## Правила тригонометрии

(1) 
$$\sin \alpha \cdot \sin \beta = \frac{1}{2} \left[ \cos (\alpha - \beta) - \cos (\alpha + \beta) \right]$$

(2) 
$$\cos \alpha \cdot \cos \beta = \frac{1}{2} \left[ \cos (\alpha - \beta) + \cos (\alpha + \beta) \right]$$

(3) 
$$\sin \alpha \cdot \cos \beta = \frac{1}{2} \left[ \sin (\alpha - \beta) + \sin (\alpha + \beta) \right]$$

(4) 
$$\cos \alpha \cdot \sin \beta = -\frac{1}{2} \left[ \sin (\alpha - \beta) - \sin (\alpha + \beta) \right]$$

Строки 31–33 в тексте программы ( $\Omega_1 << \omega_1$ ):

$$\begin{split} u_1 &= A_1 \cdot \left(1 + m_1 \cdot \sin \Omega_1 t\right) \cdot \sin \omega_1 t \\ &= A_1 \cdot \sin \omega_1 t + m_1 \cdot A_1 \cdot \sin \Omega_1 t \cdot \sin \omega_1 t \\ &= A_1 \cdot \sin \omega_1 t + m_1 \cdot A_1 \cdot \frac{1}{2} \cdot \left[\cos \left(\Omega_1 - \omega_1\right) t - \cos \left(\Omega_1 + \omega_1\right) t\right] \\ &= A_1 \cdot \sin \omega_1 t + m_1 \cdot A_1 \cdot \frac{1}{2} \cdot \left[\cos \left(\omega_1 - \Omega_1\right) t - \cos \left(\omega_1 + \Omega_1\right) t\right] \end{split}$$

Строки 34–36 в тексте программы ( $\Omega_2 << \omega_2$ ):

$$\begin{split} u_2 &= A_2 \cdot \left(1 + m_2 \cdot \cos \Omega_2 t\right) \cdot \sin \omega_2 t \\ &= A_2 \cdot \sin \omega_2 t + m_2 \cdot A_2 \cdot \cos \Omega_2 t \cdot \sin \omega_2 t \\ &= A_2 \cdot \sin \omega_2 t - m_2 \cdot A_2 \cdot \frac{1}{2} \cdot \left[\sin \left(\Omega_2 - \omega_2\right) t - \sin \left(\Omega_2 + \omega_2\right) t\right] \\ &= A_2 \cdot \sin \omega_2 t + m_2 \cdot A_2 \cdot \frac{1}{2} \cdot \left[\sin \left(\omega_2 - \Omega_2\right) t + \sin \left(\omega_2 + \Omega_2\right) t\right] \end{split}$$