My Presentation

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Question

Exercise 8.1(Q no.28)

In right triangle ABC, right angled at C, M is the mid-point of hypotenuse AB. C is joined to M and produced to a point D such that DM = CM. Point D is joined to point B. Show that:

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(a) \triangle AMC \cong \triangle BMD

(b) \triangle DBC is a right angle.

(c) \triangle DBC \cong \triangle ABC

(d) CM = \frac{1}{2}AB
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The figure shown below is the figure obtained from Latex.

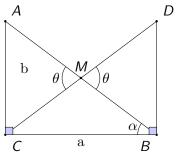


Figure: Figure: Right Angled Triangle

Solution a)

From the above figure,

$$C = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, A = \begin{pmatrix} 0 \\ b \end{pmatrix}, B = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

As, M is the midpoint of AB

$$M = \begin{pmatrix} a/2 \\ b/2 \end{pmatrix}$$

Therefore Coordinates of D are

$$D = \begin{pmatrix} a \\ b \end{pmatrix}$$

 $\triangle AMC$ and $\triangle DMB$ are congruent to each other by SAS congruency.

- (i) Side AM is equal to the corresponding side BM [As M is midpoint of AB]
- (ii)Side CM of is equal to corresponding side DM [As M is midpoint of DC]
- (iii) $\angle AMC = \angle DMB$ [Vertically Opposite Angles]

Solution b)

In $\triangle ACB$

$$(AB)^2 = a^2 + b^2$$

Since $\angle ACB = 90^{\circ}$ [Pythagorus theorem] In $\triangle DBC$

Formula

 $\cos \angle DBC =$

$$((a^2 + b^2 - (DC)^2)/2ab)$$

$$[\mathsf{DB} = \mathsf{D}\text{-}\mathsf{B} = \mathsf{b}]$$

By using distance formula i.e $\sqrt{(x1-x2)^2+(y1-y1)^2}$ we get that AB=DC from the given coordinates.

cos∠DBC =

$$((a^2 + b^2 - (AB)^2)/2ab)$$

 $\cos/DBC=0$

Therefore, $\angle DBC$ is right angle

Solution c)

 $\triangle ACB$ and $\triangle DCB$ are congruent to each other in SAS congruency.

- (i)Both the triangles have a common base , a.
- (ii)AC = DB by using distance formula
- (iii) $\angle ACB = \angle DBC = 90^{\circ}$ [From Solution b]

Solution d)

Since M is the midpoint of CD $CM=\frac{1}{2}$ DC From Solution b it is clear that DC=AB Therefore $CM=\frac{1}{2}AB$ Hence Proved.

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