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**SCHAUM'S**  
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# DATA STRUCTURES

**SEYMOUR LIPSCHUTZ**

- ▲ Details Linked representation of Stacks and Queues.
- ▲ Simplifies AVL Search Trees, m-way Search Trees and B Trees.
- ▲ Highly illustrative with over 300 figures and 375 exercises.

For sale in  
India, Pakistan,  
Nepal, Bangladesh,  
Sri Lanka and  
Bhutan Only

**Adapted by: G A V PAI**



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