

Hill Climbing algo (Basic)

$f/p \rightarrow \text{Problem}$
local variable \rightarrow Current & neighbor
Current \leftarrow Make_node (Initial state (problem))
loop
do neighbor \leftarrow a highest_valued successor of current
If Value[neighbor] \leq Value[current]
Then
Return State[current]
Current \leftarrow neighbor

```
function HILL-CLIMBING(problem) returns a state that is a local maximum
  current  $\leftarrow$  problem.INITIAL
  while true do
    neighbor  $\leftarrow$  a highest-valued successor state of current
    if VALUE(neighbor)  $\leq$  VALUE(current) then return current
    current  $\leftarrow$  neighbor
```

Figure 4.2 The hill-climbing search algorithm, which is the most basic local search technique. At each step the current node is replaced by the best neighbor.

```
function SIMULATED-ANNEALING(problem, schedule) returns a solution state
  current  $\leftarrow$  problem.INITIAL
  for t = 1 to  $\infty$  do
    T  $\leftarrow$  schedule(t)
    if T = 0 then return current
    next  $\leftarrow$  a randomly selected successor of current
     $\Delta E \leftarrow$  VALUE(current) - VALUE(next)
    if  $\Delta E > 0$  then current  $\leftarrow$  next
    else current  $\leftarrow$  next only with probability  $e^{-\Delta E/T}$ 
```

Figure 4.4 The simulated annealing algorithm, a version of stochastic hill climbing where some downhill moves are allowed. The *schedule* input determines the value of the “temperature” *T* as a function of time.

Depth limit search

Easy Engineering Classes – Free YouTube Lectures
EEC Classes GGSIPU, UPTU, Mumbai Univ., Pune Univ., GTU, Anna Univ., PTU and Others EEC Classes

Depth-Limited Search Algorithm:

- Working is similar to DFS but with a predetermined limit.
- Helps in solving the problem of DFS: **Infinite Path**

Termination Conditions:

- Failure Value:** There is no solution.
- Cutoff Failure:** Terminates on reaching predetermined depth. } no solⁿ.

Advantages:

- Memory Efficient.

Disadvantages:

- Incompleteness
- Can be terminated without finding solⁿ.
- Not optimal.

Example:-

Starting node → Level 0
Level 1
Level 2 → Goal node.
Level 3 → Goal node.

Path: $X \rightarrow A \rightarrow C \rightarrow D \rightarrow B \rightarrow I \rightarrow J$

This depth will result in no solⁿ.

Time Complexity: $O(b^d)$
Space Complexity: $O(b \times d)$

DFS

DFS: Depth-First Search.

- Recursive algorithm.
- Starts from root node and follows each path to its greatest depth node before moving to the next path.
- Implemented using **STACK** (LIFO)

ALGORITHM: (Push)

- Enter Root node on stack
- Do until stack is not empty
 - (POP) a) Remove Node
 - b) If Node = Goal stop.
 - c) Push all node in stack

Adv:- Less memory
Less time to reach goal node if traversal in right path.

Disadv:-

- No Guarantee of finding solⁿ.
- Infinite loop.

Example 1:

Start node.

Stack: A, B, C, D, E, F, G, H

No Guarantee of finding solⁿ.

BFS

BFS:- Breadth First Search.

- ↳ Explores all the nodes at given depth before proceeding to the next level.
- ↳ Uses Queue to implement.

ALGORITHM:

- Enter Starting nodes on Queue.
- If Queue is empty, then return fail and stop.
- If first element on Queue is Goal Node, then return Success and stop.
- ELSE (IMP) Remove and expand first element from Queue and place children at end of Queue.
- Goto Step (ii)

Example 1:- Starting Node.

Initial Queue $\{A\}$ = Goal node \times

Remove from Queue and add its successor to Queue.

$\{B, C\}$
 \downarrow
 $\{C, D, E\}$
 \downarrow
 $\{D, E, F\}$
 \downarrow
 $\{E, F, G\}$
 \downarrow
 $\{G, H\}$

Best first Search

BEST FIRST SEARCH: GREEDY SEARCH. (BFS DFS)

- ↳ Uses evaluation Algorithm (funcⁿ) to decide which adjacent node is most promising and then explore.
- ↳ Category of Heuristic or Informed Search.
- ↳ Priority Queue is used to store Cost of nodes.

ALGORITHM: \rightarrow Sorted order.

Priority Queue 'PQ' containing initial states

Loop

if PQ = Empty Return FAIL

else

 NODE \leftarrow Remove_First(PQ)

 if NODE = GOAL

 Return Path from Initial to NODE

 else

 Generate all Successors of NODE

 and insert newly generated NODE into PQ according to COST Value.

END LOOP

Straight Line distance.

A \rightarrow G = 40
 B \rightarrow G = 32
 C \rightarrow G = 25
 D \rightarrow G = 35
 E \rightarrow G = 19
 F \rightarrow G = 17
 G \rightarrow G = 0
 H \rightarrow G = 10

open [A]
closed []

Path = A \rightarrow C \rightarrow F \rightarrow G (44)

open [C, B, D]
closed [A]

open [B, D]
closed [A, C]

open [F, E, B, D]
closed [A, C]

open [E, B, D]
closed [A, C, F, G]

A* algo(better version of best first search)

(A156)

Ques:- Explain A* Algorithm for Search.

↳ Uses heuristic funcⁿ $h(n)$ and Cost to reach the node 'n' from start state $g(n)$.

↳ Finds shortest path through search space.

↳ Fast and optimal result.

$f(n) = g(n) + h(n)$ heuristic Value (child node)

estimated cost. ↳ Cost to reach node

ALGORITHM:

- Enter starting node in OPEN list.
- If OPEN list is empty return FAIL
- Select node from OPEN list which has smallest Value ($g+h$).
 - If node = Goal, return Success Goal
- Expand node 'n' and generate all Successors
 - Compute ($g+h$) for each Successor node.
- If node 'n' is already in OPEN/CLOSED, attach to back pointer.
- Go to (ii)

Advantages:-

- Best Searching algorithms.
- Optimal and Complete.
- Solving Complex problems.

Disadvantages:-

- Doesn't always produces shortest.
- Complexity Issues.
- Requires memory.

Start

$S \rightarrow A = 1 + 6 = 7$ ✓
 $S \rightarrow B = 4 + 2 = 6$ ✓
 $S \rightarrow B \rightarrow C = 4 + 2 + 1 = 7$ ✓
 $S \rightarrow B \rightarrow C \rightarrow D = 4 + 2 + 3 + 0 = 9$ 81
 $S \rightarrow A \rightarrow B = 1 + 2 + 2 = 5$ ✓
 $S \rightarrow A \rightarrow C = 1 + 5 + 1 = 7$ ✓
 $S \rightarrow A \rightarrow D = 1 + 12 = 13$ 13
 $S \rightarrow A \rightarrow B \rightarrow C = 1 + 2 + 2 + 1 = 6$ ✓
 $S \rightarrow A \rightarrow B \rightarrow C \rightarrow D = 1 + 2 + 2 + 3 = 8$ 23
 $S \rightarrow A \rightarrow C \rightarrow D = 1 + 5 + 3 = 9$ 14

Problem formulation of zero sum or 2 player games

Two-player Games

- A game formulated as a search problem:

- Initial state: board position and turn
- Operators: definition of legal moves
- Terminal state: conditions for when game is over
- Utility function: a numeric value that describes the outcome of the game. E.g., -1, 0, 1 for loss, draw, win. (AKA **payoff function**)

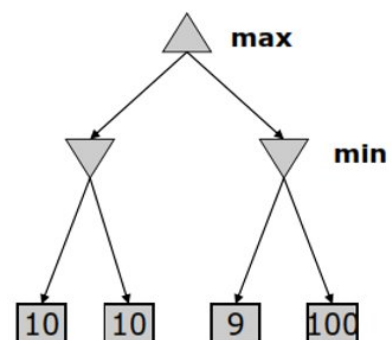
Min max algo

The minimax algorithm

- Perfect play for deterministic environments with perfect information
- **Basic idea:** choose move with highest minimax value
= best achievable payoff against best play
- **Algorithm:**
 1. Generate game tree completely
 2. Determine utility of each terminal state
 3. Propagate the utility values upward in the tree by applying MIN and MAX operators on the nodes in the current level
 4. At the root node use minimax decision to select the move with the max (of the min) utility value
- Steps 2 and 3 in the algorithm assume that the opponent will play perfectly.

The Minimax Algorithm Properties

- Performs a complete depth-first exploration of the game tree
- Optimal against a perfect player.
- Time complexity?
 - $O(b^m)$
- Space complexity?
 - $O(bm)$
- For chess, $b \sim 35$, $m \sim 100$
 - Exact solution is completely infeasible
 - But, do we need to explore the whole tree?
- Minimax serves as the basis for the mathematical analysis of games and for more practical algorithms



For alpha beta pruning the avg complexity would be $b^m/2$