Q1 Team Name

0 Points

The_Kryptonians

Q2 Commands

10 Points

List the commands used in the game to reach the ciphertext

h

go
climb
pluck
c
back
give
back
back

thrnxxtzy

read

Q3 Analysis

50 Points

Give a detailed analysis of how you figured out the password? (Explain in less than 500 words)

First, we went to a small chamber; there were two holes, one large and the other small. We plucked some mushrooms from the large hole and gave them to a rat sitting inside another hole. The rat told us the magic word "**thrnxxtzy**" for the hidden door to become visible at the main chamber. There we read the glass panel and got our ciphertext.

We were given that the password and g are the elements of a multiplicative group \mathbb{Z}_p^* where p is a prime number. The prime number was p=

455470209427676832372575348833 and three pairs of numbers were given of the form $(a, password \times g^a)$. Let the three pairs be $(a_1,b_1); (a_2,b_2); (a_3,b_3)$.

$$(a_1,b_1)=(429,431955503618234519808008749742) \ (a_2,b_2)=(1973,176325509039323911968355873643) \ (a_3,b_3)=(7596,98486971404861992487294722613)$$

$$b_1 = (password * g^{a_1})$$
 mod p $b_2 = (password * g^{a_2})$ mod p $b_3 = (password * g^{a_3})$ mod p

Our main aim was to eliminate the password and find g and then substitute the value of g in one of the above equations and solve for the password. So dividing the given equations was the best choice. For this first we calculated the modular inverses of b_1 and b_2 :

$$b_1^{-1} = 70749996790223471732904681640$$

 $b_2^{-1} = 228947149478752602606353685125$

Now, let
$$b_{21}=(rac{b_2}{b_1})\%p=(b_2 imes b_1^{-1})\%p$$
 Similarly, $b_{31}=(rac{b_3}{b_1})\%p=(b_3 imes b_1^{-1})\%p$ and $b_{32}=(rac{b_3}{b_2})\%p=(b_3 imes b_2^{-1})\%p$

So, we got three equations from these calculations :

1.
$$\frac{g^{a_2}}{g^{a_1}}=g^{1544}=b_{21}=111590994894663139264552154672$$
2. $\frac{g^{a_3}}{g^{a_1}}=g^{7167}=b_{31}=110411376670918912626907526185$
3. $\frac{g^{a_3}}{g^{a_2}}=g^{5623}=b_{32}=420413074251022028027270785553$

Let us consider equations 1 and 3. Exponent power of g in equations 1 and 3 are coprime. We used Extended Euclidean Algorithm to compute coefficients of Bézout's identity. let c = 1544 and d = 5623. By Bézout's identity:

$$c*x + d*y = gcd (c, d) = gcd (1544, 5623) = 1$$

here x and y are coefficients of Bézout's identity. By the Extended Euclidean Algorithm, $(1544) \times (-2298) +$

$$(5623) \times (631) = 1$$

Therefore,
$$g=((g^{1544})^{2298})^{-1} \times ((g^{5623})^{631}) = ((b_{21})^{2298})^{-1} \times ((b_{32})^{631}) = g\%p = ((b_{21})^{2298})\%p)^{-1})\%p \times ((b_{32})^{631})\%p)$$

 $\implies g = [(155751141548826955446696730154)^{-1} \times 347267008389877298374017667230]\% p$

 $\implies g = [(63673345919111482928118052957) \times 347267008389877298374017667230]\% p$

 \implies g = 52565085417963311027694339

This satisfied the given hint that g is of the form $5__50_4$ 31 94 9

Now, substituting this value of g in the initial step, we get :

$$egin{aligned} password &= [b_1 imes (g^{a_1})^{-1}]\%p \ password &= [(b_1\%p) imes ((g^{a_1})^{-1})\%p]\%p \ \implies password &= \ [431955503618234519808008749742 imes 442956820316148690889301696615]\%p \end{aligned}$$

Finally, the

$\mathbf{Password} = \mathbf{134721542097659029845273957}$

We have used modulus property : (a*b) % p = ((a% p) * (b % p)) % p

We have used fermat's little theroem for prime number p to calculate modular multiplicative inverse n-1

$$a^{p-1} \equiv 1 (mod p)$$

$$a^{p-2} \equiv a^{-1}(modp)$$

References:

https://www.extendedeuclideanalgorithm.com/calculator.php https://planetcalc.com/3311/ https://planetcalc.com/8326/

h

Q4 Password

What was the final command used to clear this level?

134721542097659029845273957

Q5 Codes
O Points

Upload any code that you have used to solve this level

No files uploaded

| Assignment 3 | ● GRADED |
|---|--------------------|
| GROUP Maryam Raza Khan Maulik Singhal Pranshu Gaur View or edit group | |
| TOTAL POINTS | |
| 70 / 70 pts | |
| QUESTION 1 | |
| Team Name | 0 / 0 pts |
| QUESTION 2 | |
| Commands | 10 / 10 pts |
| QUESTION 3 | |
| Analysis | 50 / 50 pts |
| QUESTION 4 | |
| Password | 10 / 10 pts |
| QUESTION 5 | |
| Codes | 0 / 0 pts |
| | |