

Функційне програмування мовою Haskell

Типи даних

Користувацькі типи даних

4.2 User-Defined Datatypes

<https://www.haskell.org/definition/haskell2010.pdf>

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type

Алгебраїчні типи даних

<https://www.haskell.org/definition/haskell2010.pdf> стор. 40/60

topdecl → **data** [context =>] *simpletype* [= *constrs*]* [*deriving*]
simpletype → *tycon* *tyvar*₁ ... *tyvar*_k ($k \geq 0$)

data [Контекст] КонструкторТипу [ЗмінніТипу] [= КонструкториДаних] [ЗмінніТипу]

data ConstrType *typeVar*₁ *typeVar*₂ ... *typeVar*_k
= Constructor₁ *typeVar*_{1,1} *typeVar*_{1,2} ... *typeVar*_{1,m1}
| Constructor₂ *typeVar*_{2,1} *typeVar*_{2,2} ... *typeVar*_{2,m2}
...
| Constructor_p *typeVar*_{p,1} *typeVar*_{p,2} ... *typeVar*_{p,mp}

де $k \geq 0$, $p \geq 0$, $m1..mp \geq 0$)

Алгебраїчні типи даних

<https://www.haskell.org/definition/haskell2010.pdf> стор. 40/60

$topdecl \rightarrow \mathbf{data} \ simpletype = constrs \ [deriving]$
 $simpletype \rightarrow \ tycon \ tyvar_1 \ \dots \ tyvar_k \quad (k \geq 1)$

data КонструкторТипу [ЗмінніТипу] = КонструкториДаних [ЗмінніТипу]

$data \ ConstrType \ typeVar_1 \ typeVar_2 \ \dots \ typeVar_k$
 $\quad = \ Constructor_1 \ typeVar_{1,1} \ typeVar_{1,2} \ \dots \ typeVar_{1,m1}$
 $\quad \quad | \ Constructor_2 \ typeVar_{2,1} \ typeVar_{2,2} \ \dots \ typeVar_{2,m2}$
 $\quad \quad \dots$
 $\quad \quad | \ Constructor_p \ typeVar_{p,1} \ typeVar_{p,2} \ \dots \ typeVar_{p,mp}$

де $k \geq 0$, $p \geq 1$, $m1 \dots mp \geq 0$)

Алгебраїчні типи даних

<https://www.haskell.org/definition/haskell2010.pdf> стор. 40/60

topdecl → **data** *simpletype* = *constrs* [*deriving*]
simpletype → *tycon* *tyvar*₁ ... *tyvar*_k ($k \geq 1$)

Ім'я/Назва типу

data КонструкторТипу [ЗмінніТипу] = КонструкториДаних [ЗмінніТипу]

data ConstrType typeVar₁ typeVar₂ ... typeVar_k
= Constructor₁ typeVar_{1,1} typeVar_{1,2} ... typeVar_{1,m1}
| Constructor₂ typeVar_{2,1} typeVar_{2,2} ... typeVar_{2,m2}
...
| Constructor_p typeVar_{p,1} typeVar_{p,2} ... typeVar_{p,mp}

де $k \geq 0$, $p \geq 1$, $m_1 \dots m_p \geq 0$)

Алгебраїчні типи даних

конструктори без параметрів

```
data Color = Red
```

```
  | Orange
```

```
  | Yellow
```

```
  | Green
```

```
  | Blue
```

```
  | Indigo
```

```
  | Violet
```

Алгебраїчні типи даних

конструктори без параметрів

```
data Color = Red
```

```
    | Orange
```

```
    | Yellow
```

```
    | Green
```

```
    | Blue
```

```
    | Indigo
```

```
    | Violet
```

```
*Main> :t Orange
```

```
Orange :: Color
```

```
*Main> Orange
```

```
<interactive>:3:1: error:
```

- * No instance for (Show Color) arising from a use of `print'
- * In a stmt of an interactive GHCi command: print it

Алгебраїчні типи даних

конструктори без параметрів

data Color = Red

| Orange

| Yellow

| Green

| Blue

| Indigo

| Violet

deriving (Show)

Алгебраїчні типи даних

конструктори без параметрів

```
data Color = Red
```

```
  | Orange
```

```
  | Yellow
```

```
  | Green
```

```
  | Blue
```

```
  | Indigo
```

```
  | Violet
```

```
  deriving (Show)
```

```
*Main> :l dataColor.hs  
[1 of 1] Compiling Main  
Ok, 1 module loaded.
```

```
( dataColor.hs, interpreted )
```

```
*Main> :t Orange  
Orange :: Color
```

```
*Main> Orange  
Orange
```

Алгебраїчні типи даних

конструктори без параметрів

> Blue > Indigo

> Blue == Indigo

> [Orange ..Indigo]

Алгебраїчні типи даних

конструктори без параметрів

```
data Color = Red
```

```
  | Orange
```

```
  | Yellow
```

```
  | Green
```

```
  | Blue
```

```
  | Indigo
```

```
  | Violet
```

```
deriving (Eq, Show, Ord, Enum)
```

Алгебраїчні типи даних

конструктори даних з параметрами

```
data Shape = Ellipse Float Float
```

```
    | Square Float
```

```
    | Polygon [(Float, Float)]
```

Алгебраїчні типи даних

конструктори з параметрами

```
data Point a = Pnt a a
```

```
dist :: Point Double -> Point Double -> Double
```

```
dist (Pnt x1 y1) (Pnt x2 y2) = sqrt ((x1-x2)^2+(y1-y2)^2)
```

Алгебраїчні типи даних

конструктори з параметрами

```
data Point a = Pnt a a
```

```
dist :: Point Double -> Point Double -> Double
```

```
dist (Pnt x1 y1) (Pnt x2 y2) = sqrt ((x1-x2)^2+(y1-y2)^2)
```

```
> :type Pnt 2 3
```

```
Pnt 2 3 :: (Num t) => Point t
```

```
> dist ( Pnt 0 0) (Pnt 1 1)
```

```
1.4142135623730951
```

Алгебраїчні типи даних

конструктори з параметрами

```
data Point a = Pnt a a
```

```
dyst :: Point Double -> Point Double -> Double
```

```
dyst (Pnt x1 y1) (Pnt x2 y2) = sqrt ((x1-x2)^2+(y1-y2)^2)
```

Алгебраїчні типи даних

конструктори з параметрами

```
data Point a = Pnt a a
```

```
dist :: Point Double -> Point Double -> Double
```

```
dist (Pnt x1 y1) (Pnt x2 y2) = sqrt ((x1-x2)^2+(y1-y2)^2)
```

назва конструктора **може** збігатись з назвою типу

можна було визначити так:

```
data Point a = Point a a
```

```
dist :: Point Double -> Point Double -> Double
```

```
dist ( Point x1 y1) ( Point x2 y2) = sqrt ((x1-x2)^2+(y1-y2)^2)
```


Алгебраїчні типи даних

конструктори з параметрами

```
data Maybe a = Just a  
              | Nothing
```

Алгебраїчні типи даних

конструктори з параметрами

```
data Maybe a =    Just a  
                | Nothing
```

```
head':: [a]->Maybe a
```

```
head' []=Nothing
```

```
head' (x:_) = Just x
```

Алгебраїчні типи даних

конструктори з параметрами

```
data Maybe a =    Just a  
                | Nothing
```

```
head':: [a]->Maybe a
```

```
head' []=Nothing
```

```
head' (x:_) = Just x
```

```
> head' []  
Nothing
```

```
> head' [1,2,3]  
Just 1
```

```
> head' "fgh"  
Just 'f'
```

Алгебраїчні типи даних

конструктори з параметрами

```
data Maybe a = Just a  
              | Nothing
```

```
> head "fgh" : "12"  
"f12"
```

```
head' :: [a] -> Maybe a
```

```
head' [] = Nothing
```

```
head' (x:_) = Just x
```

Алгебраїчні типи даних

конструктори з параметрами

```
data Maybe a = Just a  
              | Nothing
```

```
> head "fgh" : "12"  
"f12"
```

```
head "fgh" : "12" => 'f' : "12" => "f12"
```

```
head' :: [a] -> Maybe a
```

```
head' [] = Nothing
```

```
head' (x:_) = Just x
```

Алгебраїчні типи даних

конструктори з параметрами

```
data Maybe a = Just a  
              | Nothing
```

```
> head "fgh" : "12"  
"f12"
```

```
head "fgh" : "12" => 'f' : "12" => "f12"
```

```
head' :: [a] -> Maybe a
```

```
head' [] = Nothing
```

```
head' (x:_) = Just x
```

```
> head' "fgh" : "12"
```

Алгебраїчні типи даних

конструктори з параметрами

```
data Maybe a =    Just a  
                | Nothing
```

```
> head "fgh" : "12"  
"f12"
```

```
head "fgh" : "12" => 'f' : "12" => "f12"
```

```
head' :: [a] -> Maybe a
```

```
head' [] = Nothing
```

```
head' (x:_) = Just x
```

```
> head' "fgh" : "12"
```

```
<interactive>:25:15: error:
```

```
* Couldn't match type `Char' with `Maybe Char'  
   Expected type: [Maybe Char]  
   Actual type: [Char]
```

Алгебраїчні типи даних

конструктори з параметрами

```
data Maybe a = Just a  
              | Nothing
```

```
> head "fgh" : "12"  
"f12"
```

```
head "fgh" : "12" => 'f' : "12" => "f12"
```

```
head' :: [a] -> Maybe a
```

```
head' [] = Nothing
```

```
head' (x:_) = Just x
```

```
> head' "fgh" : "12"
```

```
<interactive>:25:15: error:
```

```
* Couldn't match type `Char' with `Maybe Char'
```

```
Expected type: [Maybe Char]
```

```
Actual type: [Char]
```

```
head' "fgh" : "12" => Just 'f' : "12" => ⊥
```


Алгебраїчні типи даних

конструктори з параметрами

```
fromMaybe :: (Num a) => Maybe a -> a
```

```
fromMaybe Nothing = 0
```

```
fromMaybe (Just x) = x
```

```
> fromMaybe (Just 2)
```

```
2
```

```
> fromMaybe (head' [1,2,3,4])
```

```
1
```

```
> 2 + fromMaybe (head' [1,2,3,4])
```

```
3
```

```
> 2 + fromMaybe (head' [])
```

```
2
```

Алгебраїчні типи даних

конструктори з параметрами

```
fromMaybe2 :: Maybe Char -> Char
```

```
fromMaybe2 Nothing = ' '
```

```
fromMaybe2 (Just x) = x
```

```
> head' "fgh"
```

```
Just 'f'
```

```
> fromMaybe2 (head' "fgh")
```

```
'f'
```

```
> fromMaybe2 (head' "fgh") : "123"
```

```
"f123"
```

```
> fromMaybe2 (head' "") : "123"
```

```
" 123"
```

Алгебраїчні типи даних

конструктори з параметрами

```
fromMaybe2 :: Maybe Char -> Char  
fromMaybe2 Nothing = ''  
fromMaybe2 (Just x) = x
```

```
fromMaybe :: (Num a) => Maybe a -> a  
fromMaybe Nothing = 0  
fromMaybe (Just x) = x
```

Prelude містить функцію *maybe*

```
maybe :: b -> (a -> b) -> Maybe a -> b  
maybe n _ Nothing = n  
maybe _ f (Just x) = f x
```

Алгебраїчні типи даних

конструктори з параметрами

Prelude містить функцію *maybe*

```
maybe :: b -> (a -> b) -> Maybe a -> b
```

```
maybe n _ Nothing = n
```

```
maybe _ f (Just x) = f x
```

```
> maybe 0 (*3) (Just 2)
```

```
6
```

```
> maybe 0 (*3) Nothing
```

```
0
```

```
> maybe "" show (Just 5)
```

```
"5"
```

```
> maybe "" show Nothing
```

```
""
```

Алгебраїчні типи даних

конструктори з параметрами

Prelude містить функцію *maybe*

```
maybe :: b -> (a -> b) -> Maybe a -> b
```

```
maybe n _ Nothing = n
```

```
maybe _ f (Just x) = f x
```

```
> maybe 0 (*3) (Just 2)  
6
```

```
> maybe 0 (*3) Nothing  
0
```

```
> maybe "" show (Just 5)  
"5"
```

```
> maybe "" show Nothing  
""
```

```
> maybe 0 (*1) Nothing  
0
```

```
> maybe 0 (*1) (Just 2)  
2
```

```
> maybe 0 id (Just 2)  
2
```

```
> maybe 0 id Nothing  
0
```

Алгебраїчні типи даних

Іменовані поля

```
data Configuration =  
  ConsConfig{  
    userName :: String,  
    localhost :: String,  
    remoteHost :: String,  
    isGuest :: Bool,  
    isSuperuser :: Bool,  
    currentDirectory :: String,  
    homeDirectory :: String,  
    timeConnected :: Integer  
  } deriving (Eq, Show)
```

Алгебраїчні типи даних

Іменовані поля

```
data Configuration =  
  ConsConfig{  
    userName :: String,  
    localhost :: String,  
    remoteHost :: String,  
    isGuest :: Bool,  
    isSuperuser :: Bool,  
    currentDirectory :: String,  
    homeDirectory :: String,  
    timeConnected :: Integer  
  } deriving (Eq, Show)
```

```
myconf :: Configuration  
myconf = ConsConfig {  
  userName = "User1",  
  localhost = "myComp",  
  remoteHost = "asd12",  
  isGuest = False,  
  isSuperuser = False,  
  currentDirectory = "curUser1",  
  homeDirectory = "hmUser1",  
  timeConnected = 0  
}
```

Алгебраїчні типи даних

```
data Configuration =
```

```
  ConsConfig{
```

```
    userName :: String,
```

```
    localhost :: String,
```

```
    remoteHost :: String,
```

```
    isGuest :: Bool,
```

```
    isSuperuser :: Bool,
```

```
    currentDirectory :: String,
```

```
    homeDirectory :: String,
```

```
    timeConnected :: Integer
```

```
  } deriving (Eq, Show)
```

Іменовані поля

```
myconf :: Configuration
```

```
myconf = ConsConfig {
```

```
  userName = "User1",
```

```
  localhost = "myComp",
```

```
  remoteHost = "asd12",
```

```
  isGuest = False,
```

```
  isSuperuser = False,
```

```
  currentDirectory = "curUser1",
```

```
  homeDirectory = "hmUser1",
```

```
  timeConnected = 0
```

```
> :t userName
```

```
userName :: Configuration -> String
```

```
> :t isSuperuser
```

```
isSuperuser :: Configuration -> Bool
```

```
> :t timeConnected
```

```
timeConnected :: Configuration -> Integer
```


Алгебраїчні типи даних

```
data Configuration =
```

```
  ConsConfig{
```

```
    userName :: String,
```

```
    localhost :: String,
```

```
    remoteHost :: String,
```

```
    isGuest :: Bool,
```

```
    isSuperuser :: Bool,
```

```
    currentDirectory :: String,
```

```
    homeDirectory :: String,
```

```
    timeConnected :: Integer
```

```
  } deriving (Eq, Show)
```

Іменовані поля

```
myconf :: Configuration
```

```
myconf = ConsConfig{
```

```
  userName = "User1",
```

```
  localhost = "myComp",
```

```
  remoteHost = "asd12",
```

```
  isGuest = False,
```

```
  isSuperuser = False,
```

```
  currentDirectory = "curUser1",
```

```
  homeDirectory = "hmUser1",
```

```
  timeConnected = 0
```

```
> :t userName
```

```
userName :: Configuration -> String
```

```
> userName myconf
```

```
"User1"
```

```
> :t isSuperuser
```

```
isSuperuser :: Configuration -> Bool
```

```
> isSuperuser myconf
```

```
False
```

```
> :t timeConnected
```

```
timeConnected :: Configuration -> Integer
```

```
> timeConnected myconf
```

Новий тип (ізоморфний)

4.2.3 Datatype Renamings

<https://www.haskell.org/definition/haskell2010.pdf> стор. 43/63

Єдиний конструктор з єдиним параметром

topdecl → ***newtype*** [*context* =>] *TypeName typeVars* = *Constr oneType* [*deriving*]

Новий тип (ізоморфний)

4.2.3 Datatype Renamings

<https://www.haskell.org/definition/haskell2010.pdf> стор. 43/63

Єдиний конструктор з єдиним параметром

topdecl → ***newtype*** *TypeName typeVars= Constr oneType [deriving]*

newtype MyInt = ConMyInt Int

Новий тип (ізоморфний)

4.2.3 Datatype Renamings

<https://www.haskell.org/definition/haskell2010.pdf> стор. 43/63

Єдиний конструктор з єдиним параметром

topdecl → *newtype* *TypeName* *typeVars* = *Constr oneType* [*deriving*]

newtype MyInt = ConMyInt Int

instance Eq MyInt **where**

```
ConMyInt i == ConMyInt j
  | odd i && odd j = i == j
  | otherwise = False
```

Новий тип (ізоморфний)

4.2.3 Datatype Renamings

<https://www.haskell.org/definition/haskell2010.pdf> стор. 43/63

Єдиний конструктор з єдиним параметром

topdecl → *newtype* *TypeName* *typeVars* = *Constr oneType* [*deriving*]

newtype MyInt = ConMyInt Int

instance Eq MyInt **where**

```
ConMyInt i == ConMyInt j
  | odd i && odd j = i == j
  | otherwise = False
```

```
> ConMyInt 2 == ConMyInt 2
False
```

```
> ConMyInt 3 == ConMyInt 3
True
```

```
> ConMyInt 3 == ConMyInt 5
False
```

Новий тип (ізоморфний)

4.2.3 Datatype Renamings

<https://www.haskell.org/definition/haskell2010.pdf> стор. 43/63

Єдиний конструктор з єдиним параметром

— можна визначити і інші відношення

```
instance Ord MyInt where
```

```
  ConMyInt i < ConMyInt j
```

```
  | odd' i && odd' j = i < j
```

```
  | even' i && even' j = i < j
```

```
  | even' i = True
```

```
  | otherwise = False
```

```
    where odd' x = (x `mod` 2) == 1
```

```
          even' = not . odd'
```

4.2.2 Type Synonym Declarations

<https://www.haskell.org/definition/haskell2010.pdf> стор. 42/62

topdecl \rightarrow **type** simpletype = type
simpletype \rightarrow tycon tyvar₁ . . . tyvar_k
(k \geq 0)

4.2.2 Type Synonym Declarations

<https://www.haskell.org/definition/haskell2010.pdf> стор. 42/62

type Position = (Float,Float)

type Angle = Float

type Distance = Float

4.2.2 Type Synonym Declarations

<https://www.haskell.org/definition/haskell2010.pdf> стор. 42/62

```
type Position = (Float,Float)
```

```
type Angle = Float
```

```
type Distance = Float
```

```
move :: Distance->Angle->Position->Position
```

```
move d alpha (x0,y0) = (x0+d*cos(alpha),y0+d*sin(alpha))
```

4.2.2 Type Synonym Declarations

<https://www.haskell.org/definition/haskell2010.pdf> стор. 42/62

```
type Position = (Float,Float)
```

```
type Angle = Float
```

```
type Distance = Float
```

```
move :: Distance->Angle->Position->Position
```

```
move d alpha (x0,y0) = (x0+d*cos(alpha),y0+d*sin(alpha))
```

```
>move 3 0.3 (0,0)
```

```
(2.8660095,0.8865607)
```