# Recursion

#### Overview

```
- Definition of recursion
  - The call stack

    countdown example

  - factorial example
  - Recursion and arrays, strings
  - Tips for approaching recursion problems
*/
```

#### Definition

```
/* recursion occurs when a function calls itself! */
/* recursion is an alternative to iteration (using a loop) */
/* in the real world, you may see recursion instead of iteration when a
   recursive solution is:
     - easier to reason about (recursion helps break big problems into
       small chunks
     - easier to read than an iterative solution
     - won't negatively affect performance too much (recursion can be
       a memory hog) */
```

```
/* before we talk about recursion, we have to talk about the call stack */
/* JS is "single threaded" - can only run one function at a time */
/* the call stack is the structure JS uses to figure out which function
   it should be running at any point in time */
```

```
/* whenever we call a function, it's added to the top of the call stack */
   /* JS will execute whatever function is on the top of the stack */
   function first() {
     console.log('I am first!');
                                                                  Callstack
   function second() {
     console.log('I am second!');
13 first();
14 second();
```

```
/* whenever we call a function, it's added to the top of the call stack */
   /* JS will execute whatever function is on the top of the stack */
   function first() {
     console.log('I am first!');
                                                                   Callstack
   function second() {
     console.log('I am second!');
13 first();
14 second();
                                                                   first()
```

```
/* whenever we call a function, it's added to the top of the call stack */
   /* JS will execute whatever function is on the top of the stack */
   function first() {
     console.log('I am first!');
                                                                  Callstack
   function second() {
     console.log('I am second!');
13 first();
14 second();
```

```
/* whenever we call a function, it's added to the top of the call stack */
   /* JS will execute whatever function is on the top of the stack */
   function first() {
     console.log('I am first!');
                                                                   Callstack
   function second() {
     console.log('I am second!');
13 first();
14 second();
                                                                   second()
```

```
/* whenever we call a function, it's added to the top of the call stack */
   /* JS will execute whatever function is on the top of the stack */
   function first() {
     console.log('I am first!');
                                                                  Callstack
   function second() {
     console.log('I am second!');
13 first();
14 second();
```

```
function first() {
  console.log('I am first!');
  second();
  console.log('First is finished');
function second() {
  console.log('I am second!');
first();
```

Callstack

```
function first() {
  console.log('I am first!');
  second();
  console.log('First is finished');
function second() {
  console.log('I am second!');
first();
```

Callstack

first()

```
function first() {
  console.log('I am first!');
  second();
  console.log('First is finished');
function second() {
  console.log('I am second!');
first();
```

second()

Callstack

first()

```
function first() {
  console.log('I am first!');
  second();
  console.log('First is finished'); // first "paused" while second ran
function second() {
                                                                Callstack
  console.log('I am second!');
first();
                                                                 first()
```

```
function first() {
  console.log('I am first!');
  second();
  console.log('First is finished'); // first "paused" while second ran
function second() {
                                                                Callstack
  console.log('I am second!');
first();
```

```
/* write a function that counts down to 1 */
function countdown(num) {
  for (let i = num; i >= 1; i--) {
    console.log(i);
countdown(5);
```

```
/* let's refactor our solution, writing a function that takes a number and
   and logs it out */
function countdown(num) {
  console.log(num);
countdown(5);
countdown(4);
countdown(3);
countdown(2); // notice, no loops!
countdown(1); // how do the arguments change between calls?
```

```
/* every time we called countdown, we subtracted one from the previous
      num */
   /* instead of manually calling countdown over and over, why not have
      countdown call itself, subtracting one from num each time? */
   function countdown(num) {
                                                                  Callstack
     console.log(num);
     countdown(num - 1);
10 }
   countdown(5);
```

```
/* every time we called countdown, we subtracted one from the previous
      num */
   /* instead of manually calling countdown over and over, why not have
      countdown call itself, subtracting one from num each time? */
   function countdown(num) {
                                                                   Callstack
     console.log(num);
     countdown(num - 1);
10 }
   countdown(5);
                                                                 countdown(5)
```

```
/* every time we called countdown, we subtracted one from the previous
      num */
   /* instead of manually calling countdown over and over, why not have
      countdown call itself, subtracting one from num each time? */
   function countdown(num) {
                                                                   Callstack
     console.log(num);
     countdown(num - 1);
10 }
   countdown(5);
                                                                  countdown(4)
                                                                  countdown(5)
```

```
/* every time we called countdown, we subtracted one from the previous
      num */
   /* instead of manually calling countdown over and over, why not have
      countdown call itself, subtracting one from num each time? */
   function countdown(num) {
                                                                    Callstack
     console.log(num);
     countdown(num - 1);
10 }
                                                                  countdown(3)
   countdown(5);
                                                                  countdown(4)
                                                                  countdown(5)
```

```
/* every time we called countdown, we subtracted one from the previous
      num */
   /* instead of manually calling countdown over and over, why not have
      countdown call itself, subtracting one from num each time? */
   function countdown(num) {
                                                                     Callstack
     console.log(num);
     countdown(num - 1);
                                                                   countdown(2)
10 }
                                                                   countdown(3)
   countdown(5);
                                                                   countdown(4)
                                                                   countdown(5)
```

```
/* every time we called countdown, we subtracted one from the previous
      num */
   /* instead of manually calling countdown over and over, why not have
      countdown call itself, subtracting one from num each time? */
   function countdown(num) {
                                                                     Callstack
     console.log(num);
     countdown(num - 1);
                                                                   countdown(1)
10 }
                                                                   countdown(2)
                                                                   countdown(3)
   countdown(5);
                                                                   countdown(4)
                                                                   countdown(5)
```

```
/* every time we called countdown, we subtracted one from the pr
   num */
/* instead of manually calling countdown over and over, why not have
   countdown call itself, subtracting one from num each time? */
function countdown(num) {
  console.log(num);
  countdown(num - 1);
countdown(5);
```

Callstack
countdown(0)
countdown(1)
countdown(2)
countdown(3)
countdown(4)
countdown(5)

```
^{1} /* every time we called countdown, we subtracted one from the pr ^{-1}
```

/\* instead of manually calling countdown over and over, why not have countdown call itself, subtracting one from num each time? \*/

```
function countdown(num) {
   console.log(num);
   countdown(num - 1);

10 }

11 countdown(5);

13
```

# Callstack countdown(-1) countdown(0) countdown(1) countdown(2) countdown(3) countdown(4) countdown(5)

14

```
/* every time we called countdown, we subtracted one from the pr
      num */
   /* instead of manually calling countdown over and over, why not have
      countdown call itself, subtracting one from num each time? */
   function countdown(num) {
     console.log(num);
     countdown(num - 1);
10
   countdown(5);
```

#### Callstack countdown(-2) countdown(-1) countdown(0) countdown(1) countdown(2) countdown(3) countdown(4) countdown(5)

-2

14

```
/* every time we called countdown, we subtracted one from the pr
   num */
/* instead of manually calling countdown over and over, why
   countdown call itself, subtracting one from num each ti
function countdown(num) {
  console.log(num);
  countdown(num - 1);
countdown(5);
```

y not have me? */
Callstack
(and so on)
countdown(-2)
countdown(-1)
countdown(0)
countdown(1)
countdown(2)
countdown(3)
countdown(4)
countdown(5)

(and so on)

```
/* every time we called countdown, we subtracted one from the pr
   num */
/* instead of manually calling countdown over and over, why not
   countdown call itself, subtracting one from num each time? */
function countdown(num) {
  console.log(num);
  countdown(num - 1);
countdown(5);
```

```
/* that started off so promisingly! */
/* because our function was instructed to call itself every time, the
   function ends up calling itself forever until our computer runs out of
   memory */
/* let's write in a stop condition so the function eventually stops
   calling itself */
```

```
function countdown(num) {
     // here's our stop condition, commonly known as the 'base case'
     if (num < 1) {
       console.log('done!');
     // here's our 'recursive case'
     else {
                                                                   Callstack
       console.log(num);
       countdown(num - 1);
13 countdown(3);
```

```
function countdown(num) {
     // here's our stop condition, commonly known as the 'base case'
     if (num < 1) {
       console.log('done!');
     // here's our 'recursive case'
     else {
                                                                    Callstack
       console.log(num);
       countdown(num - 1);
13 countdown(3);
                                                                  countdown(3)
```

```
function countdown(num) {
     // here's our stop condition, commonly known as the 'base case'
     if (num < 1) {
       console.log('done!');
     // here's our 'recursive case'
     else {
                                                                     Callstack
       console.log(num);
       countdown(num - 1);
                                                                   countdown(2)
13 countdown(3);
                                                                   countdown(3)
```

```
function countdown(num) {
     // here's our stop condition, commonly known as the 'base case'
     if (num < 1) {
       console.log('done!');
     // here's our 'recursive case'
     else {
                                                                     Callstack
       console.log(num);
       countdown(num - 1);
                                                                    countdown(1)
                                                                    countdown(2)
13 countdown(3);
                                                                   countdown(3)
```

```
function countdown(num) {
     // here's our stop condition, commonly known as the 'base case'
     if (num < 1) {
       console.log('done!');
     // here's our 'recursive case'
     else {
                                                                      Callstack
       console.log(num);
       countdown(num - 1);
                                                                    countdown(0)
                                                                    countdown(1)
                                                                    countdown(2)
13 countdown(3);
                                                                    countdown(3)
```

```
function countdown(num) {
     // here's our stop condition, commonly known as the 'base case'
     if (num < 1) {
       console.log('done!');
     // here's our 'recursive case'
     else {
                                                                     Callstack
       console.log(num);
       countdown(num - 1);
                                                                    countdown(1)
                                                                    countdown(2)
13 countdown(3);
                                                                   countdown(3)
```

#### 3 2 1 done!

```
function countdown(num) {
     // here's our stop condition, commonly known as the 'base case'
     if (num < 1) {
       console.log('done!');
     // here's our 'recursive case'
     else {
                                                                     Callstack
       console.log(num);
       countdown(num - 1);
                                                                   countdown(2)
13 countdown(3);
                                                                   countdown(3)
```

#### 3 2 1 done!

```
function countdown(num) {
     // here's our stop condition, commonly known as the 'base case'
     if (num < 1) {
       console.log('done!');
     // here's our 'recursive case'
     else {
                                                                    Callstack
       console.log(num);
       countdown(num - 1);
13 countdown(3);
                                                                  countdown(3)
```

#### 3 2 1 done!

#### example: countdown

```
function countdown(num) {
     // here's our stop condition, commonly known as the 'base case'
     if (num < 1) {
       console.log('done!');
     // here's our 'recursive case'
     else {
                                                                   Callstack
       console.log(num);
       countdown(num - 1);
13 countdown(3);
```

#### example: countdown

```
/* two takeaways from countdown: */
/* 1. you need to define a base case! */
/* 2. your recursive case must change the input to the function so that
      you will eventually trigger the base case! */
```

# Returning from recursive calls

```
/* recursion becomes more complicated when the function must return a
   value */
/* good practice is to start by defining a base case */
/* base cases are often occur when there is a simple input that expects a
   simple output (e.g., the sum of a single number is that number) */
/* test that the base case works before working with the recursive
   case! */
```

```
/* define a function, factorial, that take a number and returns the
      factorial of that number */
   /* as a reminder:
      0! === 1
6 1! === 1
7 	 2! === 2 (2 * 1)
     3! === 6 (3 * 2 * 1)
      4! === 24 (4 * 3 * 2 * 1)
      5! === 120 (5 * 4 * 3 * 2 * 1) */
12 /* what look like simple inputs/outputs we can use to build a base
      case? */
```

```
function factorial(num) {
 // base case: num is 0 or 1
  if (num === 0 || num === 1) {
    return 1;
factorial(0);
factorial(1);
```

```
/* ok, base case is set, just need to remember that our recursive case
   has bring num closer and closer to 1 or 0 so we eventually
   hit our base case */
/* notice an interesting pattern!
   0! === 1
   1! === 1
   2! === 2 (2 * factorial(1))
   3! === 6 (3 * factorial(2))
   4! === 24 (4 * factorial(3))
   5! === 120 (5 * factorial(4)) */
```

```
function factorial(num) {
     // base case: num is 0 or 1
     if (num === 0 || num === 1) {
       return 1;
     // recursive case: num must get closer to 0 or 1
     // TODO
  /* it's best to write your recursive case using the simplest possible
      input that will result in a recursive call */
12 let result = factorial(2);
13 console.log(result);
```

```
function factorial(num) {
     // base case: num is 0 or 1
     if (num === 0 || num === 1) {
       return 1;
     // recursive case: num must get closer to 0 or 1
     // we know we have to call factorial again in the recursive case
     // if num === 2, what do we get if we call factorial again with num - 1?
     console.log(factorial(num - 1));
10 }
12 let result = factorial(2);
13 console.log(result);
```

```
function factorial(num) {
  // base case: num is 0 or 1
  if (num === 0 || num === 1) {
    return 1;
// recursive case: num must get closer to 0 or 1
  // from that pattern we noticed earlier, we know 2! === 2 * 1!
  console.log(num * factorial(num - 1));
let result = factorial(2);
console.log(result);
```

```
function factorial(num) {
     // base case: num is 0 or 1
     if (num === 0 || num === 1) {
       return 1;
     // recursive case: num must get closer to 0 or 1
     // just have to return the result now
     let result = num * factorial(num - 1);
     return result;
10 }
12 let result = factorial(2);
13 console.log(result);
```

```
function factorial(num) {
  // base case: num is 0 or 1
  if (num === 0 || num === 1) {
    return 1;
// recursive case: num must get closer to 0 or 1
  let result = num * factorial(num - 1);
                                                      call stack
                                                                    return value
  return result;
let result = factorial(5);
console.log(result);
```

```
function factorial(num) {
  // base case: num is 0 or 1
  if (num === 0 || num === 1) {
    return 1;
// recursive case: num must get closer to 0 or 1
  let result = num * factorial(num - 1);
                                                       call stack
                                                                      return value
  return result;
let result = factorial(5);
console.log(result);
                                                     factorial(5)
                                                                   5 * factorial(4)
```

```
function factorial(num) {
  // base case: num is 0 or 1
  if (num === 0 || num === 1) {
    return 1;
// recursive case: num must get closer to 0 or 1
  let result = num * factorial(num - 1);
                                                        call stack
                                                                       return value
  return result;
let result = factorial(5);
console.log(result);
                                                      factorial(4)
                                                                    4 * factorial(3)
                                                      factorial(5)
                                                                    5 * factorial(4)
```

```
function factorial(num) {
     // base case: num is 0 or 1
     if (num === 0 || num === 1) {
        return 1;
     // recursive case: num must get closer to 0 or 1
     let result = num * factorial(num - 1);
                                                             call stack
                                                                            return value
     return result;
10
   let result = factorial(5);
                                                           factorial(3)
                                                                         3 * factorial(2)
   console.log(result);
                                                           factorial(4)
                                                                         4 * factorial(3)
                                                           factorial(5)
                                                                         5 * factorial(4)
```

```
function factorial(num) {
     // base case: num is 0 or 1
     if (num === 0 || num === 1) {
       return 1;
     // recursive case: num must get closer to 0 or 1
     let result = num * factorial(num - 1);
                                                             call stack
     return result;
10
                                                           factorial(2)
                                                                          2 * factorial(1)
   let result = factorial(5);
                                                                          3 * factorial(2)
                                                           factorial(3)
   console.log(result);
                                                           factorial(4)
                                                                         4 * factorial(3)
                                                           factorial(5)
                                                                          5 * factorial(4)
```

return value

```
function factorial(num) {
  // base case: num is 0 or 1
  if (num === 0 || num === 1) {
    return 1;
// recursive case: num must get closer to 0 or 1
  let result = num * factorial(num - 1);
  return result;
let result = factorial(5);
console.log(result);
```

call stack	return value
factorial(1)	=> 1
factorial(2)	2 * factorial(1)
factorial(3)	<pre>3 * factorial(2)</pre>
factorial(4)	4 * factorial(3)
factorial(5)	5 * factorial(4)

```
function factorial(num) {
     // base case: num is 0 or 1
     if (num === 0 || num === 1) {
        return 1;
     // recursive case: num must get closer to 0 or 1
     let result = num * factorial(num - 1);
                                                             call stack
                                                                            return value
     return result;
10
                                                           factorial(2)
                                                                               2 * 1
   let result = factorial(5);
                                                                          3 * factorial(2)
                                                           factorial(3)
   console.log(result);
                                                           factorial(4)
                                                                          4 * factorial(3)
                                                           factorial(5)
                                                                          5 * factorial(4)
```

```
function factorial(num) {
     // base case: num is 0 or 1
     if (num === 0 || num === 1) {
        return 1;
     // recursive case: num must get closer to 0 or 1
     let result = num * factorial(num - 1);
                                                             call stack
                                                                            return value
     return result;
10
                                                           factorial(2)
                                                                                => 2
   let result = factorial(5);
                                                           factorial(3)
                                                                          3 * factorial(2)
   console.log(result);
                                                           factorial(4)
                                                                          4 * factorial(3)
                                                           factorial(5)
                                                                          5 * factorial(4)
```

```
function factorial(num) {
  // base case: num is 0 or 1
  if (num === 0 || num === 1) {
    return 1;
// recursive case: num must get closer to 0 or 1
  let result = num * factorial(num - 1);
                                                         call stack
                                                                        return value
  return result;
let result = factorial(5);
                                                                          3 * 2
                                                       factorial(3)
console.log(result);
                                                       factorial(4)
                                                                     4 * factorial(3)
                                                       factorial(5)
                                                                     5 * factorial(4)
```

```
function factorial(num) {
  // base case: num is 0 or 1
  if (num === 0 || num === 1) {
    return 1;
// recursive case: num must get closer to 0 or 1
  let result = num * factorial(num - 1);
                                                         call stack
                                                                        return value
  return result;
let result = factorial(5);
                                                       factorial(3)
                                                                           => 6
console.log(result);
                                                       factorial(4)
                                                                     4 * factorial(3)
                                                       factorial(5)
                                                                     5 * factorial(4)
```

```
function factorial(num) {
  // base case: num is 0 or 1
  if (num === 0 || num === 1) {
    return 1;
// recursive case: num must get closer to 0 or 1
  let result = num * factorial(num - 1);
                                                        call stack
                                                                      return value
  return result;
let result = factorial(5);
console.log(result);
                                                      factorial(4)
                                                                    5 * factorial(4)
                                                      factorial(5)
```

```
function factorial(num) {
  // base case: num is 0 or 1
  if (num === 0 || num === 1) {
    return 1;
// recursive case: num must get closer to 0 or 1
  let result = num * factorial(num - 1);
                                                        call stack
                                                                      return value
  return result;
let result = factorial(5);
console.log(result);
                                                      factorial(4)
                                                                         => 24
                                                                    5 * factorial(4)
                                                      factorial(5)
```

```
function factorial(num) {
  // base case: num is 0 or 1
  if (num === 0 || num === 1) {
    return 1;
// recursive case: num must get closer to 0 or 1
  let result = num * factorial(num - 1);
                                                       call stack
                                                                     return value
  return result;
let result = factorial(5);
console.log(result);
                                                     factorial(5)
                                                                       5 * 24
```

```
function factorial(num) {
  // base case: num is 0 or 1
  if (num === 0 || num === 1) {
    return 1;
// recursive case: num must get closer to 0 or 1
  let result = num * factorial(num - 1);
                                                       call stack
                                                                     return value
  return result;
let result = factorial(5);
console.log(result);
                                                     factorial(5)
                                                                       => 120
```

```
function factorial(num) {
  // base case: num is 0 or 1
  if (num === 0 || num === 1) {
    return 1;
// recursive case: num must get closer to 0 or 1
  let result = num * factorial(num - 1);
                                                      call stack
                                                                    return value
  return result;
let result = factorial(5);
console.log(result);
```

```
/* three takeaways from factorial: */
   /* 1. define your base case first, using simple inputs/outputs */
   /* 2. define your base case, and test it using the simplest possible
         input that results in one recursive call to the base case */
   /* 3. test your function against more-complex inputs */
10
```

#### recursion and iterables

```
/* you can use recursion with any data type in JS */
   /* if you're asked to recurse through arrays or strings, the base case
      often occurs when the iterable is empty or has a length of one */
   /* imagine finding the sum of numbers in an array */
   sumArray([4]); // if array.length === 1, the sum is easy to calculate
   /* if the base case required the iterable to have a length of 1 or 0, it
      must mean that the recursive case has to reduce the length of the
    iterable with every recursive call */
14 /* note: nested arrays can be approached differently; see next unit! */
```

#### other recursion hints

```
/* cannot emphasize enough: start with the base case! */
   /* cannot emphasize enough: test recursive case with simplest possible
      input that will result in one recursive call to the base case */
   /* ask yourself: what type of thing should my function return? base case
      and recursive case should return the same type of thing! */
   /* use console.logs or debugger to debug */
10
```

#### Recap

```
- Definition of recursion
  - The call stack

    countdown example

  - factorial example
  - Recursion and arrays, strings
  - Tips for approaching recursion problems
*/
```