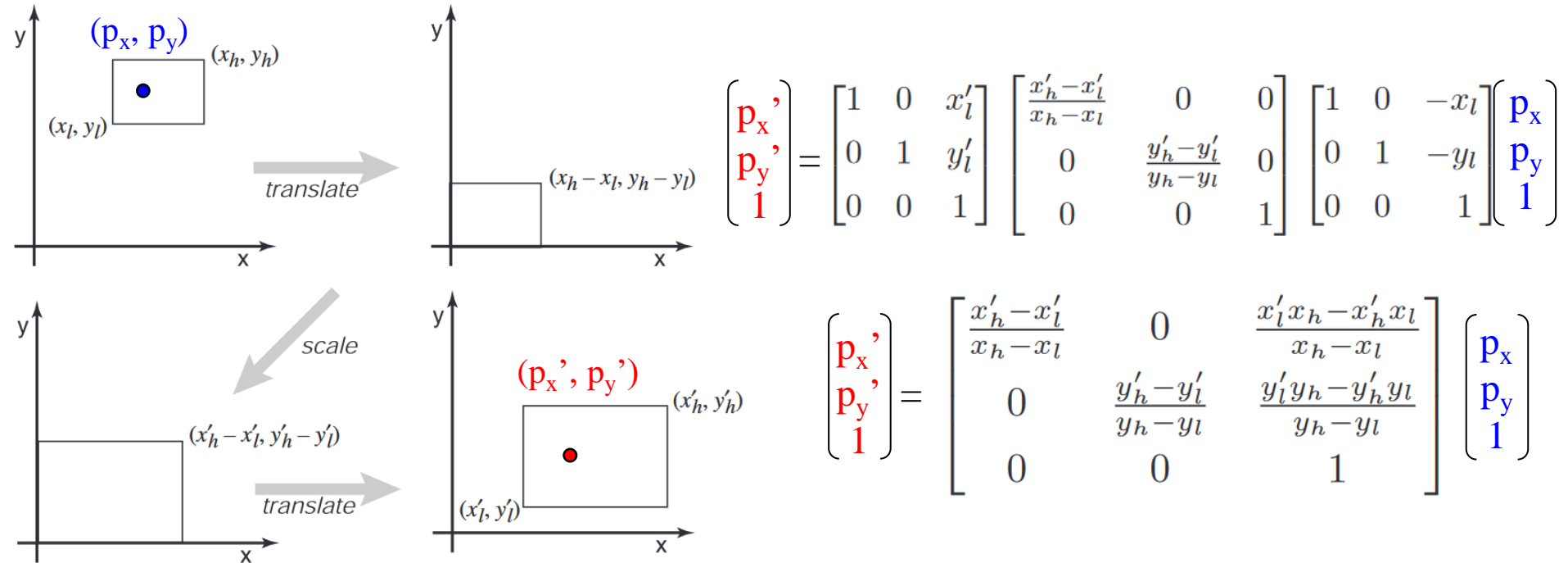
Orthographic (Orthogonal) Projection

- View volume : Cuboid (직육면체)
- Orthographic projection : Mapping from a cuboid view volume to a canonical view volume
 - Combination of scaling & translation
 - “Windowing” transformation



Windowing Transformation

- Transformation that maps a point (p_x, p_y) in a rectangular space from (x_l, y_l) to (x_h, y_h) to a point (p'_x, p'_y) in a rectangular space from (x'_l, y'_l) to (x'_h, y'_h)

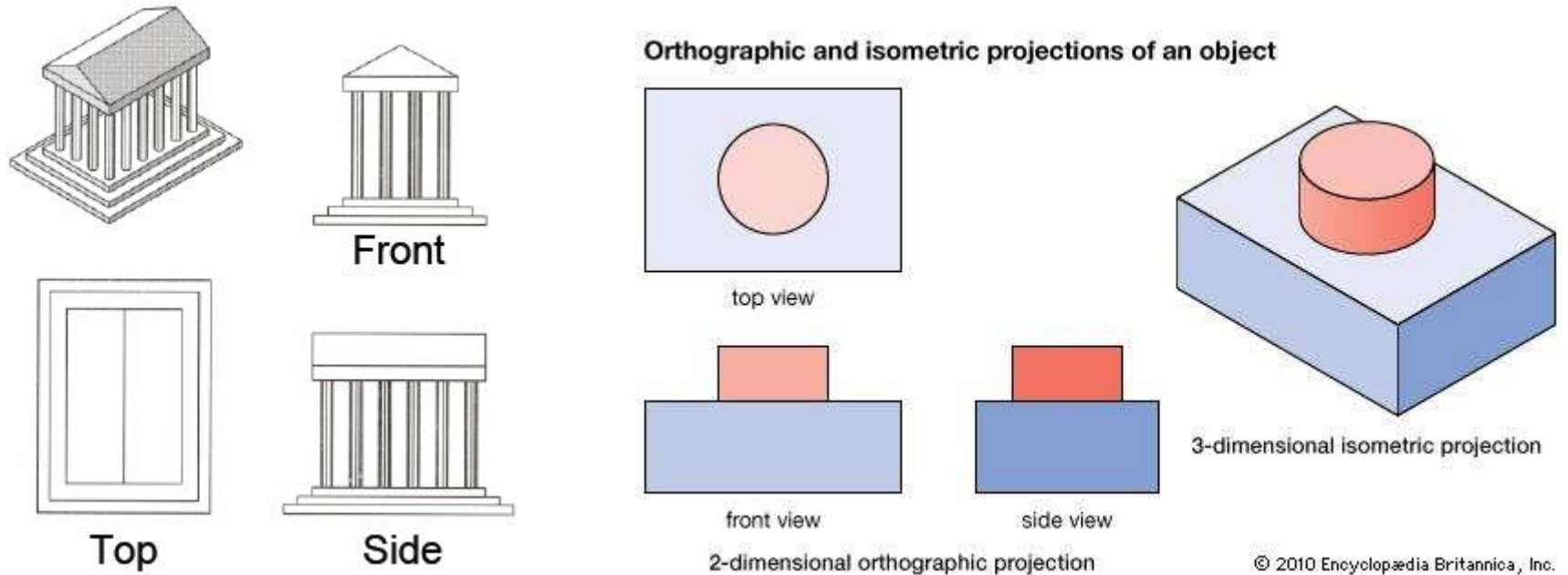


Orthographic Projection Matrix

- By extending the matrix to 3D and substituting
 - $x_h = \text{right}$, $x_l = \text{left}$, $x_h' = 1$, $x_l' = -1$
 - $y_h = \text{top}$, $y_l = \text{bottom}$, $y_h' = 1$, $y_l' = -1$
 - $z_h = -\text{far}$, $z_l = -\text{near}$, $z_h' = 1$, $z_l' = -1$

$$M_{\text{orth}} = \begin{bmatrix} \frac{2}{\text{right} - \text{left}} & 0 & 0 & -\frac{\text{right} + \text{left}}{\text{right} - \text{left}} \\ 0 & \frac{2}{\text{top} - \text{bottom}} & 0 & -\frac{\text{top} + \text{bottom}}{\text{top} - \text{bottom}} \\ 0 & 0 & \frac{-2}{\text{far} - \text{near}} & -\frac{\text{far} + \text{near}}{\text{far} - \text{near}} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

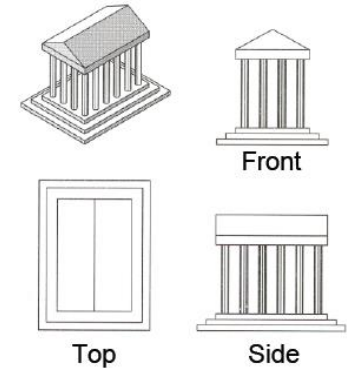
Examples of Orthographic Projection



An object always stay the same size, no matter its distance from the viewer.

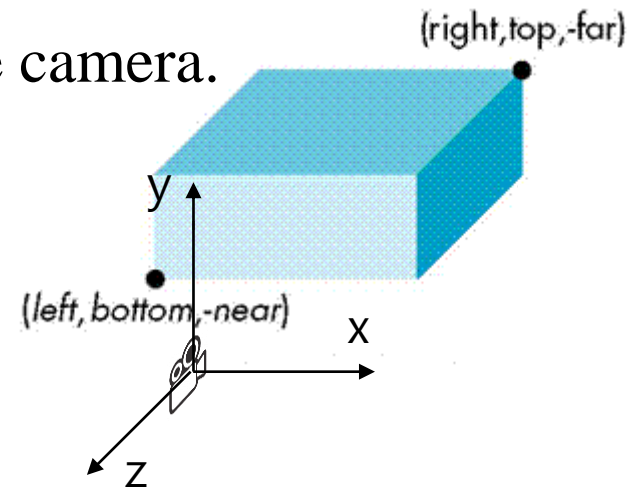
Properties of Orthographic Projection

- Not realistic looking
- Good for exact measurement
- Most often used in CAD, architectural drawings, etc. where taking exact measurement is important.
- Affine transformation
 - parallel lines remain parallel
 - ratios are preserved
 - angles are not preserved



glOrtho()

- `glOrtho(left, right, bottom, top, zNear, zFar)`
- : Creates an orthographic projection matrix and right-multiplies the current transformation matrix by it
- Sign of `zNear`, `zFar`:
 - positive value: the plane is in front of the camera
 - negative value: the plane is behind the camera.
- $C \leftarrow CM_{\text{orth}}$



[Practice] glOrtho

```
import glfw
from OpenGL.GL import *
from OpenGL.GLU import *
import numpy as np

gCamAng = 0.
gCamHeight = 1.

# draw a cube of side 1, centered at the origin.
def drawUnitCube():
    glBegin(GL_QUADS)
    glVertex3f( 0.5, 0.5,-0.5)
    glVertex3f(-0.5, 0.5,-0.5)
    glVertex3f(-0.5, 0.5, 0.5)
    glVertex3f( 0.5, 0.5, 0.5)

    glVertex3f( 0.5,-0.5, 0.5)
    glVertex3f(-0.5,-0.5, 0.5)
    glVertex3f(-0.5,-0.5,-0.5)
    glVertex3f( 0.5,-0.5,-0.5)

    glVertex3f( 0.5, 0.5, 0.5)
    glVertex3f(-0.5, 0.5, 0.5)
    glVertex3f(-0.5,-0.5, 0.5)
    glVertex3f( 0.5,-0.5, 0.5)

    glVertex3f( 0.5,-0.5,-0.5)
    glVertex3f(-0.5,-0.5,-0.5)
    glVertex3f(-0.5, 0.5,-0.5)
    glVertex3f( 0.5, 0.5,-0.5)
```

```
glVertex3f(-0.5, 0.5, 0.5)
glVertex3f(-0.5, 0.5,-0.5)
glVertex3f(-0.5,-0.5,-0.5)
glVertex3f(-0.5,-0.5, 0.5)
```

```
glVertex3f( 0.5, 0.5,-0.5)
glVertex3f( 0.5, 0.5, 0.5)
glVertex3f( 0.5,-0.5, 0.5)
glVertex3f( 0.5,-0.5,-0.5)
glEnd()
```

```
def drawCubeArray():
    for i in range(5):
        for j in range(5):
            for k in range(5):
                glPushMatrix()
                glTranslatef(i,j,-k-1)
                glScalef(.5,.5,.5)
                drawUnitCube()
                glPopMatrix()
```

```
def drawFrame():
    glBegin(GL_LINES)
    glColor3ub(255, 0, 0)
    glVertex3fv(np.array([0.,0.,0.]))
    glVertex3fv(np.array([1.,0.,0.]))
    glColor3ub(0, 255, 0)
    glVertex3fv(np.array([0.,0.,0.]))
    glVertex3fv(np.array([0.,1.,0.]))
    glColor3ub(0, 0, 255)
    glVertex3fv(np.array([0.,0.,0]))
    glVertex3fv(np.array([0.,0.,1.]))
    glEnd()
```

```

def render():
    global gCamAng, gCamHeight

    glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT)
    glEnable(GL_DEPTH_TEST)

    # draw polygons only with boundary edges
    glPolygonMode( GL_FRONT_AND_BACK, GL_LINE )

    glLoadIdentity()

    # test other parameter values
    # near plane: 10 units behind the camera
    # far plane: 10 units in front of
the camera
    glOrtho(-5,5, -5,5, -10,10)

    gluLookAt(1*np.sin(gCamAng),gCamHeight,1*np.cos(
gCamAng), 0,0,0, 0,1,0)

    drawFrame()
    glColor3ub(255, 255, 255)

    drawUnitCube()

    # test
    # drawCubeArray()

```

```

def key_callback(window, key, scancode, action,
mods):
    global gCamAng, gCamHeight
    if action==glfw.PRESS or
action==glfw.REPEAT:
        if key==glfw.KEY_1:
            gCamAng += np.radians(-10)
        elif key==glfw.KEY_3:
            gCamAng += np.radians(10)
        elif key==glfw.KEY_2:
            gCamHeight += .1
        elif key==glfw.KEY_W:
            gCamHeight += -.1

def main():
    if not glfw.init():
        return

    window =
glfw.create_window(640,640,'glOrtho()',
None,None)
    if not window:
        glfw.terminate()
        return

    glfw.make_context_current(window)
    glfw.set_key_callback(window, key_callback)

    while not glfw.window_should_close(window):
        glfw.poll_events()
        render()
        glfw.swap_buffers(window)

    glfw.terminate()

if __name__ == "__main__":
    main()

```

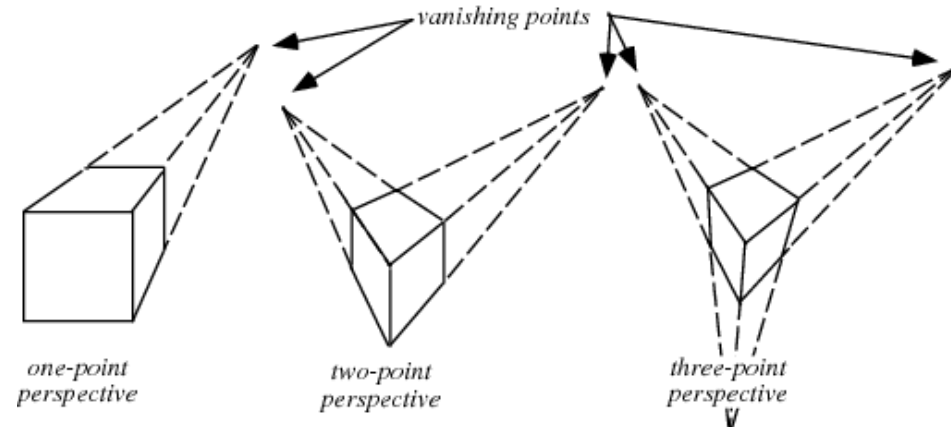
Quiz #1

- Go to <https://www.slido.com/>
- Join #cg-ys
- Click “Polls”
- Submit your answer in the following format:
 - **Student ID: Your answer**
 - e.g. **2017123456: 4)**
- Note that you must submit all quiz answers in the above format to be checked for “attendance”.

Perspective Effects

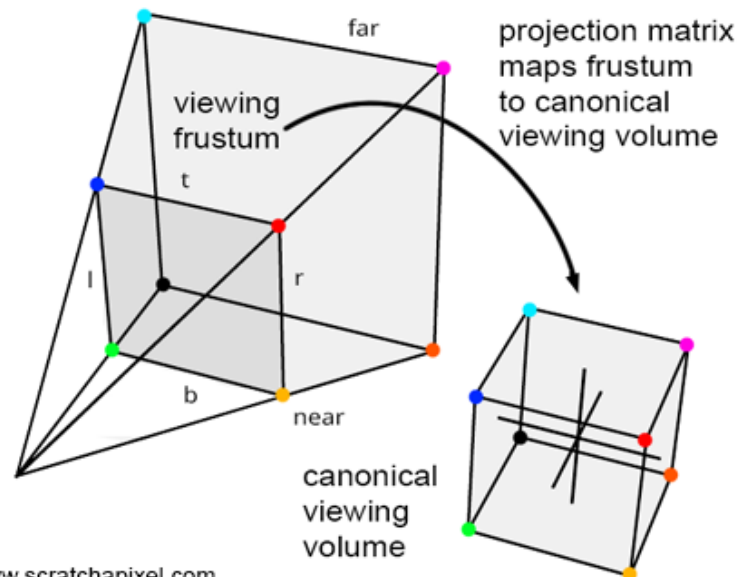
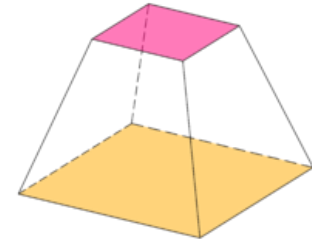
- Distant objects become small.

Vanishing point: The point or points to which the extensions of parallel lines appear to converge in a perspective drawing



Perspective Projection

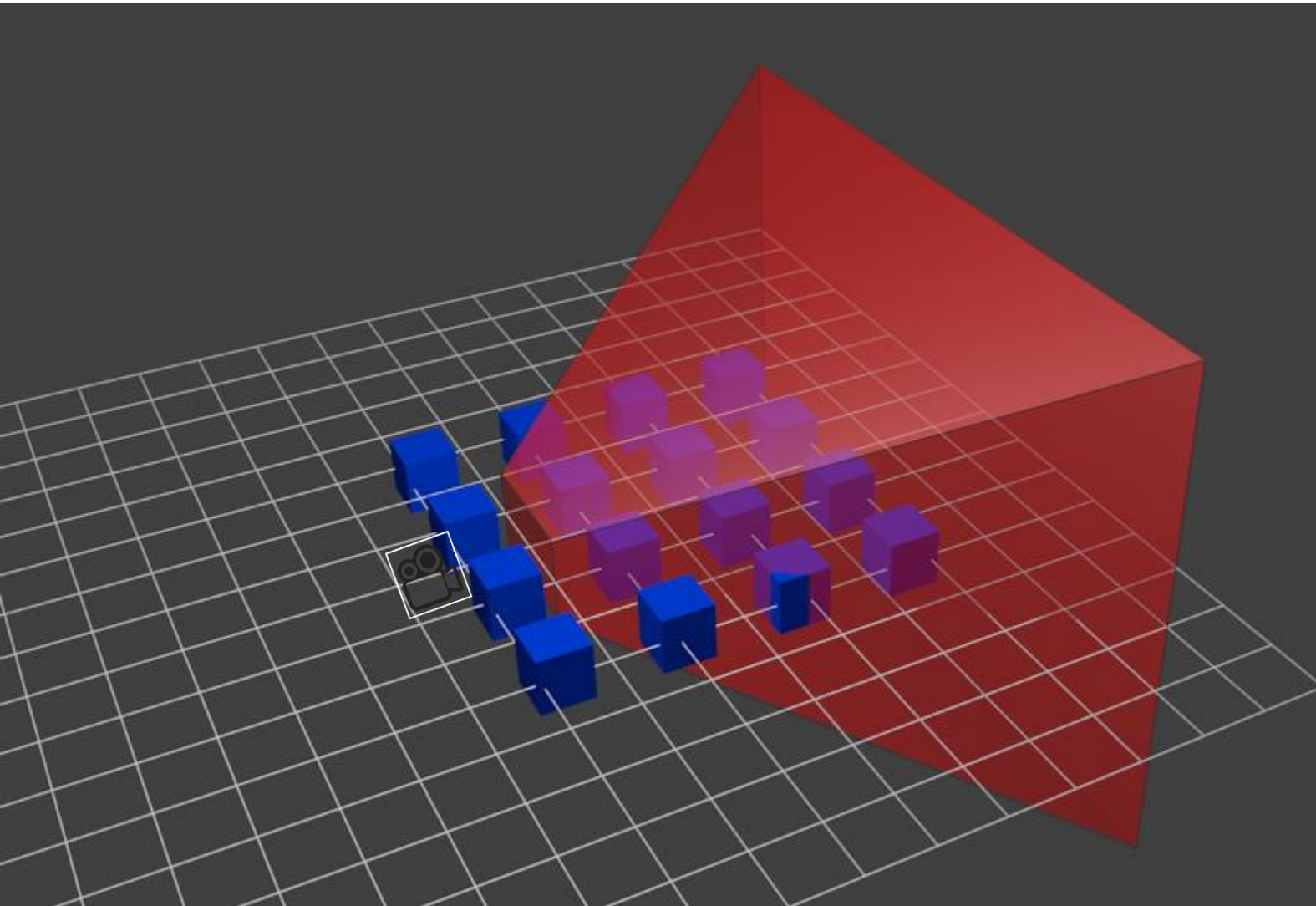
- View volume : Frustum (절두체)
- → “Viewing frustum”
- Perspective projection : Mapping from a viewing frustum to a canonical view volume



Why does this mapping generate a perspective effect?

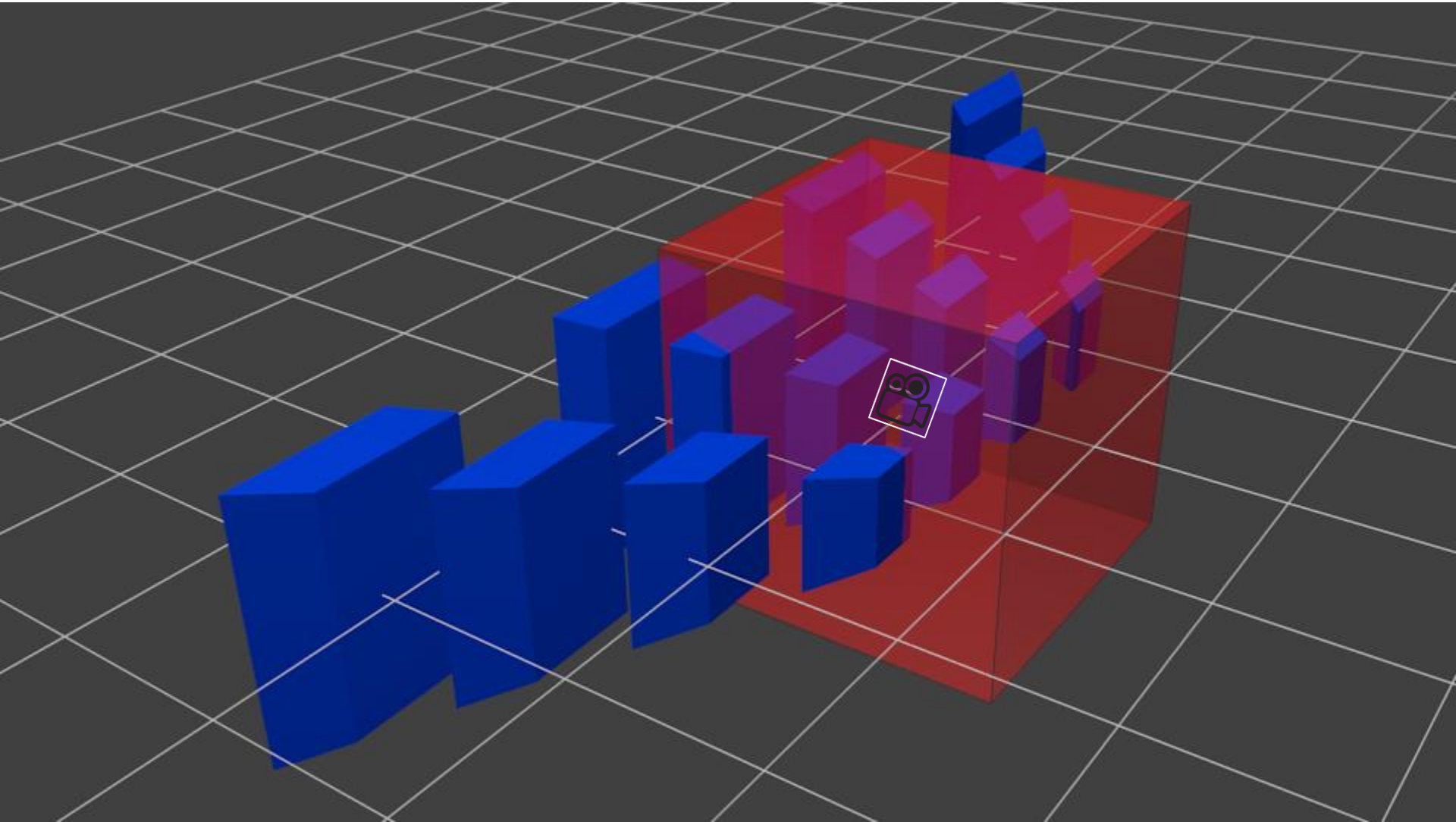
Original 3D scene

Red: viewing frustum, Blue: objects

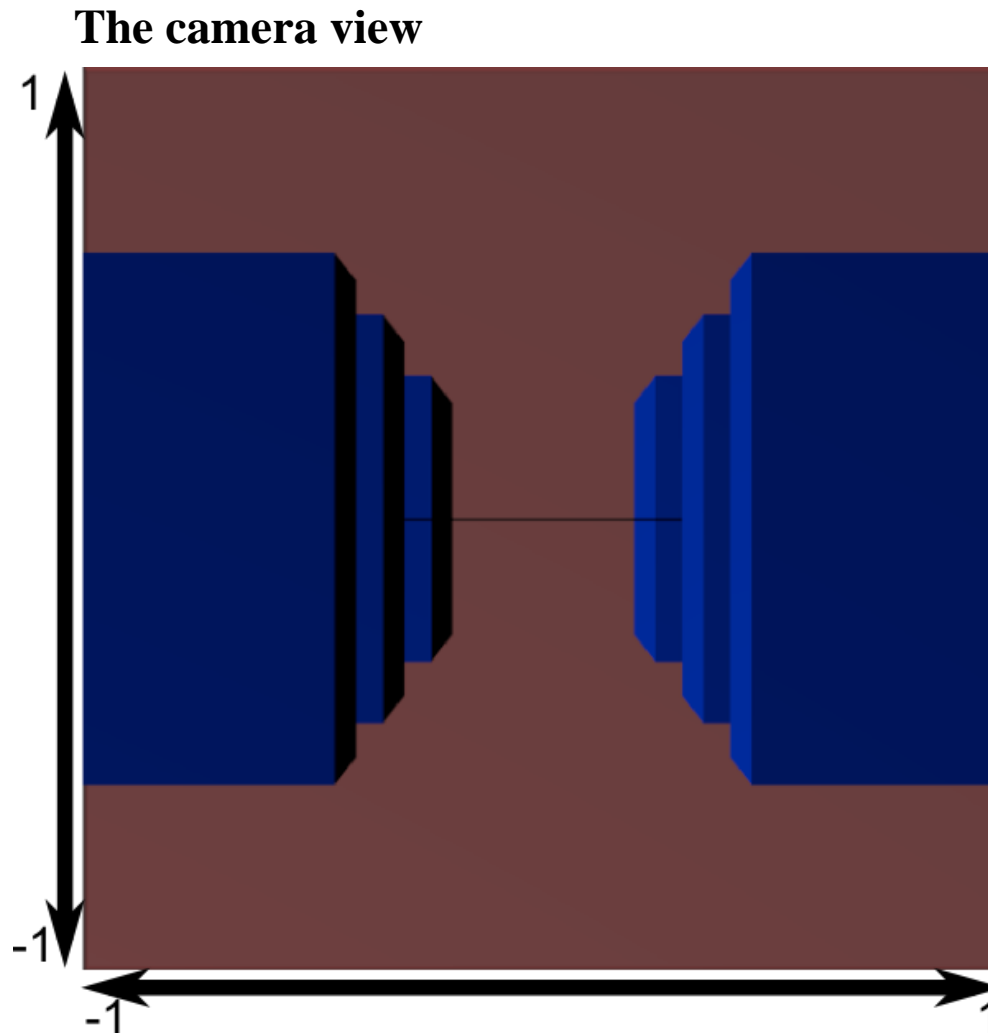


An Example of Perspective Projection

After perspective projection

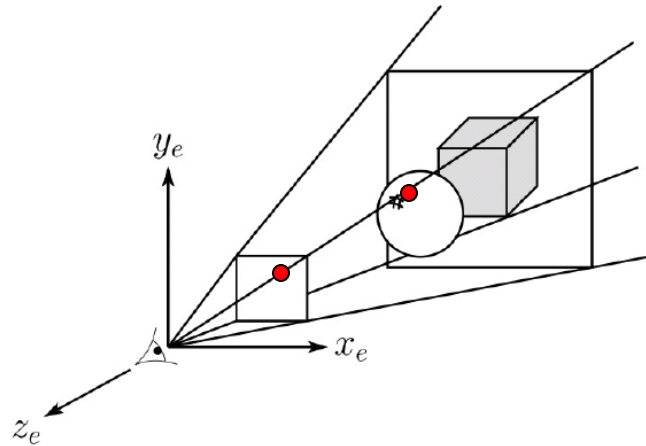


An Example of Perspective Projection



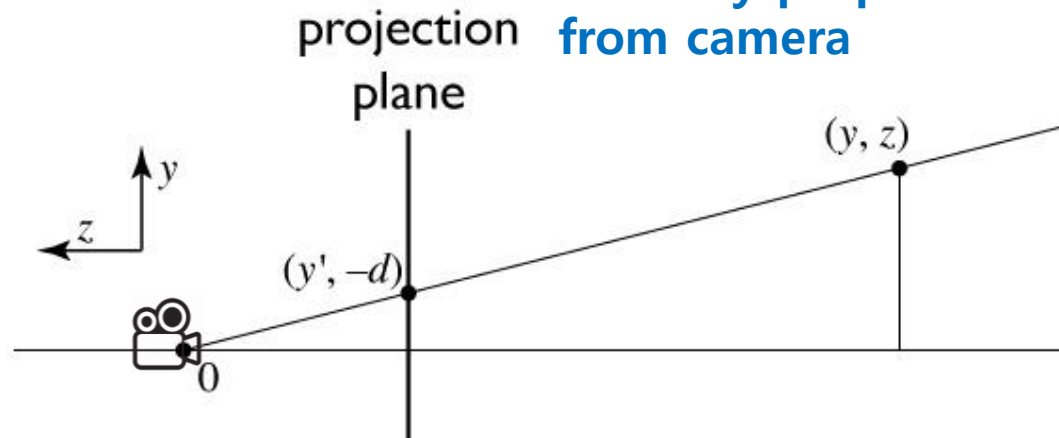
Let's first consider 3D View Frustum→2D Projection Plane

- Consider the projection of a 3D point on the camera plane



Perspective projection

The size of an object on the screen is inversely proportional to its distance from camera



similar triangles:

$$\frac{y'}{d} = \frac{y}{-z}$$

$$y' = -dy/z$$

Homogeneous coordinates revisited

- Perspective requires division
 - that is **not** part of affine transformations
 - in affine, parallel lines stay parallel
 - therefore not vanishing point
 - therefore no rays converging on viewpoint
- “True” purpose of homogeneous coords: projection

Homogeneous coordinates revisited

- Introduced $w = 1$ coordinate as a placeholder

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} \rightarrow \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

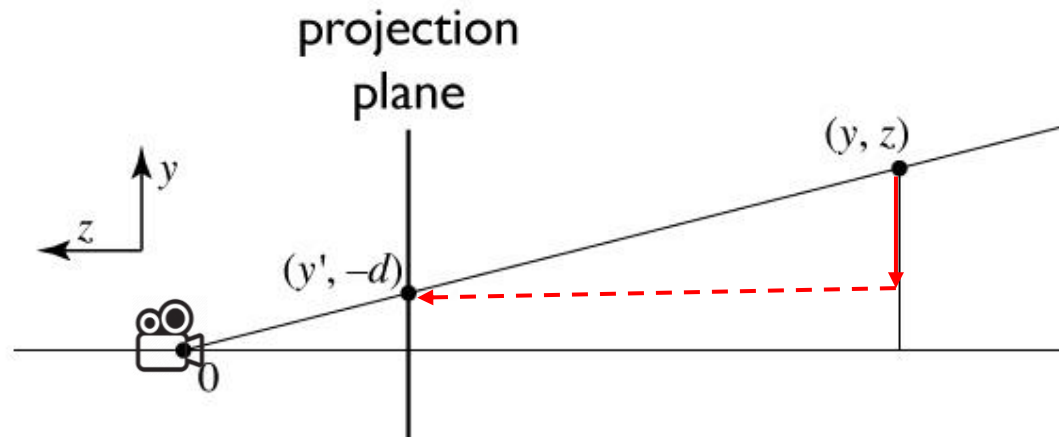
- used as a convenience for unifying translation with linear transformation

- Can also allow arbitrary w

$$\begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \sim \begin{bmatrix} wx \\ wy \\ wz \\ w \end{bmatrix}$$

All scalar multiples of a 4-vector are equivalent

Perspective projection



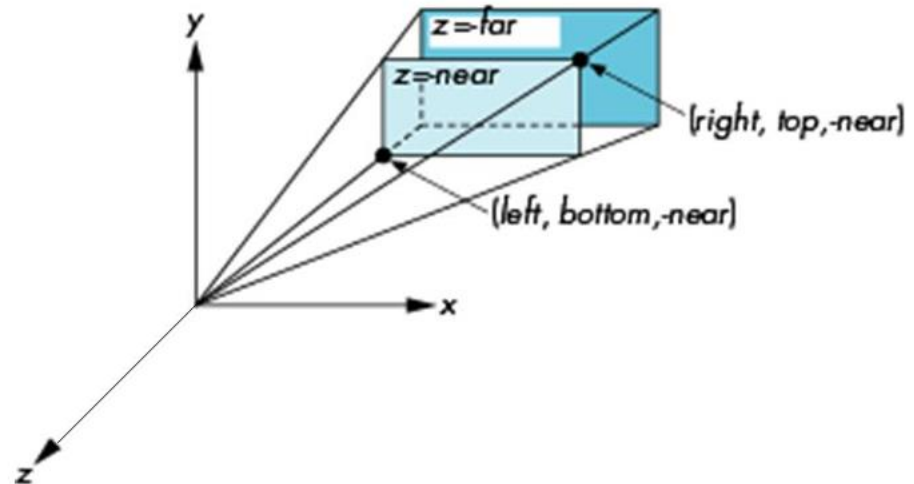
to implement perspective, just move z to w :

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} -dx/z \\ -dy/z \\ 1 \end{bmatrix} \sim \begin{bmatrix} dx \\ dy \\ -z \end{bmatrix} = \begin{bmatrix} d & 0 & 0 & 0 \\ 0 & d & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

Perspective Projection Matrix

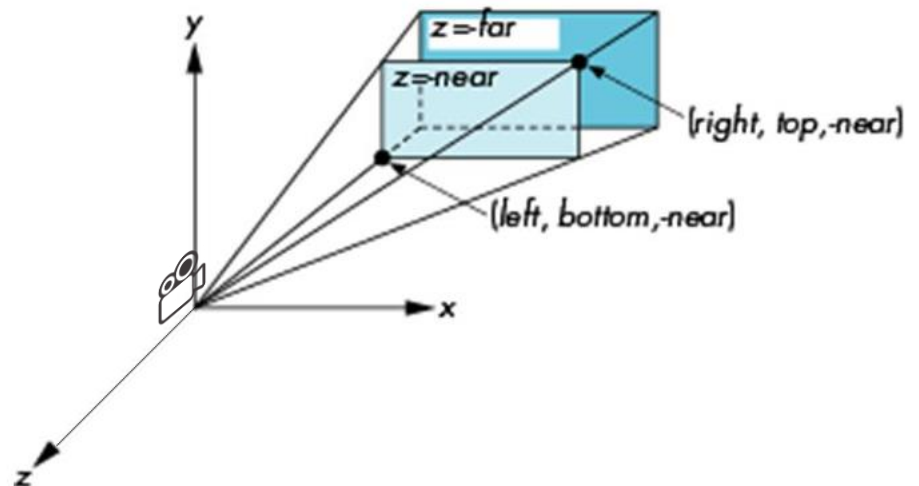
- This 3D \rightarrow 2D projection example gives the basic idea of perspective projection.
- What we really have to do is 3D \rightarrow 3D, View Frustum \rightarrow Canonical View Volume.
- For details for this process, see 6 - *reference-projection.pdf*

- $$M_{\text{pers}} = \begin{pmatrix} \frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\ 0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\ 0 & 0 & \frac{-(f+n)}{f-n} & \frac{-2fn}{f-n} \\ 0 & 0 & -1 & 0 \end{pmatrix}$$



glFrustum()

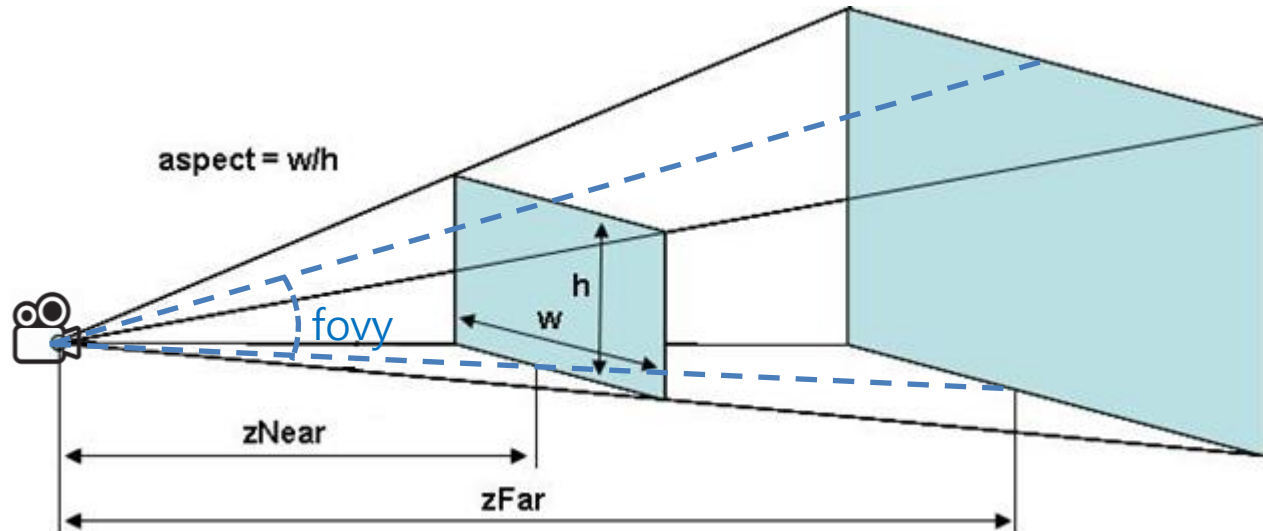
- `glFrustum(left, right, bottom, top, near, far)`
 - Note that left, right, bottom, top are those of "near" plane.
- : Creates a perspective projection matrix and right-multiplies the current transformation matrix by it
- Sign of near, far:
 - The values for both parameters **must be positive**.



- $C \leftarrow CM_{pers}$

gluPerspective()

- `gluPerspective(fovy, aspect, zNear, zFar)`
 - `fovy`: The field of view angle, in degrees, in the y-direction.
 - `aspect`: The aspect ratio that determines the field of view in the x-direction. The aspect ratio is the ratio of x (width) to y (height).
- : Creates a perspective projection matrix and right-multiplies the current transformation matrix by it
- $C \leftarrow CM_{\text{pers}}$



[Practice] glFrustum(), gluPerspective()

```
import glfw
from OpenGL.GL import *
from OpenGL.GLU import *
import numpy as np

gCamAng = 0.
gCamHeight = 1.

# draw a cube of side 1, centered at the origin.
def drawUnitCube():
    glBegin(GL_QUADS)
    glVertex3f( 0.5, 0.5,-0.5)
    glVertex3f(-0.5, 0.5,-0.5)
    glVertex3f(-0.5, 0.5, 0.5)
    glVertex3f( 0.5, 0.5, 0.5)

    glVertex3f( 0.5,-0.5, 0.5)
    glVertex3f(-0.5,-0.5, 0.5)
    glVertex3f(-0.5,-0.5,-0.5)
    glVertex3f( 0.5,-0.5,-0.5)

    glVertex3f( 0.5, 0.5, 0.5)
    glVertex3f(-0.5, 0.5, 0.5)
    glVertex3f(-0.5,-0.5, 0.5)
    glVertex3f( 0.5,-0.5, 0.5)

    glVertex3f( 0.5,-0.5,-0.5)
    glVertex3f(-0.5,-0.5,-0.5)
    glVertex3f(-0.5, 0.5,-0.5)
    glVertex3f( 0.5, 0.5,-0.5)
```

```
glVertex3f(-0.5, 0.5, 0.5)
glVertex3f(-0.5, 0.5,-0.5)
glVertex3f(-0.5,-0.5,-0.5)
glVertex3f(-0.5,-0.5, 0.5)
```

```
glVertex3f( 0.5, 0.5,-0.5)
glVertex3f( 0.5, 0.5, 0.5)
glVertex3f( 0.5,-0.5, 0.5)
glVertex3f( 0.5,-0.5,-0.5)
glEnd()
```

```
def drawCubeArray():
    for i in range(5):
        for j in range(5):
            for k in range(5):
                glPushMatrix()
                glTranslatef(i,j,-k-1)
                glScalef(.5,.5,.5)
                drawUnitCube()
                glPopMatrix()
```

```
def drawFrame():
    glBegin(GL_LINES)
    glColor3ub(255, 0, 0)
    glVertex3fv(np.array([0.,0.,0.]))
    glVertex3fv(np.array([1.,0.,0.]))
    glColor3ub(0, 255, 0)
    glVertex3fv(np.array([0.,0.,0.]))
    glVertex3fv(np.array([0.,1.,0.]))
    glColor3ub(0, 0, 255)
    glVertex3fv(np.array([0.,0.,0]))
    glVertex3fv(np.array([0.,0.,1.]))
    glEnd()
```

```

def render():
    global gCamAng, gCamHeight

    glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT)
    glEnable(GL_DEPTH_TEST)
    glPolygonMode( GL_FRONT_AND_BACK, GL_LINE )

    glLoadIdentity()

    # test other parameter values
    glFrustum(-1,1, -1,1, .1,10)
    # glFrustum(-1,1, -1,1, 1,10)

    # test other parameter values
    # gluPerspective(45, 1, 1,10)

    # test with this line
    gluLookAt(5*np.sin(gCamAng),gCamHeight,5*np.cos(
gCamAng), 0,0,0, 0,1,0)

    drawFrame()
    glColor3ub(255, 255, 255)

    drawUnitCube()

    # test
    # drawCubeArray()

```

```

def key_callback(window, key, scancode, action,
mods):
    global gCamAng, gCamHeight
    if action==glfw.PRESS or
action==glfw.REPEAT:
        if key==glfw.KEY_1:
            gCamAng += np.radians(-10)
        elif key==glfw.KEY_3:
            gCamAng += np.radians(10)
        elif key==glfw.KEY_2:
            gCamHeight += .1
        elif key==glfw.KEY_W:
            gCamHeight += -.1

def main():
    if not glfw.init():
        return

    window =
glfw.create_window(640,640,'glFrustum()',
None,None)
    if not window:
        glfw.terminate()
        return

    glfw.make_context_current(window)
    glfw.set_key_callback(window, key_callback)

    while not glfw.window_should_close(window):
        glfw.poll_events()
        render()
        glfw.swap_buffers(window)

    glfw.terminate()

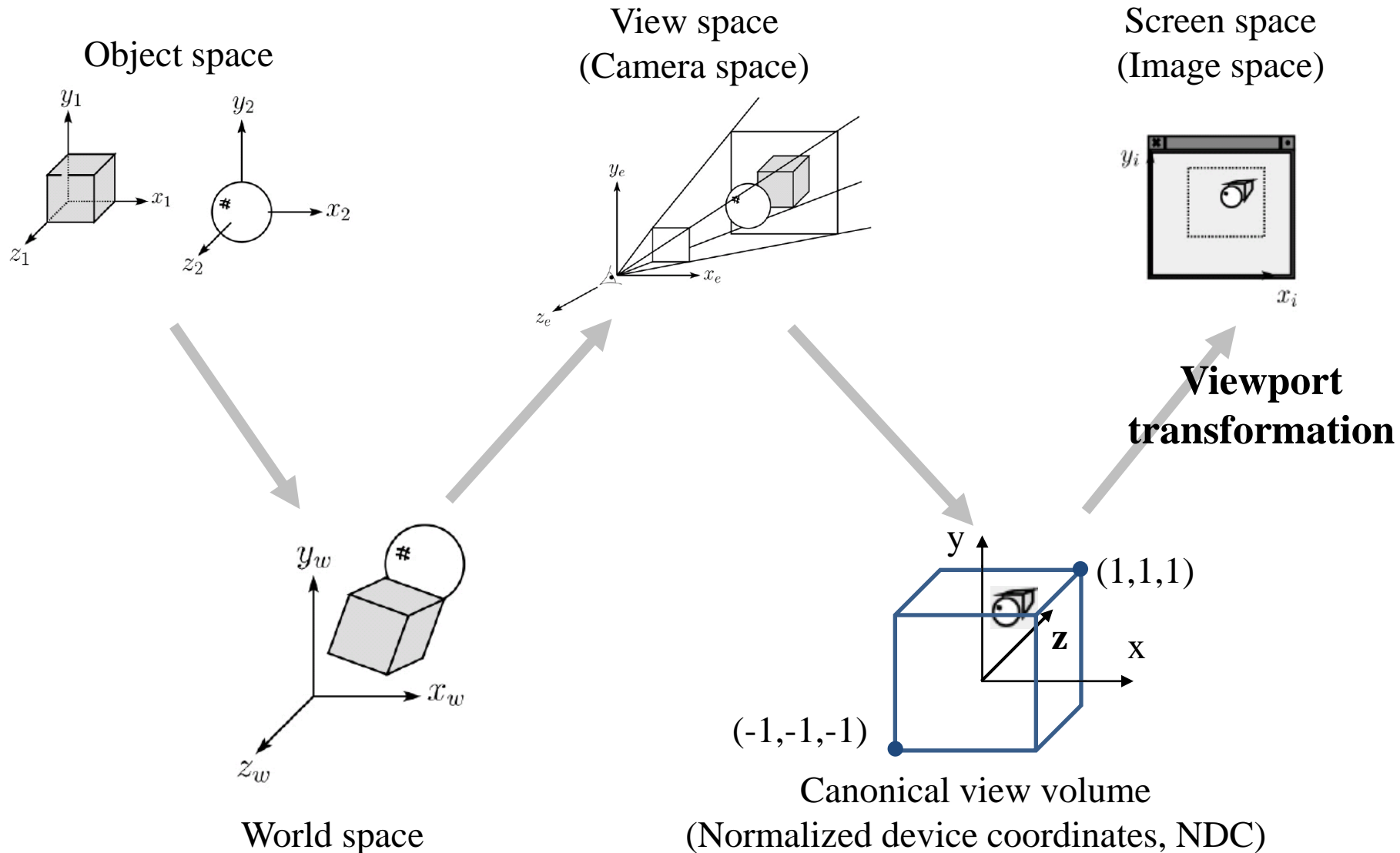
if __name__ == "__main__":
    main()

```

Quiz #2

- Go to <https://www.slido.com/>
- Join #cg-ys
- Click “Polls”
- Submit your answer in the following format:
 - **Student ID: Your answer**
 - e.g. **2017123456: 4)**
- Note that you must submit all quiz answers in the above format to be checked for “attendance”.

Viewport Transformation

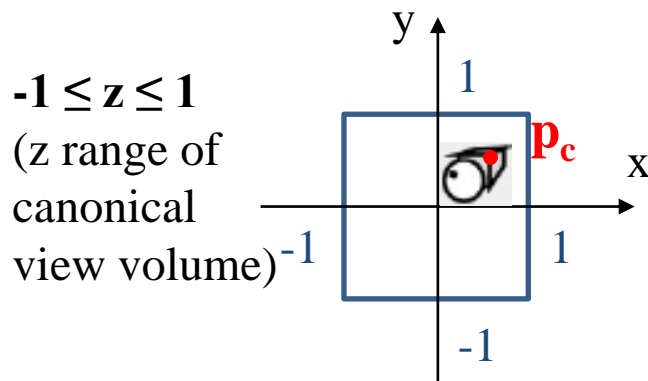


Recall that...

- 1. Placing objects
→ **Modeling transformation**
- 2. Placing the “camera”
→ **Viewing transformation**
- 3. Selecting a “lens”
→ **Projection transformation**
- 4. Displaying on a “cinema screen”
→ **Viewport transformation**

Viewport Transformation

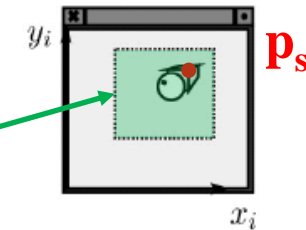
Canonical view volume
(looking down +z direction)



Viewport transformation

: M_{vp}

Screen space
(Image space)



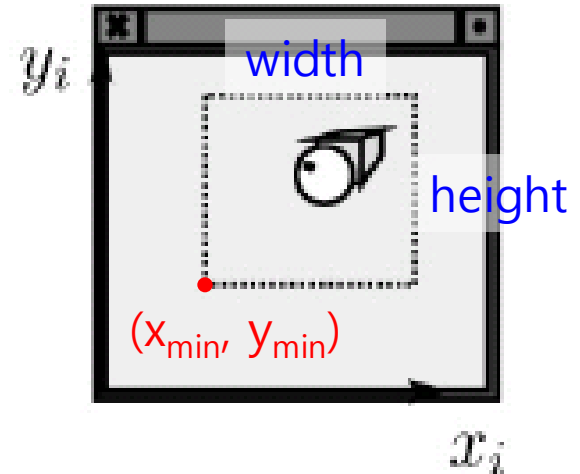
$0 \leq z \leq 1$
(default depth buffer range)

- Viewport: a rectangular viewing region of screen
- So, viewport transformation is also a kind of windowing transformation.

Viewport Transformation Matrix

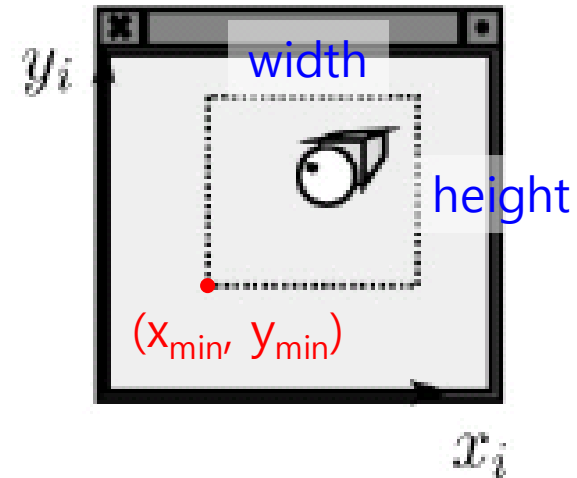
- In the windowing transformation matrix,
- By substituting x_h , x_l , x_h' , ... with corresponding variables in viewport transformation,

$$M_{vp} = \begin{bmatrix} \frac{width}{2} & 0 & 0 & \frac{width}{2} + x_{min} \\ 0 & \frac{height}{2} & 0 & \frac{height}{2} + y_{min} \\ 0 & 0 & \frac{1}{2} & \frac{1}{2} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



glViewport()

- `glViewport(xmin, ymin, width, height)`
 - `xmin, ymin, width, height`: specified **in pixels**
- `:` Sets the viewport
 - This function does NOT explicitly multiply a viewport matrix with the current matrix.
 - Viewport transformation is internally done in OpenGL, so you can apply transformation matrices **starting from a canonical view volume**, not a screen space.
- Default viewport setting for (`xmin, ymin, width, height`) is **(0, 0, window width, window height)**.
 - If you do not call `glViewport()`, OpenGL uses this default viewport setting.



[Practice] glViewport()

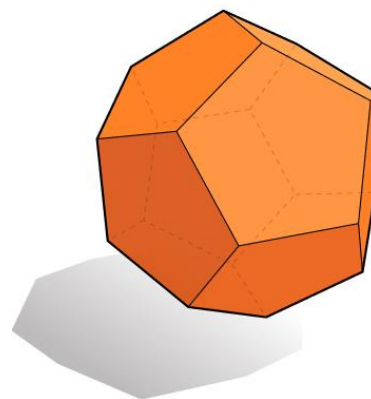
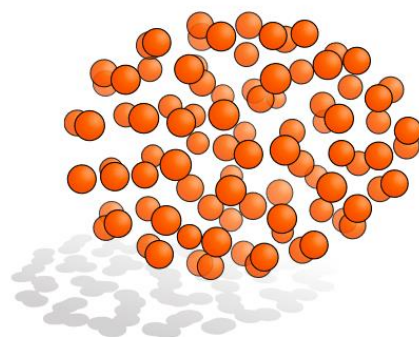
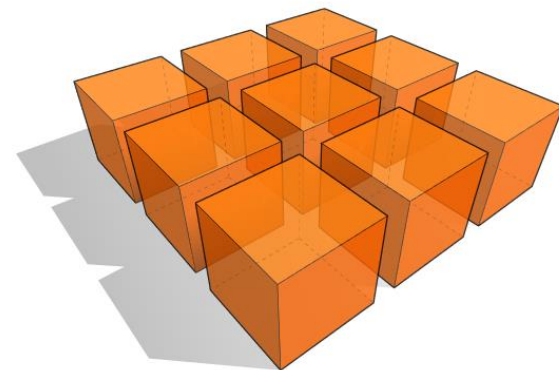
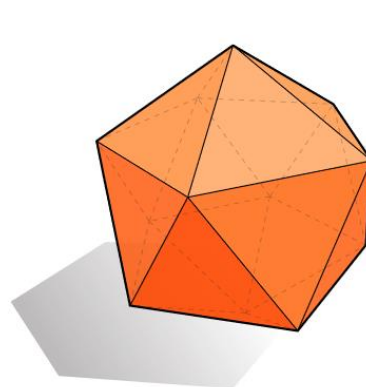
```
def main() :  
    # ...  
    glfw.make_context_current(window)  
    glViewport(100, 100, 200, 200)  
    # ...
```

Mesh

Many ways to digitally encode geometry

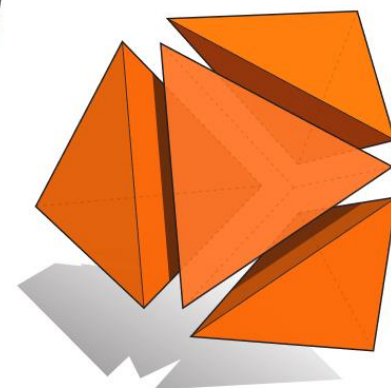
■ EXPLICIT

- point cloud
- polygon mesh
- subdivision, NURBS
- L-systems
- ...



■ IMPLICIT

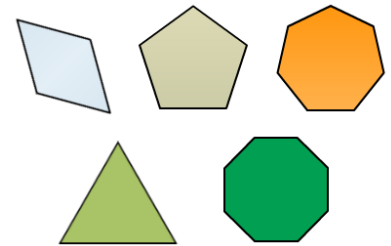
- level set
- algebraic surface
- ...



■ Each choice best suited to a different task/type of geometry

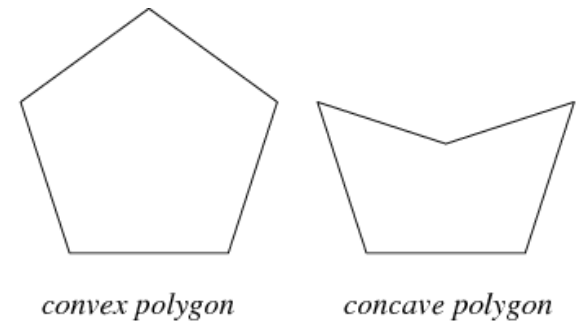
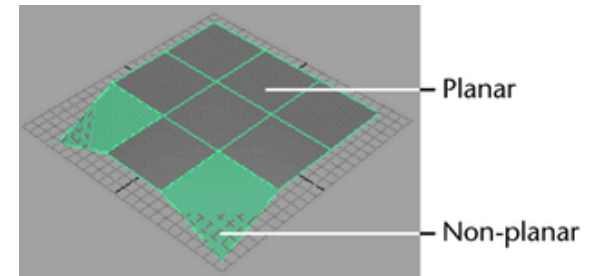
The Most Popular Representation : Polygon Mesh

- Because this can model any arbitrary complex shapes with relatively simple representations and can be rendered fast.
- **Polygon:** a “closed” shape with straight sides
- **Polygon mesh:** a bunch of polygons in 3D space that are connected together to form a surface
 - Usually use *triangles* or *quads* (4 side polygon)



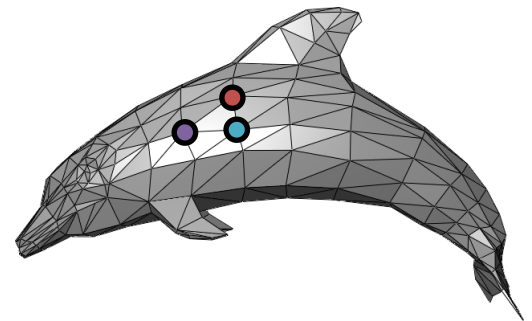
Triangle Mesh

- A general N-polygon can be
 - Non-planar
 - Non-convex
- , which are not desirable for fast rendering.
- A triangle does not have such problems. It's always planar & convex.
- and N-polygons can be composed of multiple triangles.
- That's why modern GPUs draw everything as a set of triangles.
- So, we'll focus on triangle meshes.



Representation for Triangle Mesh

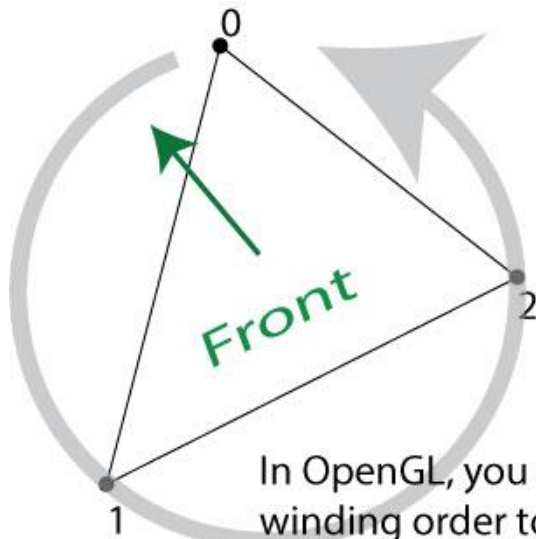
- It's about how to store
 - vertex positions
 - relationship between vertices (to make triangles)
- on memory.
- We'll see
 - Separate triangles (today)
 - Indexed triangle set (next lecture)



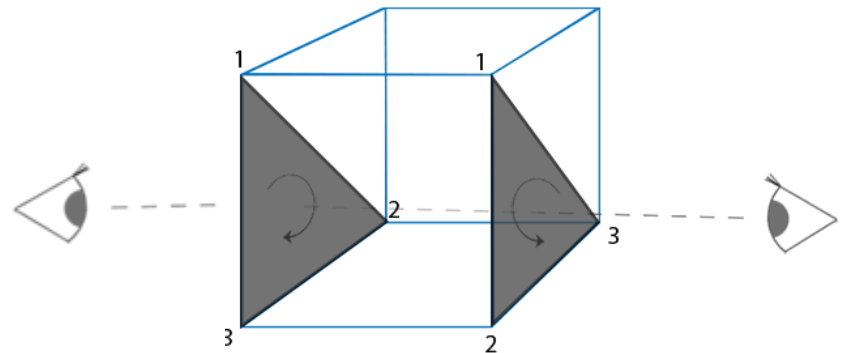
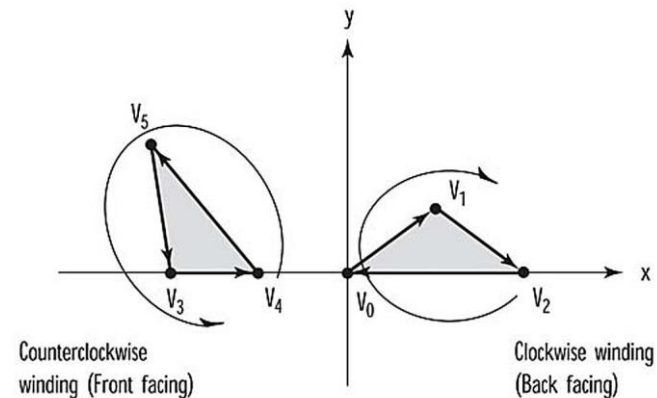
Vertex Winding Order

- In OpenGL, by default, polygons whose vertices appear in **counterclockwise** order on the screen is front-facing

The 'winding order' of a set of vertices determines which side of the surface is the front

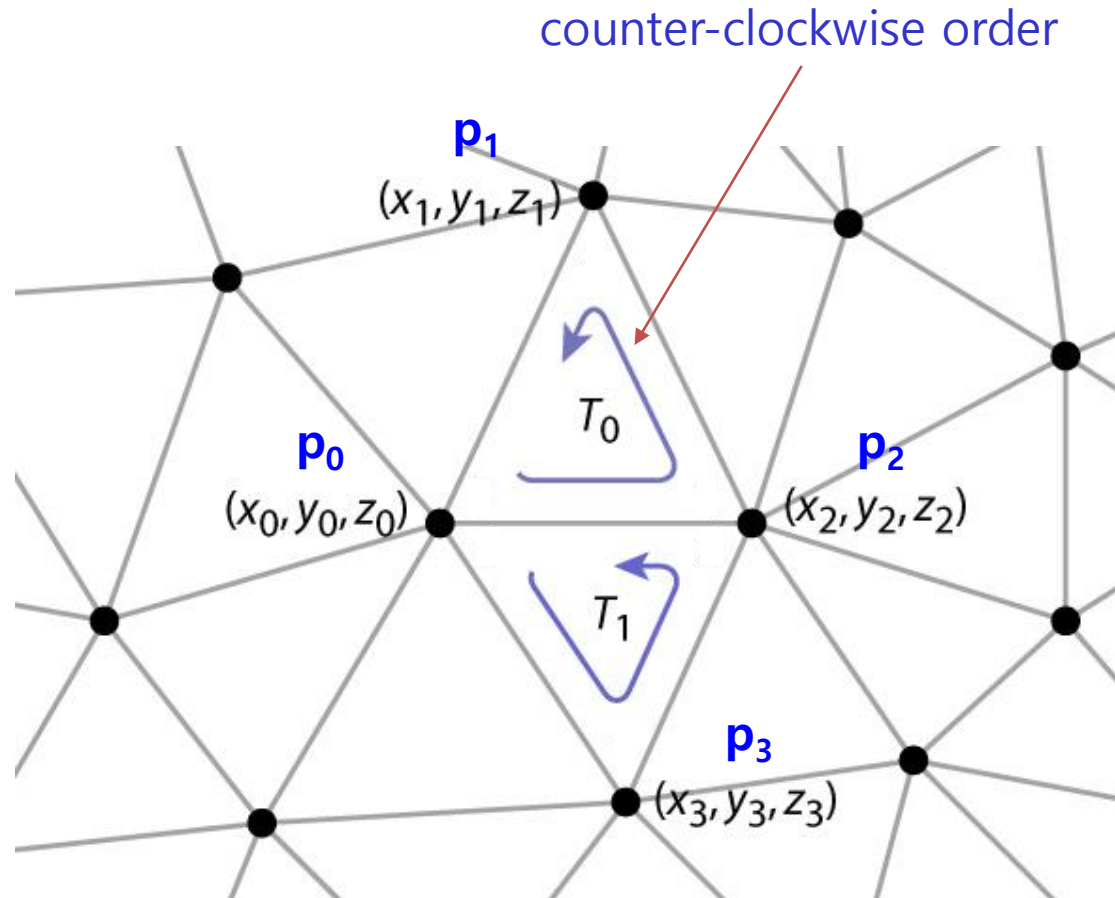


In OpenGL, you can use the winding order to define inside and outside surfaces of solids



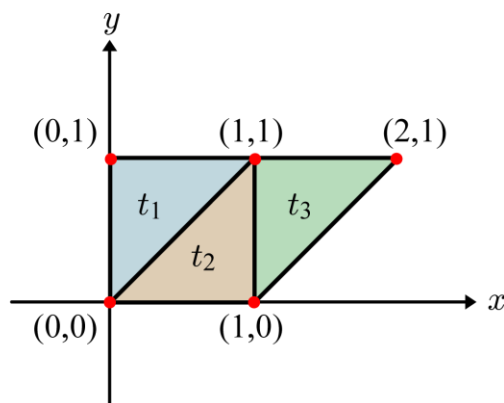
Separate triangles

	[0]	[1]	[2]
tris[0]	x_0, y_0, z_0	x_2, y_2, z_2	x_1, y_1, z_1
tris[1]	x_0, y_0, z_0	x_3, y_3, z_3	x_2, y_2, z_2
	\vdots	\vdots	\vdots



Separate Triangles

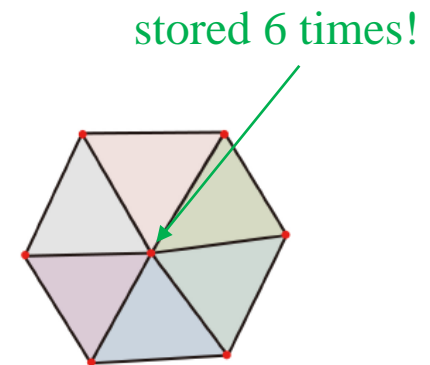
- Various problems
 - Wastes space
 - Cracks due to roundoff
 - Difficulty of finding neighbors
 - If you want find "neighbor" triangles of t_2 , you have to find all "zero-distance" vertices from t_2 's each vertex.



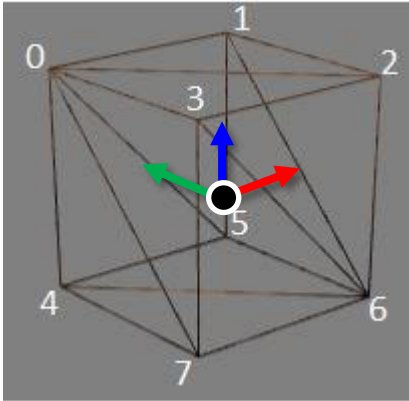
vertex buffer

(0,1)	t_1
(0,0)	
(1,1)	t_2
(0,0)	
(1,0)	
(1,1)	t_3
(1,0)	
(2,1)	

(1,1) is stored 3 times!



Example: a cube of length 2



vertex index	position
0	(-1 , 1 , 1)
1	(1 , 1 , 1)
2	(1 , -1 , 1)
3	(-1 , -1 , 1)
4	(-1 , 1 , -1)
5	(1 , 1 , -1)
6	(1 , -1 , -1)
7	(-1 , -1 , -1)

Drawing Separate Triangles using glVertex*()

- You can use glVertex*() like this:

```
def drawCube_glVertex():
    glBegin(GL_TRIANGLES)
    glVertex3f( -1 , 1 , 1 ) # v0
    glVertex3f( 1 , -1 , 1 ) # v2
    glVertex3f( 1 , 1 , 1 ) # v1

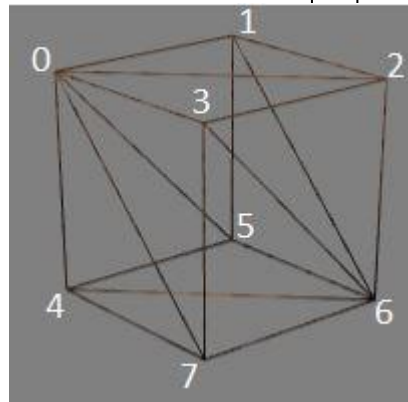
    glVertex3f( -1 , 1 , 1 ) # v0
    glVertex3f( -1 , -1 , 1 ) # v3
    glVertex3f( 1 , -1 , 1 ) # v2

    glVertex3f( -1 , 1 , -1 ) # v4
    glVertex3f( 1 , 1 , -1 ) # v5
    glVertex3f( 1 , -1 , -1 ) # v6

    glVertex3f( -1 , 1 , -1 ) # v4
    glVertex3f( 1 , -1 , -1 ) # v6
    glVertex3f( -1 , -1 , -1 ) # v7

    glVertex3f( -1 , 1 , 1 ) # v0
    glVertex3f( 1 , 1 , 1 ) # v1
    glVertex3f( 1 , 1 , -1 ) # v5

    glVertex3f( -1 , 1 , 1 ) # v0
    glVertex3f( 1 , 1 , -1 ) # v5
    glVertex3f( -1 , 1 , -1 ) # v4
```



```
glVertex3f( -1 , -1 , 1 ) # v3
glVertex3f( 1 , -1 , -1 ) # v6
glVertex3f( 1 , -1 , 1 ) # v2

    glVertex3f( -1 , -1 , 1 ) # v3
    glVertex3f( -1 , -1 , -1 ) # v7
    glVertex3f( 1 , -1 , -1 ) # v6

    glVertex3f( 1 , 1 , 1 ) # v1
    glVertex3f( 1 , -1 , 1 ) # v2
    glVertex3f( 1 , -1 , -1 ) # v6

    glVertex3f( 1 , 1 , 1 ) # v1
    glVertex3f( 1 , -1 , -1 ) # v6
    glVertex3f( 1 , 1 , -1 ) # v5

    glVertex3f( -1 , 1 , 1 ) # v0
    glVertex3f( -1 , -1 , -1 ) # v7
    glVertex3f( -1 , -1 , 1 ) # v3

    glVertex3f( -1 , 1 , 1 ) # v0
    glVertex3f( -1 , 1 , -1 ) # v4
    glVertex3f( -1 , -1 , -1 ) # v7
    glEnd()
```

Vertex Array

- But from now on, let's use a more advanced method to draw polygons: *Vertex array*
- **Vertex array**: an array of vertex data including vertex positions, normals, texture coordinates and color information
 - For now, consider vertex positions only
- By using a vertex array, you can draw a whole mesh just by calling a OpenGL function **once**! (instead of a huge number of glVertex*() calls!)
- → Tremendous increase in rendering performance!

Drawing Separate Triangles using Vertex Array

- 1. Create a vertex array for your mesh
 - Using `numpy.ndarray` or python list
- 2. Specify “pointer” to this vertex array
 - Using `glVertexPointer()`
- 3. Render the mesh using the specified “pointer”
 - Using `glDrawArrays()`

glVertexPointer() & glDrawArrays()

- **glVertexPointer(size, type, stride, pointer)**
- : specifies the location and data format of a vertex array
 - **size**: The number of vertex coordinates, 2 for 2D points, 3 for 3D points
 - **type**: The data type of each coordinate value in the array. GL_FLOAT, GL_SHORT, GL_INT or GL_DOUBLE.
 - **stride**: The byte offset to the next vertex
 - **pointer**: The pointer to the first coordinate of the first vertex in the array
- **glDrawArrays(mode , first , count)**
- : render primitives from the vertex array specified by glVertexPointer()
 - **mode**: The primitive type to render. GL_POINTS, GL_TRIANGLES, ...
 - **first**: The starting index in the array specified by glVertexPointer()
 - **count**: The number of vertices to be rendered (duplicate vertices also should be counted separately)

[Practice] Drawing Separate Triangles using Vertex Array

```
import glfw
from OpenGL.GL import *
import numpy as np
from OpenGL.GLU import *

gCamAng = 0
gCamHeight = 1.

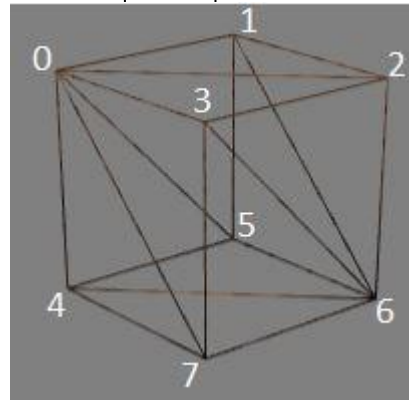
def createVertexArraySeparate():
    varr = np.array([
        (-1, 1, 1), # v0
        (1, -1, 1), # v2
        (1, 1, 1), # v1

        (-1, 1, 1), # v0
        (-1, -1, 1), # v3
        (1, -1, 1), # v2

        (-1, 1, -1), # v4
        (1, 1, -1), # v5
        (1, -1, -1), # v6

        (-1, 1, -1), # v4
        (1, -1, -1), # v6
        (-1, -1, -1), # v7

        (-1, 1, 1), # v0
        (1, 1, 1), # v1
        (1, 1, -1), # v5
```



```
(-1, 1, 1), # v0
(1, 1, -1), # v5
(-1, 1, -1), # v4

(-1, -1, 1), # v3
(1, -1, -1), # v6
(1, -1, 1), # v2

(-1, -1, 1), # v3
(-1, -1, -1), # v7
(1, -1, -1), # v6

(1, 1, 1), # v1
(1, -1, 1), # v2
(1, -1, -1), # v6

(1, 1, 1), # v1
(1, -1, -1), # v6
(1, 1, -1), # v5

(-1, 1, 1), # v0
(-1, -1, -1), # v7
(-1, -1, 1), # v3

(-1, 1, 1), # v0
(-1, 1, -1), # v4
(-1, -1, -1), # v7
], 'float32')

return varr
```

```

def render():
    global gCamAng, gCamHeight
    glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT)
    glEnable(GL_DEPTH_TEST)
    glPolygonMode( GL_FRONT_AND_BACK, GL_LINE )

    glLoadIdentity()
    gluPerspective(45, 1, 1,10)
    gluLookAt(5*np.sin(gCamAng),gCamHeight,5*np.cos(gCamAng), 0,0,0, 0,1,0)

    drawFrame()
    glColor3ub(255, 255, 255)

    # drawCube_glVertex()
    drawCube_glDrawArrays()

def drawCube_glDrawArrays():
    global gVertexArraySeparate
    varr = gVertexArraySeparate
    glEnableClientState(GL_VERTEX_ARRAY) # Enable it to use vertex array
    glVertexPointer(3, GL_FLOAT, 3*varr.itemsize, varr)
    glDrawArrays(GL_TRIANGLES, 0, int(varr.size/3))

```



```

gVertexArraySeparate = None
def main():
    global gVertexArraySeparate

    if not glfw.init():
        return
    window = glfw.create_window(640, 640, 'Lecture10', None, None)
    if not window:
        glfw.terminate()
        return
    glfw.make_context_current(window)
    glfw.set_key_callback(window, key_callback)

    gVertexArraySeparate = createVertexArraySeparate()

    while not glfw.window_should_close(window):
        glfw.poll_events()
        render()
        glfw.swap_buffers(window)

    glfw.terminate()

if __name__ == "__main__":
    main()

```

```

def drawFrame():
    glBegin(GL_LINES)
    glColor3ub(255, 0, 0)
    glVertex3fv(np.array([0.,0.,0.]))
    glVertex3fv(np.array([1.,0.,0.]))
    glColor3ub(0, 255, 0)
    glVertex3fv(np.array([0.,0.,0.]))
    glVertex3fv(np.array([0.,1.,0.]))
    glColor3ub(0, 0, 255)
    glVertex3fv(np.array([0.,0.,0]))
    glVertex3fv(np.array([0.,0.,1.]))
    glEnd()

```

```

def key_callback(window, key, scancode, action,
mods):
    global gCamAng, gCamHeight
    if action==glfw.PRESS or action==glfw.REPEAT:
        if key==glfw.KEY_1:
            gCamAng += np.radians(-10)
        elif key==glfw.KEY_3:
            gCamAng += np.radians(10)
        elif key==glfw.KEY_2:
            gCamHeight += .1
        elif key==glfw.KEY_W:
            gCamHeight += -.1

```

Quiz #3

- Go to <https://www.slido.com/>
- Join #cg-ys
- Click “Polls”
- Submit your answer in the following format:
 - **Student ID: Your answer**
 - e.g. **2017123456: 4)**
- Note that you must submit all quiz answers in the above format to be checked for “attendance”.

Next Time

- Lab for this lecture (next Monday):
 - Lab assignment 6
- Next lecture:
 - 7 - Mesh 2, Lighting & Shading 1
- Acknowledgement: Some materials come from the lecture slides of
 - Prof. Jinxiang Chai, Texas A&M Univ., http://faculty.cs.tamu.edu/jchai/csce441_2016spring/lectures.html
 - Prof. Taesoo Kwon, Hanyang Univ., <http://calab.hanyang.ac.kr/cgi-bin/cg.cgi>
 - Prof. Steve Marschner, Cornell Univ., <http://www.cs.cornell.edu/courses/cs4620/2014fa/index.shtml>