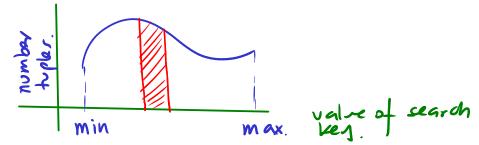
Selectivity of matching a primary Key: 1

Selection of matching a nonprimary vey:
We need a distribution.



We need to compute proportion of the tuples that match the predicate.

Example:

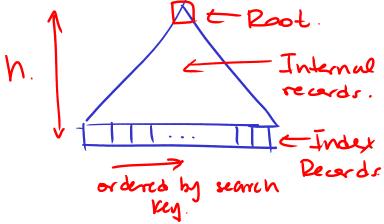
- · Relation R(9,6)
- · Assume a mifern distribution et valer et b, min 1, max 100.

Selection (b>20 and b<30) = 
$$\frac{9}{100}$$
  
Selection (b>200) =  $\emptyset$ 

Indexer.

B+-tree

- · Atomakcally Balanud
- · Finder records are at the leaves



- · Every record is a block.
- · Index records from a list
  - . They can be traversed in the order of the search Key

Internal records

pointers

Ki kz ... Kny Kny C at most n

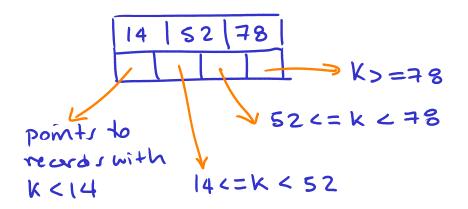
Key r.

to other

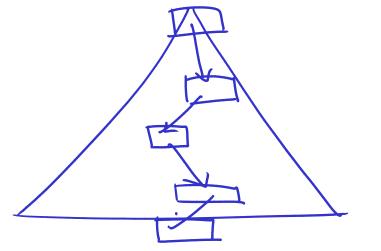
Index records.

Example.

Assume n = 3



Index is traversed from root to leaf



We assume noot is always in memory hence, to reach the leaf we read h blocks.

Cost =  $h - 1 + 0.5 \cdot 10^4 + 10^6$  $\approx 10^6!!$ 

Approximately 2 o times more than Sparse index! !

How do we know how many typer match a given greny?

selections (p) = probability that a type in R matcher predicate P.

Example.

R(a,b) |R| = 106 tuples.
heap: 10 tuples per block

Dense index on R(a)

Effective index records per block: 100

Assume h = 4

a)  $\sigma_{a=s} R$ if type exists: cost = h+1.

if type does not exist: cost = h.

Similar to sparse!!.

b) Ta>10 R Assume 50% of types match.



We need to scan 50% of them.

Cost of index:

· Cost of reaching the leafs · Cost of reading the matching records.

Example:

1) Assume 2(a,b)

Oa = 5 R

Only one or zero matching typles

> We must traverse the index h

The least either

contains a = 5 or not

Cost of index = h of index.

What if all types match?

We traverse index (cast h)

Peads first leaf.

We must read all leaves of

index

Cost of index = h + # leaves -1

To be able to compute the cost of an index we need:

Calalate # of leaf blocks of index proportional to # index records per block.

# of index records depends you a) type of index Sparse ss. Dense

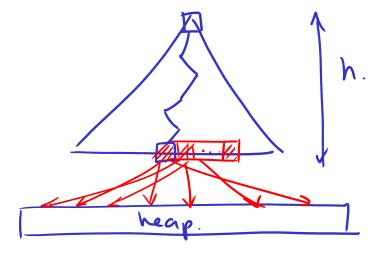
b) Number of types in Rel.

#index reards per block depends upon:

- a) size of search lay
- h) occupancy rate =) How much waste spece is there in the index (to Keep it balanced).

We assume that occupancy rate of inner nodes and leaves is the same as internal nodes.

Dense Index.



Cost:

h-1+# leaves in Index + 1 bbck per matching typle.

- · Traverse tree to first leaf: h · Might need to read Ø or more leafs.
- · For every type in result, read one

Example.

$$R(a,b)$$
  $|R| = 10^6$  typles.  
heap: 10 typles per block  
Sparse index on  $R(a)$   
Assume  $h = 3$ 

a) 
$$\sigma_{a=s} R$$
if type exists: cost = h+1.
if type does not exist: cost = h.

b) Ja>10 R

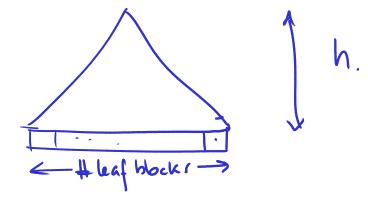
Assume 50% of tiples match gueny:

 $\Rightarrow$  We must scan 50% of sorted heap. Cost = h +  $\frac{B(R)}{Z}$ 

$$B(R) = \frac{10^6}{10} = 10^5$$

Cost =  $3 + 0.5 \cdot 10^5$  blocks.
Approx:  $0.5 \cdot 10^5$  blocks;

Hence, height of tree depends upon # of leaf records.



n = max number of keys per record.

fill = occupancy rate (between 0-1,
but usally around 1/2 to 3/4)

For h, we simplify calculations:

## Example:

Assume 
$$n = 150$$
,  $fill = \frac{2}{3}$ 

How many index records can we store in an index of height 1,2,3,4,5,6.

Let is wary about max # index leards

h # index Pecard ()

1 100 = 
$$10^2$$

2 100<sup>2</sup> =  $10^4$ 

3 100<sup>3</sup> =  $10^6$ 

4 100<sup>5</sup> =  $10^9$ 

With 5 block reads we can find a leaf with a given search key in an index of 10 giga-records!!

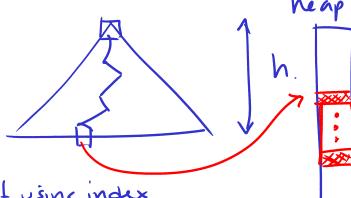
How many search lays do we need to store?

- · Sparse index: B(R)
- · Dense index: [R]

Sparse index is marginally shorter than dense index.

Cost of Using an Index

Sparce Index.



Cost of using index h + #blocks read in heap.

- · We only read one reard in index
- · We read 1 or more blocks from heap