

Matlab Code

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1  syms m1 m2 m3 m4 m5 m6;
2  syms q1 q2 q3 q4 q5 q6;
3  syms dq1 dq2 dq3 dq4 dq5 dq6;
4  syms ddq1 ddq2 ddq3 ddq4 ddq5 ddq6;
5  syms l1 l2 l3 l4 l5 l6;
6  syms u1 u2 u3 u4 u5 u6;
7  syms g
8  %equations
9  x1 = l1*cos(q1);
10 x2 = x1+l2*cos(q2);
11 x3 = x2+l3*cos(q2+q3);
12 x4 = x3+l4*cos(q1+q4);
13 x5 = x4;
14 x6 = x5+l6*cos(q1+q4+q6);
15
16 y1 = l1*sin(q1);
17 y2 = y1;
18 y3 = y2;
19 y4 = y3+l4*sin(q1+q4);
20 y5 = y4+l5*cos(q5);
21 y6 = y5+l6*sin(q1+q4+q6);
22
23 z1 = 0;
24 z2 = z1+l2*sin(q2);
25 z3 = z2+l3*cos(q2+q3);
26 z4 = z3;
27 z5 = z4+l5*sin(q5);
28 z6 = z5;
29
30 %translation jacobians
31 jv1=[diff(x1,q1) diff(x1,q2) diff(x1,q3) diff(x1,q4) diff
      (x1,q5) diff(x1,q6); ...
32      diff(y1,q1) diff(y1,q2) diff(y1,q3) diff(y1,q4) diff
      (y1,q5) diff(y1,q6); ...
33      diff(z1,q1) diff(z1,q2) diff(z1,q3) diff(z1,q4) diff
      (y1,q5) diff(z1,q6)];
34
35 jv2=[diff(x2,q1) diff(x2,q2) diff(x2,q3) diff(x2,q4) diff
      (x2,q5) diff(x2,q6); ...
36      diff(y2,q1) diff(y2,q2) diff(y2,q3) diff(y2,q4) diff
      (y2,q5) diff(y2,q6); ...
37      diff(z2,q1) diff(z2,q2) diff(z2,q3) diff(z2,q4) diff
      (y2,q5) diff(z2,q6)];

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38
39 jv3=[diff(x3,q1) diff(x3,q2) diff(x3,q3) diff(x3,q4) diff
      (x3,q5) diff(x3,q6); ...
40      diff(y3,q1) diff(y3,q2) diff(y3,q3) diff(y3,q4) diff
      (y3,q5) diff(y3,q6); ...
41      diff(z3,q1) diff(z3,q2) diff(z3,q3) diff(z3,q4) diff
      (y3,q5) diff(z3,q6)];
42
43 jv4=[diff(x4,q1) diff(x4,q2) diff(x4,q3) diff(x4,q4) diff
      (x4,q5) diff(x4,q6); ...
44      diff(y4,q1) diff(y4,q2) diff(y4,q3) diff(y4,q4) diff
      (y4,q5) diff(y4,q6); ...
45      diff(z4,q1) diff(z4,q2) diff(z4,q3) diff(z4,q4) diff
      (y4,q5) diff(z4,q6)];
46
47 jv5=[diff(x5,q1) diff(x5,q2) diff(x5,q3) diff(x5,q4) diff
      (x5,q5) diff(x5,q6); ...
48      diff(y5,q1) diff(y5,q2) diff(y5,q3) diff(y5,q4) diff
      (y5,q5) diff(y5,q6); ...
49      diff(z5,q1) diff(z5,q2) diff(z5,q3) diff(z5,q4) diff
      (y5,q5) diff(z5,q6)];
50
51 jv6=[diff(x6,q1) diff(x6,q2) diff(x6,q3) diff(x6,q4) diff
      (x6,q5) diff(x6,q6); ...
52      diff(y6,q1) diff(y6,q2) diff(y6,q3) diff(y6,q4) diff
      (y6,q5) diff(y6,q6); ...
53      diff(z6,q1) diff(z6,q2) diff(z6,q3) diff(z6,q4) diff
      (y6,q5) diff(z6,q6)];
54
55 %rotation jacobians
56 jw1=[0 0 0 0 0 0;...
57      0 0 0 0 0 0;...
58      1 0 0 0 0 0];
59
60 jw2=[0 0 0 0 0 0;...
61      0 1 0 0 0 0;...
62      0 0 0 0 0 0];
63
64 jw3=[0 0 0 0 0 0;...
65      0 0 1 0 0 0;...
66      0 0 0 0 0 0];
67
68 jw4=[0 0 0 0 0 0;...
69      0 0 0 0 0 0;...
70      0 0 0 1 0 0];
71

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72 jw5=[0 0 0 0 1 0;...
73       0 0 0 0 0 0;...
74       0 0 0 0 0 0];
75
76 jw6=[0 0 0 0 0 0;...
77       0 0 0 0 0 0;...
78       0 0 0 0 0 1];
79
80 %rotation matrices
81 R1= [cos(q1) -sin(q1) 0;...
82       sin(q1)  cos(q1) 0;...
83       0         0      1];
84
85 R2= [cos(q2) 0 sin(q2);...
86       0      1 0;...
87       -sin(q2) 0 cos(q2)];
88
89 R3= [cos(q3) 0 sin(q3);...
90       0      1 0;...
91       -sin(q3) 0 cos(q3)];
92
93 R4= [cos(q4) -sin(q4) 0;...
94       sin(q4)  cos(q4) 0;...
95       0         0      1];
96
97 R5= [1      0      0;...
98       0      cos(q5) -sin(q5);...
99       0      sin(q5)  cos(q5)];
100
101 R6= [cos(q6) -sin(q6) 0;...
102       sin(q6)  cos(q6) 0;...
103       0         0      1];
104 %Inertia matrix
105 I= [1 0 0;...
106     0 1 0;...
107     0 0 1];
108
109 %Math Matrix M(q)
110 Mq= m1*jv1'*jv1 + jw1'*R1*I*R1'*jw1+...
111     m1*jv2'*jv2 + jw2'*R2*I*R2'*jw2+...
112     m1*jv3'*jv3 + jw3'*R3*I*R3'*jw3+...
113     m1*jv4'*jv4 + jw4'*R4*I*R4'*jw4+...
114     m1*jv5'*jv5 + jw5'*R5*I*R5'*jw5+...
115     m1*jv6'*jv6 + jw5'*R6*I*R6'*jw6;
116
117 M=(simplify(Mq))

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118
119 %Colriolis Matrix C(q,dq)
120 m11= Mq(1,1); m12= Mq(1,2); m13= Mq(1,3); m14= Mq(1,1);
      m15= Mq(1,2); m16= Mq(1,3);
121 m21= Mq(2,1); m22= Mq(2,2); m23= Mq(2,2); m24= Mq(2,1);
      m25= Mq(2,2); m26= Mq(2,2);
122 m31= Mq(3,1); m32= Mq(3,1); m33= Mq(3,3); m34= Mq(3,1);
      m35= Mq(3,1); m36= Mq(3,3);
123 m41= Mq(4,1); m42= Mq(4,2); m43= Mq(4,3); m44= Mq(4,1);
      m45= Mq(4,2); m46= Mq(4,3);
124 m51= Mq(5,1); m52= Mq(5,2); m53= Mq(5,2); m54= Mq(5,1);
      m55= Mq(5,2); m56= Mq(5,2);
125 m61= Mq(6,1); m62= Mq(6,1); m63= Mq(6,3); m64= Mq(6,1);
      m65= Mq(6,1); m66= Mq(6,3);

126
127 c111= 0.5*( diff(m11,q1)+diff(m11,q1)-diff(m11,q1));
128 c112= 0.5*( diff(m11,q2)+diff(m12,q1)-diff(m12,q1));
129 c113= 0.5*( diff(m11,q3)+diff(m13,q1)-diff(m13,q1));
130 c114= 0.5*( diff(m11,q4)+diff(m14,q1)-diff(m14,q1));
131 c115= 0.5*( diff(m11,q5)+diff(m15,q1)-diff(m15,q1));
132 c116= 0.5*( diff(m11,q6)+diff(m16,q1)-diff(m16,q1));

133
134 c121= 0.5*( diff(m12,q1)+diff(m11,q2)-diff(m21,q1));
135 c122= 0.5*( diff(m12,q2)+diff(m12,q2)-diff(m22,q1));
136 c123= 0.5*( diff(m12,q3)+diff(m13,q2)-diff(m23,q1));
137 c124= 0.5*( diff(m12,q4)+diff(m14,q2)-diff(m24,q1));
138 c125= 0.5*( diff(m12,q5)+diff(m15,q2)-diff(m25,q1));
139 c126= 0.5*( diff(m12,q6)+diff(m16,q2)-diff(m26,q1));

140
141 c131= 0.5*( diff(m13,q1)+diff(m11,q3)-diff(m31,q1));
142 c132= 0.5*( diff(m13,q2)+diff(m12,q3)-diff(m32,q1));
143 c133= 0.5*( diff(m13,q3)+diff(m13,q3)-diff(m33,q1));
144 c134= 0.5*( diff(m13,q4)+diff(m14,q3)-diff(m34,q1));
145 c135= 0.5*( diff(m13,q5)+diff(m15,q3)-diff(m35,q1));
146 c136= 0.5*( diff(m13,q6)+diff(m16,q3)-diff(m36,q1));

147
148 c141= 0.5*( diff(m14,q1)+diff(m11,q4)-diff(m41,q1));
149 c142= 0.5*( diff(m14,q2)+diff(m12,q4)-diff(m42,q1));
150 c143= 0.5*( diff(m14,q3)+diff(m13,q4)-diff(m43,q1));
151 c144= 0.5*( diff(m14,q4)+diff(m14,q4)-diff(m44,q1));
152 c145= 0.5*( diff(m14,q5)+diff(m15,q4)-diff(m45,q1));
153 c146= 0.5*( diff(m14,q6)+diff(m16,q4)-diff(m46,q1));

154
155 c151= 0.5*( diff(m15,q1)+diff(m11,q5)-diff(m51,q1));
156 c152= 0.5*( diff(m15,q2)+diff(m12,q5)-diff(m52,q1));
157 c153= 0.5*( diff(m15,q3)+diff(m13,q5)-diff(m53,q1));

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158 c154= 0.5*( diff(m15,q4)+diff(m14,q5)-diff(m54,q1));
159 c155= 0.5*( diff(m15,q5)+diff(m15,q5)-diff(m55,q1));
160 c156= 0.5*( diff(m15,q6)+diff(m16,q5)-diff(m56,q1));
161
162 c161= 0.5*( diff(m16,q1)+diff(m11,q6)-diff(m61,q1));
163 c162= 0.5*( diff(m16,q2)+diff(m12,q6)-diff(m62,q1));
164 c163= 0.5*( diff(m16,q3)+diff(m13,q6)-diff(m63,q1));
165 c164= 0.5*( diff(m16,q4)+diff(m14,q6)-diff(m64,q1));
166 c165= 0.5*( diff(m16,q5)+diff(m15,q6)-diff(m65,q1));
167 c166= 0.5*( diff(m16,q6)+diff(m16,q6)-diff(m66,q1));
168
169 c211= 0.5*( diff(m21,q1)+diff(m21,q1)-diff(m11,q2));
170 c212= 0.5*( diff(m21,q2)+diff(m22,q1)-diff(m12,q2));
171 c213= 0.5*( diff(m21,q3)+diff(m23,q1)-diff(m13,q2));
172 c214= 0.5*( diff(m21,q4)+diff(m24,q1)-diff(m14,q2));
173 c215= 0.5*( diff(m21,q5)+diff(m25,q1)-diff(m15,q2));
174 c216= 0.5*( diff(m21,q6)+diff(m26,q1)-diff(m16,q2));
175
176 c221= 0.5*( diff(m22,q1)+diff(m21,q2)-diff(m21,q2));
177 c222= 0.5*( diff(m22,q2)+diff(m22,q2)-diff(m22,q2));
178 c223= 0.5*( diff(m22,q3)+diff(m23,q2)-diff(m23,q2));
179 c224= 0.5*( diff(m22,q4)+diff(m24,q2)-diff(m24,q2));
180 c225= 0.5*( diff(m22,q5)+diff(m25,q2)-diff(m25,q2));
181 c226= 0.5*( diff(m22,q6)+diff(m26,q2)-diff(m26,q2));
182
183 c231= 0.5*( diff(m23,q1)+diff(m21,q3)-diff(m31,q2));
184 c232= 0.5*( diff(m23,q2)+diff(m22,q3)-diff(m32,q2));
185 c233= 0.5*( diff(m23,q3)+diff(m23,q3)-diff(m33,q2));
186 c234= 0.5*( diff(m23,q4)+diff(m24,q3)-diff(m34,q2));
187 c235= 0.5*( diff(m23,q5)+diff(m25,q3)-diff(m35,q2));
188 c236= 0.5*( diff(m23,q6)+diff(m26,q3)-diff(m36,q2));
189
190 c241= 0.5*( diff(m24,q1)+diff(m21,q4)-diff(m41,q2));
191 c242= 0.5*( diff(m24,q2)+diff(m22,q4)-diff(m42,q2));
192 c243= 0.5*( diff(m24,q3)+diff(m23,q4)-diff(m43,q2));
193 c244= 0.5*( diff(m24,q4)+diff(m24,q4)-diff(m44,q2));
194 c245= 0.5*( diff(m24,q5)+diff(m25,q4)-diff(m45,q2));
195 c246= 0.5*( diff(m24,q6)+diff(m26,q4)-diff(m46,q2));
196
197 c251= 0.5*( diff(m25,q1)+diff(m21,q5)-diff(m51,q2));
198 c252= 0.5*( diff(m25,q2)+diff(m22,q5)-diff(m52,q2));
199 c253= 0.5*( diff(m25,q3)+diff(m23,q5)-diff(m53,q2));
200 c254= 0.5*( diff(m25,q4)+diff(m24,q5)-diff(m54,q2));
201 c255= 0.5*( diff(m25,q5)+diff(m25,q5)-diff(m55,q2));
202 c256= 0.5*( diff(m25,q6)+diff(m26,q5)-diff(m56,q2));
203

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204 c261= 0.5*( diff(m26,q1)+diff(m21,q6)-diff(m61,q2));
205 c262= 0.5*( diff(m26,q2)+diff(m22,q6)-diff(m62,q2));
206 c263= 0.5*( diff(m26,q3)+diff(m23,q6)-diff(m63,q2));
207 c264= 0.5*( diff(m26,q4)+diff(m24,q6)-diff(m64,q2));
208 c265= 0.5*( diff(m26,q5)+diff(m25,q6)-diff(m65,q2));
209 c266= 0.5*( diff(m26,q6)+diff(m26,q6)-diff(m66,q2));
210
211 c311= 0.5*( diff(m31,q1)+diff(m31,q1)-diff(m11,q3));
212 c312= 0.5*( diff(m31,q1)+diff(m32,q1)-diff(m12,q3));
213 c313= 0.5*( diff(m31,q3)+diff(m33,q1)-diff(m13,q3));
214 c314= 0.5*( diff(m31,q4)+diff(m34,q1)-diff(m14,q3));
215 c315= 0.5*( diff(m31,q5)+diff(m35,q1)-diff(m15,q3));
216 c316= 0.5*( diff(m31,q6)+diff(m36,q1)-diff(m16,q3));
217
218 c321= 0.5*( diff(m32,q1)+diff(m31,q2)-diff(m21,q3));
219 c322= 0.5*( diff(m32,q1)+diff(m32,q2)-diff(m22,q3));
220 c323= 0.5*( diff(m32,q3)+diff(m33,q2)-diff(m23,q3));
221 c324= 0.5*( diff(m32,q4)+diff(m34,q2)-diff(m24,q3));
222 c325= 0.5*( diff(m32,q5)+diff(m35,q2)-diff(m25,q3));
223 c326= 0.5*( diff(m32,q6)+diff(m36,q2)-diff(m26,q3));
224
225 c331= 0.5*( diff(m33,q1)+diff(m31,q3)-diff(m31,q3));
226 c332= 0.5*( diff(m33,q1)+diff(m32,q3)-diff(m32,q3));
227 c333= 0.5*( diff(m33,q3)+diff(m33,q3)-diff(m33,q3));
228 c334= 0.5*( diff(m33,q4)+diff(m34,q3)-diff(m34,q3));
229 c335= 0.5*( diff(m33,q5)+diff(m35,q3)-diff(m35,q3));
230 c336= 0.5*( diff(m33,q6)+diff(m36,q3)-diff(m36,q3));
231
232 c341= 0.5*( diff(m34,q1)+diff(m31,q4)-diff(m41,q3));
233 c342= 0.5*( diff(m34,q1)+diff(m32,q4)-diff(m42,q3));
234 c343= 0.5*( diff(m34,q3)+diff(m33,q4)-diff(m43,q3));
235 c344= 0.5*( diff(m34,q4)+diff(m34,q4)-diff(m44,q3));
236 c345= 0.5*( diff(m34,q5)+diff(m35,q4)-diff(m45,q3));
237 c346= 0.5*( diff(m34,q6)+diff(m36,q4)-diff(m46,q3));
238
239 c351= 0.5*( diff(m35,q1)+diff(m31,q5)-diff(m51,q3));
240 c352= 0.5*( diff(m35,q1)+diff(m32,q5)-diff(m52,q3));
241 c353= 0.5*( diff(m35,q3)+diff(m33,q5)-diff(m53,q3));
242 c354= 0.5*( diff(m35,q4)+diff(m34,q5)-diff(m54,q3));
243 c355= 0.5*( diff(m35,q5)+diff(m35,q5)-diff(m55,q3));
244 c356= 0.5*( diff(m35,q6)+diff(m36,q5)-diff(m56,q3));
245
246 c361= 0.5*( diff(m36,q1)+diff(m31,q6)-diff(m61,q3));
247 c362= 0.5*( diff(m36,q1)+diff(m32,q6)-diff(m62,q3));
248 c363= 0.5*( diff(m36,q3)+diff(m33,q6)-diff(m63,q3));
249 c364= 0.5*( diff(m36,q4)+diff(m34,q6)-diff(m64,q3));

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250 c365= 0.5*( diff(m36,q5)+diff(m35,q6)-diff(m65,q3));
251 c366= 0.5*( diff(m36,q6)+diff(m36,q6)-diff(m66,q3));
252
253 c411= 0.5*( diff(m41,q1)+diff(m41,q1)-diff(m11,q4));
254 c412= 0.5*( diff(m41,q2)+diff(m42,q1)-diff(m12,q4));
255 c413= 0.5*( diff(m41,q3)+diff(m43,q1)-diff(m13,q4));
256 c414= 0.5*( diff(m41,q4)+diff(m44,q1)-diff(m14,q4));
257 c415= 0.5*( diff(m41,q5)+diff(m45,q1)-diff(m15,q4));
258 c416= 0.5*( diff(m41,q6)+diff(m46,q1)-diff(m16,q4));
259
260 c421= 0.5*( diff(m42,q1)+diff(m41,q2)-diff(m21,q4));
261 c422= 0.5*( diff(m42,q2)+diff(m42,q2)-diff(m22,q4));
262 c423= 0.5*( diff(m42,q3)+diff(m43,q2)-diff(m23,q4));
263 c424= 0.5*( diff(m42,q4)+diff(m44,q2)-diff(m24,q4));
264 c425= 0.5*( diff(m42,q5)+diff(m45,q2)-diff(m25,q4));
265 c426= 0.5*( diff(m42,q6)+diff(m46,q2)-diff(m26,q4));
266
267 c431= 0.5*( diff(m43,q1)+diff(m41,q3)-diff(m31,q4));
268 c432= 0.5*( diff(m43,q2)+diff(m42,q3)-diff(m32,q4));
269 c433= 0.5*( diff(m43,q3)+diff(m43,q3)-diff(m33,q4));
270 c434= 0.5*( diff(m43,q4)+diff(m44,q3)-diff(m34,q4));
271 c435= 0.5*( diff(m43,q5)+diff(m45,q3)-diff(m35,q4));
272 c436= 0.5*( diff(m43,q6)+diff(m46,q3)-diff(m36,q4));
273
274 c441= 0.5*( diff(m44,q1)+diff(m41,q4)-diff(m41,q4));
275 c442= 0.5*( diff(m44,q2)+diff(m42,q4)-diff(m42,q4));
276 c443= 0.5*( diff(m44,q3)+diff(m43,q4)-diff(m43,q4));
277 c444= 0.5*( diff(m44,q4)+diff(m44,q4)-diff(m44,q4));
278 c445= 0.5*( diff(m44,q5)+diff(m45,q4)-diff(m45,q4));
279 c446= 0.5*( diff(m44,q6)+diff(m46,q4)-diff(m46,q4));
280
281 c451= 0.5*( diff(m45,q1)+diff(m41,q5)-diff(m51,q4));
282 c452= 0.5*( diff(m45,q2)+diff(m42,q5)-diff(m52,q4));
283 c453= 0.5*( diff(m45,q3)+diff(m43,q5)-diff(m53,q4));
284 c454= 0.5*( diff(m45,q4)+diff(m44,q5)-diff(m54,q4));
285 c455= 0.5*( diff(m45,q5)+diff(m45,q5)-diff(m55,q4));
286 c456= 0.5*( diff(m45,q6)+diff(m46,q5)-diff(m56,q4));
287
288 c461= 0.5*( diff(m46,q1)+diff(m41,q6)-diff(m61,q4));
289 c462= 0.5*( diff(m46,q2)+diff(m42,q6)-diff(m62,q4));
290 c463= 0.5*( diff(m46,q3)+diff(m43,q6)-diff(m63,q4));
291 c464= 0.5*( diff(m46,q4)+diff(m44,q6)-diff(m64,q4));
292 c465= 0.5*( diff(m46,q5)+diff(m45,q6)-diff(m65,q4));
293 c466= 0.5*( diff(m46,q6)+diff(m46,q6)-diff(m66,q4));
294
295 c511= 0.5*( diff(m51,q1)+diff(m51,q1)-diff(m11,q5));

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296 c512= 0.5*( diff(m51,q2)+diff(m52,q1)-diff(m12,q5));
297 c513= 0.5*( diff(m51,q3)+diff(m53,q1)-diff(m13,q5));
298 c514= 0.5*( diff(m51,q4)+diff(m54,q1)-diff(m14,q5));
299 c515= 0.5*( diff(m51,q5)+diff(m55,q1)-diff(m15,q5));
300 c516= 0.5*( diff(m51,q6)+diff(m56,q1)-diff(m16,q5));
301
302 c521= 0.5*( diff(m52,q1)+diff(m51,q2)-diff(m21,q5));
303 c522= 0.5*( diff(m52,q2)+diff(m52,q2)-diff(m22,q5));
304 c523= 0.5*( diff(m52,q3)+diff(m53,q2)-diff(m23,q5));
305 c524= 0.5*( diff(m52,q4)+diff(m54,q2)-diff(m24,q5));
306 c525= 0.5*( diff(m52,q5)+diff(m55,q2)-diff(m25,q5));
307 c526= 0.5*( diff(m52,q6)+diff(m56,q2)-diff(m26,q5));
308
309 c531= 0.5*( diff(m53,q1)+diff(m51,q3)-diff(m31,q5));
310 c532= 0.5*( diff(m53,q2)+diff(m52,q3)-diff(m32,q5));
311 c533= 0.5*( diff(m53,q3)+diff(m53,q3)-diff(m33,q5));
312 c534= 0.5*( diff(m53,q4)+diff(m54,q3)-diff(m34,q5));
313 c535= 0.5*( diff(m53,q5)+diff(m55,q3)-diff(m35,q5));
314 c536= 0.5*( diff(m53,q6)+diff(m56,q3)-diff(m36,q5));
315
316 c541= 0.5*( diff(m54,q1)+diff(m51,q4)-diff(m41,q5));
317 c542= 0.5*( diff(m54,q2)+diff(m52,q4)-diff(m42,q5));
318 c543= 0.5*( diff(m54,q3)+diff(m53,q4)-diff(m43,q5));
319 c544= 0.5*( diff(m54,q4)+diff(m54,q4)-diff(m44,q5));
320 c545= 0.5*( diff(m54,q5)+diff(m55,q4)-diff(m45,q5));
321 c546= 0.5*( diff(m54,q6)+diff(m56,q4)-diff(m46,q5));
322
323 c551= 0.5*( diff(m55,q1)+diff(m51,q5)-diff(m51,q5));
324 c552= 0.5*( diff(m55,q2)+diff(m52,q5)-diff(m52,q5));
325 c553= 0.5*( diff(m55,q3)+diff(m53,q5)-diff(m53,q5));
326 c554= 0.5*( diff(m55,q4)+diff(m54,q5)-diff(m54,q5));
327 c555= 0.5*( diff(m55,q5)+diff(m55,q5)-diff(m55,q5));
328 c556= 0.5*( diff(m55,q6)+diff(m56,q5)-diff(m56,q5));
329
330 c561= 0.5*( diff(m56,q1)+diff(m51,q6)-diff(m61,q5));
331 c562= 0.5*( diff(m56,q2)+diff(m52,q6)-diff(m62,q5));
332 c563= 0.5*( diff(m56,q3)+diff(m53,q6)-diff(m63,q5));
333 c564= 0.5*( diff(m56,q4)+diff(m54,q6)-diff(m64,q5));
334 c565= 0.5*( diff(m56,q5)+diff(m55,q6)-diff(m65,q5));
335 c566= 0.5*( diff(m56,q6)+diff(m56,q6)-diff(m66,q5));
336
337 c611= 0.5*( diff(m61,q1)+diff(m61,q1)-diff(m11,q6));
338 c612= 0.5*( diff(m61,q1)+diff(m62,q1)-diff(m12,q6));
339 c613= 0.5*( diff(m61,q3)+diff(m63,q1)-diff(m13,q6));
340 c614= 0.5*( diff(m61,q4)+diff(m64,q1)-diff(m14,q6));
341 c615= 0.5*( diff(m61,q5)+diff(m65,q1)-diff(m15,q6));

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342 c616= 0.5*( diff(m61,q6)+diff(m66,q1)-diff(m16,q6));
343
344 c621= 0.5*( diff(m62,q1)+diff(m61,q2)-diff(m21,q6));
345 c622= 0.5*( diff(m62,q1)+diff(m62,q2)-diff(m22,q6));
346 c623= 0.5*( diff(m62,q3)+diff(m63,q2)-diff(m23,q6));
347 c624= 0.5*( diff(m62,q4)+diff(m64,q2)-diff(m24,q6));
348 c625= 0.5*( diff(m62,q5)+diff(m65,q2)-diff(m25,q6));
349 c626= 0.5*( diff(m62,q6)+diff(m66,q2)-diff(m26,q6));
350
351 c631= 0.5*( diff(m63,q1)+diff(m61,q3)-diff(m31,q6));
352 c632= 0.5*( diff(m63,q1)+diff(m62,q3)-diff(m32,q6));
353 c633= 0.5*( diff(m63,q3)+diff(m63,q3)-diff(m33,q6));
354 c634= 0.5*( diff(m63,q4)+diff(m64,q3)-diff(m34,q6));
355 c635= 0.5*( diff(m63,q5)+diff(m65,q3)-diff(m35,q6));
356 c636= 0.5*( diff(m63,q6)+diff(m66,q3)-diff(m36,q6));
357
358 c641= 0.5*( diff(m64,q1)+diff(m61,q4)-diff(m41,q6));
359 c642= 0.5*( diff(m64,q1)+diff(m62,q4)-diff(m42,q6));
360 c643= 0.5*( diff(m64,q3)+diff(m63,q4)-diff(m43,q6));
361 c644= 0.5*( diff(m64,q4)+diff(m64,q4)-diff(m44,q6));
362 c645= 0.5*( diff(m64,q5)+diff(m65,q4)-diff(m45,q6));
363 c646= 0.5*( diff(m64,q6)+diff(m66,q4)-diff(m46,q6));
364
365 c651= 0.5*( diff(m65,q1)+diff(m61,q5)-diff(m51,q6));
366 c652= 0.5*( diff(m65,q1)+diff(m62,q5)-diff(m52,q6));
367 c653= 0.5*( diff(m65,q3)+diff(m63,q5)-diff(m53,q6));
368 c654= 0.5*( diff(m65,q4)+diff(m64,q5)-diff(m54,q6));
369 c655= 0.5*( diff(m65,q5)+diff(m65,q5)-diff(m55,q6));
370 c656= 0.5*( diff(m65,q6)+diff(m66,q5)-diff(m56,q6));
371
372 c661= 0.5*( diff(m66,q1)+diff(m61,q6)-diff(m61,q6));
373 c662= 0.5*( diff(m66,q1)+diff(m62,q6)-diff(m62,q6));
374 c663= 0.5*( diff(m66,q3)+diff(m63,q6)-diff(m63,q6));
375 c664= 0.5*( diff(m66,q4)+diff(m64,q6)-diff(m64,q6));
376 c665= 0.5*( diff(m66,q5)+diff(m65,q6)-diff(m65,q6));
377 c666= 0.5*( diff(m66,q6)+diff(m66,q6)-diff(m66,q6));
378
379 c11= c111*diff(q1)+c112*diff(q2)+c113*diff(q3)+c114*diff(
    q4)+c115*diff(q5)+c116*diff(q6);
380 c12= c121*diff(q1)+c122*diff(q2)+c123*diff(q3)+c124*diff(
    q4)+c125*diff(q5)+c126*diff(q6);
381 c13= c131*diff(q1)+c132*diff(q2)+c133*diff(q3)+c134*diff(
    q4)+c135*diff(q5)+c136*diff(q6);
382 c14= c141*diff(q1)+c142*diff(q2)+c143*diff(q3)+c144*diff(
    q4)+c145*diff(q5)+c146*diff(q6);
383 c15= c151*diff(q1)+c152*diff(q2)+c153*diff(q3)+c154*diff(

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    q4)+c155*diff(q5)+c156*diff(q6);
384 c16= c161*diff(q1)+c162*diff(q2)+c163*diff(q3)+c164*diff(
    q4)+c165*diff(q5)+c166*diff(q6);
385 c21= c211*diff(q1)+c212*diff(q2)+c213*diff(q3)+c214*diff(
    q4)+c215*diff(q5)+c216*diff(q6);
386 c22= c221*diff(q1)+c222*diff(q2)+c223*diff(q3)+c224*diff(
    q4)+c225*diff(q5)+c226*diff(q6);
387 c23= c231*diff(q1)+c232*diff(q2)+c233*diff(q3)+c234*diff(
    q4)+c235*diff(q5)+c236*diff(q6);
388 c24= c241*diff(q1)+c242*diff(q2)+c243*diff(q3)+c244*diff(
    q4)+c245*diff(q5)+c246*diff(q6);
389 c25= c251*diff(q1)+c252*diff(q2)+c253*diff(q3)+c254*diff(
    q4)+c255*diff(q5)+c256*diff(q6);
390 c26= c261*diff(q1)+c262*diff(q2)+c263*diff(q3)+c264*diff(
    q4)+c265*diff(q5)+c266*diff(q6);
391 c31= c311*diff(q1)+c312*diff(q2)+c313*diff(q3)+c314*diff(
    q4)+c315*diff(q5)+c316*diff(q6);
392 c32= c321*diff(q1)+c322*diff(q2)+c323*diff(q3)+c324*diff(
    q4)+c325*diff(q5)+c326*diff(q6);
393 c33= c331*diff(q1)+c332*diff(q2)+c333*diff(q3)+c334*diff(
    q4)+c335*diff(q5)+c336*diff(q6);
394 c34= c341*diff(q1)+c342*diff(q2)+c343*diff(q3)+c344*diff(
    q4)+c345*diff(q5)+c346*diff(q6);
395 c35= c351*diff(q1)+c352*diff(q2)+c353*diff(q3)+c354*diff(
    q4)+c355*diff(q5)+c356*diff(q6);
396 c36= c361*diff(q1)+c362*diff(q2)+c363*diff(q3)+c364*diff(
    q4)+c365*diff(q5)+c366*diff(q6);
397 c41= c411*diff(q1)+c412*diff(q2)+c413*diff(q3)+c414*diff(
    q4)+c415*diff(q5)+c416*diff(q6);
398 c42= c421*diff(q1)+c422*diff(q2)+c423*diff(q3)+c424*diff(
    q4)+c425*diff(q5)+c426*diff(q6);
399 c43= c431*diff(q1)+c432*diff(q2)+c433*diff(q3)+c434*diff(
    q4)+c435*diff(q5)+c436*diff(q6);
400 c44= c441*diff(q1)+c442*diff(q2)+c443*diff(q3)+c444*diff(
    q4)+c445*diff(q5)+c446*diff(q6);
401 c45= c451*diff(q1)+c452*diff(q2)+c453*diff(q3)+c454*diff(
    q4)+c455*diff(q5)+c456*diff(q6);
402 c46= c461*diff(q1)+c462*diff(q2)+c463*diff(q3)+c464*diff(
    q4)+c465*diff(q5)+c466*diff(q6);
403 c51= c511*diff(q1)+c512*diff(q2)+c513*diff(q3)+c514*diff(
    q4)+c515*diff(q5)+c516*diff(q6);
404 c52= c521*diff(q1)+c522*diff(q2)+c523*diff(q3)+c524*diff(
    q4)+c525*diff(q5)+c526*diff(q6);
405 c53= c531*diff(q1)+c532*diff(q2)+c533*diff(q3)+c534*diff(
    q4)+c535*diff(q5)+c536*diff(q6);
406 c54= c541*diff(q1)+c542*diff(q2)+c543*diff(q3)+c544*diff(

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    q4)+c545*diff(q5)+c546*diff(q6);
407 c55= c551*diff(q1)+c552*diff(q2)+c553*diff(q3)+c554*diff(
    q4)+c555*diff(q5)+c556*diff(q6);
408 c56= c561*diff(q1)+c562*diff(q2)+c563*diff(q3)+c564*diff(
    q4)+c565*diff(q5)+c566*diff(q6);
409 c61= c611*diff(q1)+c612*diff(q2)+c613*diff(q3)+c614*diff(
    q4)+c615*diff(q5)+c616*diff(q6);
410 c62= c621*diff(q1)+c622*diff(q2)+c623*diff(q3)+c624*diff(
    q4)+c625*diff(q5)+c626*diff(q6);
411 c63= c631*diff(q1)+c632*diff(q2)+c633*diff(q3)+c634*diff(
    q4)+c635*diff(q5)+c636*diff(q6);
412 c64= c641*diff(q1)+c642*diff(q2)+c643*diff(q3)+c644*diff(
    q4)+c645*diff(q5)+c646*diff(q6);
413 c65= c651*diff(q1)+c652*diff(q2)+c653*diff(q3)+c654*diff(
    q4)+c655*diff(q5)+c656*diff(q6);
414 c66= c661*diff(q1)+c662*diff(q2)+c663*diff(q3)+c664*diff(
    q4)+c665*diff(q5)+c666*diff(q6);
415
416 Cq=[c11 c12 c13 c14 c15 c26;...
417      c21 c22 c23 c24 c25 c26;...
418      c31 c32 c33 c34 c35 c36;...
419      c41 c42 c43 c44 c45 c46;...
420      c51 c52 c53 c54 c55 c56;...
421      c61 c62 c63 c64 c65 c66];
422
423 C=simplify(Cq)
424
425 %Gravity
426 g0=[0;0;-g];
427
428 g1= m1*g0'*jv1(:,1)+m2*g0'*jv1(:,2)+m3*g0'*jv1(:,3)+m4*g0
    '*jv1(:,4)+m5*g0'*jv1(:,5)+m6*g0'*jv1(:,6);
429 g2= m1*g0'*jv2(:,1)+m2*g0'*jv2(:,2)+m3*g0'*jv2(:,3)+m4*g0
    '*jv2(:,4)+m5*g0'*jv2(:,5)+m6*g0'*jv2(:,6);
430 g3= m1*g0'*jv3(:,1)+m2*g0'*jv3(:,2)+m3*g0'*jv3(:,3)+m4*g0
    '*jv3(:,4)+m5*g0'*jv3(:,5)+m6*g0'*jv3(:,6);
431 g4= m1*g0'*jv4(:,1)+m2*g0'*jv4(:,2)+m3*g0'*jv4(:,3)+m4*g0
    '*jv4(:,4)+m5*g0'*jv4(:,5)+m6*g0'*jv4(:,6);
432 g5= m1*g0'*jv5(:,1)+m2*g0'*jv5(:,2)+m3*g0'*jv5(:,3)+m4*g0
    '*jv5(:,4)+m5*g0'*jv5(:,5)+m6*g0'*jv5(:,6);
433 g6= m1*g0'*jv6(:,1)+m2*g0'*jv6(:,2)+m3*g0'*jv6(:,3)+m4*g0
    '*jv6(:,4)+m5*g0'*jv6(:,5)+m6*g0'*jv6(:,6);
434
435 gq=[g1; g2; g3; g4; g5; g6];
436
437 g=simplify(gq)

```

```

438
439 ddq= [diff(diff(q1)); diff(diff(q2)); diff(diff(q3));
         diff(diff(q4)); diff(diff(q5)); diff(diff(q6))];
440 dq = [diff(q1); diff(q2); diff(q3); diff(q4); diff(q5);
         diff(q6)];
441
442 tau= simplify(M*ddq + C*dq + g)

```