

Assignment - 1

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Attributes taken = Day, season, fog, rain

Categories =

ON Time	Late	very late	Cancelled
14/20	2/20	3/20	1/20

$$P(Y|x_1, \dots, x_n) = \frac{P(x_1|Y)P(x_2|Y) \dots P(x_n|Y)}{P(x_1)P(x_2)P(x_3) \dots P(x_n)}$$

		class			
Day	Attribute	ON Time	LATE	very late	Cancelled
	weekday	9/14 = 0.64	1/2 = 0.5	3/3 = 1	0/1 = 0
	saturday	2/14 = 0.14	1/2 = 0.5	0/3 = 0	1/1 = 1
	sunday	1/14 = 0.07	0/2 = 0	0/3 = 0	0/1 = 0
	holiday	2/14 = 0.14	0/2 = 0	0/3 = 0	0/1 = 0
Season	Attribute	ON Time	LATE	very late	Cancelled
	Spring	4/14 = 0.29	0/2 = 0	0/3 = 0	0/1 = 0
	Summer	6/14 = 0.43	0/2 = 0	0/3 = 0	0/1 = 0
	Autumn	2/14 = 0.14	0/2 = 0	1/3 = 0.33	0/1 = 0
	winter	2/14 = 0.14	2/2 = 1	2/3 = 0.67	0/1 = 0
Fog	Attribute	ON Time	LATE	very late	Cancelled
	None	5/14 = 0.36	0/2 = 0	0/3 = 0	0/1 = 0
	High	4/14 = 0.29	1/2 = 0.5	1/3 = 0.33	1/1 = 1
	Normal	5/14 = 0.36	1/2 = 0.5	2/3 = 0.67	0/1 = 0
	None	5/14 = 0.36	1/2 = 0.5	1/3 = 0.33	0/1 = 0
Rain	Attribute	ON Time	LATE	very late	Cancelled
	slight	8/14 = 0.57	0/2 = 0	0/3 = 0	0/1 = 0
	heavy	4/14 = 0.29	1/2 = 0.5	2/3 = 0.67	1/1 = 1
		ON Time	LATE	very late	Cancelled
		14/20 = 0.7	2/20 = 0.1	3/20 = 0.15	1/20 = 0.05

FOR EDUCATIONAL USE

$$\chi^2 = \sum_{i=1}^m \sum_{j=1}^n \frac{(O_{ij} - E_{ij})^2}{E_{ij}}$$

2. H_0 = Reading preferred & gender are not correlated in the group.

H_1 = Both are correlated.

Computing the χ^2 ,

$$E_{ij} = \frac{\text{Count}(A=a_i) \times \text{Count}(B=b_j)}{n}$$

$$\chi^2 = \frac{(250-90)^2}{90} + \frac{(50-210)^2}{210} + \frac{(200-360)^2}{360} + \frac{(1000-840)^2}{840}$$

$$= 284.44 + 121.90 + 71.11 + 30.48 = 507.93$$

$$\text{For } 2 \times 2 = \text{Degree of freedom} = (2-1)(2-1) = 1$$

For 1 degree of freedom, χ^2 value needed to reject the hypothesis at 0.01 significance level is 10.828 (from table)

We reject the null hypothesis that gender and preferred reading are independent (∵ the calculated value is above it)

∴ we conclude that 2 attributes are correlated for the given group.