MA-202 Numerical Techniques (2022)

Assignment - 07 Submission

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Exercise 1

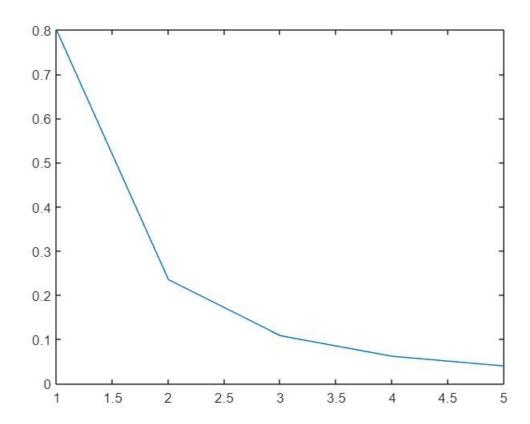
A) Consider $g(x) = \frac{1}{x^2 + 0.25}$ the function where is a real number. data

random data set having n+1 data points in the interval . At each of these points evaluate the function , and construct the data . Now write a program to find the interpolating polynomial using both the Lagrange method and the Newton divided difference method. Use the above generated data to find the interpolating polynomial using both these methods. Plots the results obtained, along with the original function and the original data. Do this exercise for n = 3,5,8,10,20

B) Do the same exercise but now take the data points $\{x0, x1, \dots xn\}$ to be equispaced in the interval. Comment on the results obtained in both the cases and with both the methods.

```
1011 ×
                        0.0000
    0.0000
            0.0000
                                  0.0000
                                            3.6002
A = 1 \times 5
    0.8000
              0.2353
                        0.1081
                                  0.0615
                                            0.0396
disp(A)
    0.8000
              0.2353
                        0.1081
                                  0.0615
                                            0.0396
```

```
% here we are plotting a point (xi , yi).
plot(x, A);
```



```
%Interpolating method (Lagrange's)
sum = 0;
vals = [3, 5, 8, 10, 20];
ans = [];
syms a for
k = 1:5
    for i = 1:length(x)
        u = 1;
l = 1;
    for j = 1:length(x)
if j ~= i
        u = u * (a - x(j));
l = l * (x(i) - x(j));
    end
end
```

```
sum= sum + u / l * A(i);
end
ans = [ans subs(sum, vals(k))];
end
ans =
```

$$\left(\frac{4}{37} \ \frac{8}{101} \ \frac{10097916}{825877} \ \frac{64103504}{825877} \ \frac{215073380}{48581}\right)$$

```
fprintf("Interpolating Polynomial Using Lagrange's .....\n")
```

Interpolating Polynomial Using Lagrange's

disp(sum);

$$\frac{5\;(a-1)\;(a-2)\;(a-3)\;(a-4)}{606} - \frac{2\;(a-1)\;(a-2)\;(a-3)\;(a-5)}{39} + \frac{5\;(a-1)\;(a-2)\;(a-4)\;(a-5)}{37} - \frac{1}{37} - \frac{$$

```
Newton's Divided Difference Implementation and finding polynomial. ddTable = divDiff(x, A); disp('the divided difference table is : ')
```

the divided difference table is :

disp(ddTable)

```
0.8000 -0.5647
                 0.2188 -0.0595
                                   0.0125
0.2353 -0.1272 0.0403 -0.0093
                                   0
0.1081
     -0.0466
              0.0123
                        0
                                    0
0.0615
      -0.0219
                0
                            0
   0.0396
                       0
                                       0
```

```
syms X newSum =
[]; sum = 0; for k
= 1:5 for i =
1:size(x,2)
        sum = sum + prod(X - x(:,1:i))*divDiff(1,i+1);
end
Y = A(1) + sum;
newSum = [newSum subs(Y, vals(k))];
end
newSum
```

newSum =

$$\left(\frac{54}{5} \quad \frac{2604}{5} \quad \frac{304504}{5} \quad \frac{2161804}{5} \quad \frac{221540004}{5}\right)$$

```
disp('Newton"s divided difference polynomial');
```

Newton"s divided difference polynomial

```
disp(Y)
10 X + 15 (X - 1) (X - 2) + 20 (X - 1) (X - 2) (X - 3) + 25 (X - 1) (X - 2) (X - 3) (X - 4) + 30 (X - 4)
```

Exercise 2

Do the same exercise as above, now for the function $g(x) = xe^{-x^2}$. Comment on the results obtained in this case.

```
for i=1:length(x)
                               A(i) =
x(i)*(exp((-x(i))^2)) end
A = 1 \times 5
    2.7183
                0.2353
                            0.1081
                                       0.0615
                                                   0.0396
A = 1 \times 5
                            0.1081
    2.7183 109.1963
                                       0.0615
                                                   0.0396
A = 1 \times 5
10<sup>4</sup> ×
    0.0003
                0.0109
                            2.4309
                                       0.0000
                                                   0.0000
A = 1 \times 5
10<sup>7</sup> ×
    0.0000
                0.0000
                            0.0024
                                       3.5544
                                                   0.0000
A = 1 \times 5
1011 X
    0.0000
                0.0000
                            0.0000
                                       0.0004
                                                   3.6002
disp(A)
   1.0e+11 *
    0.0000
                0.0000
                            0.0000
                                       0.0004
                                                   3.6002
```

Interpolating Polynomial Using Lagrange's

```
disp(sum)
```

```
\frac{5898641353718651\ (a-1)\ (a-2)\ (a-3)\ (a-4)}{393216} - \frac{149084195602433\ (a-1)\ (a-2)\ (a-3)\ (a-5)}{25165824} + \frac{149084195602433\ (a-1)\ (a-2)\ (a-3)\ (a-3)\ (a-1)\ (a-2)\ (a-3)\ (a-1)\ (a-3)\ (a-1)\ (a-2)\ (a-3)\ (a-1)\ (a-3)\ (a-3)\ (a-1)\ (a-3)\ (a-3)\ (a-1)\ (a-3)\ (a-3
```

```
Newton's Divided Difference Implementation and finding polynomial. ddTable = divDiff(x, A); disp('the divided difference table is : ')
```

the divided difference table is :

disp(ddTable)

```
1.0e+11 *
   0.0000
             0.0000
                        0.0000
                                  0.0001
                                             0.1500
0.0000
          0.0000
                    0.0002
                              0.5999
0.0000
          0.0004
                    1.7998
                                   0
                                              0
0.0004
          3.5999
                         0
                                   0
                                              0
   3.6002
                             0
                                       0
                                                  0
```

```
syms X
sum = 0;
for i = 1:size(x,2)
        sum = sum + prod(X - x(:,1:i))*divDiff(1,i+1);
end
Y = A(1) + sum;
disp('Newton"s divided difference polynomial');
```

Newton"s divided difference polynomial

```
disp(Y)
```

```
2X + 3(X - 1)(X - 2) + 4(X - 1)(X - 2)(X - 3) + 5(X - 1)(X - 2)(X - 3)(X - 4) + 6(X - 1)(X - 3)(X - 4) + 6(X - 3)(X - 4)(X - 3)(X - 4) + 6(X - 3)(X - 4)(X - 3)(X - 4) + 6(X - 3)(X - 4)(X - 3)(X - 4)(X - 3)(X - 4) + 6(X - 3)(X - 4)(X - 3)(X - 4)(X - 3)(X - 4)(X - 4)(X
```