# Math Document Template

# Pothukuchi Siddhartha

Download all python codes from

svn co https://github.com/SiddharthPh/ Summer2020/trunk/geometry/Probstat/codes

#### 1 Probability Exercises

#### 1.1 Exercise 1

1.1.1 Problem: Suppose you drop a die at random on the rectangular region shown in Fig.15.6. What is the probability that it will land inside the circle with diameter 1m?

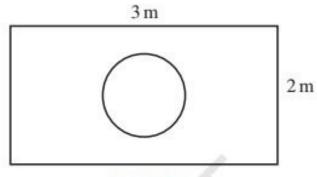


Fig. 15.6

## 1.1.2 Solution:

1. In the given question,

The sample size = Total Area of the rectangle=

$$3x2 = 6m^2 \tag{1.1.2.1.1}$$

Favourable outcome = Area of Circle=

$$\pi \left(\frac{1}{2}\right)^2 = \frac{\pi}{4}m^2 \tag{1.1.2.1.2}$$

Probabilty(P) of the dice landing in the circle= $\frac{\pi}{24}$ 

$$P = 0.131$$

The python code for the figure 1.1.2.1

# prob/codes/prob1.py

shows the Bernouli distribution of data. The Bernoulli Distribution of data is given

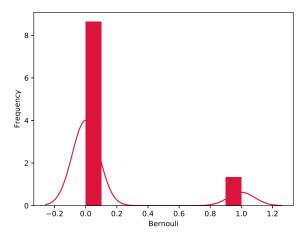


Fig. 1.1.2.1: Bernoulli Distribution.

below

Probability mass function(P(X))= $p^x (1-p)^{1-x}$ 

$$P(X=0) = 1 - p (1.1.2.1.3)$$

$$P(X=1) = p (1.1.2.1.4)$$

1

where p=0.131 given by 1.2.2.1a

## 1.1.3 Understanding Graph:

- 1. From the graph (1.1.2.1),
  - a) Values on X-axis represent the Bernoulli distribution of data.
  - b) Values on Y-axis represent the density of frequency(Histogram estimator) of the data. To calculate the histogram estimator, we have to define the number of bins(Intervals) For the graph in the question,

$$bins = 10$$
 (1.1.3.1.1)

$$h(binwidth) = \frac{(1-0)}{10}$$
 (1.1.3.1.2)

For bin-width h, number of observations n, for bin j, proportion of observations is

$$p_j = \frac{y_j}{n} \tag{1.1.3.1.3}$$

(Where  $y_i$  is the frequency of  $j^t h$  bin.)

$$p_0 = \frac{869}{1000} = 0.869 \tag{1.1.3.1.4}$$

$$p_1 = \frac{131}{1000} = 0.131 \tag{1.1.3.1.5}$$

The density estimate is

$$y(x) = \frac{p_j}{h}$$
 (1.1.3.1.6)

$$y(0) = \frac{0.869}{0.1} = 8.69$$
 (1.1.3.1.7)

$$y(0) = \frac{0.131}{0.1} = 1.31$$
 (1.1.3.1.8)

To draw the Gaussian Kernel Density curve, Calculate mean and standard deviation for the centre and bandwidth.

See 1.1.3.1 for clear understanding.

$$\mu(Mean) = 0.861$$
(1.1.3.1.9)
 $\sigma^2(\text{Standard Deviation}) = 0.1189$ 
(1.1.3.1.10)

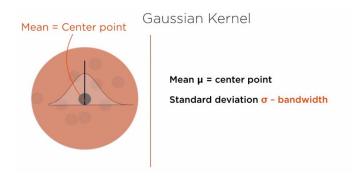


Fig. 1.1.3.1: Gaussian Kernel

#### 1.2 Exercise 2

1.2.1 Problem: A lot consists of 144 ball pens of which 20 are defective and the others are good. Nuri will buy a pen if it is good, but will not buy if it is defective. The shopkeeper draws one pen at random and gives it to her. What is the probability that

- (i) She will buy it?
- (ii) She will not buy it?

## 1.2.2 Solution:

1. In the given question,

a) The sample size = Total number of pens(S)=

$$S = 144$$
 (1.2.2.1.1)

Favourable outcome = Pens purchased(F1)=

$$F1 = 124$$
 (1.2.2.1.2)

Probabilty(P) of the pens purchased by her from the shopkeeper= $\frac{124}{144}$ 

$$\therefore P = 0.861$$

The python code for the figure 1.2.2.1

shows the Bernouli distribution of data.

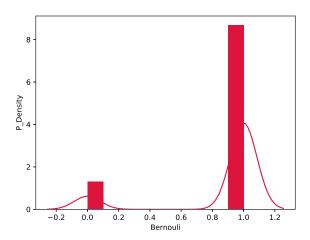


Fig. 1.2.2.1: Bernoulli Distribution.

The Bernoulli Distribution of data is given below

Probability mass function(P(X))= $p^x (1-p)^{1-x}$ 

$$P(X=0) = 1 - p (1.2.2.1.3)$$

$$P(X = 1) = p$$
 (1.2.2.1.4)

where p is the probability of occurence of (X=1)

- $\therefore$  p=0.861 given by 1.2.2.1a
- 2. The sample size = Total number of pens(S)=

$$S = 144$$
 (1.2.2.2.1)

Favourable outcome = Pens not purchased(F2)=

$$F2 = 20 \tag{1.2.2.2.2}$$

Probabilty(P) of the pens not purchased by her from the shopkeeper= $\frac{20}{144}$ 

$$\therefore P = 0.139$$

The python code for the figure 1.2.2.2

shows the Bernouli distribution of data.

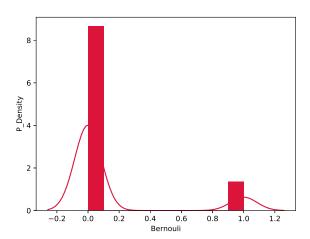


Fig. 1.2.2.2: Bernoulli Distribution.

The Bernoulli Distribution of data is given below

Probability mass function(P(X))= $p^x (1-p)^{1-x}$ 

$$P(X = 0) = 1 - p (1.2.2.2.3)$$

$$P(X=1) = p (1.2.2.2.4)$$

where p is the probability of occurence of (X=1)

 $\therefore$  p=0.139 given by 1.2.2.1a

The understanding of the curves 1.2.2.1 and 1.2.2.2 can be seen in (1.1.3.1b)