

Функційне програмування мовою Haskell

Класи типів

Класи типів

4.3 Type Classes and Overloading

<https://www.haskell.org/definition/haskell2010.pdf>

4.3.1 Class Declarations

<i>topdecl</i>	→	<code>class [scontext =>] tycls tyvar [where cdecls]</code>	
<i>scontext</i>	→	<code>simpleclass</code>	
		<code>(simpleclass₁ , ... , simpleclass_n)</code>	$(n \geq 0)$
<i>simpleclass</i>	→	<code>qtycls tyvar</code>	
<i>cdecls</i>	→	<code>{ cdecl₁ ; ... ; cdecl_n }</code>	$(n \geq 0)$
<i>cdecl</i>	→	<code>gendecl</code>	
		<code>(funlhs var) rhs</code>	

A *class declaration* introduces a new class and the operations (*class methods*) on it. A class declaration has the general form:

$$\text{class } cx \Rightarrow C \ u \text{ where } cdecls$$

This introduces a new class name C ; the type variable u is scoped only over the class method signatures in the class body. The context cx specifies the superclasses of C , as described below; the only type variable that may be referred to in cx is u .

The superclass relation must not be cyclic; i.e. it must form a directed acyclic graph.

Оголошення класів

4.3.1 Class Declarations

<https://www.haskell.org/definition/haskell2010.pdf> стор. 40/60

class [context =>] *Class_name type_var* [**where** cdecls]

Декларація класу представляє *новий клас* і операції (методи класу).

Визначаються:

- сигнатури операцій (методів)
- infix – оголошення
- означення методів-за-замовчуванням

Оголошення класів

4.3.1 Class Declarations

<https://www.haskell.org/definition/haskell2010.pdf> стор. 40/60

class [context =>] *Class_name* *type_var* [**where** cdecls]

class cx => *C u* **where** cdecls

Декларація класу представляє *новий клас* і операції (методи класу).

Визначаються:

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- infix – оголошення
- означення методів-за-замовчуванням

```
Prelude> :i Num
```

```
class Num a where
```

```
  (+) :: a -> a -> a
```

```
  (-) :: a -> a -> a
```

```
  (*) :: a -> a -> a
```

```
  negate :: a -> a
```

```
  abs :: a -> a
```

```
  signum :: a -> a
```

```
  fromInteger :: Integer -> a
```

```
  {-# MINIMAL (+), (*), abs, signum, fromInteger, (negate | (-)) #-}
```

```
    -- Defined in `GHC.Num'
```

```
instance Num Word -- Defined in `GHC.Num'
```

```
instance Num Integer -- Defined in `GHC.Num'
```

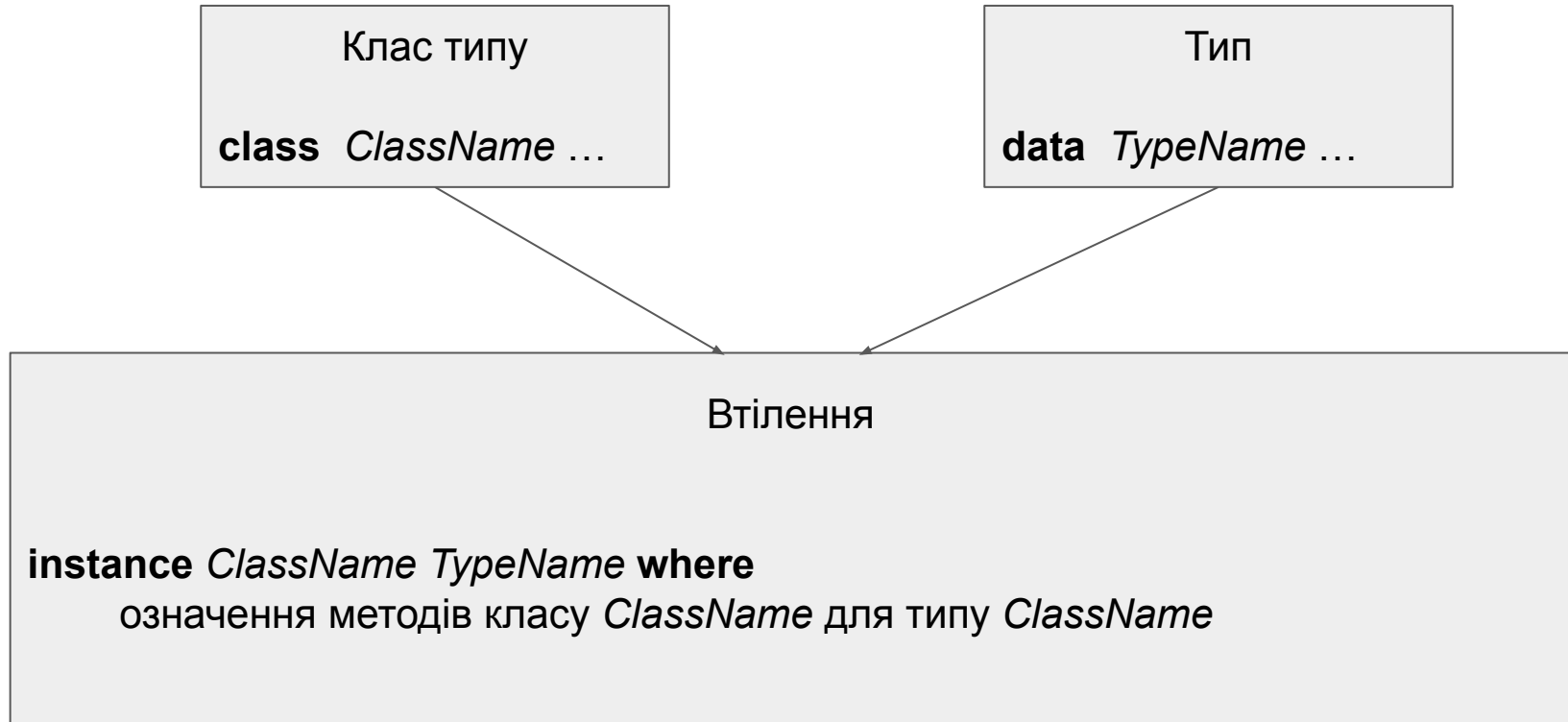
```
instance Num Int -- Defined in `GHC.Num'
```

```
instance Num Float -- Defined in `GHC.Float'
```

```
instance Num Double -- Defined in `GHC.Float'
```

Оголошення втілень (екземплярів) класу

4.3.2 Instance Declarations



Оголошення втілень (екземплярів) класу

-- декларація класу

class MyClass a where

eq :: a -> a -> Bool

mul :: a -> a -> Int

-- декларація типу

newtype MyInt = ConMyInt Int

-- втілення (класу в типі)

instance MyClass MyInt **where**

(ConMyInt x) `eq` (ConMyInt y) = abs(x-y) < 3

(ConMyInt 2) `mul` (ConMyInt 2) = 5

(ConMyInt i) `mul` (ConMyInt j) = i * j

Оголошення втілень (екземплярів) класу

> ConMyInt 2 `mul` ConMyInt 3

6

> :t ConMyInt 2 `mul` ConMyInt 3
ConMyInt 2 `mul` ConMyInt 3 :: Int

> ConMyInt 3 `mul` ConMyInt 3

9

> ConMyInt 3 `mul` ConMyInt 2

6

> ConMyInt 2 `mul` ConMyInt 2

5

Оголошення втілень (екземплярів) класу

```
> ConMyInt 2 `eq` ConMyInt 2  
True
```

```
> ConMyInt 2 `eq` ConMyInt 3  
True
```

```
> ConMyInt 2 `eq` ConMyInt 4  
True
```

```
> ConMyInt 2 `eq` ConMyInt 5  
False
```

Оголошення втілень (екземплярів) класу

> ConMyInt 2

<interactive>:12:1: error:

- * No instance for (Show MyInt) arising from a use of `print'
- * In a stmt of an interactive GHCi command: print it

Оголошення втілень (екземплярів) класу

> ConMyInt 2

<interactive>:12:1: error:

- * No instance for (Show MyInt) arising from a use of `print'
- * In a stmt of an interactive GHCi command: print it

```
newtype MyInt = ConMyInt Int  
deriving Show
```

Оголошення втілень (екземплярів) класу

```
> ConMyInt 2
```

```
<interactive>:12:1: error:
```

- * No instance for (Show MyInt) arising from a use of `print'
- * In a stmt of an interactive GHCi command: print it

```
newtype MyInt = ConMyInt Int  
deriving Show
```

```
> ConMyInt 2
```

```
ConMyInt 2
```

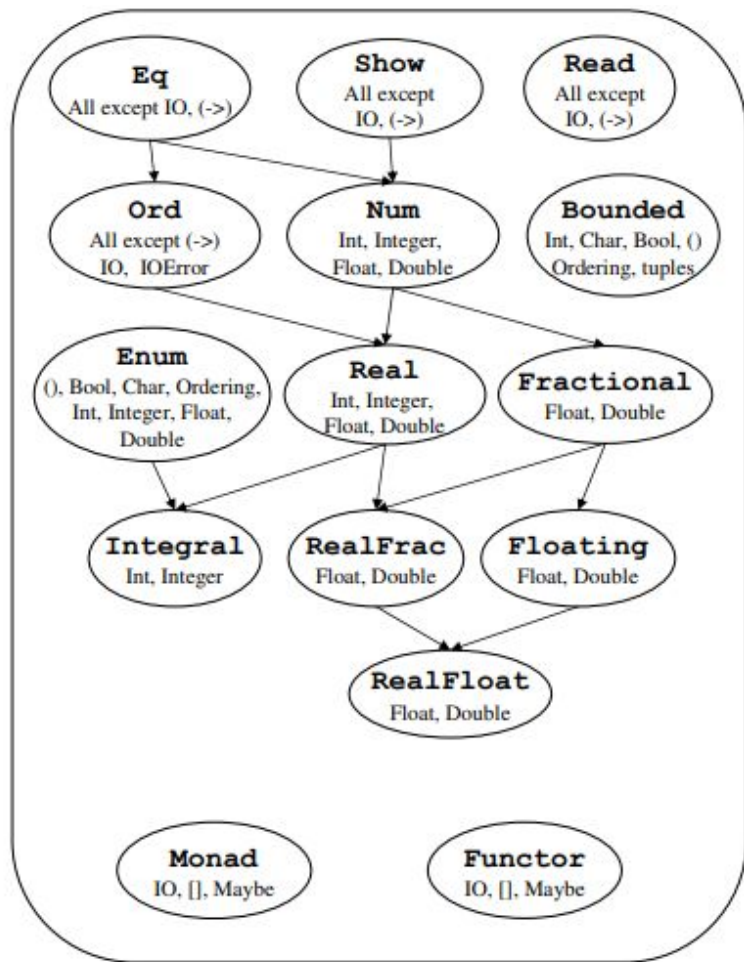


Figure 6.1: Standard Haskell Classes

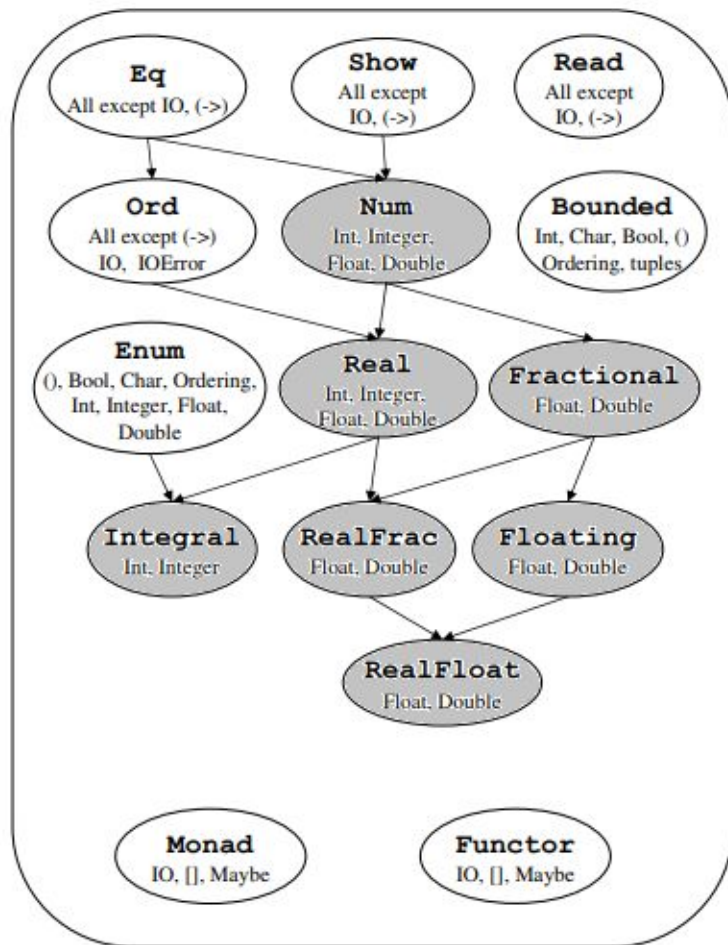


Figure 6.1: Standard Haskell Classes

```
Prelude> :i Num
```

```
class Num a where
```

```
  (+) :: a -> a -> a
```

```
  (-) :: a -> a -> a
```

```
  (*) :: a -> a -> a
```

```
  negate :: a -> a
```

```
  abs :: a -> a
```

```
  signum :: a -> a
```

```
  fromInteger :: Integer -> a
```

```
  {-# MINIMAL (+), (*), abs, signum, fromInteger, (negate | (-))
```

```
  #-}
```

```
    -- Defined in `GHC.Num'
```

```
instance Num Word -- Defined in `GHC.Num'
```

```
instance Num Integer -- Defined in `GHC.Num'
```

```
instance Num Int -- Defined in `GHC.Num'
```

```
instance Num Float -- Defined in `GHC.Float'
```

```
instance Num Double -- Defined in `GHC.Float'
```

```
Prelude> :i Real
```

```
class (Num a, Ord a) => Real a where
  toRational :: a -> Rational
  {-# MINIMAL toRational #-}
  -- Defined in `GHC.Real'
instance Real Word -- Defined in `GHC.Real'
instance Real Integer -- Defined in `GHC.Real'
instance Real Int -- Defined in `GHC.Real'
instance Real Float -- Defined in `GHC.Float'
instance Real Double -- Defined in `GHC.Float'
```


Prelude> :i Floating

class Fractional a => Floating a where

```
pi :: a
exp :: a -> a
log :: a -> a
sqrt :: a -> a
(**) :: a -> a -> a
logBase :: a -> a -> a
sin :: a -> a
cos :: a -> a
tan :: a -> a
asin :: a -> a
acos :: a -> a
atan :: a -> a
sinh :: a -> a
cosh :: a -> a
tanh :: a -> a
asinh :: a -> a
acosh :: a -> a
atanh :: a -> a
GHC.Float.log1p :: a -> a
GHC.Float.expm1 :: a -> a
GHC.Float.log1pexp :: a -> a
GHC.Float.log1mexp :: a -> a
{-# MINIMAL pi, exp, log, sin, cos, asin, acos, atan, sinh, cosh,
    asinh, acosh, atanh #-}
-- Defined in `GHC.Float'
instance Floating Float -- Defined in `GHC.Float'
instance Floating Double -- Defined in `GHC.Float'
```

```
> :i Real
```

```
class (Num a, Ord a) => Real a where
  toRational :: a -> Rational
  {-# MINIMAL toRational #-}
  -- Defined in `GHC.Real'
instance Real Word -- Defined in `GHC.Real'
instance Real Integer -- Defined in `GHC.Real'
instance Real Int -- Defined in `GHC.Real'
instance Real Float -- Defined in `GHC.Float'
instance Real Double -- Defined in `GHC.Float'
```

```
> toRational 24
```

```
24 % 1
```

```
> toRational 24/18
```

```
4 % 3
```

```
> toRational 1.25
```

```
5 % 4
```

```
> :t it
```

```
it :: Rational
```

```
Prelude> :i Fractional
```

```
class Num a => Fractional a where
```

```
  (/) :: a -> a -> a
```

```
  recip :: a -> a
```

```
  fromRational :: Rational -> a
```

```
  {-# MINIMAL fromRational, (recip | (/)) #-}
```

```
    -- Defined in `GHC.Real'
```

```
instance Fractional Float -- Defined in `GHC.Float'
```

```
instance Fractional Double -- Defined in `GHC.Float'
```

```
> :i Fractional
```

```
class Num a => Fractional a where
```

```
  (/) :: a -> a -> a
```

```
  recip :: a -> a
```

```
  fromRational :: Rational -> a
```

```
  {-# MINIMAL fromRational, (recip | (/)) #-}
```

```
    -- Defined in `GHC.Real'
```

```
instance Fractional Float -- Defined in `GHC.Float'
```

```
instance Fractional Double -- Defined in `GHC.Float'
```

```
> toRational 1.25
```

```
5 % 4
```

```
> :t it
```

```
it :: Rational
```

```
> fromRational $ toRational 1.25
```

```
1.25
```

```
> :t it
```

```
it :: Fractional a => a
```

```
> :i Fractional
```

```
class Num a => Fractional a where
  (/) :: a -> a -> a
  recip :: a -> a
  fromRational :: Rational -> a
  {-# MINIMAL fromRational, (recip | (/)) #-}
  -- Defined in `GHC.Real'
instance Fractional Float -- Defined in `GHC.Float'
instance Fractional Double -- Defined in `GHC.Float'
```

```
> toRational 1.25
5 % 4
```

```
> :t it
it :: Rational
```

```
> fromRational $ toRational 1.25
1.25
```

```
> :t it
it :: Fractional a => a
```

```
> recip 2
0.5
```

```
> :t it
it :: Fractional a => a
```

```
Prelude> :i RealFrac
```

```
class (Real a, Fractional a) => RealFrac a where
  properFraction :: Integral b => a -> (b, a)
  truncate :: Integral b => a -> b
  round :: Integral b => a -> b
  ceiling :: Integral b => a -> b
  floor :: Integral b => a -> b
  {-# MINIMAL properFraction #-}
  -- Defined in `GHC.Real'
instance RealFrac Float -- Defined in `GHC.Float'
instance RealFrac Double -- Defined in `GHC.Float'
```

> :i RealFrac

```
class (Real a, Fractional a) => RealFrac a where
  properFraction :: Integral b => a -> (b, a)
  truncate :: Integral b => a -> b
  round :: Integral b => a -> b
  ceiling :: Integral b => a -> b
  floor :: Integral b => a -> b
  {-# MINIMAL properFraction #-}
  -- Defined in `GHC.Real'
instance RealFrac Float -- Defined in `GHC.Float'
instance RealFrac Double -- Defined in `GHC.Float'
```

```
properFraction :: Integral b => a -> (b, a)Source#
```

The function **properFraction** takes a real fractional number x and returns a pair (n,f) such that $x = n+f$, and:

- n is an integral number with the same sign as x ; and
- f is a fraction with the same type and sign as x , and with absolute value less than 1.

The default definitions of the **ceiling**, **floor**, **truncate** and **round** functions are in terms of **properFraction**.

```
Prelude> :i Integral
```

```
class (Real a, Enum a) => Integral a where
```

```
  quot :: a -> a -> a
```

```
  rem  :: a -> a -> a
```

```
  div  :: a -> a -> a
```

```
  mod  :: a -> a -> a
```

```
  quotRem :: a -> a -> (a, a)
```

```
  divMod  :: a -> a -> (a, a)
```

```
  toInteger :: a -> Integer
```

```
  {-# MINIMAL quotRem, toInteger #-}
```

```
    -- Defined in `GHC.Real'
```

```
instance Integral Word -- Defined in `GHC.Real'
```

```
instance Integral Integer -- Defined in `GHC.Real'
```

```
instance Integral Int -- Defined in `GHC.Real'
```

Integral numbers, supporting integer division

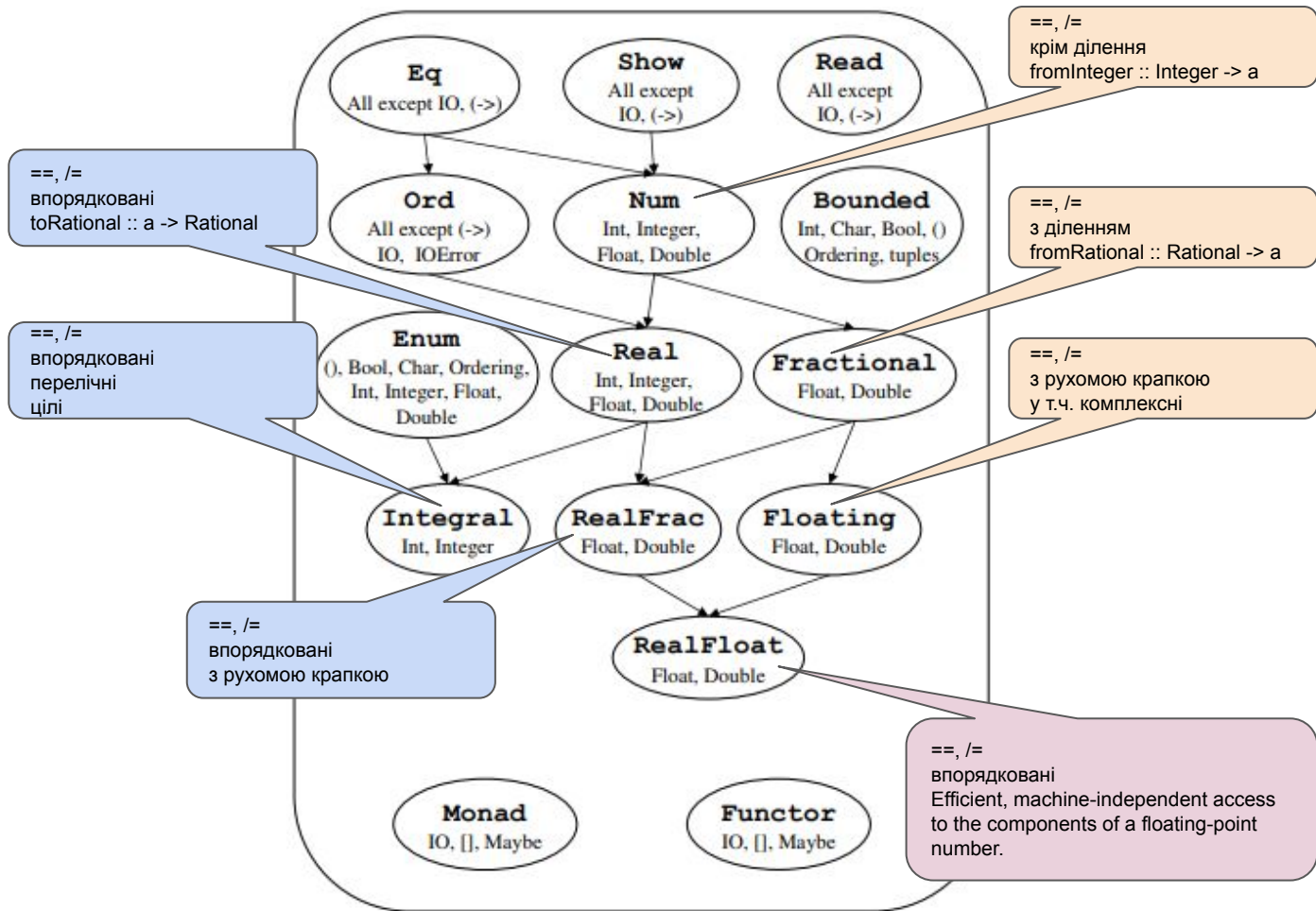


Figure 6.1: Standard Haskell Classes

Infix-оголошення

4.4.2 Fixity Declarations

`infix[l|r]` пріоритет ім'я_оператора

`infix` - неасоціативний

`infixl`- лівоасоціативний

`infixr`- правоасоціативний

пріоритет 0-9

Infix-оголошення

4.4.2 Fixity Declarations

infixr 6 `|-`

`(|-) :: Num a => a -> a -> a`

`(|-) x y = x - y`

4.4.2 Fixity Declarations

infixr 6 `|-`

`(|-) :: Num a => a -> a -> a`

`(|-) x y = x - y`

`> 3 |- 1 |- 1`

`3`

Infix-оголошення

4.4.2 Fixity Declarations

infixr 6 $|-$

$(| -) :: \text{Num } a \Rightarrow a \rightarrow a \rightarrow a$

$(| -) \ x \ y = x - y$

$> 3 \ | - \ 1 \ | - \ 1$
3

infix 5 $\sim =$

$a \sim = b = a - b < h \ \&\& \ b - a < h$

where $h = 0.001$

Infix-оголошення

4.4.2 Fixity Declarations

infixr 6 `|-`

`(|-) :: Num a => a->a->a`

`(|-) x y = x-y`

`> 3 |- 1 |- 1`
`3`

infix 5 `~=`

`a ~= b = a-b<h && b-a<h`

where `h=0.001`

`> 1 ~= 1`
`True`

`> 1 ~= 2`
`False`

`> 1 ~= 1.0005`
`True`

`> 1 ~= 1.005`
`False`

`> 1 ~= 1 ~= 1` ?

Infix-оголошення

4.4.2 Fixity Declarations

infixr 6 `|-`

`(|-) :: Num a => a->a->a`

`(|-) x y = x-y`

`> 3 |- 1 |- 1`

`3`

infix 5 `~=`

`a ~= b = a-b<h && b-a<h`

where `h=0.001`

`> 1 ~= 1 ~= 1`

`<interactive>:45:1: error:`

`Precedence parsing error`

`cannot mix `~=' [infix 5] and `~=' [infix 5] in the same infix expression`