22b2153

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2 Steps and Major Decisions Taken to arrive at Solution

2.1 Steps:

- 1. Initial Data Exploration: Imported Libraries: Utilized Pandas, NumPy, Matplotlib, Seaborn, Statsmodels, and Scikit-learn. Loaded Dataset: Read and examined the "toptex.csv" dataset containing customer information. Data Information: Explored data types, non-null counts, and descriptive statistics to understand the dataset.
- 2. Data Visualization: Pair Plot: Employed pair plots to visualize relationships between different variables. Correlation Heatmap: Created a heatmap to highlight correlations among variables.
- 3. Linear Regression Modeling: Feature Selection: Chose 'accompanying_people', 'time_in_store', and 'Residence_distance_from_store' based on correlation analysis. Data Splitting: Segregated the data into training and testing sets. Linear Regression: Utilized Ordinary Least Squares (OLS) to build a regression model. Model Evaluation: Assessed model performance using R-squared, Mean Squared Error (MSE), and related metrics.
- 4. Random Forest Modeling: Data Preprocessing: Applied standard scaling and feature engineering. Model Building: Constructed Linear Regression and Random Forest models. Model Evaluation: Examined model performance using Mean Squared Error. Feature Importance: Analyzed feature importance using Random Forest models.
- 5. Overall Purchase Prediction: Linear Regression Model: Employed a Linear Regression model to predict the overall value of purchases. Visualization: Plotted predictions against actual values using scatter plots and a 3D scatter plot.
- 6. Principal Component Analysis (PCA): Feature Reduction: Applied PCA for dimensionality reduction. Linear Regression: Built a Linear Regression model using the reduced feature set. Model Evaluation: Assessed the model's performance.
- 7. Hypothesis Testing and Correlation Analysis: T-tests: Conducted t-tests to compare total purchase amounts between gender groups. Pearson Correlation: Calculated the correlation between time in store and total purchase amount.
- 8. Executive Recommendations: Actionable Insights: Provided targeted recommendations based on analysis results, such as gender-specific marketing and strategies to increase time spent in the store.
- 9. Additional Analysis and Visualizations: Distribution Plots: Visualized the distribution of each variable. Residual Analysis: Examined residuals through scatter plots. Scree Plot: Visualized explained variance in PCA using a scree plot.
- 10. Statistical Testing: Durbin-Watson and Jarque-Bera Tests: Ensured normal distribution of errors in regression models.

- 11. Communication: Clear Explanations: Presented results with clear explanations, interpretations, and visualizations. Structured Documentation: Organized the analysis into well-defined steps.
- 12. Additional Model Evaluation: Comparative Analysis: Evaluated the performance of Linear Regression and Random Forest models for both purchase and engagement predictions.

3 Importing Required Libraries and Packages

```
[21]: import pandas as pd
  import numpy as np
  import matplotlib.pyplot as plt
  import seaborn as sns
  import statsmodels.api as sm
  from sklearn.model_selection import train_test_split
  from sklearn.linear_model import LinearRegression
  from sklearn.ensemble import RandomForestRegressor
  from sklearn.metrics import mean_squared_error, r2_score
  from sklearn.preprocessing import StandardScaler
```

4 Importing "toptex.csv" data set using Pandas

```
[22]: data=pd.read_csv("toptex.csv")
      data
                       Gender_F_Flag
[23]:
             Cust ID
                                        Gender M Flag
                                                         Residence distance from store
                    2
      1
                                     1
                                                      0
                                                                                         4
      2
                    3
                                     1
                                                      0
                                                                                         4
      3
                    4
                                     0
                                                      1
                                                                                         8
      4
                    5
                                                                                         2
                                     1
                                                      0
      4375
                4376
                                     0
                                                                                         0
                                                      1
      4376
                4377
                                                      0
                                                                                         4
                                     1
                                                                                         7
      4377
                4378
                                     1
                                                      0
      4378
                4379
                                     0
                                                                                         3
                                                      1
      4379
                                                                                         3
                4380
                                     1
             time in store
                              accompanying_people
                                                      family_size
                                                                     total purchase amount
      0
                          49
                                                                                         113
      1
                          52
                                                   3
                                                                 4
                                                                                         959
                                                                 5
      2
                          51
                                                   1
                                                                                        1247
      3
                          38
                                                   3
                                                                 4
                                                                                        2116
      4
                                                   4
                          52
                                                                 6
                                                                                        1472
```

4375	34	3	4	1337
4376	50	0	4	1094
4377	54	5	5	1954
4378	37	3	2	1074
4379	51	1	4	1464

[4380 rows x 8 columns]

[24]: data.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 4380 entries, 0 to 4379
Data columns (total 8 columns):

#	Column	Non-Null Count	Dtype
0	Cust_ID	4380 non-null	int64
1	Gender_F_Flag	4380 non-null	int64
2	Gender_M_Flag	4380 non-null	int64
3	Residence_distance_from_store	4380 non-null	int64
4	time_in_store	4380 non-null	int64
5	accompanying_people	4380 non-null	int64
6	family_size	4380 non-null	int64
7	total_purchase_amount	4380 non-null	int64

dtypes: int64(8)

memory usage: 273.9 KB

[25]: data.describe()

[25]:		${\tt Cust_ID}$	${\tt Gender_F_Flag}$	${\tt Gender_M_Flag}$,
	count	4380.000000	4380.000000	4380.000000	
	mean	2190.500000	0.702511	0.297489	
	std	1264.541419	0.457205	0.457205	
	min	1.000000	0.000000	0.000000	
	25%	1095.750000	0.000000	0.000000	
	50%	2190.500000	1.000000	0.000000	
	75%	3285.250000	1.000000	1.000000	
	max	4380.000000	1.000000	1.000000	

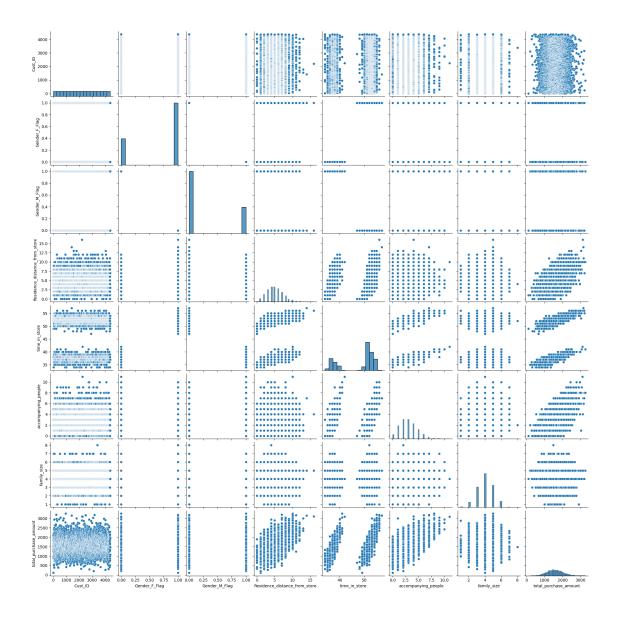
	Residence_distance_from_store	time_in_store	accompanying_people	\
count	4380.000000	4380.000000	4380.000000	
mean	5.003425	47.952740	3.019635	
std	2.226137	6.982038	1.721425	
min	0.000000	34.000000	0.000000	
25%	3.000000	39.000000	2.000000	
50%	5.000000	52.000000	3.000000	
75%	6.000000	53.000000	4.000000	
max	16.000000	57.000000	11.000000	

\

	<pre>family_size</pre>	total_purchase_amount
count	4380.000000	4380.000000
mean	4.034475	1580.639498
std	1.043668	439.721994
min	1.000000	113.000000
25%	3.000000	1274.750000
50%	4.000000	1566.000000
75%	5.000000	1874.000000
max	8.000000	3259.000000

- 4.1 The Average Purchase Amount =1580.639498
- 4.2 The Average Time in Store =47.95

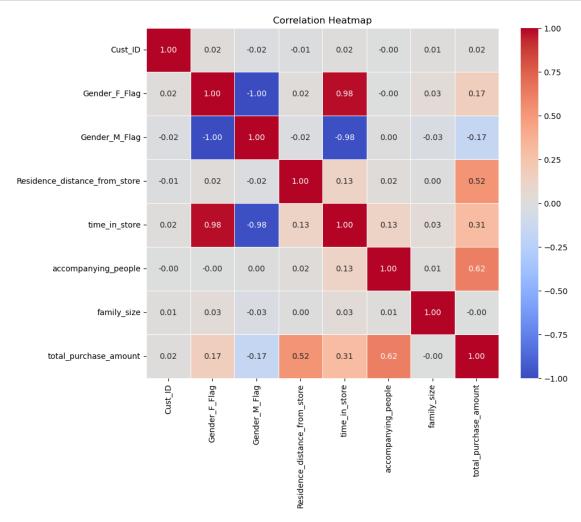
```
[30]: sns.pairplot(data) plt.show()
```



- 5 From the Pairplot the Information we get about Total Purchase Amount is that it is normally distributed
- 6 Thier is relation between Residence Distance from Store ,Time in Store,Accompanying People with Total Purchase Amount

```
[31]: # Calculate the correlation matrix
correlation_matrix = data.corr()

# Create a heatmap
plt.figure(figsize=(10, 8))
```



- 7 Making and Testing a Regression Model using the three parameters
- $7.0.1 \verb| `accompanying_people', 'time_in_store', 'Residence_distance_from_store' | |$
- 8 This decision is taken as in correlation heat map this parameters show resemblance to a great factor and also thier is a visible pattern in pair plot

```
[]:
[44]: from sklearn.metrics import r2 score, mean squared error
     from sklearn.model_selection import train_test_split
     data_df = data
     # Step 2: Split the data into training and testing sets
     train_data_df, test_data_df = train_test_split(data_df, test_size=0.2,_
      →random_state=42)
     # Step 3: Fit a Linear Regression model using OLS on train_data
      strain_data_df[['accompanying_people','time_in_store','Residence_distance_from_store']]_
      → # assuming 'y' is the dependent variable
     X_train = sm.add_constant(X_train)
     y_train = train_data_df['total_purchase_amount']
     model = sm.OLS(y_train, X_train).fit()
     # Step 4: Print out a summary of the model
     print("-----
     print(model.summary())
     # Step 5: Print out R2 and MSE using train_data
     y train pred = model.predict(X train)
     r2_train = r2_score(y_train, y_train_pred)
     mse_train = mean_squared_error(y_train, y_train_pred)
     print("----")
     print(f"R2 on train_data: {r2_train}")
     print(f"MSE on train_data: {mse_train}")
     # Step 6: Using test_data, predict 'y' values and calculate test R2 and MSE
      -dest_data_df[['accompanying_people','time_in_store','Residence_distance_from_store']]
     X_test = sm.add_constant(X_test)
```

OLS Regression Results

=

Dep. Variable: total_purchase_amount R-squared:

0.679

Model: OLS Adj. R-squared:

0.679

Method: Least Squares F-statistic:

2469.

Date: Fri, 01 Mar 2024 Prob (F-statistic):

0.00

Time: 12:49:20 Log-Likelihood:

-24305.

No. Observations: 3504 AIC:

4.862e+04

Df Residuals: 3500 BIC:

4.864e+04

Df Model: 3
Covariance Type: nonrobust

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accompanying_people 151.2708 2.457 61.575 0.000 146.454 156.087

time_in_store 10.3466 0.611 16.922 0.000 9.148 11.545

Residence_distance_from_store 96.7812 1.913 93.031 100.531

50.602

0.000

Omnibus: 0.038 Durbin-Watson: 1.976

- 9 R 2 value of model is 0.679 (quite low in accuracy).
- 10 Durbin watson and Jarque bera test suggest error follow normal distribution which is good
- Omnibus test shows low value and high p value reveling same normal distribution of errors when using this model
- 12 The most significant Outcome is the Conditional No. which is 346 and is very high and thus revealing our current model is too much unreliable and needs to be made more significant
- 13 Evaluation of Linear Regression and RF on data

```
X train, X test, y_train_purchase, y_test_purchase, y_train_engagement,_

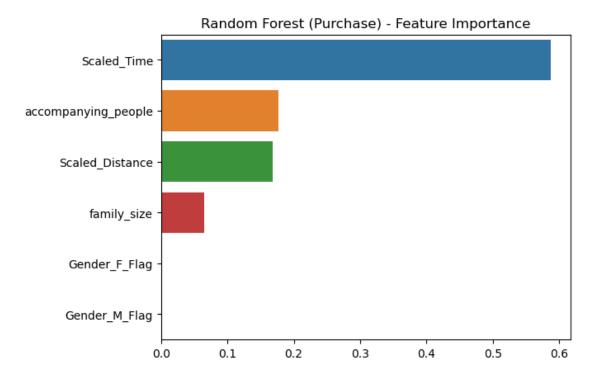
    y_test_engagement = train_test_split(
         X, y_purchase, y_engagement, test_size=0.2, random_state=42
     # Build Linear Regression models
     lr_purchase = LinearRegression()
     lr_engagement = LinearRegression()
     lr_purchase.fit(X_train, y_train_purchase)
     lr_engagement.fit(X_train, y_train_engagement)
     # Build Random Forest models
     rf purchase = RandomForestRegressor()
     rf_engagement = RandomForestRegressor()
     rf_purchase.fit(X_train, y_train_purchase)
     rf_engagement.fit(X_train, y_train_engagement)
     # Evaluate models
     def evaluate_model(model, X_test, y_test, model_name):
         y_pred = model.predict(X_test)
         mse = mean_squared_error(y_test, y_pred)
         print(f"{model_name} Mean Squared Error: {mse}")
[51]: # Evaluate Linear Regression models
     evaluate_model(lr_purchase, X_test, y_test_purchase, "Linear Regression_
      evaluate_model(lr_engagement, X_test, y_test_engagement, "Linear Regression_u
       ⇔(Engagement)")
      # Evaluate Random Forest models
     evaluate_model(rf_purchase, X_test, y_test_purchase, "Random Forest (Purchase)")
     evaluate_model(rf_engagement, X_test, y_test_engagement, "Random Forest_
       # Feature Importance Analysis for Random Forest models
     def plot_feature_importance(model, feature_names, model_name):
         feature_importance = model.feature_importances_
          sorted_idx = feature_importance.argsort()[::-1]
          sns.barplot(x=feature_importance[sorted_idx], y=feature_names[sorted_idx])
         plt.title(f"{model_name} - Feature Importance")
         plt.show()
```

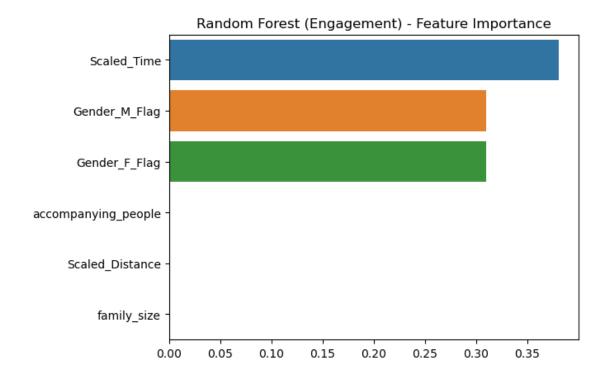
Model Building

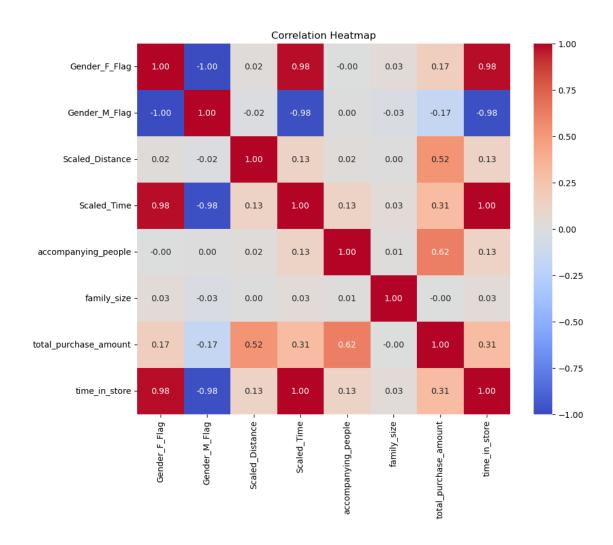
Linear Regression (Purchase) Mean Squared Error: 62621.71732305936

```
Linear Regression (Engagement) Mean Squared Error: 9.665167036022917e-29 Random Forest (Purchase) Mean Squared Error: 73494.81880476882 Random Forest (Engagement) Mean Squared Error: 0.001142694063926941
```

14 Here Indeed Linear Regression Performed better than RF.

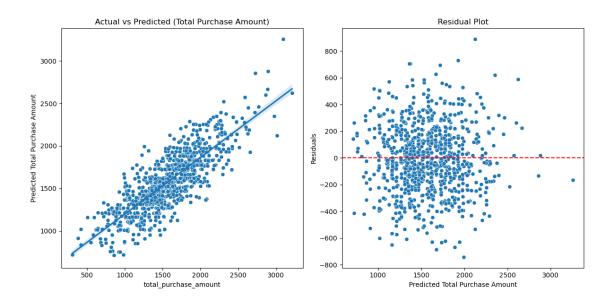




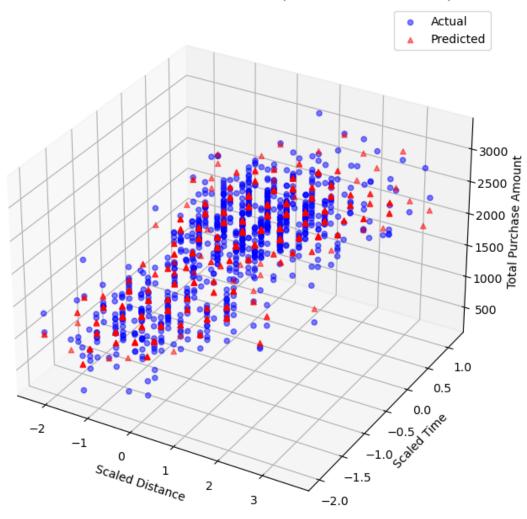


15 Making Prediction Model for Overall Value of Purchases

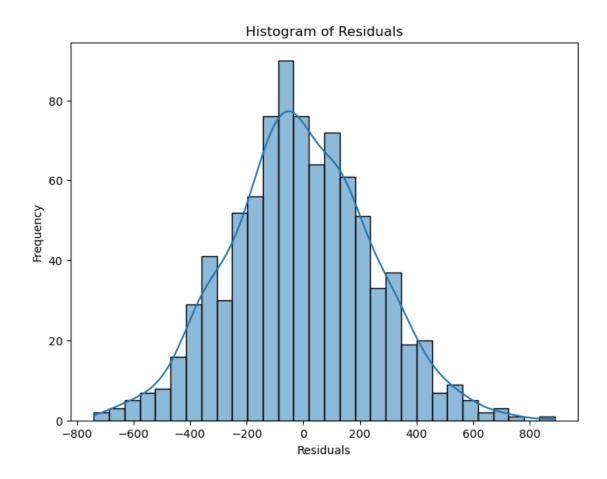
```
plt.subplot(1, 2, 1)
sns.scatterplot(x=y_test_purchase, y=y_pred_purchase)
plt.title('Actual vs Predicted (Total Purchase Amount)')
plt.xlabel('Actual Total Purchase Amount')
plt.ylabel('Predicted Total Purchase Amount')
sns.regplot(x=y_test_purchase, y=y_pred_purchase, scatter=False, ax=plt.gca())
# Residual plot
plt.subplot(1, 2, 2)
residuals = y_test_purchase - y_pred_purchase
sns.scatterplot(x=y_pred_purchase, y=residuals)
plt.title('Residual Plot')
plt.xlabel('Predicted Total Purchase Amount')
plt.ylabel('Residuals')
plt.axhline(y=0, color='r', linestyle='--')
plt.tight_layout()
plt.show()
# 3D Scatter plot for multivariate linear regression
fig = plt.figure(figsize=(12, 8))
ax = fig.add_subplot(111, projection='3d')
ax.scatter(X_test['Scaled_Distance'], X_test['Scaled_Time'], y_test_purchase,__
⇔c='blue', marker='o', alpha=0.5, label='Actual')
ax.scatter(X_test['Scaled_Distance'], X_test['Scaled_Time'], y_pred_purchase,__
⇔c='red', marker='^', alpha=0.5, label='Predicted')
ax.set_xlabel('Scaled Distance')
ax.set_ylabel('Scaled Time')
ax.set_zlabel('Total Purchase Amount')
plt.title('3D Scatter Plot - Actual vs Predicted (Total Purchase Amount)')
plt.legend()
plt.show()
```



3D Scatter Plot - Actual vs Predicted (Total Purchase Amount)



```
[60]: # Histogram of Residuals
plt.figure(figsize=(8, 6))
sns.histplot(residuals, kde=True, bins=30)
plt.title('Histogram of Residuals')
plt.xlabel('Residuals')
plt.ylabel('Frequency')
plt.show()
```

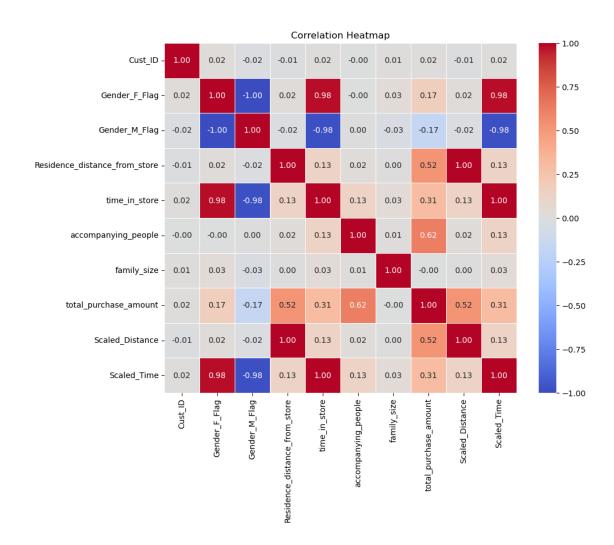


16 Errors follow Normal Distribution

17 Now we would be working to predict Time duration of Customer in store

```
[64]: # Calculate the correlation matrix
correlation_matrix = data.corr()

# Create a heatmap
plt.figure(figsize=(10, 8))
sns.heatmap(correlation_matrix, cmap='coolwarm', annot=True, fmt=".2f", \( \_\text{\text{\text{olinewidths}}} \)
plt.title('Correlation Heatmap')
plt.show()
```



Here total duration is store is mostly dependent on parameters 'Gender_F_Flag' ,'Gender_M_Flag' and Total Purchasing Amount and slightly on parameters like

```
X_train = train_data_df[['Gender_F_Flag'_
⇔, 'Gender_M_Flag', 'total_purchase_amount']] # assuming 'y' is the dependent \( \)
\rightarrow variable
X train = sm.add constant(X train)
y_train = train_data_df['time_in_store']
model = sm.OLS(y_train, X_train).fit()
# Step 4: Print out a summary of the model
print("----")
print(model.summary())
# Step 5: Print out R2 and MSE using train_data
y_train_pred = model.predict(X_train)
r2_train = r2_score(y_train, y_train_pred)
mse_train = mean_squared_error(y_train, y_train_pred)
print("-----")
print(f"R2 on train data: {r2 train}")
print(f"MSE on train_data: {mse_train}")
# Step 6: Using test_data, predict 'y' values and calculate test R2 and MSE
X_test = test_data_df[['Gender_F_Flag'_
→, 'Gender_M_Flag', 'total_purchase_amount']]
X_test = sm.add_constant(X_test)
y_test = test_data_df['time_in_store']
y_test_pred = model.predict(X_test)
r2_test = r2_score(y_test, y_test_pred)
mse_test = mean_squared_error(y_test, y_test_pred)
print("----")
print(f"R2 on test_data: {r2_test}")
print(f"MSE on test data: {mse test}")
print("----")
```

OLS Regression Results

______ Dep. Variable: time_in_store R-squared: 0.987 Model: OLS Adj. R-squared: 0.987 Method: Least Squares F-statistic: 1.376e+05 Fri, 01 Mar 2024 Prob (F-statistic): Date: 0.00 Time: 13:33:25 Log-Likelihood: -4127.7No. Observations: 3504 AIC: 8261. Df Residuals: 3501 BIC: 8280. Df Model:

Covariance Type:	nonrol	nonrobust				
0.975]	coef	std	err	t	P> t	[0.025
const 27.666	27.6005	0	.033	832.014	0.000	27.535
Gender_F_Flag 21.174	21.1297	0	.023	927.920	0.000	21.085
<pre>Gender_M_Flag 6.513</pre>	6.4708	0	.022	300.114	0.000	6.429
total_purchase_amount 0.002	0.0023	3.07	e-05	73.902	0.000	0.002
Omnibus:	 48	 .300	 Durbi	n-Watson:	=======	1.987
<pre>Prob(Omnibus):</pre>	0	.000	Jarqu	e-Bera (JB):		50.827
Skew:	-0	.270	Prob(JB):			9.19e-12
Kurtosis:		. 236	Cond.			2.36e+18

Notes

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The smallest eigenvalue is 1.71e-27. This might indicate that there are strong multicollinearity problems or that the design matrix is singular.

R2 on train_data: 0.9874347706331874 MSE on train_data: 0.617619986591757

R2 on test_data: 0.986908418947786 MSE on test_data: 0.6160179031190275

19 From the Above Tests it was clear making a Linear Regression model for such would be very unhelpful thus we thought to proceed to using PCA

```
[71]: from sklearn.model_selection import train_test_split
from sklearn.linear_model import LinearRegression
from sklearn.metrics import mean_absolute_error, mean_squared_error, r2_score
from sklearn.decomposition import PCA
from sklearn.preprocessing import StandardScaler

# Assuming your data is stored in a DataFrame called 'df'
```

```
\# Drop Cust_ID as it's not informative for the model
df=data
df = df.drop('Cust_ID', axis=1)
# Handling categorical variables (if needed)
# e.g., df['Gender'] = df['Gender_F_Flag'] + 2 * df['Gender_M_Flag']
# Feature scaling
scaler = StandardScaler()
df_scaled = scaler.fit_transform(df)
# Apply PCA
pca = PCA(n_components=2) # Choose the number of components based on explained_
 →variance
df_pca = pca.fit_transform(df_scaled)
# Split the data
X_train, X_test, y_train, y_test = train_test_split(df_pca,__

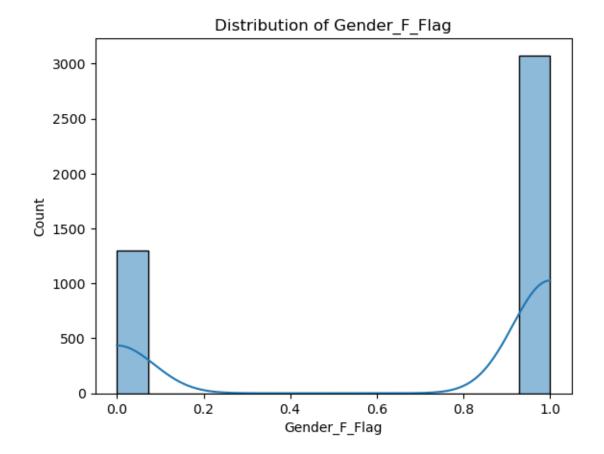
df['time_in_store'], test_size=0.2, random_state=42)
# Train Linear Regression model
model = LinearRegression()
model.fit(X_train, y_train)
# Predictions
predictions = model.predict(X_test)
# Model Evaluation
mae = mean_absolute_error(y_test, predictions)
mse = mean_squared_error(y_test, predictions)
r2 = r2_score(y_test, predictions)
# Print metrics
print(f'Mean Absolute Error: {mae}')
print(f'Mean Squared Error: {mse}')
print(f'R-squared: {r2}')
```

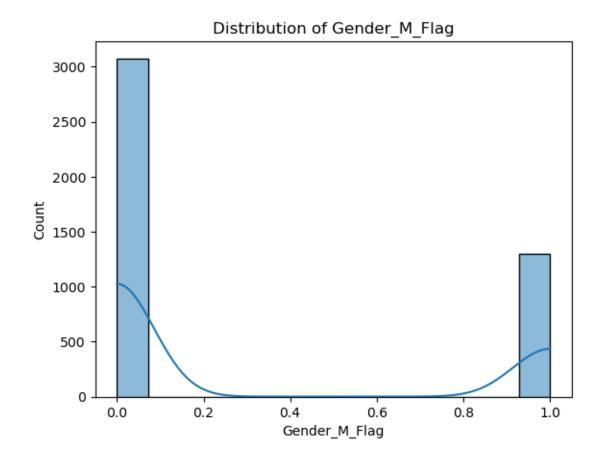
Mean Absolute Error: 0.2492366594029411
Mean Squared Error: 0.10154349207478548

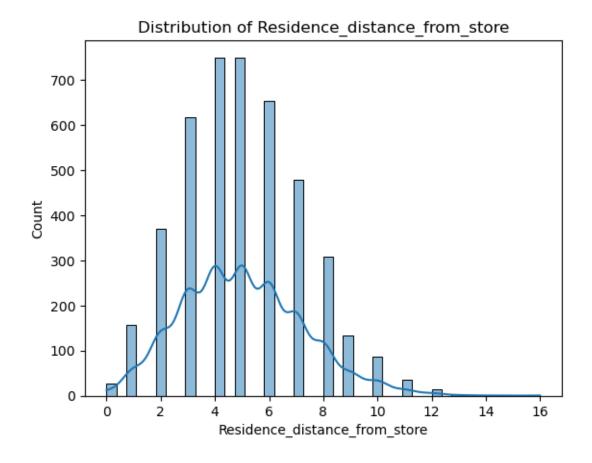
R-squared: 0.9978420028864566

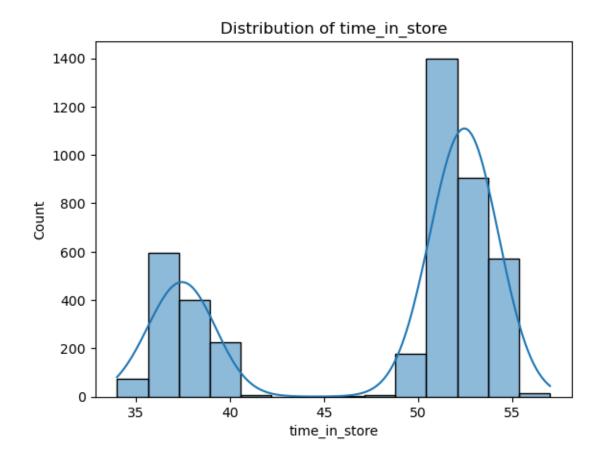
20 Distribution Plot for Feature Analysis

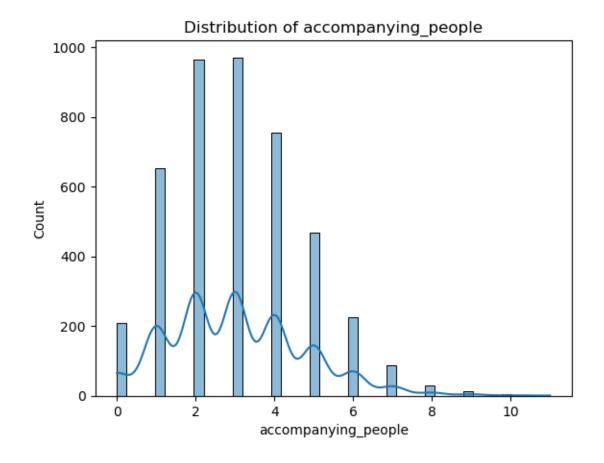
```
[75]: for column in df.columns:
    sns.histplot(df[column], kde=True)
    plt.title(f'Distribution of {column}')
```

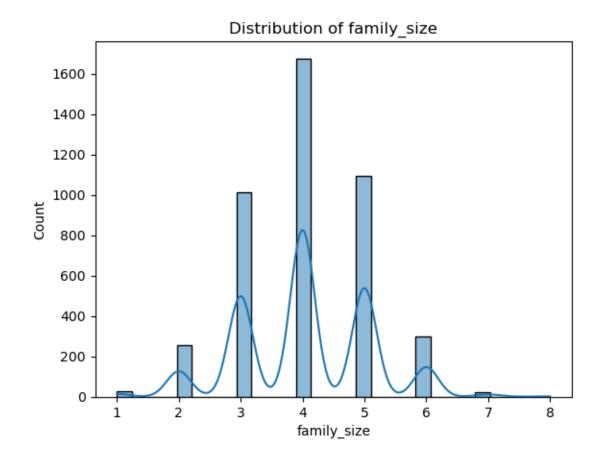


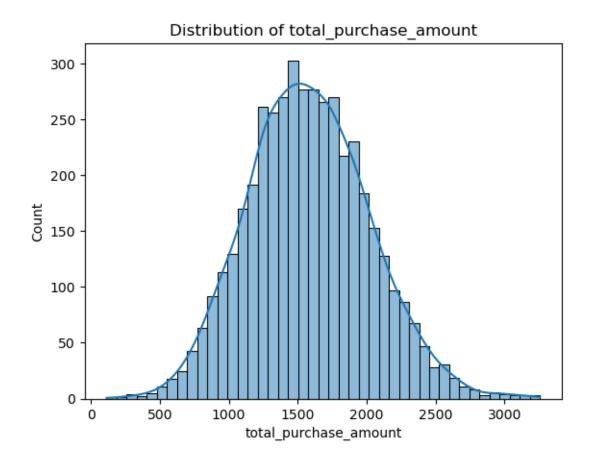


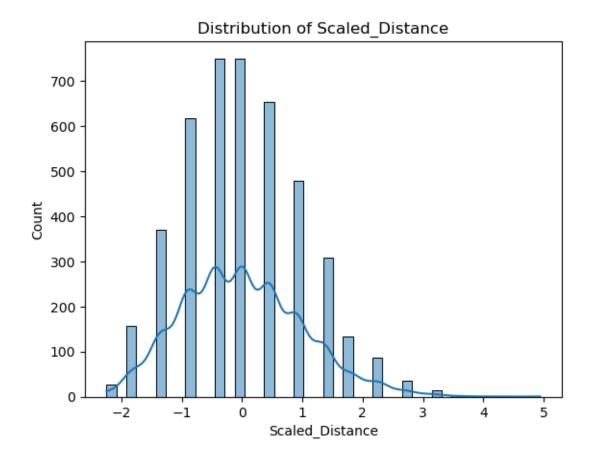


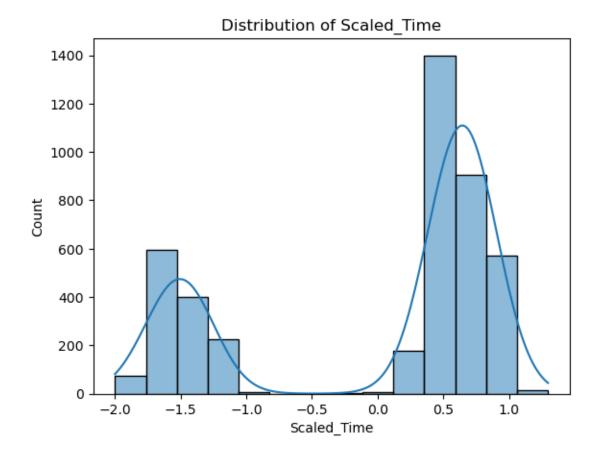












```
[84]: df=data
      # Assuming your data is stored in a DataFrame called 'df'
      # Drop Cust_ID as it's not informative for the model
      df = df.drop('Cust_ID', axis=1)
      # Handling categorical variables (if needed)
      # e.g., df['Gender'] = df['Gender_F_Flag'] + 2 * df['Gender_M_Flag']
      # Feature scaling
      scaler = StandardScaler()
      df_scaled = scaler.fit_transform(df)
      # Apply PCA
      pca = PCA(n_components=2) # Choose the number of components based on explained_
       ⇔variance
      df_pca = pca.fit_transform(df_scaled)
      # Split the data
      X_train, X_test, y_train, y_test = train_test_split(df_pca,__
       →df['time_in_store'], test_size=0.2, random_state=42)
```

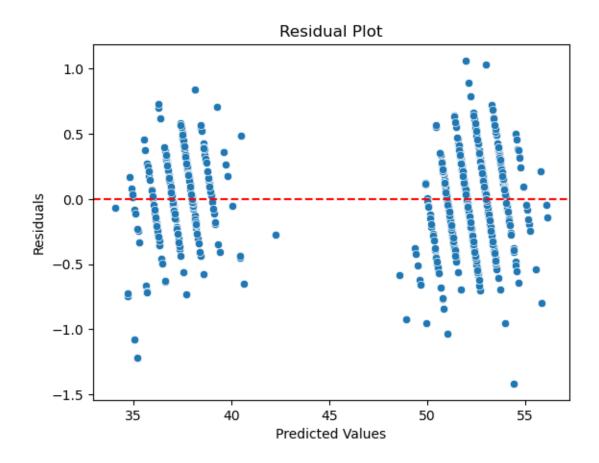
```
# Train Linear Regression model
model = LinearRegression()
model.fit(X_train, y_train)
# Predictions
predictions = model.predict(X_test)
# Model Evaluation
mae = mean_absolute_error(y_test, predictions)
mse = mean_squared_error(y_test, predictions)
r2 = r2_score(y_test, predictions)
# Print metrics
print(f'Mean Absolute Error: {mae}')
print(f'Mean Squared Error: {mse}')
print(f'R-squared: {r2}')
# Residual Plot
residuals = y_test - predictions
sns.scatterplot(x=predictions, y=residuals)
plt.axhline(y=0, color='r', linestyle='--')
plt.title('Residual Plot')
plt.xlabel('Predicted Values')
plt.ylabel('Residuals')
plt.show()
# Actual vs. Predicted Plot
plt.scatter(y_test, predictions)
plt.plot([min(y_test), max(y_test)], [min(y_test), max(y_test)], '--',__

color='red', linewidth=2)

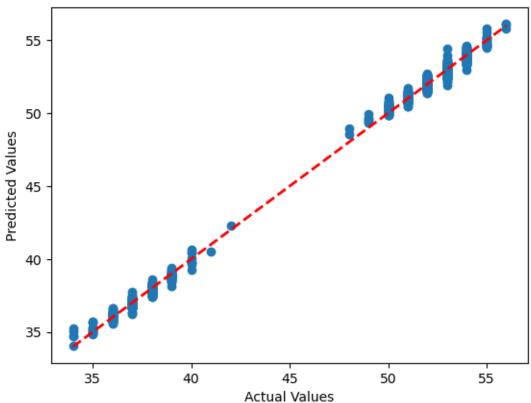
plt.title('Actual vs. Predicted Values')
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.show()
```

Mean Absolute Error: 0.24923665940294143 Mean Squared Error: 0.1015434920747856

R-squared: 0.9978420028864566

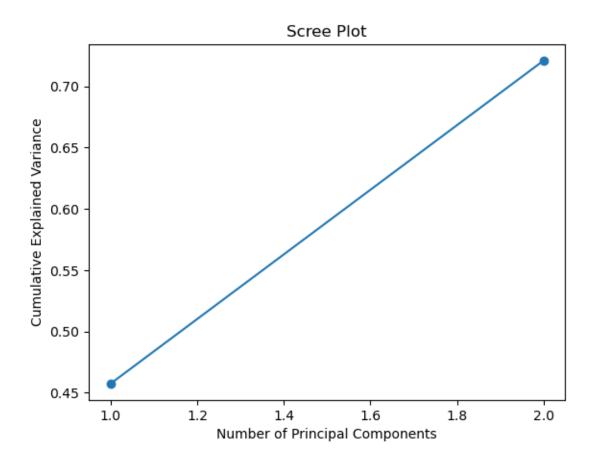






```
[85]: explained_var = pca.explained_variance_ratio_
    cumulative_var = explained_var.cumsum()

plt.plot(range(1, len(explained_var)+1), cumulative_var, marker='o')
    plt.title('Scree Plot')
    plt.xlabel('Number of Principal Components')
    plt.ylabel('Cumulative Explained Variance')
    plt.show()
```



21 1. T-test for Gender_F_Flag:

21.1 Interpretation:

T-statistic: 11.34 ### P-value: 2.09e-29 (very close to zero) Analysis: The t-test results suggest a significant difference in total purchase amounts between customers identified as female (Gender_F_Flag = 1) and customers identified as male (Gender_M_Flag = 1). The extremely low p-value indicates strong evidence against the null hypothesis of no difference.

Recommendations: Targeted Marketing: Given the significant difference in purchase amounts, consider targeted marketing strategies for each gender group. Gender-Specific Offers: Tailor promotional offers or incentives to appeal to the purchasing patterns of each gender group. 2. Pearson Correlation between Time in Store and Total Purchase Amount: Interpretation: Correlation Coefficient: 0.31 P-value: 4.81e-95 (very close to zero) Analysis: The Pearson correlation results indicate a moderate positive correlation (0.31) between the time a customer spends in the store and their total purchase amount. The extremely low p-value suggests that this correlation is statistically significant.

Recommendations: Enhance In-Store Experience: Focus on initiatives that encourage customers to spend more time in the store, such as interactive displays, events, or promotions. Optimize Staffing: Since time in store is correlated with purchase amount, optimize staffing levels during peak times to ensure adequate assistance for customers. Addressing Executive Questions: a. Increase Sales: Leverage the insights from the t-test to tailor marketing strategies for different gender groups. Consider implementing gender-specific promotions or advertising campaigns to enhance engagement. b. Impact of Increased Time in Store: Communicate the positive correlation between time in store and total purchase amount. Suggest strategies to motivate customers to stay longer, such as creating a more engaging in-store environment.

[]: