Homework-1

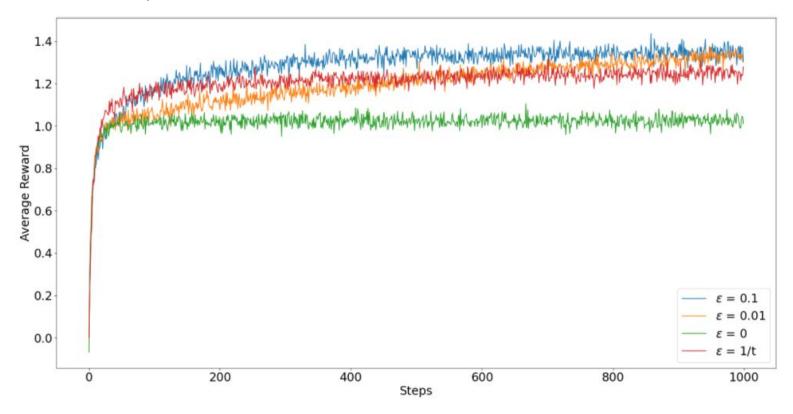
Question 1:

The 10-armed testbed with q*(a), a=1,2,.....,10 selected according to a normal distribution with mean 0 and variance 1.

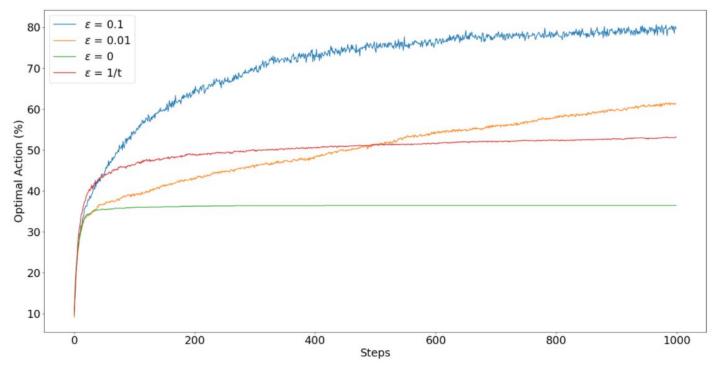
Rewards for each arm are selected using normal distribution with mean $q^*(A_t)$ and variance 1.

Graph drawn for ε = 0.1, 0.01, 0 and 1/t.

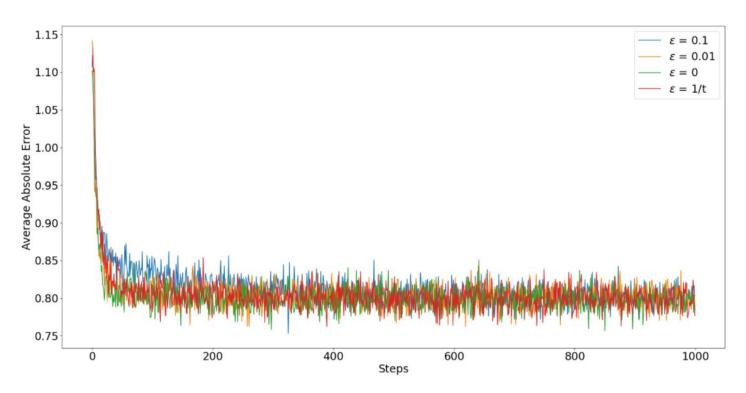
Time steps=1000, Number of simulations=2000



Average Reward



Optimal Action (%)



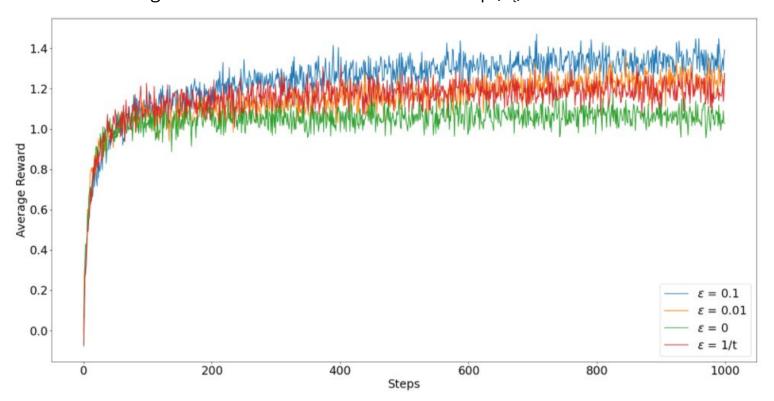
Average Absolute Error

Result: For time steps=1000, ϵ = 0.1 gives the better result but this is not true for long runs as then ϵ = 0.01 gives the better result as it picks up optimal action throughout the simulation with greater probability as compared to ϵ = 0.1.

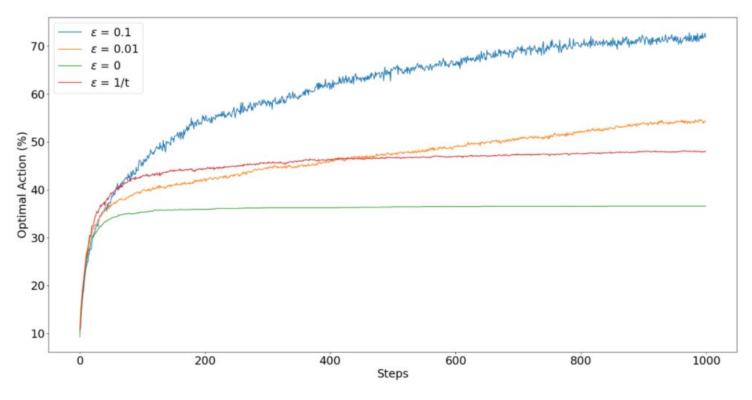
Also, for long runs, ε = 1/t gives us the best result as it increases its probability to exploit as t increases thus motivating exploration early on to find optimal estimate and then exploiting once it has been found (as $t \to \infty$, $\varepsilon \to 0$)

Question 2:

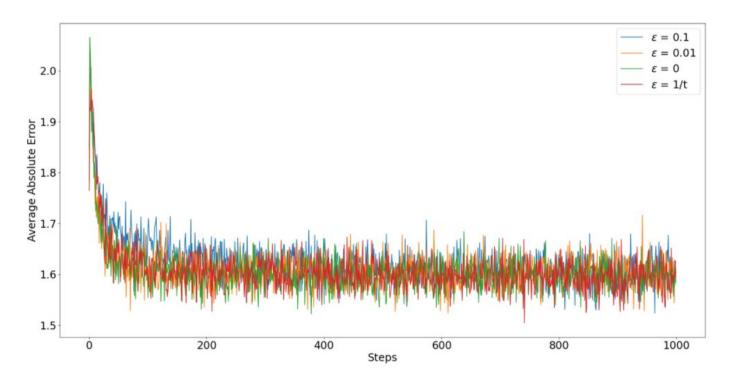
Same as Question1 but now rewards for each arm are selected according to a normal distribution with mean $q*(A_t)$ and variance 4.



Average Reward



Optimal Action (%)



Average Absolute Error

Result: The same trend follows as in Question1 for different values of ε . But, now the rewards and estimates are much noisier and variance= 4 also negatively effects the optimal action for time steps=1000 (can be seen through the range of values on the y-axis)

	Page No.
	Question 3
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	when compared to E=0.1 case but.
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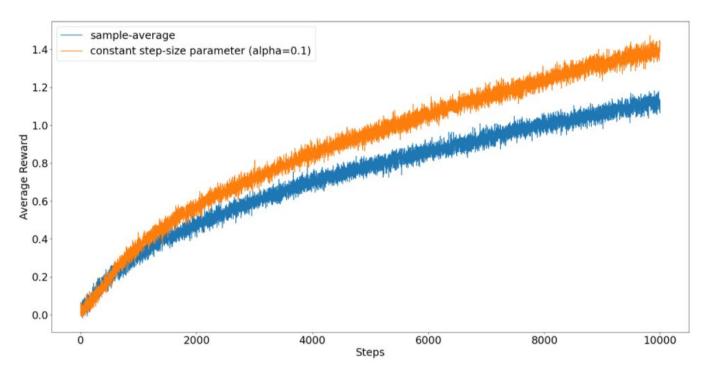
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· · · · · · · · · · · · · · · · · · ·	Question-4
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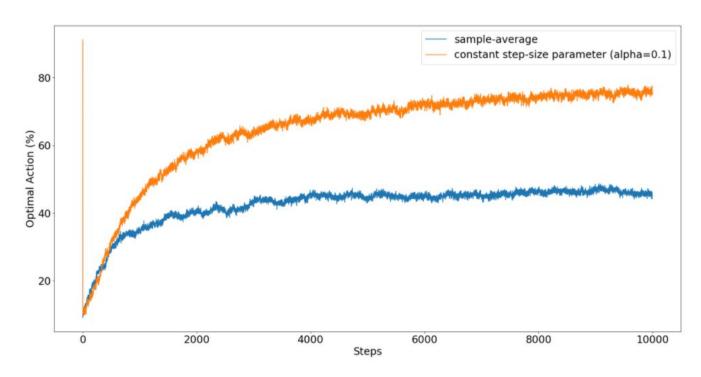
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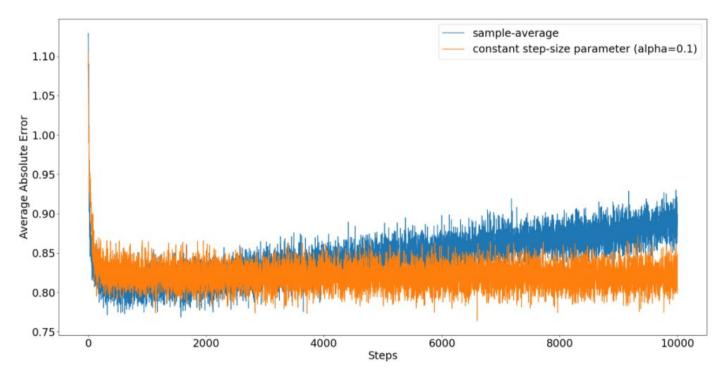
Question 5



Average Reward



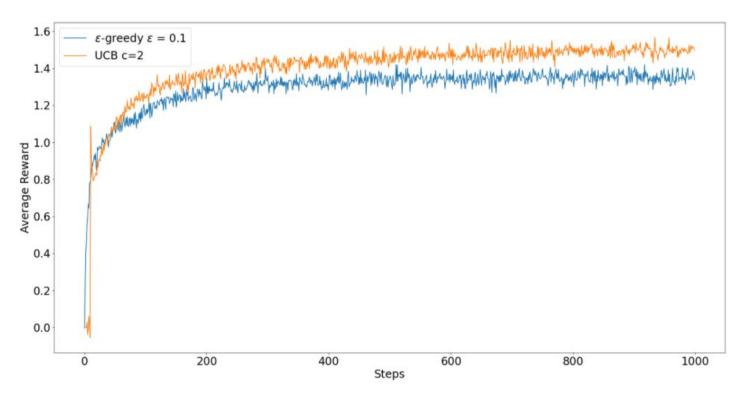
Optimal Action (%)

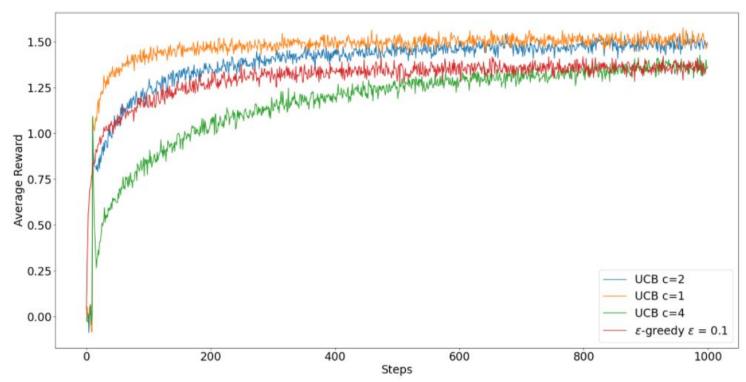


Average Absolute Error

Result: For non-stationary setting, constant step-size parameter tends to give better results as they, unlike sample-average, do not converge and thus readjust themselves according to any change in the distribution of the arms.

Question 6:



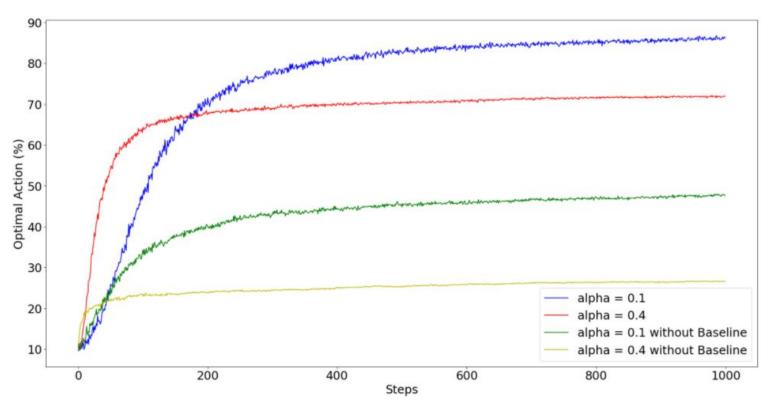


Result: According to UCB, when $N_t(a)=0$ for any arms A_t , then that arm is considered to be the maximizing action.

Now, this occurs for all the 10 arms initially in random order. Thus, we see the low average reward for the first 10 steps as then we are exploring and picking a different arm each step.

Now for the 11th step, the term $c * \sqrt{lnt/Nt(a)}$ is the same irrespective of the picked arm. Thus, now the discriminatory factor will only be the value of Q_t which is dependent on the first round of exploration (affected by the reward of each arm and Q_1). Now, that action is picked whose Q_t is greater and this would be seen across all 2000 simulations, thus a spike in average reward can be seen for the 11th step. Further onwards $c * \sqrt{lnt/Nt(a)}$ is different for each arm and thus average rewards progress steadily as the model acquires more certainty about the system.

Question 7:



Result: The optimal action is better for a = 0.1 and with Baseline rather than for without baseline. It is because the Baseline is used to capture the deviation from the mean rather than the absolute value.

Both lower α and Baseline lead to lower variance changes thus performing better.