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Operations Research (Paper III) MSc. (Computer Science) Semester III 2022-23

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Aim: Use graphical method to solve the following LPP:

```
Max Z = 3x + 5y
w.r.t.
x + 2y \le 2000,
x + y \le 1500,
y \le 600,
x, y \ge 0
```

Source Code:

```
require(lpSolve)
C \leftarrow c(3, 5)
A \leftarrow matrix(c(1, 2,
               1, 1,
               0, 1), nrow = 3, byrow = T)
B \leftarrow c(2000, 1500, 600)
constraint direction \leftarrow c("\leq", "\leq", "\leq")
plot.new()
plot.window(xlim = c(0, 2000), ylim = c(0, 2000))
axis(1)
axis(2)
title(main = "LPP using graphical method", xlab = "X-axis", ylab = "Y-
axis")
box()
segments(x0 = 2000, y0 = 0, x1 = 0, y1 = 1000, col = "green")
segments(x0 = 1500, y0 = 0, x1 = 0, y1 = 1500, col = "red")
segments(x0 = 0, y0 = 0, x1 = 600, y1 = 0, col = "blue")
z \leftarrow lp(direction = "max",
```

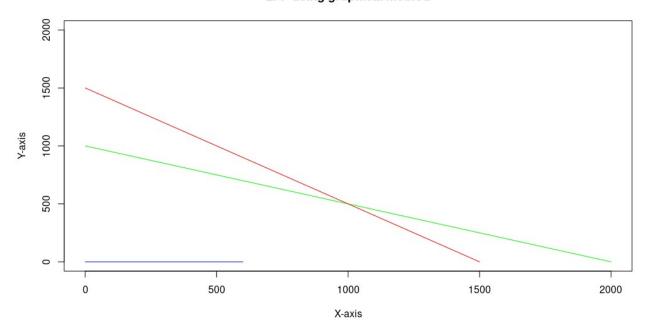
```
objective.in = C,
    const.mat = A,
    const.dir = constraint_direction,
    const.rhs = B,
    all.int = T
    )

print(z$status)

best_sol \(
< z$solution
    names(best_sol) \(
< c("x1", "x2")
    print(paste("Total cost: ", z$objval, sep = ""))</pre>
```

```
> best_sol ← z$solution
> names(best_sol) ← c("x1", "x2")
> print(paste("Total cost: ", z$objval, sep = ""))
[1] "Total cost: 5500"
> |
```

LPP using graphical method



Aim: Use simplex method to solve the following LPP:

```
Max Z = 3x + 2y
w.r.t.
x + y \le 4,
x - y \le 2,
x, y \ge 0
```

Source Code:

```
from scipy.optimize import linprog
```

```
obj = [-3, -2]
lhs_ineq = [[1, 1], [1, -1]]

In[1]:

rhs_ineq = [4, 2]

bound = [(0, float("inf")), (0, float("inf"))]

z = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq,
bounds = bound, method = "revised simplex")

z

In[2]:

print(z.fun)
print(z.success)
print(z.x)
```

```
1 from scipy.optimize import linprog
In [1]:
          3 obj = [-3, -2]
          4 lhs_ineq = [[1, 1], 5 [1, -1]]
          7 rhs_ineq = [4,
         10 bound = [(0, float("inf")),
                      (0, float("inf"))]
         1 z = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq,
2 bounds = bound, method = "revised simplex")
In [2]:
          3
          4 Z
Out[2]:
          con: array([], dtype=float64)
             fun: -11.0
          message: 'Optimization terminated successfully.'
             nit: 2
           slack: array([0., 0.])
          status: 0
          success: True
               x: array([3., 1.])
In [3]:
         1 print(z.fun)
          print(z.success)
          3 print(z.x)
         -11.0
         True
         [3. 1.]
```

Aim: Use simplex method to solve the following LPP:

Min Z =
$$x_1 - 3x_2 + 2x_3$$

w.r.t
 $3x_1 - x_2 + 3x_3 \le 7$,
 $-2x_1 + 4x_2 \le 12$,
 $-4x_1 + 3x_2 + 8x_3 \le 10$,
 $x_1, x_2, x_3 \ge 0$

Source Code:

from scipy.optimize import linprog

 \mathbf{Z}

```
In [1]:
         1 from scipy.optimize import linprog
          3 \text{ obj = } [1, -3, 2]
          4
          5 lhs_ineq = [[3, -1, 3],
                         [-2, 4, 0],
                          [-4, 3, 8]]
          7
          8
          9 rhs_ineq = [7,
         10
         11
                          10]
         12
         15
                       (0, float("inf"))]
        1 z = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq,
2 bounds = bound, method = "revised simplex")
In [2]:
          3
          4 z
Out[2]:
              con: array([], dtype=float64)
         fun: -11.0
message: 'Optimization terminated successfully.'
              nit: 2
            slack: array([ 0., 0., 11.])
           status: 0
          success: True
               x: array([4., 5., 0.])
```

Aim: Use simplex method to solve the following LPP:

Max
$$Z = x + 2y$$

w.r.t.
 $2x + y \le 20$,
 $-4x + 5y \le 10$,
 $-x + 2y \ge -2$,
 $-x + 5y = 15$,
 $x, y \ge 0$

Source code:

from scipy.optimize import linprog

```
1 from scipy.optimize import linprog
In [1]:
           3 obj = [-1, -2]
           4
           5 lhs_ineq = [[2, 1],
                            [-4, 5],
[1, -2]]
           7
           8
           9 rhs_ineq = [20,
          10
                           10,
                            2]
          11
          12
          13 lhs_eq = [[-1, 5]]
14 rhs_eq = [15]
          15
          16 bound = [(0, float("inf")),
          17
                        (0, float("inf"))]
           z = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq,
A_eq = lhs_eq, b_eq = rhs_eq,
bounds = bound, method = "revised simplex")
In [2]:
           4
           5 z
Out[2]:
               con: array([0.])
               fun: -16.8181818181817
           message: 'Optimization terminated successfully.'
               nit: 3
             slack: array([ 0. , 18.18181818, 3.36363636])
           status: 0
           success: True
           ____ x: array([7.72727273, 4.54545455])
```

Aim: Use Big M method to solve the following LPP:

Min
$$Z = 4x_1 + x_2$$

w.r.t.
 $3x_1 + 4x_2 \ge 12$,
 $x_1 + 5x_2 \ge 15$,
 $x_1, x_2 \ge 0$

Source code:

opt

from scipy.optimize import linprog

11

```
In [1]:
          1
            from scipy.optimize import linprog
          2
          3
            obj = [4, 1]
            lhs_ineq = [[-3, -4],
          4
          5
                         [-1, -5]
          6
          7
            rhs_ineq = [-20,
          8
                         -15]
          9
            bound = [(0, float("inf")),
         10
                      (0, float("inf"))]
         11
             opt =linprog(c=obj,A_ub=lhs_ineq,b_ub=rhs_ineq,
In [2]:
          2
                            bounds=bound,method="interior-point")
          3
          4
            opt
Out[2]:
             con: array([], dtype=float64)
             fun: 5.0000000002364455
         message: 'Optimization terminated successfully.'
             nit: 5
           slack: array([1.64270375e-10, 1.00000000e+01])
          status: 0
         success: True
               x: array([6.01160437e-11, 5.00000000e+00])
```

Aim: Use any method to solve the following resource allocation problem:

Max
$$Z = 20x_1 + 12x_2 + 50x_3 + 25x_4$$
(profit) w.r.t.
$$x_1 + x_2 + x_3 + x_4 \le 50$$
(manpower)
$$3x_1 + 2x_2 + x_3 \le 100$$
(material A)
$$x_2 + 2x_3 \le 90$$
,(material B)
$$x_1, x_2, x_3 \ge 0$$

Source code:

from scipy.optimize import linprog

```
In [1]: 1 from scipy.optimize import linprog
         3 obj = [-20, -12, -40, -25]
         5 lhs_ineq = [[1, 1, 1, 1],
                      [3, 2, 1, 0],
[0, 1, 2, 3]]
         6
         8
         9 rhs_ineq = [50,
                      100,
         11
                      90]
In [2]:
         opt = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq, method="revised simplex")
          3 opt
Out[2]:
             con: array([], dtype=float64)
             fun: -1900.0
         message: 'Optimization terminated successfully.'
             nit: 2
           slack: array([ 0., 40., 0.])
          status: 0
         success: True
               x: array([ 5., 0., 45., 0.])
```

Aim: Use simplex method to solve the following LPP:

```
Max Z = 200x + 300y
w.r.t.
2x + 3y \ge 1200,
x + y \le 400,
2x + 1.5y \ge 900,
x, y \ge 0
```

Source code:

```
from scipy.optimize import linprog
```

Aim: Use dual simplex method to solve the following LPP:

```
Max Z = 40x_1 + 50x_2
w.r.t.
2x_1 + 3x_2 \le 3,
8x_1 + 4x_2 \le 5,
x_1, x_2 \ge 0
```

Source code:

```
require(lpSolve) f.obj \leftarrow c(40, 50) f.con \leftarrow matrix(c(2, 3, 8, 4), nrow = 2, byrow = T) f.dir \leftarrow c(" \leq ", " \leq ") f.rhs \leftarrow c(3, 5) lp("max", f.obj, f.con, f.dir, f.rhs) solution \\ lp("max", f.obj, f.con, f.dir, f.rhs, compute.sens = T) sens.coef.from \\ lp("max", f.obj, f.con, f.dir, f.rhs, compute.sens = T) sens.coef.to \\ lp("max", f.obj, f.con, f.dir, f.rhs, compute.sens = T) duals \\ lp("max", f.obj, f.con, f.dir, f.rhs, compute.sens = T) duals.to
```

```
> lp("max", f.obj, f.con, f.dir, f.rhs, compute.sens = T)$duals
[1] 15.00 1.25 0.00 0.00
> lp("max", f.obj, f.con, f.dir, f.rhs, compute.sens = T)$duals.to
[1] 3.75e+00 1.20e+01 1.00e+30 1.00e+30
> |
```

Aim: Solve following transportation problem in which each cell represents unit costs:

	Customers			Cumply		
	1	2	3	4	Supply	
	10	2	20	11	15	
Suppliers	12	7	9	20	25	
	4	14	16	18	10	
Demand	5	15	15	15		

Source code:

```
library(lpSolve) cost \leftarrow matrix(c(10, 2, 20, 11, 12, 7, 9, 20, 4, 14, 16, 18), nrow = 3, byrow = T) colnames(cost) \leftarrow c("Customer 1", "Customer 2", "Customer 3", "Customer 4") rownames(cost) \leftarrow c("Supplier 1", "Supplier 2", "Supplier 3") row.signs \leftarrow rep("\leq", 3) row.rhs \leftarrow c(15, 25, 10) col.signs \leftarrow rep("\geq", 4) col.rhs \leftarrow c(5, 15, 15, 15) total.cost \leftarrow lp.transport(cost, "min", row.signs, row.rhs, col.signs, col.rhs) total.cost$\solution$ print(total.cost)
```

```
> total.cost ← lp.transport(cost, "min", row.signs, row.rhs, col.signs, col.rhs)
> total.cost$solution
      [,1] [,2] [,3] [,4]
[1,] 0 5 0 10
[2,] 0 10 15 0
[3,] 5 0 0 5
> print(total.cost)
Success: the objective function is 435
```

Aim: Solve following assignment problem represented in this matrix:

		Jobs			
		1	2	3	
	1	15	10	9	
Workers	2	9	15	10	
	3	10	12	8	

Source Code:

```
> #SOLVE FOLLOWING ASSIGNMENT PROBLEM REPRESENTED IN FOLLOWING MATRIX USING R PROGRAMMING
> # Assignment Problem
> # JOB1 JOB2 JOB3
> #W1 15 10 9
> #W2 9 15 10
> #W3 10 12 8
>
> library(lpSolve)
> cost ← matrix(c(15, 10, 9,
+ 9, 15, 10,
+ 10, 12, 8), nrow = 3, byrow = T)
> cost
[,1] [,2] [,3]
[1,] 15 10 9
[2,] 9 15 10
[3,] 10 12 8
> answer ← lp.assign(cost)
```

```
> answer ← lp.assign(cost)
> answer$solution
      [,1] [,2] [,3]
[1,] 0 1 0
[2,] 1 0 0
[3,] 0 0 1
> |
```