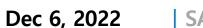
Highly-Efficient Reasoning via Trigger

Graphs

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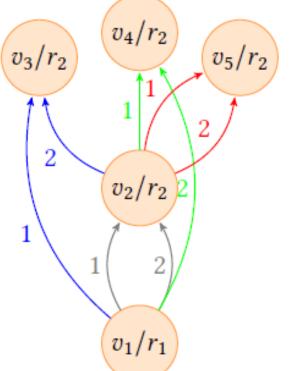
Disclaimer

This talk is **not** about stream reasoning...

...however, it presents a reasoning technique that can be naturally extended to reasoning in an incremental fashion.

The reasoning technique is based on a notion called Trigger Graphs

(TGs).



$$p(X,Y) \leftarrow e(X,Y)$$
 (r_1)
 $p(X,Y) \leftarrow p(X,Z) \wedge p(Z,Y)$ (r_2)

"Materializing Knowledge Bases via Trigger Graphs", VLDB 2021

"Probabilistic Reasoning at Scale: Trigger Graphs to the Rescue", **SIGMOD 2023**

Performance benefits of Trigger Graphs: nonprobabilistic reasoning

Table 4: Datalog scenarios. Runtime is in sec and memory in MB. * denotes timeout after 1h.

| | VI | Log | RD | Fox | CC | OM | \mathbf{GL} | og Runti | ime | GLog Memory | | | |
|-----------|----------------|--------|----------------|------|---------|--------|---------------|----------|--------|-------------|-------|--------|--|
| Scenario | Runtime Memory | | Runtime Memory | | Runtime | Memory | No opt | No opt m | | No opt | m | m+r | |
| LUBM-L | 1.5 | 324 | 23 | 2301 | 20.4 | 4479 | 2.4 | 2.2 | 1.0 | 446 | 424 | 264 | |
| LUBM-LE | 170.5 | 2725 | 116.6 | 3140 | 115.9 | 3610 | 17.3 | 17.2 | 16.1 | 1340 | 1310 | 1338 | |
| UOBM-L | 7.3 | 1021 | 10 | 784 | 10 | 4215 | 2.6 | 2.4 | 2.6 | 335 | 335 | 342 | |
| DBpedia-L | 41.6 | 827 | 64.4 | 3290 | 198.4 | 3878 | 20 | 19 | 19 | 1341 | 1352 | 1339 | |
| Claros-L | 431 | 3170 | 2512 | 5491 | 2373.0 | 6453 | 122 | 118.3 | 119 | 6076 | 6077 | 6078 | |
| Claros-LE | 2771.8 | 11 895 | * | * | * | * | 1040.8 | 1012.2 | 1053.9 | 48 464 | 48474 | 48 455 | |

Performance benefits of Trigger Graphs: probabilistic reasoning

Table 3: Total time (default is ms) to answer the queries in LUBM010 and LUBM100 with ProbLog2 (P), Scallop (S), vProbLog (vP) and LTGs (L). Probabilities are computed via PySDD (SDD), d-tree and c2d. Shaded cells contain the best times.

| | Q_1 | Q_2 | Q_3 | Q_4 | Q_5 | Q_6 | Q_7 | Q_8 | Q_9 | Q_{10} | Q_{11} | Q_{12} | Q_{13} | Q_{14} | Q_1 | Q_2 | Q_3 | Q_4 | Q_5 | Q_6 | Q_7 | Q_8 | Q_9 | Q_{10} | Q_{11} | Q_{12} | Q_{13} | Q_{14} |
|-------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|----------|----------|----------|----------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|----------|----------|----------|----------|
| P+SDD | 59 | NA | NA | 78 | NA | 150 | NA | NA | NA | NA | NA |
| S(30)+SDD | 1.3s | NA | 729 | NA | 4.5s | 817s | 6s | NA | NA | NA | 63 | 165s | 30s | 326 | 15.5 | NA | 8.9s | NA | 372 | NA | NA | 3.3s |
| vP+SDD | 587 | 7.2s | 306 | 5.6s | 13.6s | NA | 6.3s | NA | NA | 1.3s | 2s | 17.3s | 12.4s | 3.1s | 7.3s | NA | 2.5s | NA | 2s | NA | NA | 38.7s |
| L w/o+SDD | 57 | 420 | 38 | 1.1s | 1.3s | NA | 353 | 35.1s | 348s | 187 | 7 | 10.6s | 541 | 337 | 647 | 52s | 455 | 2.4s | 4.7s | NA | 2s | 51.8s | NA | 1.7s | 31 | 12.7s | 6.1s | 4.9s |
| L w/+SDD | 49 | 383 | 38 | 175 | 365 | NA | 315 | 21.8s | 174s | 162 | 5 | 387 | 176 | 273 | 617 | 46.1s | 444 | 1.5s | 3.7s | NA | 1.9s | 71.4s | NA | 1.6s | 21 | 1.6s | 2.8s | 6s |
| L w/+d-tree | 49 | 676 | 40 | 461 | 595 | NA | 4.9s | 668s | 108s | 1.5s | 6 | 1s | 206 | 273 | 617 | 42s | 411 | 1.7s | 2.7s | NA | 6.3s | 658s | NA | 2.9s | 21 | 2s | 2.4s | 6s |
| L w/+c2d | 49 | 41s | 316 | 3.9s | 62s | NA | 27s | NA | NA | 2.4s | 6 | 13s | 6.2s | 273 | 617 | NA | 1s | 7.4s | 113s | NA | 32s | NA | NA | 4.2s | 21 | 16s | 16s | 6s |

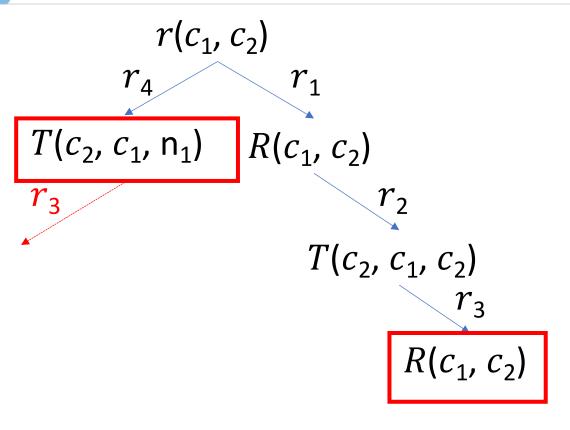
| | | \$ | \$ | & | Ş | 8 |
|-------------|----------|--|--|--|----------|--|
| | | 23.438 A | Service Control of the Control of th | Server Constitution of the | 24 1615g | 53.05.75 |
| | | S. S | .X | N | 26 | ************************************** |
| | Query ID | ₹, | ₹. | ₹, | S. | ₹, |
| Runtime | S(1) | 1.5s | 800ms | 721ms | 793ms | 1.1s |
| | S(20) | 1311s | 148s | 88s | 45s | 40s |
| | S(30) | TO | 1415s | 89s | 42s | 41s |
| ~ | LTGs w/ | 353s | 7.3s | 6.1s | 20s | 17.6s |
| ity | S(1) | 0.03 | 0.003 | 0.04 | 0.006 | 0.68 |
| bil | S(20) | 0.12 | 0.02 | 0.05 | 0.007 | 0.97 |
| Probability | S(30) | TO | 0.02 | 0.05 | 0.007 | 0.97 |
| Pro | LTGs w/ | 0.13 | 0.02 | 0.11 | 0.015 | 0.97 |
| | | | | | | |

Table. Results over the VQAR benchmark (NeurIPS 2021).

Overview

- TGs: non-probabilistic case
- TGs: probabilistic case

Motivation



$$r(X,Y) \rightarrow R(X,Y) \qquad (r_1)$$

$$R(X,Y) \rightarrow T(Y,X,Y) \qquad (r_2)$$

$$T(Y,X,Y) \rightarrow R(X,Y) \qquad (r_3)$$

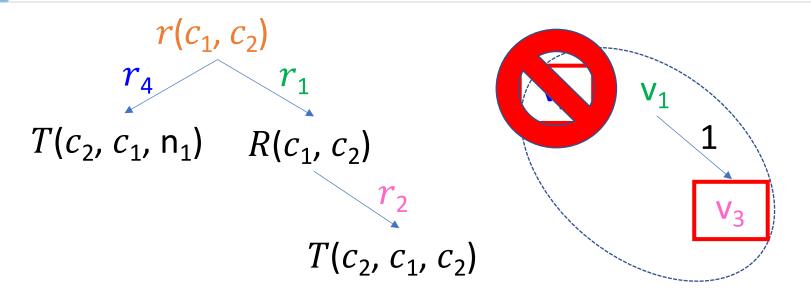
$$r(X,Y) \rightarrow \exists Z. \ T(Y,X,Z) \quad (r_4)$$

$$B = \{r(c_1, c_2)\}$$

Standard bottom-up seminaive evaluation

- □ cannot prevent the derivation of logically redundant facts
- □ cannot prevent redundant homomorphism checks

TG Construction for Linear Rules: Intuition



$$r(X,Y) \rightarrow R(X,Y)$$
 (r_1)
 $R(X,Y) \rightarrow T(Y,X,Y)$ (r_2)
 $T(Y,X,Y) \rightarrow R(X,Y)$ (r_3)
 $r(X,Y) \rightarrow \exists Z. \ T(Y,X,Z)$ (r_4)

- Reason over an instance
 B* that captures *all*
 possible rule execution
 patterns.
- Build a TG that captures the derivations over B*.
- Eliminate nodes producing logically redundant facts:
 - preserving homomorph isms

TG-Based Reasoning: Datalog Rules

No time to cover. Read our VLDB 2021 paper!

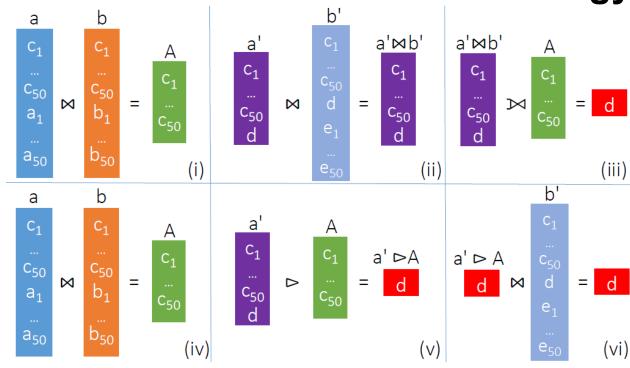
TG minimization

- □Computing rewritings over the TG.
- □Reduce to query containment (de cidable as the check does not con sider the rules).

Theoretical results:

- ☐ Produce a minimal (all instance g uarantees) TG.
- ☐ Decision problem is co-NP-complete

TG-based rule execution strategy

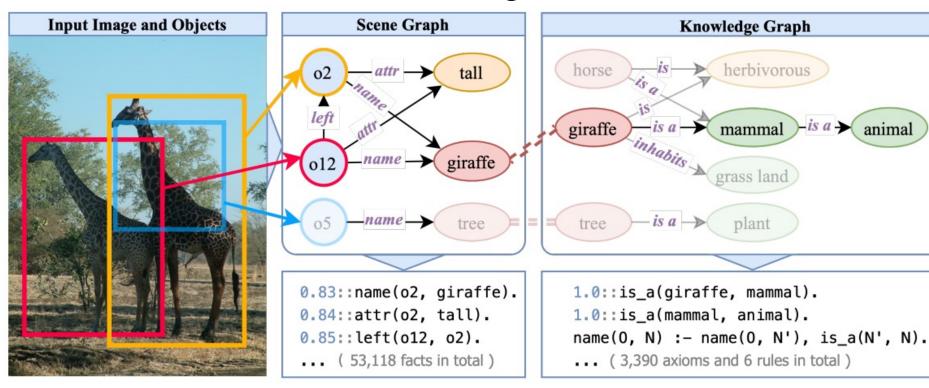


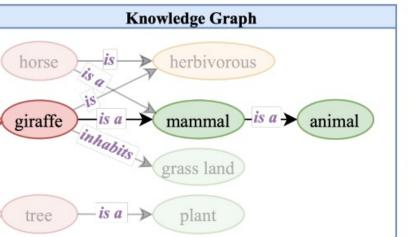
Overview

- TGs: non-probabilistic case
- TGs: probabilistic case (actually Datalog reasoning over tuple-independent PDBs)

Probabilities into the game

- Auto-mined KGs
 - -Google's Knowledge Vault
 - Microsoft's Concept Graph
- Visual Question Answering

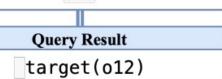




Natural Language Question "Identify the tall animal on the left"

Answer

012

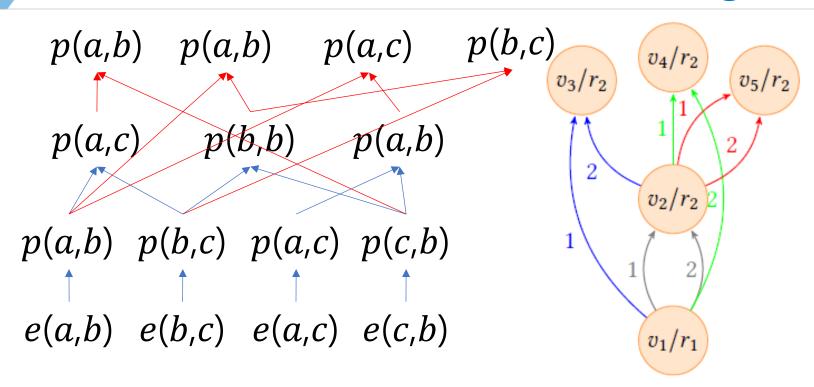


```
Programmatic Query
target(0) :- name(0, animal),
             left(0, 0'),
             attr(0, tall).
```

TG extensions to account for probabilities

- Why TGs should be extended?
 - -We need to account for **all** possible non-redundant ways to de rive each fact
 - -Then, the derivations are compiled in a formula to compute the probability a derived fact is true.

TG-Based Probabilistic Reasoning: Intuition



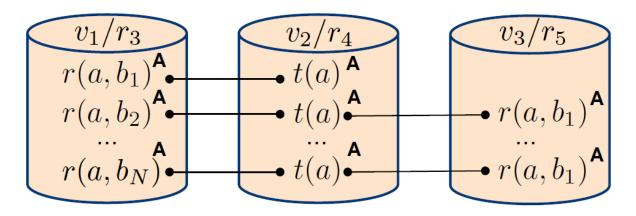
- Keep the provenance at reasoning-time within the nodes of the TG (this can be done efficiently).
- Stop when the derivation of a fact depends on itself.

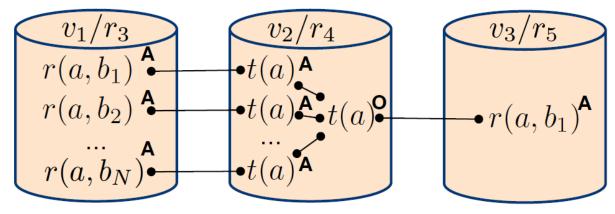
$$p(X,Y) \leftarrow e(X,Y) \qquad (r_1)$$

$$p(X,Y) \leftarrow p(X,Z) \land p(Z,Y) \qquad (r_2)$$

$$e(a,b), e(b,c), e(a,c), e(c,b)$$

TG-Based Probabilistic Reasoning: Collapsing





$$r(X,Y) \leftarrow q(X,Y)$$
 (r_3)
 $t(X) \leftarrow r(X,Y)$ (r_4)
 $r(X,Y) \leftarrow t(X) \land s(X,Y)$ (r_5)
 $q(a,b_i)$ for $1 \le i \le N$, and $s(a,b_1)$

- The previous technique is sound... however, it can explode space-wise.
- Keep only one derivation per fact within each node.
- Extends the notion of absorptive provenance circuits [D. Deutch, ICDT 2014], but we decide when to collapse or not.

Probabilistic reasoning: prior art

- How prior art [Tsamoura et al., AAAI 2020] works? Read our SIGMOD 2023 where we explain via an example!
 - -They are based on **provenance semirings** [T.J. Green, PODS 2007] and have **exponential space complexity** [D. Deutch, IC DT 2014].

Connections to incremental reasoning

• ???

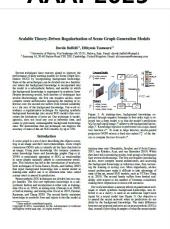
A few last things about my research

Scene graph generation





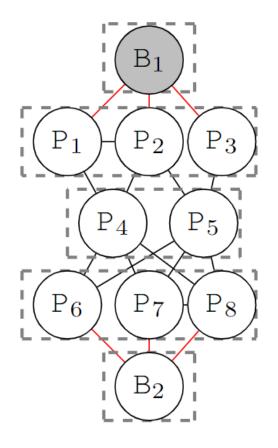
AAAI 2023



AAAI 2023



Structural motifs mining for lifted graphical models under (ϵ,α) -guarantees ...and some nice complexity results.



Thanks!

- Please feel free to reach out if
 - □you want to visit me in Cambridge, UK, or
 - □you have a nice idea to work on, or
 - □you want to learn more about my projects including TGs!