# Computational Linguistics

Natural Language Processing

University of Maryland

Classification Examples

## Reminder: Logistic Regression

$$P(Y=0|X) = \frac{1}{1 + \exp\left[\beta_0 + \sum_i \beta_i X_i\right]}$$
(1)

$$P(Y=1|X) = \frac{\exp\left[\beta_0 + \sum_i \beta_i X_i\right]}{1 + \exp\left[\beta_0 + \sum_i \beta_i X_i\right]}$$
(2)

- Discriminative prediction: p(y|x)
- Classification uses: ad placement, spam detection
- What we didn't talk about is how to learn  $\beta$  from data

#### Logistic Regression: Objective Function

$$\mathcal{L} \equiv \ln \rho(Y|X,\beta) = \sum_{j} \ln \rho(y^{(j)}|x^{(j)},\beta)$$

$$= \sum_{j} y^{(j)} \left(\beta_0 + \sum_{i} \beta_i x_i^{(j)}\right) - \ln \left[1 + \exp\left(\beta_0 + \sum_{i} \beta_i x_i^{(j)}\right)\right]$$
(4)

#### Algorithm

- 1. Initialize a vector B to be all zeros
- 2. For t = 1, ..., T
  - For each example  $\vec{x}_i$ ,  $y_i$  and feature j:
- 3. Output the parameters  $\beta_1, \ldots, \beta_d$ .

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
  
$$\vec{\beta} = \langle \beta_{bias} = 0, \beta_A = 0, \beta_B = 0, \beta_C = 0, \beta_D = 0 \rangle$$

 $y_1 = 1$ 

#### AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

$$y_2 = 0$$

BCCCDDDD

You first see the positive example. First, compute  $\pi_1$ 

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
$$\vec{\beta} = \langle 0, 0, 0, 0, 0 \rangle$$

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You first see the positive example. First, compute  $\pi_1$ 

$$\pi_1 = \Pr(y_1 = 1 \mid \vec{x_1}) = \frac{\exp \beta^T x_i}{1 + \exp \beta^T x_i} =$$

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(Assume step size  $\lambda = 1.0$ .)

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BCCCDDDD

You first see the positive example. First, compute 
$$\pi_1$$
  $\pi_1 = \Pr(y_1 = 1 \mid \vec{x_1}) = \frac{\exp \beta^T x_i}{1 + \exp \beta^T x_i} = \frac{\exp 0}{\exp 0 + 1} = 0.5$ 

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
$$\vec{\beta} = \langle 0, 0, 0, 0, 0 \rangle$$

 $y_1 = 1$ 

AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

$$y_2 = 0$$

BCCCDDDD

 $\pi_1 = 0.5$  What's the update for  $\beta_{bias}$ ?

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
$$\vec{\beta} = \langle 0, 0, 0, 0, 0 \rangle$$

 $y_1 = 1$ 

#### AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

$$y_2 = 0$$

BCCCDDDD

What's the update for  $\beta_{\it bias}$ ?

$$\beta_{bias} = \beta'_{bias} + \lambda \cdot (y_1 - \pi_1) \cdot x_{1,bias} = 0.0 + 1.0 \cdot (1.0 - 0.5) \cdot 1.0$$

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What's the update for  $\beta_{\it bias}$ ?

$$\beta_{bias} = \beta'_{bias} + \lambda \cdot (y_1 - \pi_1) \cdot x_{1,bias} = 0.0 + 1.0 \cdot (1.0 - 0.5) \cdot 1.0 = 0.5$$

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AAAABBBC

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BCCCDDDD

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AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

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BCCCDDDD

$$\beta_A = \beta_A' + \lambda \cdot (y_1 - \pi_1) \cdot x_{1,A} = 0.0 + 1.0 \cdot (1.0 - 0.5) \cdot 4.0$$

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AAAABBBC

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BCCCDDDD

$$\beta_A = \beta_A' + \lambda \cdot (y_1 - \pi_1) \cdot x_{1,A} = 0.0 + 1.0 \cdot (1.0 - 0.5) \cdot 4.0 = 2.0$$

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BCCCDDDD

What's the update for 
$$\beta_B$$
?

$$\beta_B = \beta_B' + \lambda \cdot (y_1 - \pi_1) \cdot x_{1,B} = 0.0 + 1.0 \cdot (1.0 - 0.5) \cdot 3.0$$

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AAAABBBC

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BCCCDDDD

$$\beta_B = \beta_B' + \lambda \cdot (y_1 - \pi_1) \cdot x_{1,B} = 0.0 + 1.0 \cdot (1.0 - 0.5) \cdot 3.0$$
 =1.5

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
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AAAABBBC

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BCCCDDDD

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
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 $y_1 = 1$ 

AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

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BCCCDDDD

What's the update for  $\beta_C$ ?  $\beta_C = \beta_C' + \lambda \cdot (y_1 - \pi_1) \cdot x_{1,C} = 0.0 + 1.0 \cdot (1.0 - 0.5) \cdot 1.0$ 

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
$$\vec{\beta} = \langle 0, 0, 0, 0, 0 \rangle$$

 $y_1 = 1$ 

AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

 $y_2 = 0$ 

BCCCDDDD

$$\beta_C = \beta_C' + \lambda \cdot (y_1 - \pi_1) \cdot x_{1,C} = 0.0 + 1.0 \cdot (1.0 - 0.5) \cdot 1.0 = 0.5$$

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
$$\vec{\beta} = \langle 0, 0, 0, 0, 0 \rangle$$

 $y_1 = 1$ 

AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

 $y_2 = 0$ 

BCCCDDDD

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
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AAAABBBC

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BCCCDDDD

$$\beta_D = \beta_D' + \lambda \cdot (y_1 - \pi_1) \cdot x_{1,D} = 0.0 + 1.0 \cdot (1.0 - 0.5) \cdot 0.0$$

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
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AAAABBBC

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BCCCDDDD

$$\beta_D = \beta_D' + \lambda \cdot (y_1 - \pi_1) \cdot x_{1,D} = 0.0 + 1.0 \cdot (1.0 - 0.5) \cdot 0.0 = 0.0$$

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
  
$$\vec{\beta} = \langle .5, 2, 1.5, 0.5, 0 \rangle$$

$$y_1 = 1$$

#### AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

$$y_2 = 0$$

BCCCDDDD

Now you see the negative example. What's  $\pi_2$ ?

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
  
$$\vec{\beta} = \langle .5, 2, 1.5, 0.5, 0 \rangle$$

$$v_1 = 1$$

#### AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

$$y_2 = 0$$

BCCCDDDD

Now you see the negative example. What's 
$$\pi_2$$
? 
$$\pi_2 = \Pr(y_2 = 1 \mid \vec{x_2}) = \frac{\exp \beta^T x_i}{1 + \exp \beta^T x_i} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\}} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\}} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\}} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 0\}} = \frac{\exp \{.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 0\}} = \frac{\exp \{.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 0\}} = \frac{\exp \{.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 0\}} = \frac{\exp \{.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 0\}} = \frac{\exp \{.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 0\}} = \frac{\exp \{.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 0\}} = \frac{\exp \{.5 + 1.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0\}}{\exp \{.5 + 0.5 + 0\}} = \frac{\exp \{.5 + 0.5 + 0.5 + 0\}}{\exp \{.5$$

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
  
$$\vec{\beta} = \langle .5, 2, 1.5, 0.5, 0 \rangle$$

$$y_1 = 1$$

#### AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

$$y_2 = 0$$

BCCCDDDD

Now you see the negative example. What's 
$$\pi_2$$
?  

$$\pi_2 = \Pr(y_2 = 1 \mid \vec{x_2}) = \frac{\exp \beta^T x_i}{1 + \exp \beta^T x_i} = \frac{\exp \{.5 + 1.5 + 1.5 + 0\}}{\exp \{.5 + 1.5 + 1.5 + 0\} + 1} = 0.97$$

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
$$\vec{\beta} = \langle .5, 2, 1.5, 0.5, 0 \rangle$$

 $y_1 = 1$ 

#### AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

 $y_2 = 0$ 

BCCCDDDD

Now you see the negative example. What's  $\pi_2$ ?

 $\pi_2 = 0.97$ 

What's the update for  $\beta_{\it bias}$ ?

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
$$\vec{\beta} = \langle .5, 2, 1.5, 0.5, 0 \rangle$$

$$y_1 = 1$$

#### AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

$$y_2 = 0$$

BCCCDDDD

What's the update for  $\beta_{bias}$ ?

$$\beta_{bias} = \beta'_{bias} + \lambda \cdot (y_2 - \pi_2) \cdot x_{2,bias} = 0.5 + 1.0 \cdot (0.0 - 0.97) \cdot 1.0$$

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
$$\vec{\beta} = \langle .5, 2, 1.5, 0.5, 0 \rangle$$

$$y_1 = 1$$

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(Assume step size  $\lambda = 1.0$ .)

$$y_2 = 0$$

BCCCDDDD

What's the update for  $\beta_{bias}$ ?

$$\beta_{bias} = \beta'_{bias} + \lambda \cdot (y_2 - \pi_2) \cdot x_{2,bias} = 0.5 + 1.0 \cdot (0.0 - 0.97) \cdot 1.0 = -0.47$$

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
  
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$$y_1 = 1$$

#### AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

$$y_2 = 0$$

BCCCDDDD

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
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$$y_1 = 1$$

#### AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

$$y_2 = 0$$

BCCCDDDD

What's the update for 
$$\beta_A$$
?  
 $\beta_A = \beta'_A + \lambda \cdot (y_2 - \pi_2) \cdot x_{2,A} = 2.0 + 1.0 \cdot (0.0 - 0.97) \cdot 0.0$ 

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
$$\vec{\beta} = \langle .5, 2, 1.5, 0.5, 0 \rangle$$

$$y_1 = 1$$

#### AAAABBBC

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BCCCDDDD

What's the update for 
$$\beta_A$$
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 $\beta_A = \beta'_A + \lambda \cdot (y_2 - \pi_2) \cdot x_{2,A} = 2.0 + 1.0 \cdot (0.0 - 0.97) \cdot 0.0 = 2.0$ 

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
  
$$\vec{\beta} = \langle .5, 2, 1.5, 0.5, 0 \rangle$$

$$y_1 = 1$$

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$$y_2 = 0$$

BCCCDDDD

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
$$\vec{\beta} = \langle .5, 2, 1.5, 0.5, 0 \rangle$$

$$y_1 = 1$$

#### AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

$$y_2 = 0$$

BCCCDDDD

$$\beta_B = \beta_B' + \lambda \cdot (y_2 - \pi_2) \cdot x_{2,B} = 1.5 + 1.0 \cdot (0.0 - 0.97) \cdot 1.0$$

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
  
$$\vec{\beta} = \langle .5, 2, 1.5, 0.5, 0 \rangle$$

 $y_1 = 1$ 

AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

 $y_2 = 0$ 

BCCCDDDD

$$\beta_B = \beta_B' + \lambda \cdot (y_2 - \pi_2) \cdot x_{2,B} = 1.5 + 1.0 \cdot (0.0 - 0.97) \cdot 1.0 = 0.53$$

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
  
$$\vec{\beta} = \langle .5, 2, 1.5, 0.5, 0 \rangle$$

$$y_1 = 1$$

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$$y_2 = 0$$

BCCCDDDD

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AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

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BCCCDDDD

$$\beta_C = \beta_C' + \lambda \cdot (y_2 - \pi_2) \cdot x_{2,C} = 0.5 + 1.0 \cdot (0.0 - 0.97) \cdot 3.0$$

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
  
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$$y_1 = 1$$

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(Assume step size  $\lambda = 1.0$ .)

$$y_2 = 0$$

BCCCDDDD

What's the update for 
$$\beta_C$$
?

$$\beta_C = \beta_C' + \lambda \cdot (y_2 - \pi_2) \cdot x_{2,C} = 0.5 + 1.0 \cdot (0.0 - 0.97) \cdot 3.0 = -2.41$$

$$\beta[j] = \beta[j] + \lambda(y_i - \pi_i)x_i$$
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$$y_1 = 1$$

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(Assume step size  $\lambda = 1.0$ .)

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BCCCDDDD

What's the update for 
$$\beta_D$$
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$$\beta_D = \beta_D' + \lambda \cdot (y_2 - \pi_2) \cdot x_{2,D} = 0.0 + 1.0 \cdot (0.0 - 0.97) \cdot 4.0$$

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 $y_1 = 1$ 

AAAABBBC

(Assume step size  $\lambda = 1.0$ .)

 $y_2 = 0$ 

BCCCDDDD

$$\beta_D = \beta_D' + \lambda \cdot (y_2 - \pi_2) \cdot x_{2,D} = 0.0 + 1.0 \cdot (0.0 - 0.97) \cdot 4.0$$
 =-3.88

#### Different Activation Function

Your boss demands that you replace the sigmoid function in logistic regression with the trigonometric sin function because it looks the same and he has a sin button on his calculator.

- Plot both between -1 and 1. What would a choice of constants A and B be that would make Asin(Bz) look as much like the logistic function?
- 2. What would be the gradient for an example? How is it different?
- 3. Would there be any other problems with using this formulation?