

# Hierarchical Memory Algorithms - Mid Semester Examinations

14:00 -16:00

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## INSTRUCTIONS

1. All questions carry 10 marks
2. **DO NOT DISCUSS OR SEARCH THE INTERNET.**
3. For every question, assume that the input could be much larger than the internal memory.
4. Argue clearly about the I/O complexity of your algorithm.
5. If your work is not legible, I won't be able to read it and you may not get credits for your work.
6. Keep your video feeds on throughout the examination. You are allowed to take a single biobreak of at most 5 minute.

1. Design an algorithm to compute the product of two numbers.
2. Assume that you are given a number  $n$  in binary. Design an algorithm to compute  $n \bmod 3$ .
3. Assume that you are given a number  $n$  is binary. Design an algorithm to compute  $n \bmod 13$ .
4. Assume that you are given two sorted arrays  $A$  and  $B$  of integers. Compute the median of the  $A$  and  $B$  combined. You may assume that the elements are distinct.
5. Consider  $n$  water tanks in  $\mathbb{R}^2$ . Assume that each tank has a height and associated list of neighboring tanks. If tank  $A$  is a neighbour of tank  $B$  and height of  $A$  is greater than height of  $B$ , water from  $A$  will be eventually drained to  $B$ . If there are multiple neighbors at lower height, water flow into all those neighbors. Design an algorithm to find all the tanks that can contain water in the steady state.

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